## BUBBLE SORT

CS302 - Introduction to Programming
University of Wisconsin - Madison
Lecture 12

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## Bubble Sort

- The idea of bubble sort is that we iterate through our array repeatedly. For each iteration, every time we see a pair of elements that are out of order (i.e. $a_{2}$ precedes $a_{1}$ when $a_{1}<a_{2}$ ), then we swap the two elements. If we ever iterate through the array and we never have to swap, this means that the array is in order and we can terminate the algorithm.

Suppose we have the following array:

$$
\begin{array}{llllll}
2 & 6 & 4 & 3 & 1 & 5
\end{array}
$$

## 1st Iteration

$i$.

$$
\begin{array}{llllll}
2 & 6 & 4 & 3 & 1 & 5
\end{array}
$$

Look at this pair of elements.
Are the two elements in order?
Yes. Because 2 precedes 6.
So we do not swap them
iii.


Look at this pair of elements. Are the two elements in order?
No. Because 6 precedes 3.
So we DO swap them.


Look at this pair of elements. Are the two elements in order?
No. Because 6 precedes 4.
So we DO swap them.


Look at this pair of elements. Are the two elements in order?
No. Because 6 precedes 1.
So we DO swap them.

## $1^{\text {st }}$ Iteration Continued

v. $\quad$|  | 4 | 3 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- |

Look at this pair of elements.
Are the two elements in order?
No. Because 6 precedes 5.
So we DO swap them
vi.
$\begin{array}{llllll}2 & 4 & 3 & 1 & 5 & 6\end{array}$

This is the array we are left with after the first iteration. Now we ask ourselves: During this iteration, did we perform any swaps?

Answer:
Yes, we performed many
swaps. This means we go on
to the next iteration

## $2^{\text {nd }}$ Iteration

$i$.


Look at this pair of elements. Are the two elements in order? Yes. We don't swap them.
iii.


Look at this pair of elements. Are the two elements in order?
No. So we swap them.
ii.


Look at this pair of elements. Are the two elements in order? No.. So we swap them.
iv.


Look at this pair of elements. Are the two elements in order?
Yes. We don't swap them.

## 2nd Iteration Continued



Look at this pair of elements.
Are the two elements in order?
Yes. We don't swap them.
vi.
$\begin{array}{llllll}2 & 3 & 1 & 4 & 5 & 6\end{array}$

This is the array we are left with after the second iteration.

Did we perform any swaps during this iteration?

Yes, so we go on to another iteration.

## $3^{\text {rd }}$ Iteration

i. $2 \begin{array}{llllll} & 3 & 1 & 4 & 5 & 6\end{array}$
$4^{\text {th }}$ Iteration
i. $\quad \begin{array}{llllll}2 & \mathbf{1} & 3 & 4 & 5 & 6 \\ \leftarrow & & & & \text { Swap } 2 \text { and } 1\end{array}$
ii. $\begin{array}{llllll}1 & 2 & 3 & 4 & 5 & 6\end{array}$

ii. | 2 | 3 | $\begin{array}{llll}1 & 4 & 5 & 6\end{array}$ |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |

iii. $2 \begin{array}{llllll} & 1 & 3 & 4 & 5 & 6\end{array}$
iv. $2 \begin{array}{llllll} & 1 & 3 & 4 & 5 & 6\end{array}$

v. 21 |  |  |
| :--- | :--- | :--- | :--- | :--- |

vi. $2 \begin{array}{llllll} & 1 & 3 & 4 & 5 & 6\end{array}$
iv. $1 \begin{array}{llllll} & 2 & 3 & 4 & 5\end{array}$
v. 1223456
vi. $1 \begin{array}{llllll} & 2 & 3 & 4 & 5 & 6\end{array}$

## $5^{\text {th }}$ Iteration

i. $\begin{array}{llllll}1 & 2 & 3 & 4 & 5 & 6\end{array}$
ii. $\begin{array}{llllll}1 & 2 & 3 & 4 & 5 & 6\end{array}$

During the $5^{\text {th }}$ iteration, we performed no swaps
iii. $1 \begin{array}{llllll} & 2 & 3 & 4 & 5 & 6\end{array}$
iv. $\begin{array}{lllllll} & 2 & 3 & 4 & 5 & 6\end{array}$ So the algorithm terminates. We're finished and we see that the array is now ordered.
v. $1 \begin{array}{llllll} & 3 & 4 & 6\end{array}$
vi. $1 \begin{array}{llllll} & 2 & 3 & 4 & 5 & 6\end{array}$

## Pseudocode for Bubble Sort

procedure bubbleSort( A : list of sortable items )

```
repeat
    swapped = false
    for i = 1 to length(A) - }1\mathrm{ inclusive do:
        if A[i-1] > A[i] then
        swap(A[i-1], A[i] )
        swapped = true
    end if
    end for
    until not swapped
```

end procedure

## Cool CS Link of the Day

- Website for Android Development
- http://developer.android.com/index.html


