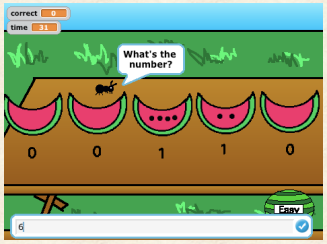
Announcements

- Vote for Homework 8 (Trivia Games) by NOON today
- Homeworks 9 and 10 NOW Available
  - HW 9 Due before Thanksgiving
  - HW 10 Due after Thanksgiving
  - No programming for HW 9 or 10
  - Final Project will be to use Scratch to prototype some design
- Exam 2 graded and returned by Monday
- No lecture Wednesday before Thanksgiving

UNIVERSITY of WISCONSIN-MADISON
Computer Sciences Department

CS 202: Introduction to Computation — Professor Andrea Arpaci-Dusseau

How does a computer… represent information and data?



Theme 3: How do computers…

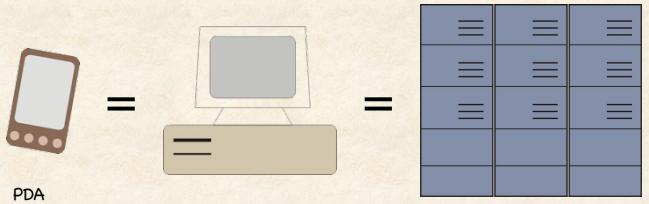
… Represent data and information?
… Represent numbers, words, pictures, and movies?
… Act so logically?

… Manipulate and remember data?
… Execute instructions?
… Access data quickly?

… Run multiple programs simultaneously?
… Store data permanently?
… Send messages?

Big Idea: Universal Computing Device

All computers (given enough time and storage) are capable of computing exactly the same things



PDA = Workstation = Supercomputer or Server Farm

From Theory to Practice

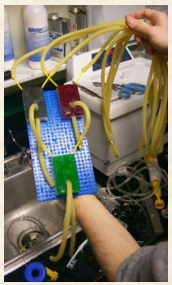
Theory: Computer can *compute* anything that's possible to compute (given enough time and storage)

Practice: S*olving problems* involves computing under constraints

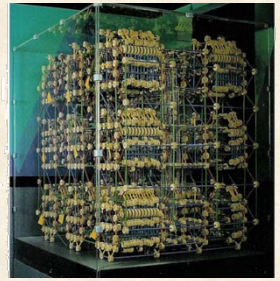
- Time
  - weather forecast, next frame of animation, ...
- Cost
  - cell phone, automotive engine controller, ...
- Power
  - cell phone, handheld video game, ...

Can Compute with Different Technologies

Flowing Water



Moving Tinkertoys



Bacteria with modified DNA

Big Idea: Abstractions Hide Complexity

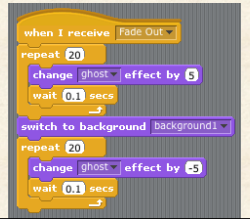
Abstractions in Software:

Sprite wants Stage to "Fade Out"

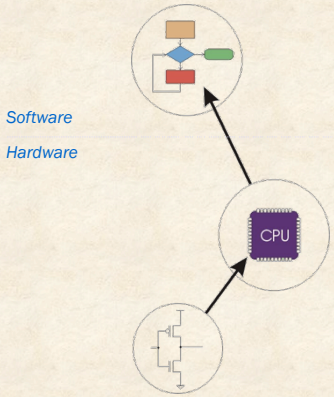
- Doesn't know how Stage does this

Stage implements abstraction

- Script runs when recv "Fade Out" message
- Can change details later and caller never knows!



Big Idea: Abstractions Hide Complexity



Problem to be Solved

Algorithms

Application Program

Instruction Set Architecture (and I/O Interfaces)

Microarchitecture

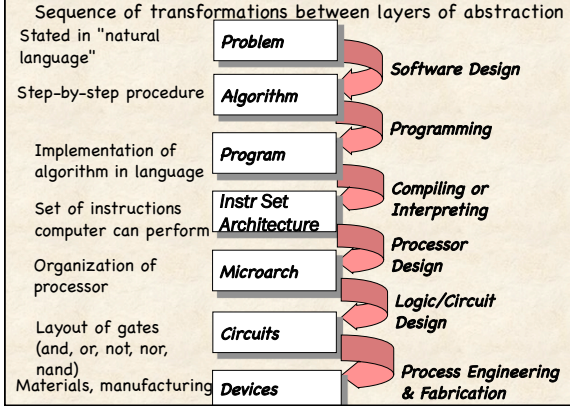
Circuits

Devices

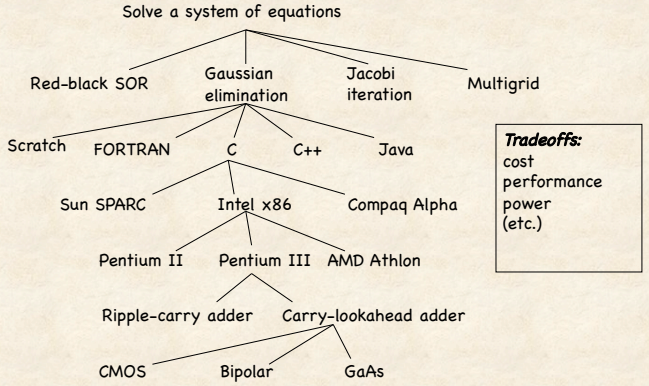
Abstractions Hide Complexity

How do we solve a problem using a computer?

Sequence of transformations between layers of abstraction



Example: Many Choices at Each Level



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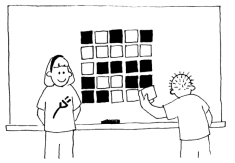
Magic Trick

Students place cards with 2 values on board in 5x5 grid



Instructor observes

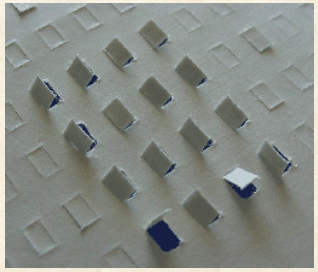
Student switches one card to other value (Instructor does not look)

Instructor magically identifies switched card!

Representing Data

Recognize this photo?

Was a vote cast or not?



Modern Computers = Binary Digital Systems

Digital system (not analog)
- finite number of symbols

Binary (base two) system:
- has two states: 0 and 1

Basic unit of information is *binary digit*, or *bit*
- Can be represented in any technology with two states


1


1


1


1

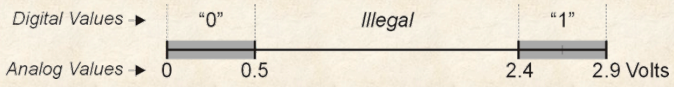

1

How do computers... Represent data?

Lowest level: modern computer = electronic machine
- Works by controlling the flow of electrons

Easy to recognize two conditions:
- presence of voltage – state "1"
- absence of voltage - state "0

More difficult to detect and control analog values



Bits in Computers

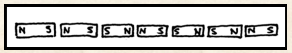
Transistors and wires: electrons flowing or not?

Capacitors and memory: holding a charge or not?

Optical CD-ROMs and DVDs: Reflecting or not?

01011010110100101O

Hard disk drive: Magnetized north or south?



0010110

How Can Bits represent Data?

Everything in computer is represented with 1 and 0

- All text you see or type, movies you watch, music you listen to
- Everything stored on disk, CD, or flash drive
- Everything you send between computers
  - Email, web pages
- Even instructions computer uses to run programs

What kinds of data must bits represent?

Logical: True, False

- Straight-forward: Two states
- True: 1, False: 0

Numbers

- Signed, unsigned, integers, floating point, complex, rational, irrational, …

Text

- Characters, words, strings, …

Images

- Pixels, colors, shapes, movies …

Sound

Instructions

Unsigned Integers

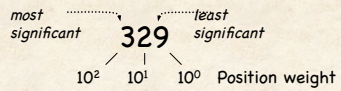
Approach 1: Non-positional notation

- Represent a number ("5") w/ string of ones ("11111")
- Problems?

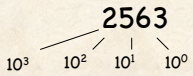
Unsigned Integers: Weighted Positional Notation

- Position and base determines value of symbol
- Example: Decimal numbers (base-ten)
  - Base-ten implies digit can be one of 10 different symbols: 0, 1, 2, 3, 4, 5, 6, 7, 8 and 9

Base-10



$3x100 + 2x10 + 9x1 = 329$



$2x1000 + 5x100 + 6x10 + 3x1 = 2563$

Unsigned Integers: Weighted Positional Notation

- Same properties hold for binary numbers (base-two)
- Base-two: Each digit holds two different symbols: 0 or 1

Base-10

329

10^2 10^1 10^0

3x100 + 2x10 + 9x1 = 329

Base-2

most significant 101 *least significant*

2^2 2^1 2^0

1x4 + 0x2 + 1x1 = 5 (decimal)

2563

10^3 10^2 10^1 10^0

2x1000+ 5x100 + 6x10 + 3x1 = 2563

most significant 1011 *least significant*

2^3 2^2 2^1 2^0

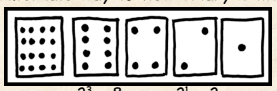
1x8 + 0x4 + 1x2 + 1x1 = 11 decimal

Handout

Count in binary from 0 to 7

Decimal #	Bit 2	Bit 1	Bit 0
0			
1			
2			
3			
4			
5			
6			
7			

Alternate way to view binary numbers



$2^4 = 16$ $2^3 = 8$ $2^2 = 4$ $2^1 = 2$ $2^0 = 1$

Convert to decimal:	Convert to binary:
00011	2
00101	6
10000	9
01011	19
01111	10

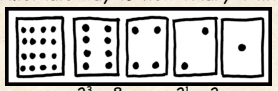
Counting in Binary

Binary	Decimal
000	0
001	1
010	2
011	3
100	4
101	5
110	6
111	7

What do you notice about bits in binary number?

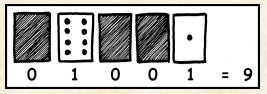
Converting Binary to Decimal

Alternate way to view binary numbers



$2^4 = 16$ $2^3 = 8$ $2^2 = 4$ $2^1 = 2$ $2^0 = 1$

What would 01001 be in decimal?



00011?

2 + 1 = 3

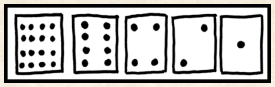
10001?

16 + 1 = 17

11111?

16 + 8 + 4 + 2 + 1 = 31 (also, 32 – 1)

Converting Decimal to Binary



How would you make decimal 5 in binary?
4 + 1 → 00101

16?
16 → 10000

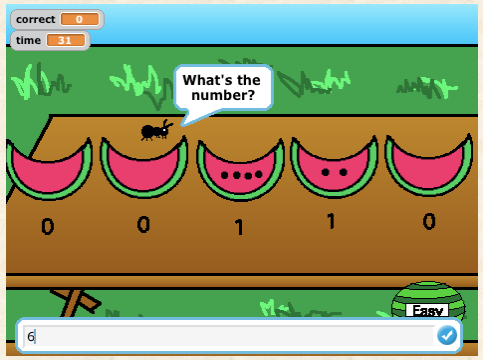
21?
16 + 4 + 1 → 10101

How many different numbers can you make with 5 cards?
$2 * 2 * 2 * 2 * 2 = 2^5 = 32$

What is the largest number you can make with 5 cards?
$2^5-1 = 31$

What is the largest number you can make with N cards?
2^N-1

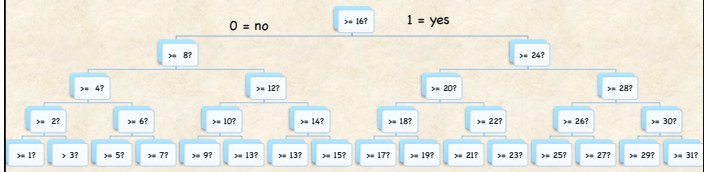
Practice Available with Scratch Game



Decision Tree for 0..31

How many questions needed to find answer between 0 and 31 (32 numbers)?

If 0 represents "no" or "false" and 1 represents "yes" or "true" what do you notice about the answers?



What is the height of this tree? (i.e. how many questions?)
5 questions for 32 numbers; $\log_2(32) = 5$

How many bits are needed to represent number between 0..31?
5 bits

Other Useful Units

Bytes

- Collection of 8 bits: 1101 0011
- How many different values represented in a byte?
  - $2^8 = 256$ values
- Abbreviation: Use B for Bytes vs. b for bits

Hexadecimal numbers

- Base-16
- Why might hexadecimal numbers be useful?
  - Two hex digits per byte
- What characters should we use?
  - 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, a, b, c, d, e, f
- 1101 0011 in hex is 0xd3

Today's Summary

Today's topics

- All computing devices equivalent given sufficient time and storage
- Abstractions of lower layers hide complexity
- Bits: Two states (on vs. off, true vs. false)
- Represent unsigned numbers with binary numbers
  - N bits can represent 2^N different values

Announcements

- Homeworks 9 and 10 Available
  - 9 Due before Thanksgiving; 10 after
  - No programming
  - Final Project will be to use Scratch to prototype some deign
- Exam 2 graded by Monday