

Taking CIE Out of the Lab

An Adaptive Color Difference Model

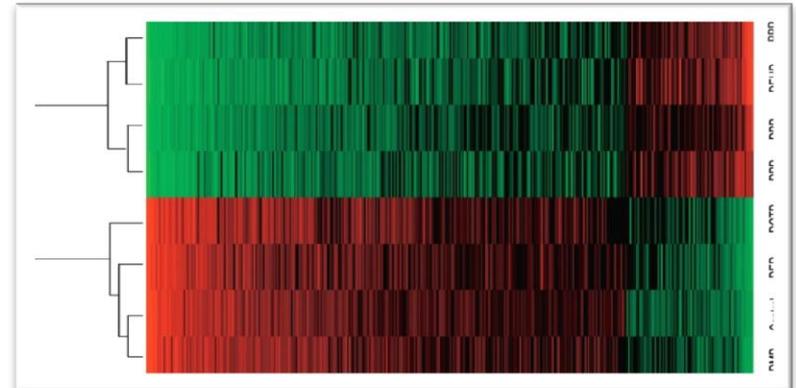
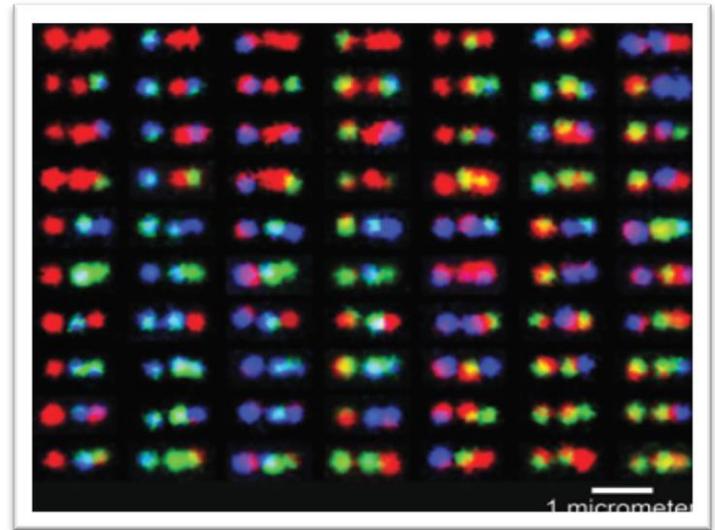
Danielle Albers and Michael Gleicher
University of Wisconsin-Madison
Department of Computer Sciences
SIGGRAPH Submission 2013



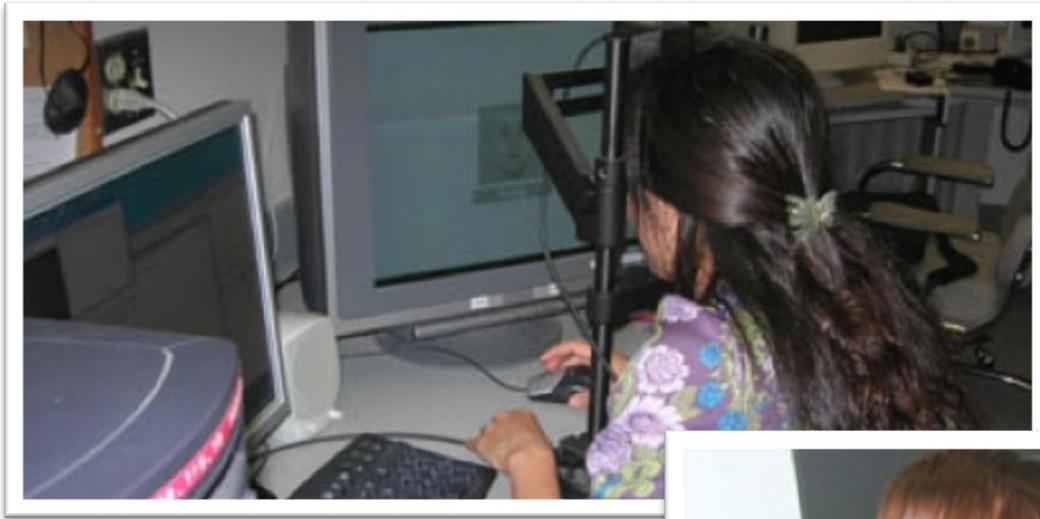
*University of Wisconsin, Madison
Computer Graphics*



Motivation



Motivation

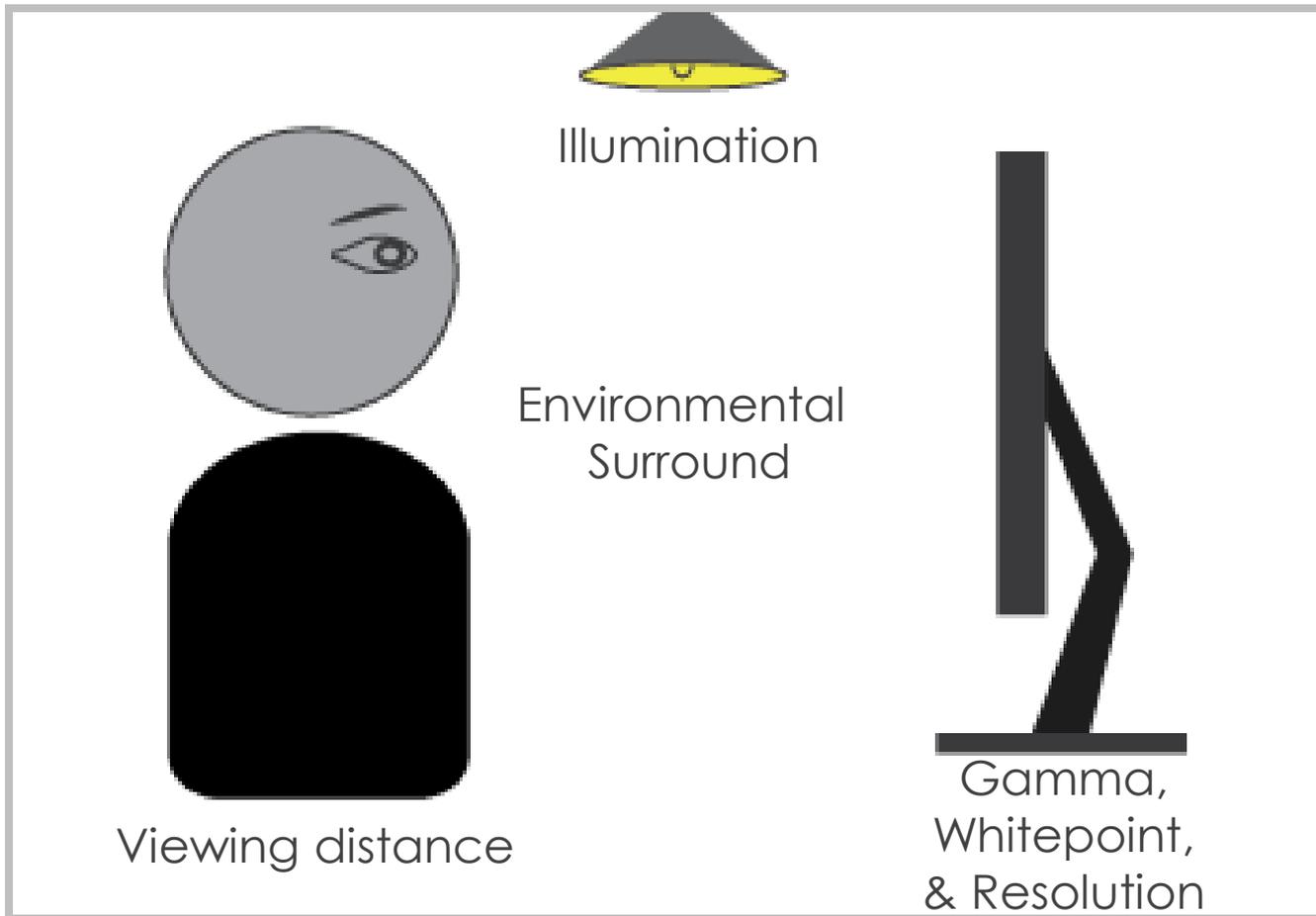


Motivation



Motivation

Apparent color depends on viewing conditions.



Make informed decisions
about color that hold across a
variety of viewing conditions.

Our Target Model Is:

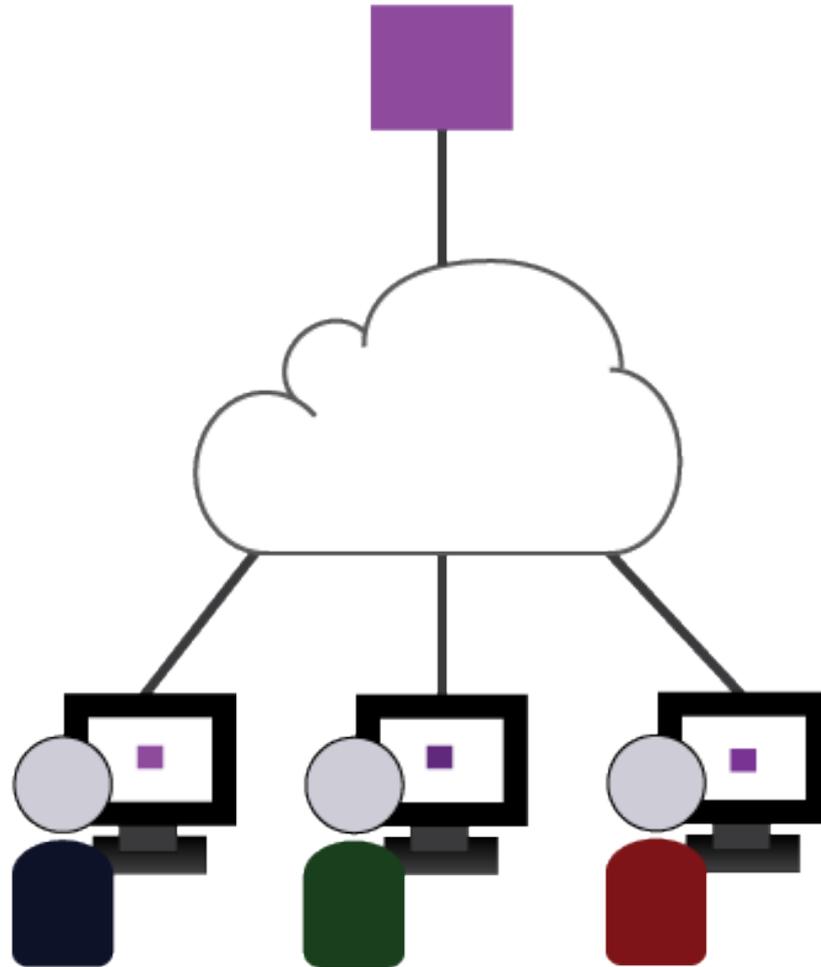
Parametric – Tuned to a range of viewers

Data-Driven – Adaptable to specific conditions

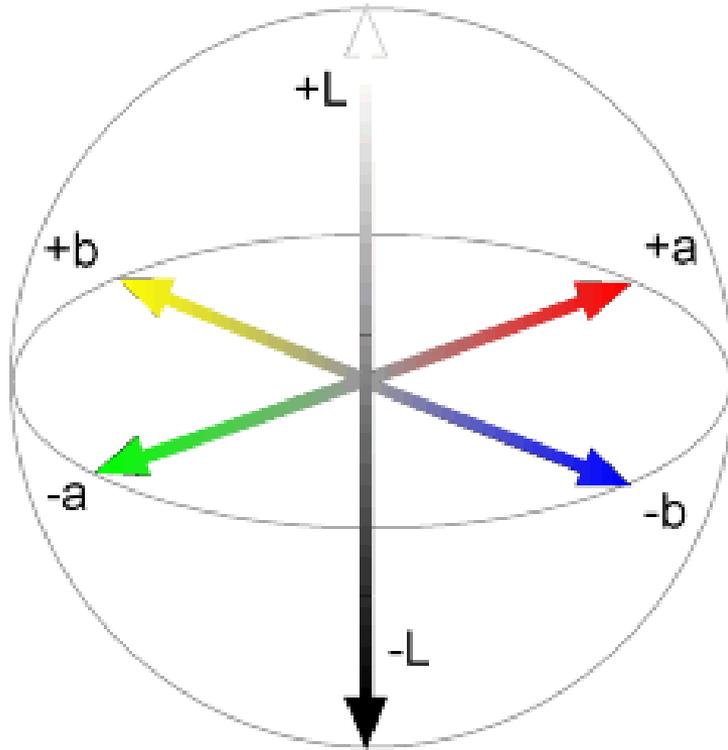
Practical – Straight-forward to use and generate

Probabilistic – Accounts for uncertainty in the data

Model Problem – Web Viewing



Theoretical CIELab Color Space

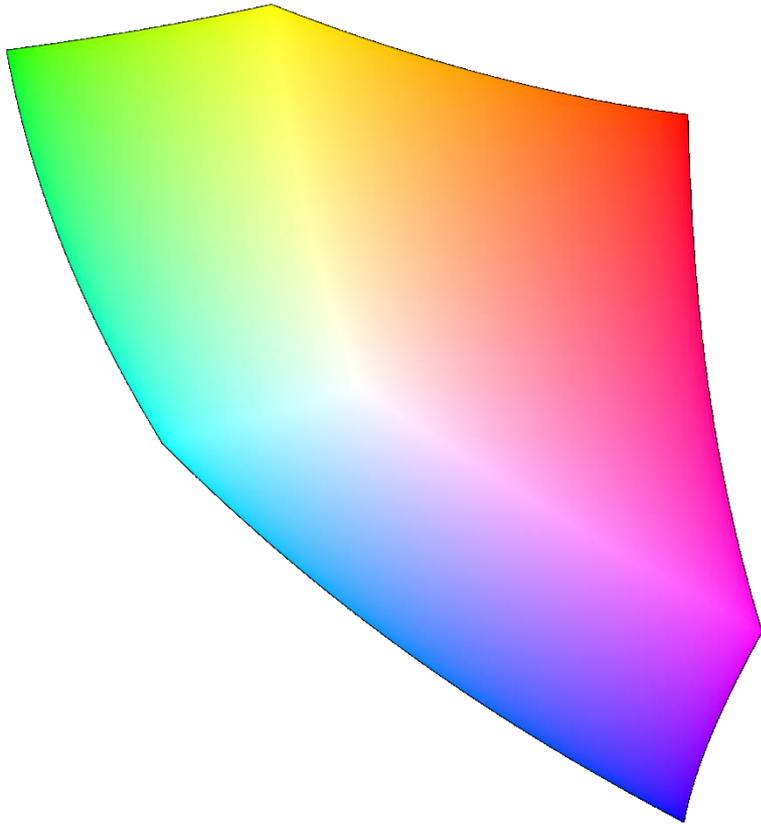


Perceptually-based color difference space

Approximately perceptual uniform

1 JND = 1 unit Euclidean distance

Practical CIELab Color Space



Bound by monitor
gamut and whitepoint

Over-extended along
yellow-blue

**1 JND = ~2.3 units
Euclidean distance**

CIELab Difference Model

$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

$$C_1 = (L_1, a_1, b_1)$$

$$C_2 = (L_2, a_2, b_2)$$

Adapted CIE Lab Difference Model

$$\Delta C = \sqrt{\left(\frac{L_1 - L_2}{s_L}\right)^2 + \left(\frac{a_1 - a_2}{s_a}\right)^2 + \left(\frac{b_1 - b_2}{s_b}\right)^2}$$

$$C_1 = (L_1, a_1, b_1)$$

$$C_2 = (L_2, a_2, b_2)$$

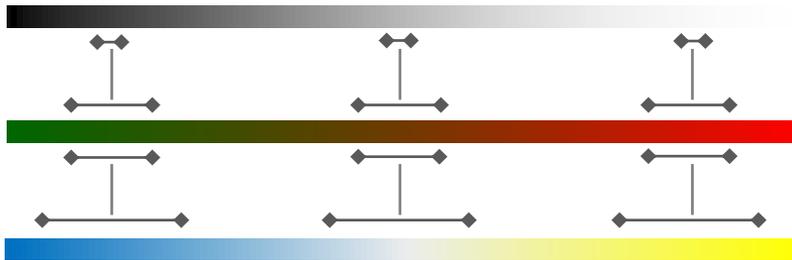
$\Delta C = 1$ is detectable for p% of viewers

$$s_x \in \mathbf{R}^1$$

Do CIE Lab's theoretical
assertions about color hold across
the target viewing conditions?

Color Space Assumptions

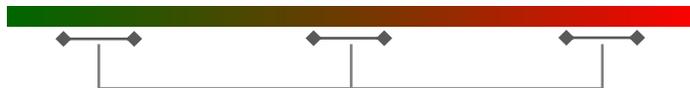
A1: Axes are perceptually orthogonal.



A2: Euclidean distance is an effective metric for perceptual distance.

$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

A3: Axes are perceptually uniform.

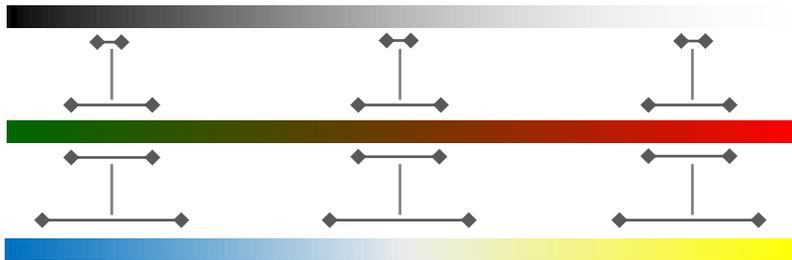


A4: Axes are scaled such that one unit corresponds to one JND.



Color Space Assumptions

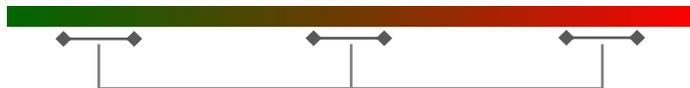
A1: Axes are perceptually orthogonal.



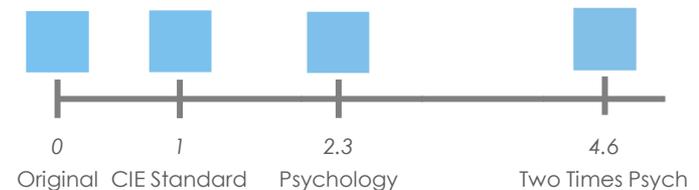
A2: Euclidean distance is an effective metric for perceptual distance.

$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

A3: Axes are perceptually uniform.

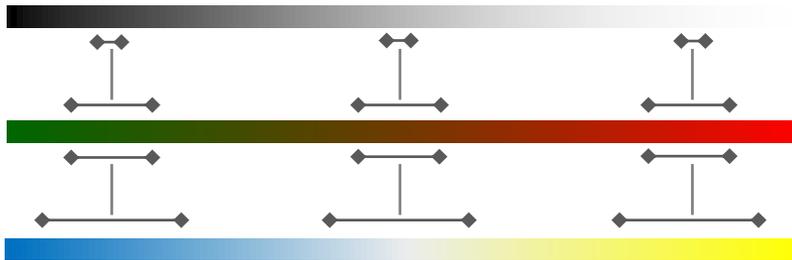


A4: Axes are scaled such that one unit corresponds to one JND.



Color Space Assumptions

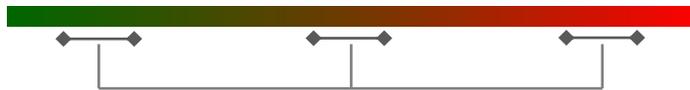
A1: Axes are perceptually orthogonal.



A2: Euclidean distance is an effective metric for perceptual distance.

$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

A3: Axes are perceptually uniform.

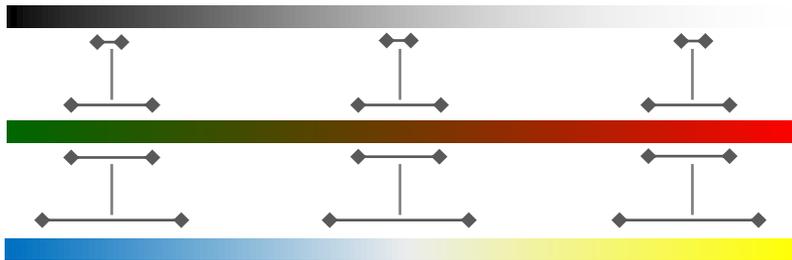


A4: Axes are scaled such that one unit corresponds to one JND.

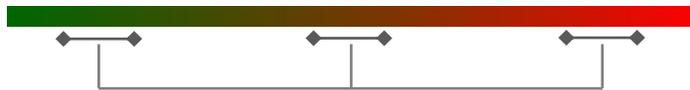


Color Space Assumptions

A1: Axes are perceptually orthogonal.



A3: Axes are perceptually uniform.



A2: Euclidean distance is an effective metric for perceptual distance.

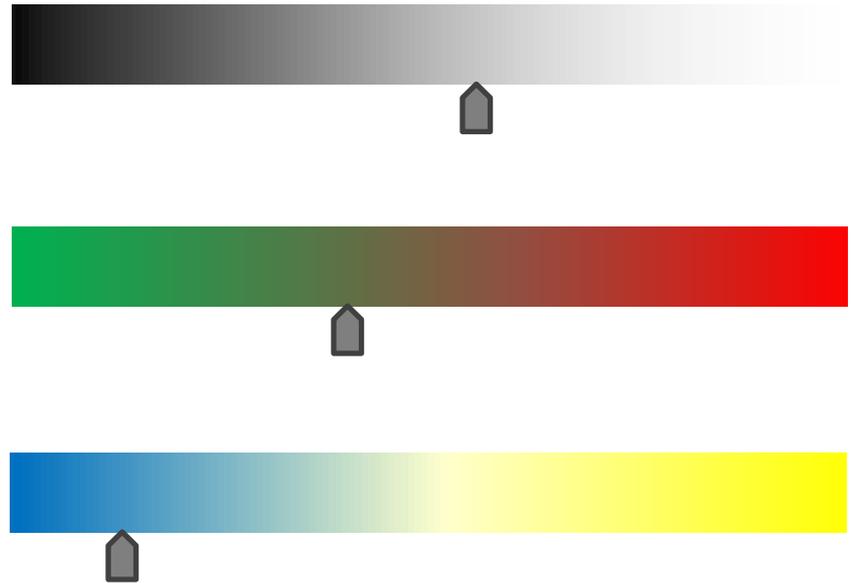
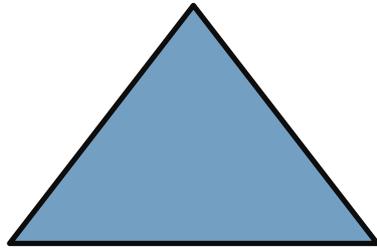
$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

A4: Axes are scaled such that one unit corresponds to one JND.



Validating Color Space

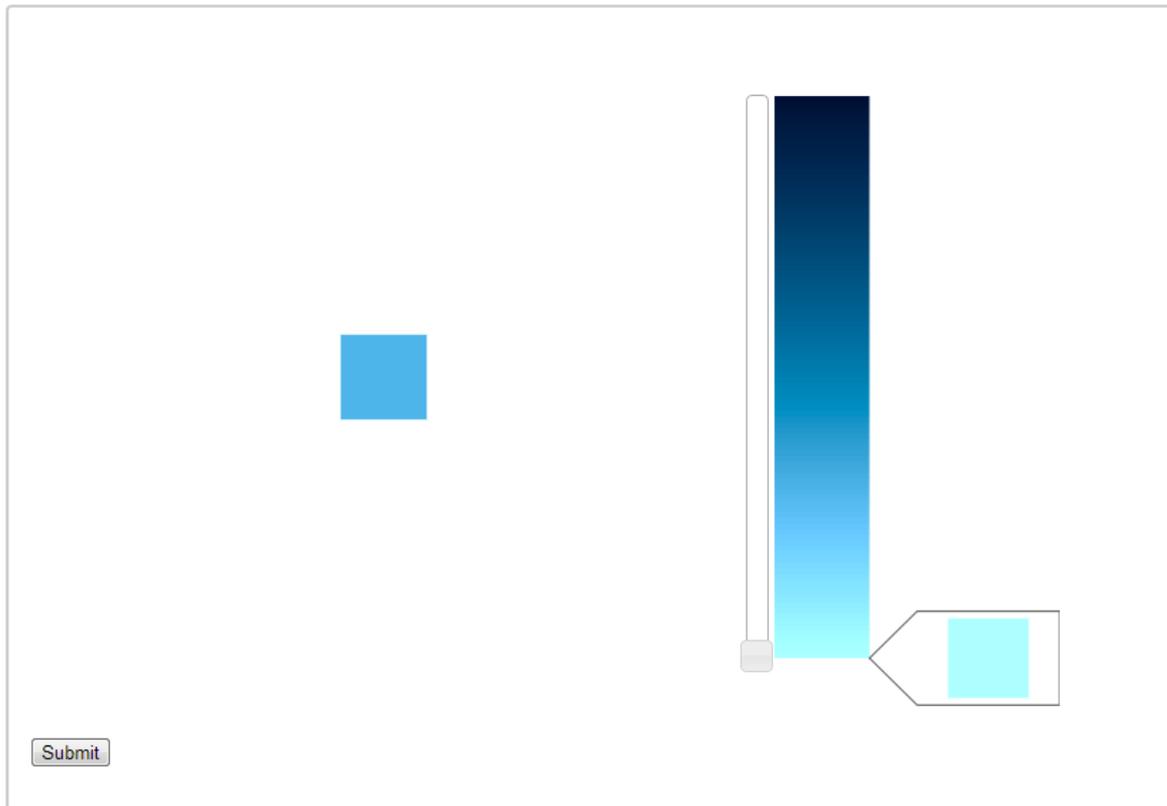
Given:



Modern Maxwell Color Matching Experiment

Validating Color Space

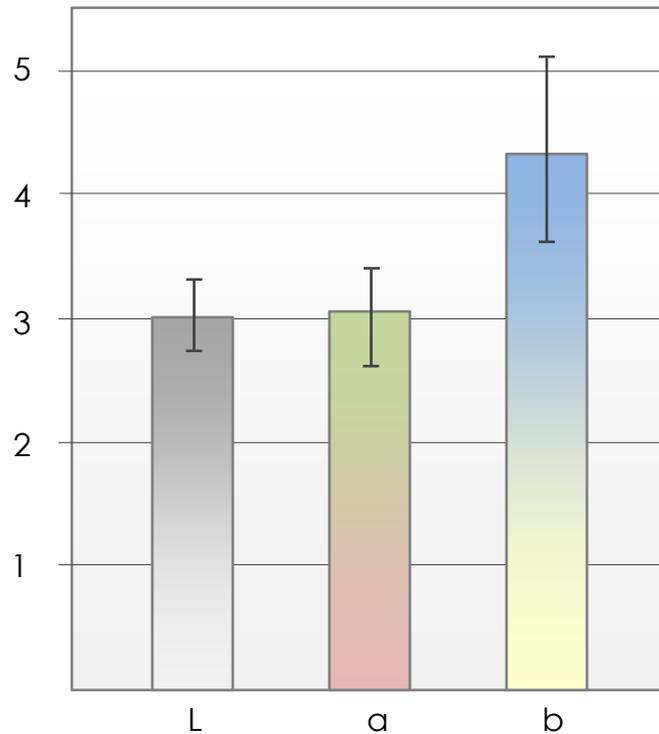
Determine color error using a single-axis Maxwell task on Mechanical Turk.



Validating Color Space – Web Viewing

A4:

Per-Axis Color Matching Error



A3:

Within Axis Color Matching Error

L Axis:

$$\mu = 3.025$$

$$\text{within: } p = 0.2008, F = 1.6437$$

insert gradient from both ends of the axis

a Axis:

$$\mu = 3.44$$

$$\text{within: } p = 0.5711, F = 0.3215$$

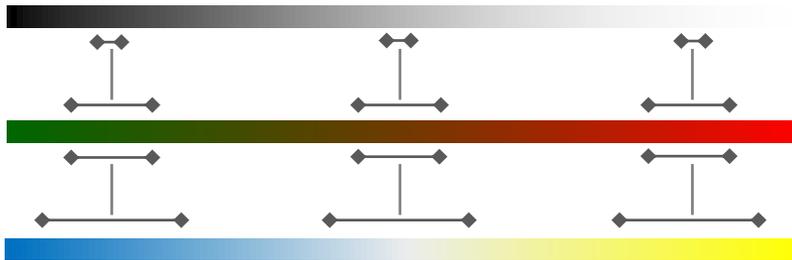
b Axis:

$$\mu = 4.327$$

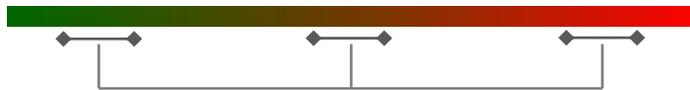
$$\text{within: } p = 0.5154, F = 0.4240$$

Color Space Assumptions

A1: Axes are perceptually orthogonal.



A3: Axes are perceptually uniform.



A2: Euclidean distance is an effective metric for perceptual distance.

$$\Delta C = \sqrt{(L_1 - L_2)^2 + (a_1 - a_2)^2 + (b_1 - b_2)^2}$$

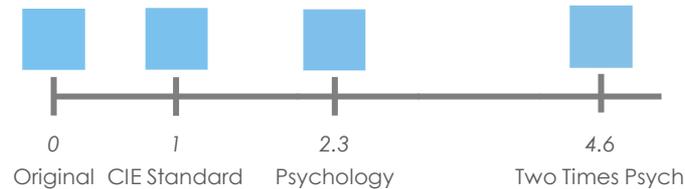
A4: Axes are scaled such that one unit corresponds to one JND.



Parameters account for how
different must two colors be to
appear different across a
variety of viewing conditions.

Adapted CIELab Difference Model

A4: Axes are scaled such that one unit corresponds to one JND.



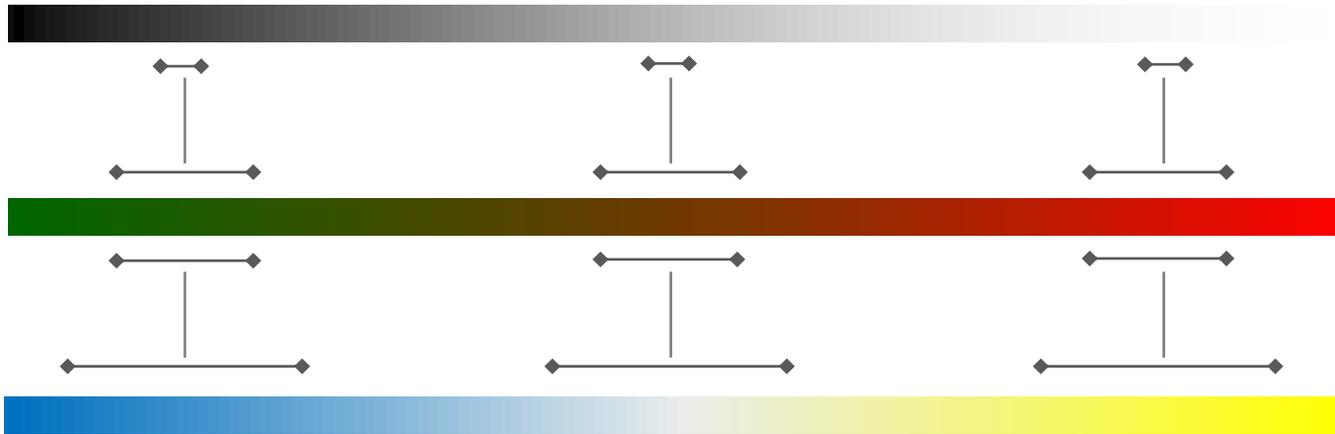
$$\Delta C = \sqrt{\left(\frac{L_1 - L_2}{s_L}\right)^2 + \left(\frac{a_1 - a_2}{s_a}\right)^2 + \left(\frac{b_1 - b_2}{s_b}\right)^2}$$

$\Delta C = 1$ is detectable for p% of viewers

$$s_x \in \mathbf{R}^1$$

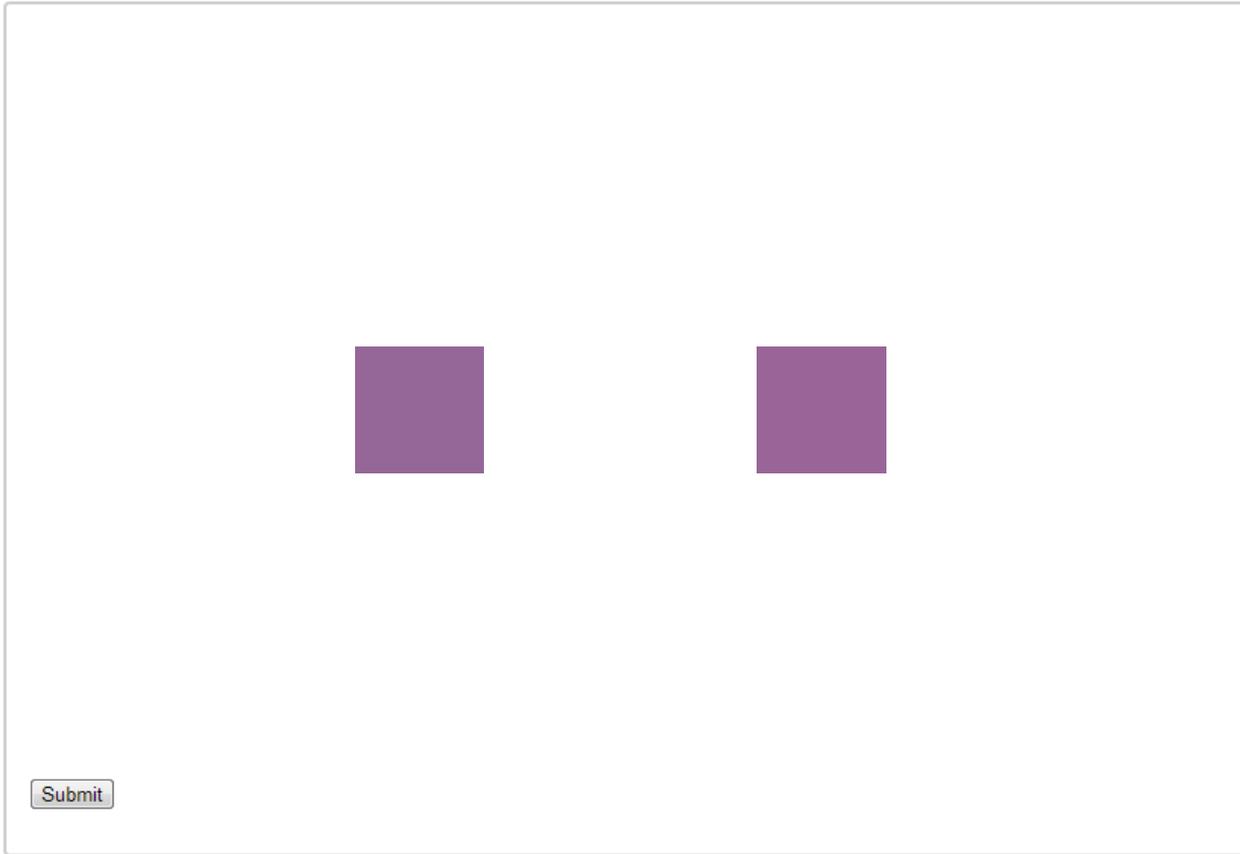
Adapting the Model

How do we scale each axis?



Adapting the Model

Do these two colors match?

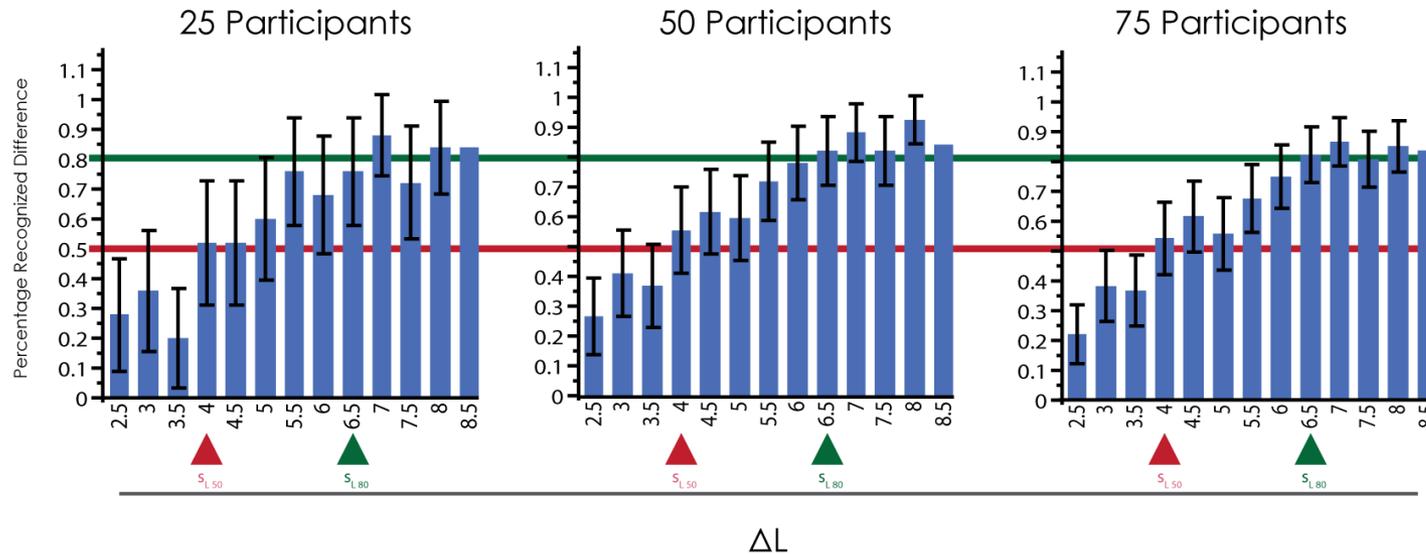


Adapting the Model

$$D = \text{[purple square]} - \text{[purple square]}$$

- 1) Determine the **proportion of samples** where colors were accurately identified as different.
- 2) Fit a function to these proportions to identify the **discriminability distribution**.*
- 3) Identify the point at which this function equals some **threshold p** .

Adapting the Model – Web Viewing



50% of samples are discriminable:

$$s_L = 4.0$$

$$s_a = 5.5$$

$$s_b = 6.0$$

80% of samples are discriminable:

$$s_L = 6.5$$

$$s_a = 8.5$$

$$s_b = 9.0$$

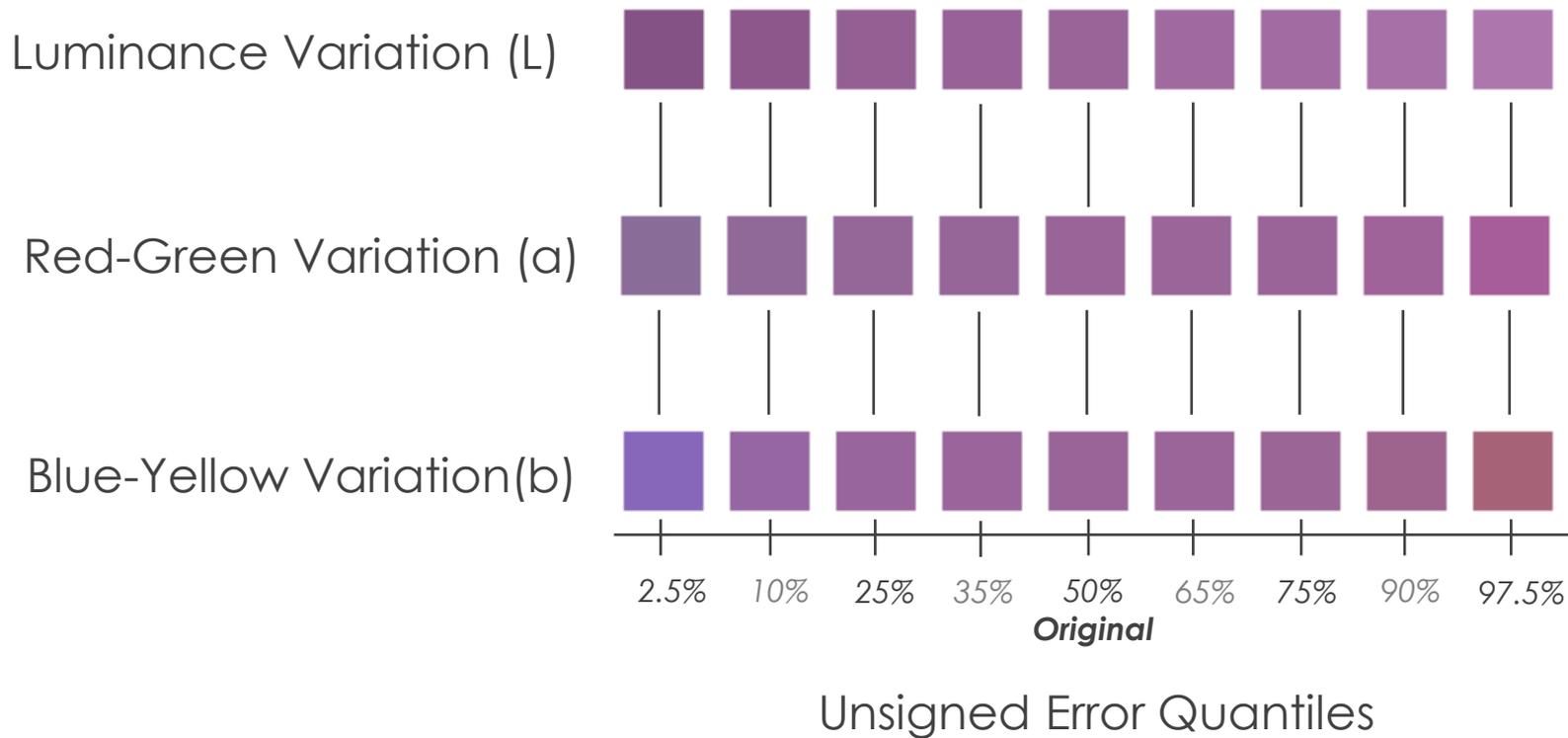
Does our adapted color
difference model work for
web viewing conditions?

Validating the Model – Web Viewing

$$\Delta C = \sqrt{\left(\frac{L_1 - L_2}{4.0}\right)^2 + \left(\frac{a_1 - a_2}{5.5}\right)^2 + \left(\frac{b_1 - b_2}{6.0}\right)^2}$$

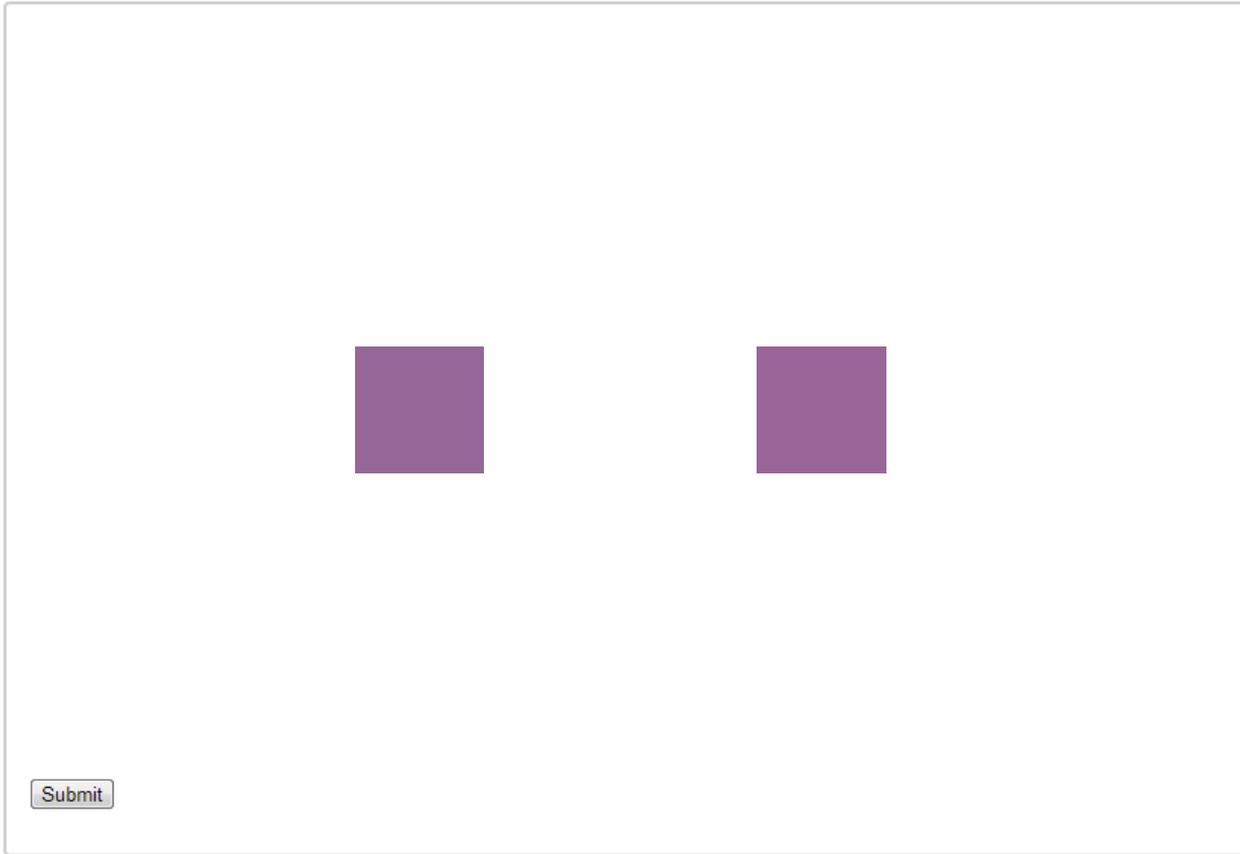
$$\Delta C = \sqrt{\left(\frac{L_1 - L_2}{6.5}\right)^2 + \left(\frac{a_1 - a_2}{8.5}\right)^2 + \left(\frac{b_1 - b_2}{9.0}\right)^2}$$

Validating the Model – Web Viewing



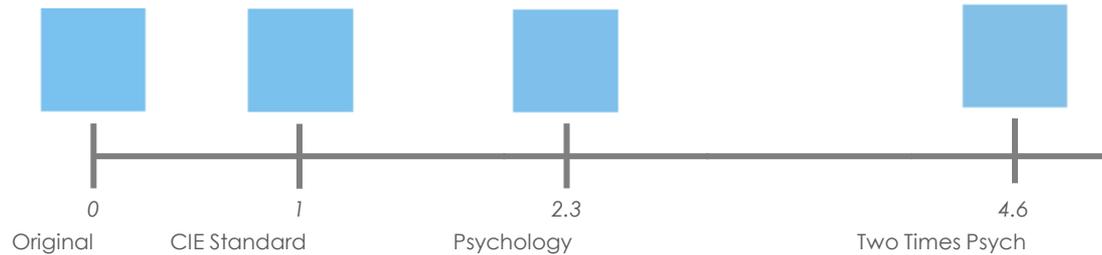
Validating the Model – Web Viewing

Do these two colors match?



Validating the Model – Web Viewing

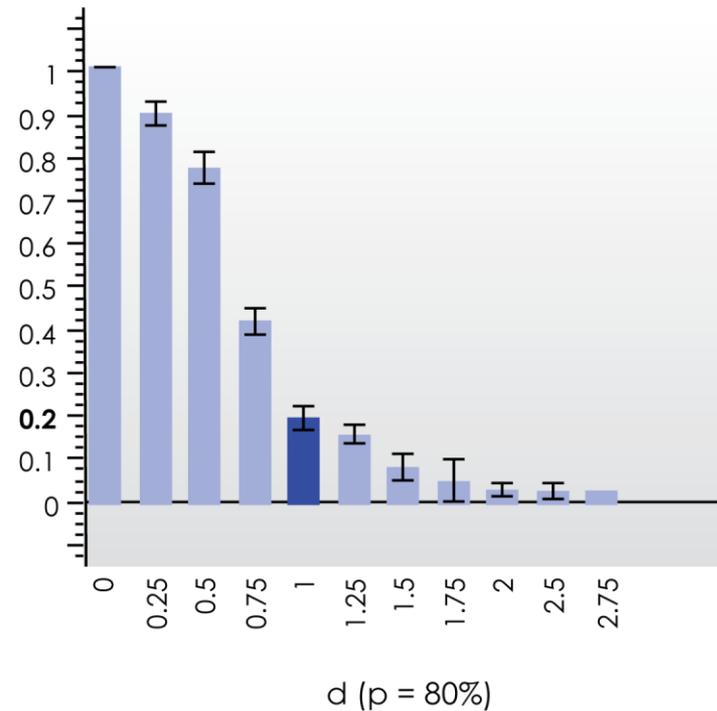
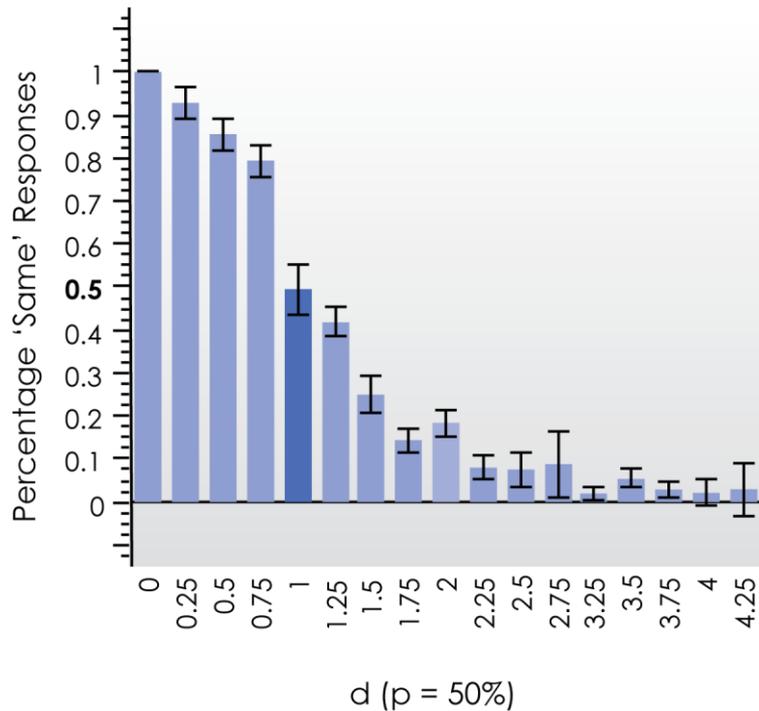
A4: Axes are **scaled** such that one unit corresponds to one JND.



***p%** of viewers will identify a difference at $d = 1$*

Validating the Model – Web Viewing

Percentage Similarity for a Web-Adapted Color Difference Model at Multiple Parameter Scales



Contributions

Taking CIE **out of the Lab**

Model is **parametric, data driven, probabilistic,**
and **practical**

Validation color space for **web-viewed** color

Limitations

Data-driven implies data-based

Limited validation to date

Thank you!

Danielle Albers (dalbers@cs.wisc.edu)



graphics.cs.wisc.edu

Where should we send this?