

# A Framework for Incorporating General Domain Knowledge into Latent Dirichlet Allocation using First-Order Logic

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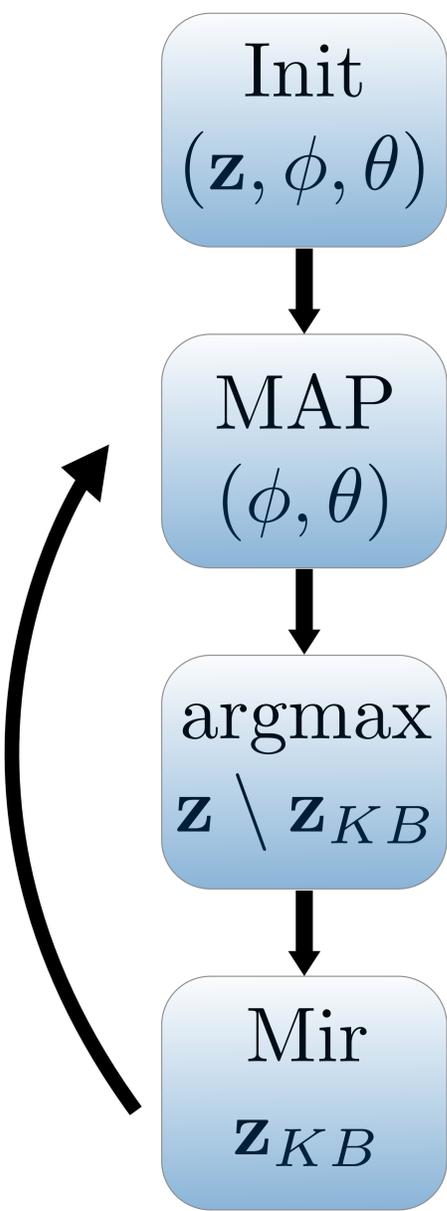
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## Summary

Latent topic models have emerged as a versatile tool for data exploration. Researchers often extend the base Latent Dirichlet Allocation (LDA) [1] model in order to capture domain knowledge or side information relevant to a particular application, but constructing these extensions is non-trivial. We propose a general framework for encoding domain knowledge as First-Order Logic (FOL), allowing users to adapt topic modeling to their needs.

## Scalable MAP Inference



The combinatorial explosion in rule groundings is a challenge, as in general MLNs. We use a continuous relaxation scheme along with random sampling of groundings to do stochastic Mirror Descent (Mir) over the latent topic assignments affected by logic rules.

## Example Rules

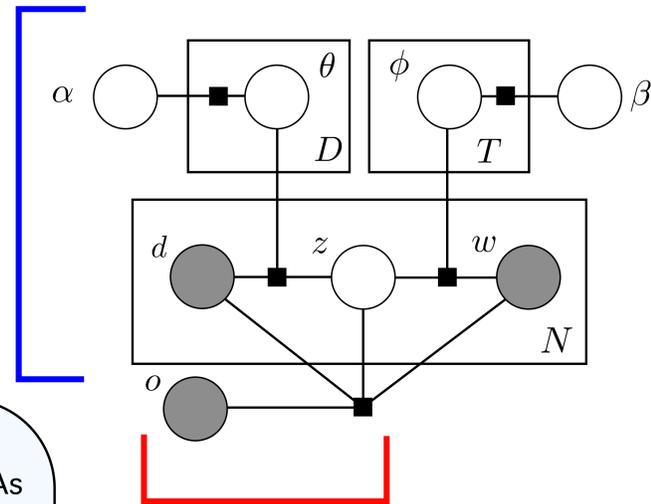
Rule Type	Logical form	Meaning
Seed word	$W(i, embryo) \Rightarrow Z(i, 3)$	Assign "embryo" to topic 3
Doc label	$D(i, j) \wedge \text{HasLabel}(j, +) \Rightarrow \neg Z(i, 3)$	Do not use topic 3 in docs with label +
Cannot-link	$W(i, neural) \wedge W(j, disorder) \Rightarrow \neg Z(i, t) \vee \neg Z(j, t)$	Do not assign "neural" and "disorder" to the same topic
Must-link	$W(i, neural) \wedge W(j, cortex) \Rightarrow \neg Z(i, t) \vee Z(j, t)$	Assign "neural" and "cortex" to the same topic
Bigram (1)	$W(i, stem) \wedge W(i+1, cell) \Rightarrow Z(i, 1)$	Assign "stem" in "stem cell" to topic 1
Bigram (2)	$W(i-1, stem) \wedge W(i, cell) \Rightarrow Z(i, 1)$	Assign "cell" in "stem cell" to topic 1
Sent Incl	$\text{Sentence}(i, i_1, \dots) \wedge \neg Z(i_1, 6) \wedge \dots \Rightarrow \neg Z(i, 0)$	Topic 6 is required for topic 0 to occur in the same sentence
Sent Excl	$S(i, s) \wedge S(j, s) \wedge Z(i, 7) \Rightarrow \neg Z(j, 0)$	Topic 7 prevents topic 0 from occurring in the same sentence

## The Model

### First-Order Logic latent Dirichlet ALlocation(Fold-all)

#### Latent Dirichlet Allocation (LDA)

Topic-word	$\phi_z(w) = P(w z)$
Doc weights	$\theta_d(z) = P(z d)$
Topic assign	$\mathbf{z} = z_1 \dots z_N$



#### Side Information and Logic Factor (MLN)

Rule	$\psi_\ell$
Weight	$\lambda_\ell$
Groundings	$G(\psi_\ell)$
Indicator	$\delta_g(\mathbf{z}, \mathbf{w}, \mathbf{d}, \mathbf{o})$

The user encodes domain knowledge into a knowledge base (KB) of weighted logic rules. As in Markov Logic Networks (MLNs) [2], these rules are then grounded, and each grounding is associated with a potential function. The learned topics will then reflect both the document-word statistics (as in LDA) and the user-defined rules (as in MLNs). This model can be considered an instance of a Hybrid MLN [3], specialized for topic modeling.

## Biological Concept Expansion (Human Development Genes)

A biological expert is interested in expanding a set of seed terms related to human developmental biology. The table below shows blind relevance accuracy judgments on the Top 50 recovered words for both standard LDA and several different KBs. Exploiting expert knowledge and sentence annotations (FULL-KB) leads to improved results.

**Given** neuro dendro(cy)te, glia, synapse, neural crest

**LDA** disease, disorders, schizophrenia, syndrome, abnormal

**SEED** myelin, astrocytes, oligodendrocytes

**FULL KB** dendritic, forebrain, hindbrain, microglial, motoneurons, neuroblasts, neurogenesis, retinal

	KBs				
	FULL-KB	INCL	EXCL	SEED	LDA
Neural	0.59	0.57	0.54	0.54	0.31
Embryo	0.24	0.24	0.23	0.23	0.07
Blood	0.46	0.47	0.40	0.39	0.13
Gast.	0.18	0.18	0.16	0.16	0.00
Cardiac	0.36	0.37	0.34	0.35	0.08
Limb	0.18	0.18	0.15	0.14	0.09

## References

- [1] Blei, D. M., Ng, A. Y., and Jordan, M. I. (2003). Latent Dirichlet Allocation. *Journal of Machine Learning Research (JMLR)* 3 (Mar. 2003), 993-1022.
- [2] Domingos, P. and Lowd, D. (2009). *Markov Logic: An Interface Layer for Artificial Intelligence*. Synthesis Lectures on Artificial Intelligence and Machine Learning, Morgan and Claypool Publishers.
- [3] Wang, J. and Domingos, P. (2008) Hybrid Markov Logic Networks. *Proceedings of the Twenty-Third AAAI Conference on Artificial Intelligence*, 1106-1111. AAAI Press.

## Acknowledgments

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## Source Code

<https://github.com/davidandrzej/LogicLDA>

