

Final Examination

CS540: Introduction to Artificial Intelligence

December 19, 2005 Instructor: Jerry Zhu

CLOSED BOOK

(Two letter-size notes allowed. You don't need to hand them in)

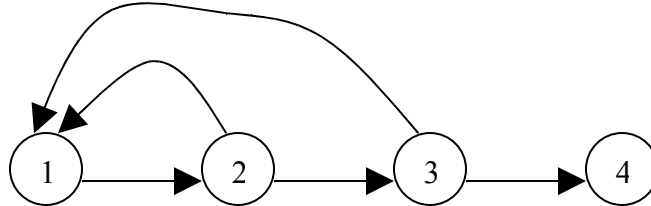
LAST (FAMILY) NAME: _____

FIRST NAME: _____

Problem	Score	Max Score: 5 points each
1	=====	
2	=====	
3	=====	
4	=====	
5	=====	
6	=====	
7	=====	
8	=====	
9	=====	
10	=====	
11	=====	
12	=====	
13	=====	
14	=====	
15	=====	
16	=====	
17	=====	
18	=====	
19	=====	
20	=====	
Total	=====	100

1. Iterative deepening search

Run iterative deepening search on the following graph, starting from node 1. Node 4 is the goal node. Write down the node numbers as they are expanded. Do NOT use any loop avoidance method. Everything being equal, expand node with the lowest number.

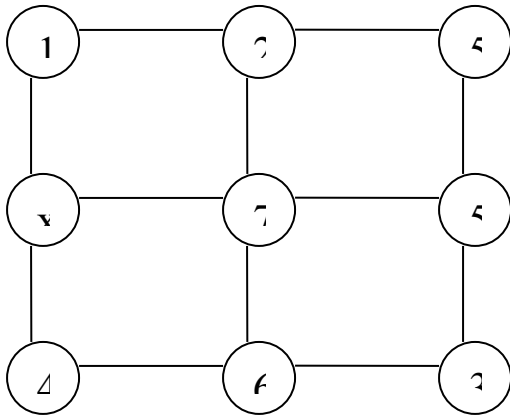


2. Optimization

In the following electric network, each node is connected by resistors (the edges) of unit resistance to some other nodes. Each node (except node x) is fixed at the voltage shown in the circle. The heat generated by the electric network is

$$E = \sum_{i \sim j} (v_i - v_j)^2,$$

where the sum is over all resistors, i and j are the two nodes connected by the resistor, and v_i, v_j are the voltages at node i, j respectively. What should the voltage x be to minimize the heat?



3. Heuristic search

In standard A* search the objective function at each node n is $f(n)=g(n)+h(n)$, where $g(n)$ is the cost from start to this node, and $h(n)$ is an admissible heuristic from n to goal. Now let us use a different objective function:

$$f(n) = w * g(n) + (1-w) * h(n)$$

where $w \geq 0$.

- What kind of search does this perform when $w=0$?
- What about when $w=0.5$?
- What about when $w=1$?
- For what values of w is this algorithm guaranteed to be optimal?

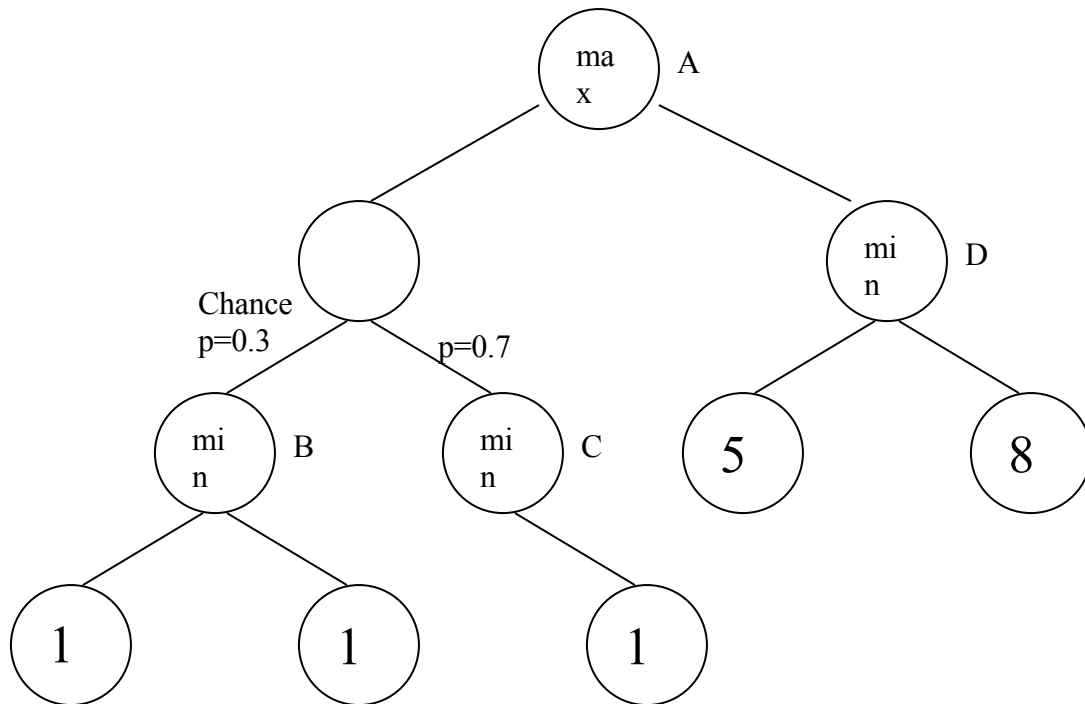
4. Nash equilibrium

Circle all Nash equilibria in the following zero-sum game. A is the maximizer and B is the minimizer.

		B		
		I	II	III
A	I	6	3	7
	II	29	11	17
	III	4	9	15

5. Matrix normal form with Chance node

Write down the matrix normal form of the following zero-sum game with chance node.



6. Dominate strategy

Perform iterative elimination of strictly dominated strategies on the following matrix normal form for non-zero sum game. Each cell contains (A's score, B's score).

		B		
		2	3	4
A	1	2, 4	3, 7	4, 5
	2	1, 2	5, 4	2, 3
	3	4, 1	2, 8	5, 3
	4	3, 6	4, 0	1, 9

7. Propositional logic

The propositional logic connective NAND is defined as:

P	Q	P NAND Q
T	T	F
T	F	T
F	T	T
F	F	T

Express (P AND Q) using and only using NAND, P, Q. (Hint: you need 3 NAND)

8. Unification

Write down the Most General Unifier for the following pairs of FOL clauses.

A. $\text{See}(\text{I}, \text{Duck}, \text{Telescope}), \text{See}(x, y, z)$.

B. $\text{Like}(x, \text{Hate}(\text{Mary}, \text{Mary})), \text{Like}(\text{Hate}(y, y), x)$.

C. $\text{Like}(\text{Hate}(y, y), x), \text{Like}(x, \text{Hate}(\text{Mary}, \text{John}))$.

D. $\text{Wiser}(\text{Father}(x), x), \text{Wiser}(\text{Father}(y), \text{Tom})$.

E. $\text{Knows}(\text{Self}(x), x), \text{Knows}(y, y)$.

9. Given KB:

$$P \Rightarrow Q$$

$$Q \Rightarrow R$$

Use resolution refutation to prove $P \Rightarrow R$. Clearly write down all the steps.

10. K-nearest-neighbor

Given the following dataset:

$\{(x=1, y=+), (x=2, y=+), (x=4, y=-), (x=8, y=-), (x=16, y=-)\}$

- a) What is the leave-one-out accuracy with 1-nearest-neighbor classifier? Use Euclidean distance.
- b) What is the leave-one-out accuracy with 3-nearest-neighbor classifier? Use Euclidean distance.

11. Entropy

I have a book with 1024 pages. I randomly flip to a page and ask you to determine the page number. You can only ask questions with yes/no answers.

- a) How many questions do you have to ask to guarantee an answer, if you design your questions optimally?
- b) How do you design your questions?
- c) If you observe that I tend to flip to the first half of the book, does it make the number of questions needed: smaller, the same, or bigger in theory?

12. Speech recognition

In one sentence, describe the significance of McGurk effect.

13. Mutual information

Given the dataset

x	y
1	+
1	+
1	+
1	+
0	-
0	-
0	-
0	-

What is the entropy $H(y)$? What is the conditional entropy $H(y|x)$? What is the mutual information $I(x;y)$? Use bits as the unit.

14. K-means Clustering

Given dataset $\{1, 2, 3, 6, 7, 8, 11, 12, 100\}$ and three cluster centers $c_1=1.4$, $c_2=6.9$, $c_3=12$

- a) List the cluster assignment (i.e. which point is in which cluster) in the next step.
- b) Compute the new cluster centers after a)
- c) List the cluster assignment after b)
- d) Compute the new cluster centers after c)
- e) In b) compute the new cluster centers using the median instead of the mean

15. Support Vector Machines (SVM)

Let $X=(x_1, x_2)$ be a point in 2-dimensional space. Given two points

$$X_1=(0,0), y_1=+1$$

$$X_2=(1,1), y_2=-1$$

$X'W + 1=0$ defines a line, where W is a vector of length 2. What W separates X_1, X_2 with the largest margin?

16. Perceptron

In question 7 we defined NAND. Let $T=1$ and $F=0$. Using a perceptron with step function activation ($a(x)=0$ if $x \leq 0$, 1 otherwise), implement NAND. You need to 1) draw the perceptron, 2) mark the inputs, 3) define the weights.

17. Neural network

- a) In a neural network with x inputs, one hidden layer with y units, and one output layer with z units, assuming each input is connected to all hidden units, and each hidden unit is connected to all output units, how many weights are there in the neural network altogether?
- b) Same as above, but each input is connected to all hidden units AND all output units, how many weights are there?

18. Probability

In a bag there are two envelopes, one has a red ball (worth \$100) and a black ball (worth nothing), the other has two black balls. You randomly chose an envelope.

- a) From the envelope your friend randomly took out one ball, and told you “it’s black”. Given the chance, should you switch to the other envelope? What is the probability that you get the red ball if you switch?
- b) Instead of a), your friend looked into the envelope, and told you “there is at least one black ball”. Given the chance, should you switch to the other envelope? What is the probability that you get the red ball if you switch?

19. Statistics

In your 10-day vacation in Alaska, you kept the following log:

- | | |
|---------------------|--------|
| (Rainy, Saw bear) | 0 day |
| (~Rainy, Saw bear) | 3 days |
| (Rainy, ~Saw bear) | 6 days |
| (~Rainy, ~Saw bear) | 1 day |
- a) Using add-one smoothing, estimate the complete joint probability distribution. It is ok to use fractional numbers.
 - b) From a), compute the conditional probability $P(\text{Saw bear} \mid \sim\text{Rainy})$

20. Bayes Net

Given the Bayes Net, compute $P(B|C)$. Show your steps. You can leave the numbers in the answer without computing the multiplications / divisions.

