

CS367 Announcements

Thurs, July 24th, 2013

- H6 due Mon 6pm
- P3 due Wed July, 31st 11:59pm

Last Time

- Priority Queues
- Heaps

Today

- Heaps (cont.)

Heaps

Heap is a complete binary tree with the ordering constraint that for each node N , the value in N is larger than (or equal to) any of the values in N 's subtrees

A heap as an array of values:

- root is at $A[1]$
- for each "node" $A[i]$
 - parent is at $A[i/2]$
 - left child is at $A[2i]$
 - right child is at $A[2i+1]$

Example: given the following heap (represented as an array):

| | | | | | | | | | | | | |
|--|----|----|----|----|----|----|----|----|----|----|--|--|
| | 64 | 52 | 35 | 46 | 17 | 15 | 34 | 12 | 23 | 14 | | |
|--|----|----|----|----|----|----|----|----|----|----|--|--|

What does it look like as a binary tree?

Inserting into a Heap

Practice:

initial heap:

| | | | | | | | | | | | | |
|--|----|----|----|----|----|----|----|----|----|----|--|--|
| | 64 | 52 | 35 | 46 | 17 | 15 | 34 | 12 | 23 | 14 | | |
|--|----|----|----|----|----|----|----|----|----|----|--|--|

Show the heap after adding 36 and 57:

| | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|

Inserting into a Heap (cont.)

Heap class data members:

```
private Comparable[] items;  
private int nextLoc;
```

Pseudo-code:

```
private void insert(Comparable data) {
```

Removing from a Heap

Practice:

Heap after adding 36 and 57:

| | | | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|

What will the heap look like after doing 2 remove operations?

| | | | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|

Heap Complexity

Is a heap *value*-oriented or *position*-oriented?

Complexities:

isEmpty

getMax

insert

removeMax

Using a Heap for Sorting: