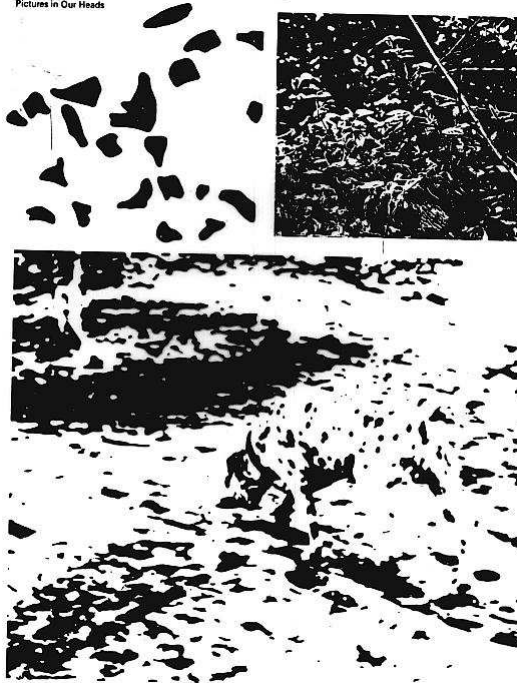


# Object Recognition

- REPRESENTATION PROBLEM  
2D & 3D OBJECT MODELING  
SHAPE, COLOR, TEXTURE, ...
- MODEL ACQUISITION PROBLEM
- SEARCH PROBLEM  
HOW TO SELECT IMAGE  
FEATURES & INDEX  
INTO DB of ALL OBJECTS  
TO FIND BEST MATCH ?  
⇒ SELECTION/SEGMENTATION < FEATURE DETECTION  
INDEXING < PERCEPTUAL  
MATCHING (SIMILARITY) < GROUPING  
CORRESPONDENCE  
VERIFICATION

Pictures in Our Heads



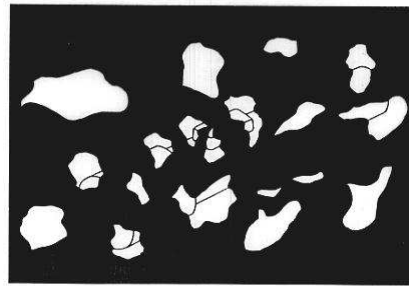
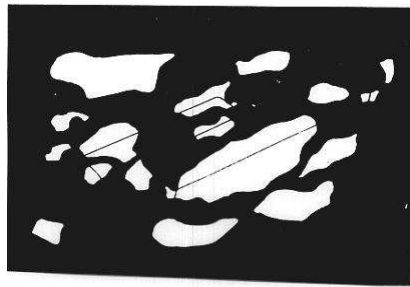
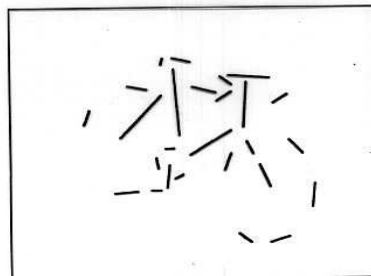
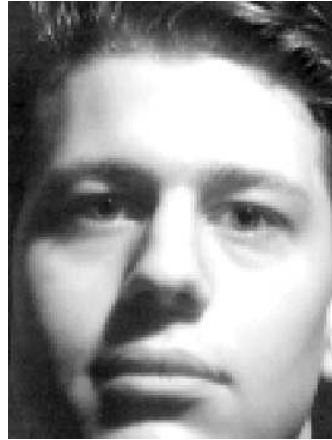


Figure 76. Reversible image of an object where the contour definition produced by an enclosing surface. The object is a flat object, is the same as that shown in Figure 75. The reader may note that the three-dimensional percept in this figure does not occur instantaneously.





Lighting affects appearance



The "Margaret Thatcher Illusion" by Peter Thompson



The “Margaret Thatcher Illusion” by Peter Thompson

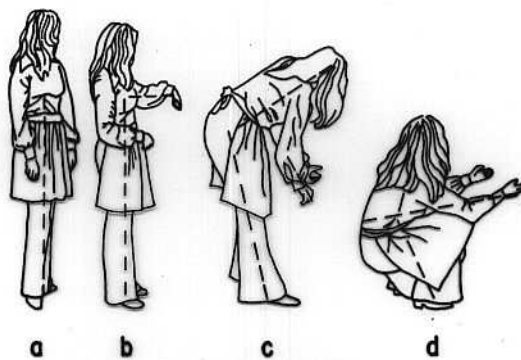
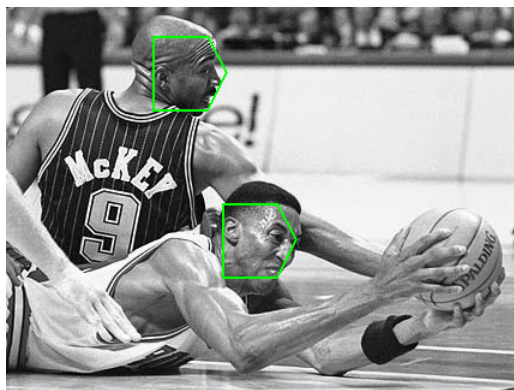


Figure 29. Four configurations of a nonrigid object.

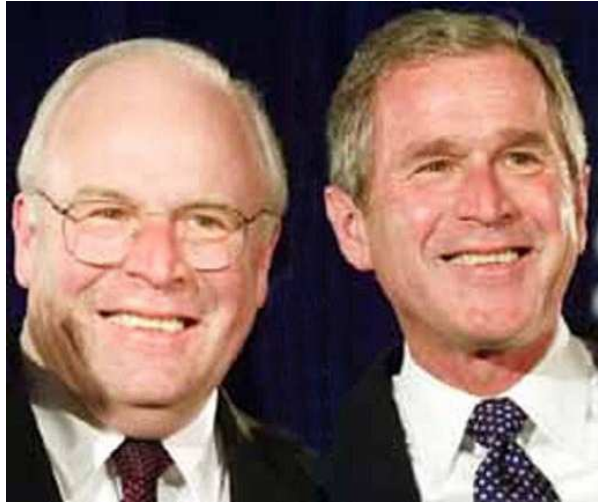
# Recognition Problems

- What is it?
  - Object detection
- Who is it?
  - Recognizing identity
    - Object recognition
    - Category recognition
- What are they doing?
  - Activity recognition
- All of these are **classification** problems
  - Choose one class from a list of possible candidates

## Face Detection



# Face Recognition



P. Sinha and T. Poggio, Last but not least, *Perception* 31, 2002, 133.

## 3D OBJECT RECOGNITION FROM A SINGLE 2D IMAGE

- SOLUTION REQUIRES:
  - OBJECT IDENTIFICATION
  - VIEWPOINT IDENTIFICATION (POSE IDENTIFICATION)
- REQUIREMENTS:
  - INTERNAL MODEL of OBJECT(S)
  - METHOD for SEARCHING "VIEWPOINT SPACE", i.e.,  
SOLVE for ALL VIEWING  
PARAMETERS s.t. 2D IMAGE  
FEATURES BEST MATCH (FIT)  
PROJECTED 3D MODEL FEATURES
  - METHOD for PREDICTING APPEARANCE  
i.e., verify viewpoint consistency

# What Makes Recognition Hard?

- Intrinsic variability within each class
- Pose variability
- Illumination variability
- Background variability
- Segmentation problem
  - What region within an image contains the object?
- Feature selection problem
  - What features describe shape and appearance?

## UNKNOWN

### DATA SELECTION :

WHAT SUBSET OF DATA  
CORRESPONDS TO A SINGLE OBJECT?

### OBJECT IDENTIFICATION :

WHICH OBJECT MODEL  
CORRESPONDS TO DATA SUBSET

### OBJECT INSTANCE :

FOR NON-RIGID OBJECTS OR OBJECT  
CLASSES, SPECIFICATION OF THE  
PARAMETERS THAT COMPLETELY  
DESCRIBE A GIVEN LEGAL  
INSTANCE OF OBJECT

### FEATURE CORRESPONDENCE :

WHICH INDIVIDUAL MODEL  
FEATURES CORRESPOND TO  
EACH DATA FEATURE?

POSE : POSITION & ORIENTATION OF VIEWER  
WRT OBJECT IN SCENE

## RECOGNITION INVARIANTS

METHOD SHOULD BE INVARIANT UNDER

- VIEWPOINT INVARIANTS
  - TRANSLATION
  - ROTATION
  - SCALE
  - PARTIAL OCCLUSION  
(SELF & FROM OTHER OBJECTS)
- SENSOR INVARIANTS
  - SENSOR NOISE
  - ILLUMINATION / SHADOWS
  - "LOCAL" ERRORS IN EARLY PROCESSING MODULES  
(E.G., EDGE DETECTION)
- OBJECT INVARIANCE
  - INTRINSIC SHAPE "DISTORTIONS"  
(E.G. ARTICULATED OBJECTS)

## SEARCH SPACES

DATA SPACE:  $2^n$ ,  $n = \# \text{ image features}$

OBJECT-MODEL SPACE:  $M$ ,  $\# \text{ models}$

MODEL-PARAMETERIZATION SPACE:  $d^k$   
 where  $k = \# \text{ parameters}$   
 $d = \# \text{ values per parameter}$

CORRESPONDENCE SPACE:  $(m+1)^n$   
 where  $m = \# \text{ model features}$   
 $n = \# \text{ image features}$   
 (assuming all  $n$  features part of 1 object)

POSE SPACE: (TRANSFORMATION SPACE)

2D objects: 3D or 4D  
 (2: translation, 1 rotation, 1 scale)

3D objects:

Orthography: 5D

(2: viewing direction, 1: rotation in image plane, 2: translation)

Perspective: 6D

(3: translation, 3: rotation)

## MATCHING MODELS w/ IMAGES

### 2D-2D MATCH

- SMALL # "CHARACTERISTIC VIEWS"
  - MAY BE USEFUL FOR FAMILIAR OBJECTS w/ FEW "TYPICAL" VIEWS
- VIEWER-CENTERED MODELS

### 2D/3D-3D MATCH

- RECOVER BOTTOM-UP FROM IMAGE(S)  
2D to 3D DATA
  - E.G. STEREO
  - SHAPE-FROM-X [Biederman]
  - GEONS
  - GENERALIZED CYLINDERS [Marr]

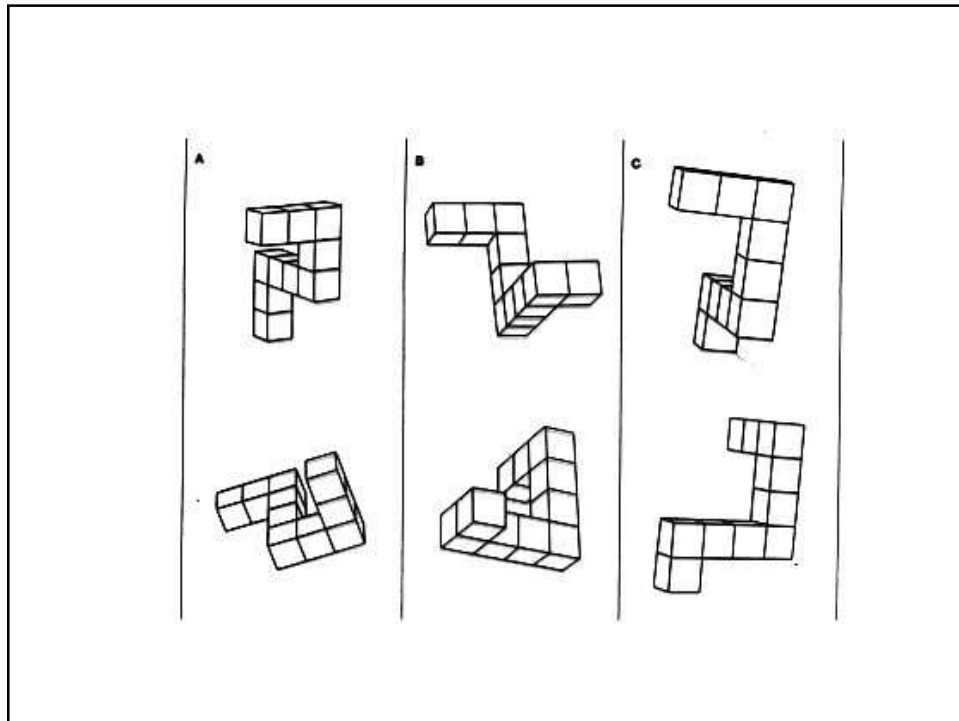
### 2D-3D MATCH

- OBJECT-CENTERED MODELS
- VIEWPOINT-INVARIANT FEATURES  
OR VIEWPOINT-VARIANT FEATURES

## METHOD 0: DIRECT APPROACH

- FOR EACH <sup>MODEL</sup> OBJECT, STORE A SUFFICIENTLY LARGE NUMBER OF DIFFERENT VIEWS
- DEFINE A SIMILARITY MEASURE TO FIND BEST MATCH BETWEEN IMAGE DATA AND DIFFERENT VIEWS OF ALL OBJECT MODELS
  - E.G. CROSS-CORRELATION w/ A TEMPLATE
- DISADVANTAGES:
  - VERY LARGE SPACE OF POSSIBLE VIEWS (TRANSFORMATIONS)
  - BRUTE-FORCE SEARCH OF "POSE SPACE"
  - OBJECTS <sup>SHOULD</sup> BE RECOGNIZED IN NOVEL VIEWS

Ex. 2D position & 2D orientation invariant  
to 1 pixel and 1°  $\Rightarrow$   
 $512 \times 512 \times 360 \approx 90,000,000$   
poses



### METHOD 10: INVARIANT GLOBAL PROPERTIES

- SELECT A SET OF GLOBAL, INVARIANT PROPERTIES — EXPLOITS REGULARITIES ACROSS VIEWPOINTS — VIEWPOINT-INVARIANT FEATURES

E.G. COMPACTNESS ( $P^2/A$ )  
AREA ( $A$ ), MOMENTS ( $\sum x^p y^q f(x,y)$ )

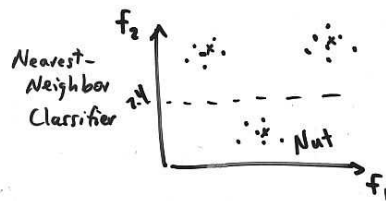
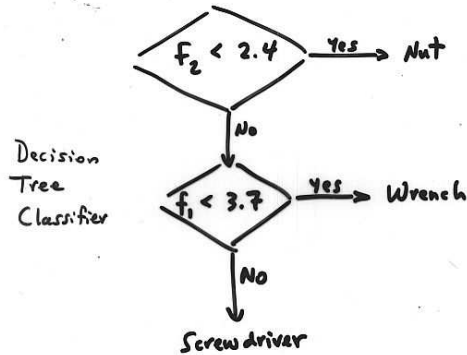
- FEATURES MUST BE RELATIVELY SIMPLE TO COMPUTE  $\Rightarrow$  NEED PROCEDURE FOR DETECTING/COMPUTING EACH SUCH PROPERTY

- IF OBJECT'S PROPERTIES HAVE CHARACTERISTIC RANGES OF VALUES  $\Rightarrow$  POLYTOPE IN  $n$ -D FEATURE SPACE

- PATTERN RECOGNITION  
GIBSON  
SRI VISION MODULE

- ARE THERE INVARIANT FEATURES FOR REAL, 3D OBJECTS??

Given  $n$ -D feature vector,  $\langle f_1, f_2, \dots, f_n \rangle$ ,  
match w/  $N$  possible objects:



## A Geometric Invariant

### CROSS RATIO

Given 4 points  $(x_i, y_i, z_i)$   
that are collinear in scene

let  $(x_{ik}, y_{ik}, z_{ik})$  be the  
perspective projection of those  
4 points into an image.

$$\begin{aligned}
 \text{Cross Ratio} &= \frac{(x_3 - x_1)(x_4 - x_2)}{(x_3 - x_2)(x_4 - x_1)} \\
 &= \frac{(x_{i3} - x_{i1})(x_{i4} - x_{i2})}{(x_{i3} - x_{i2})(x_{i4} - x_{i1})}
 \end{aligned}$$

and similarly for  $y$ 's.

⇒ If we know coords of 3 collinear  
points, we can compute coords of any  
other point on same line from its image coords

## Approximate Invariants

- Over a limited range of viewpoint variation
- Parallelism
- Collinearity
- Angle between a pair of lines
- Co-termination

### MATCHING using OCCULding CONTOURS

Kriegman & Ponce, 1990, PAMI

- Given: Smooth, 3D shape
- Calculate (offline) the implicit equation of the occluding contour  
 $F(u, v, V) = 0$

- (For each aspect)

Solve for pose by minimizing average distance between model contour and image edges

$$\min \sum_i F^2(u_i, v_i, V)$$

where  $(u_i, v_i)$  are image edge pts.

(Nonlinear least-squares minimization of an expression for the distance b/w contour & image  $\Rightarrow$  Iterative techniques)

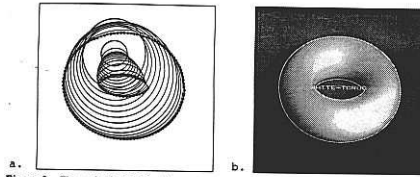


Figure 3. The result of minimizing the mean square error of the implicit contour equation: (a). The contours at each iteration of the minimization are shown overlaid on the edge points used in the minimization; the Canny edges are drawn as little circles. (b). The result of recognition for the white torus.

To conclude, let us give an example. Consider a torus. The expression  $C$  is too complex to be given here. With the following substitutions:  $\hat{x} = \hat{z} \sin \beta$ ,  $\hat{y} = \hat{y} \sin \beta$ ,  $c = \cos^2 \beta$ , the expression  $C_1$  is:

$$\begin{aligned}
 0 = C_1(\hat{z}, \hat{y}, c) = & R^4 \hat{c}^4 - 6R^4 \hat{c}^3 + 15R^4 \hat{c}^2 - 20R^4 \hat{c} + 15R^4 - 6R^4 \hat{c}^3 + R^4 \hat{c}^2 - 2R^4 \hat{c} + 10R^4 \hat{c}^2 \hat{r}^2 \\
 & + 2R^4 \hat{c}^2 \hat{z}^2 - 18R^4 \hat{c}^2 \hat{r}^4 + 12R^4 \hat{c}^2 \hat{z}^4 + 4R^4 \hat{c}^2 \hat{y}^2 + 10R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 28R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 18R^4 \hat{c}^2 \hat{y}^4 \\
 & + 10R^4 \hat{c}^2 \hat{z}^4 - 32R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 + 32R^4 \hat{c}^2 \hat{y}^4 - 18R^4 \hat{c}^2 \hat{r}^2 + 18R^4 \hat{c}^2 \hat{z}^2 - 28R^4 \hat{c}^2 \hat{y}^2 + 10R^4 \hat{c}^2 \hat{r}^4 \\
 & - 4R^4 \hat{c}^2 \hat{z}^4 + 12R^4 \hat{c}^2 \hat{y}^4 + 2R^4 \hat{c}^2 - 2R^4 \hat{c}^2 \hat{r}^2 + R^4 \hat{c}^2 \hat{r}^4 + 2R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 2R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 - 8R^4 \hat{c}^2 \hat{r}^4 \\
 & - 10R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 - 6R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + R^4 \hat{c}^2 \hat{z}^4 + 34R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 + 26R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 26R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 - 8R^4 \hat{c}^2 \hat{z}^4 \\
 & + 6R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 50R^4 \hat{c}^2 \hat{r}^4 - 44R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 46R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 - 18R^4 \hat{c}^2 \hat{z}^4 + 32R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 18R^4 \hat{c}^2 \hat{y}^4 \\
 & + 6R^4 \hat{c}^2 \hat{r}^4 - 26R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 - 26R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + 6R^4 \hat{c}^2 \hat{z}^4 - 22R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 + 19R^4 \hat{c}^2 \hat{r}^4 - 2R^4 \hat{c}^2 \hat{r}^2 \\
 & + 6R^4 \hat{c}^2 \hat{z}^2 + 10R^4 \hat{c}^2 \hat{y}^2 + 6R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 8R^4 \hat{c}^2 \hat{r}^4 + R^4 \hat{c}^2 - 2R^4 \hat{c}^2 \hat{r}^2 + 10R^4 \hat{c}^2 \hat{r}^4 \\
 & - 6R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 4R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + 10R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 - 46R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + 26R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 22R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 \\
 & - 14R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 6R^4 \hat{c}^2 \hat{r}^2 \hat{z}^4 - 2R^4 \hat{c}^2 \hat{r}^2 \hat{y}^4 + 2R^4 \hat{c}^2 \hat{z}^4 + 10R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 + 44R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \\
 & - 44R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 - 32R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 10R^4 \hat{c}^2 \hat{r}^2 \hat{z}^4 + 22R^4 \hat{c}^2 \hat{r}^2 \hat{y}^4 + 6R^4 \hat{c}^2 \hat{z}^4 - 4R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 \\
 & + 6R^4 \hat{c}^2 \hat{z}^2 \hat{y}^4 - 18R^4 \hat{c}^2 \hat{r}^4 - 26R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 46R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + 22R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 10R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 \\
 & - 32R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 4R^4 \hat{c}^2 \hat{z}^4 + 8R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 8R^4 \hat{c}^2 \hat{r}^4 + 4R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 10R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 \\
 & - 26R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 6R^4 \hat{c}^2 \hat{r}^2 \hat{z}^4 - 14R^4 \hat{c}^2 \hat{r}^2 \hat{y}^4 + 22R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 6R^4 \hat{c}^2 \hat{z}^4 + 4R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 6R^4 \hat{c}^2 \hat{y}^4 \\
 & - 2R^4 \hat{c}^2 \hat{r}^4 - 2R^4 \hat{c}^2 \hat{r}^2 \hat{z}^2 + 6R^4 \hat{c}^2 \hat{r}^2 \hat{y}^2 + 4R^4 \hat{c}^2 \hat{z}^4 - 6R^4 \hat{c}^2 \hat{z}^2 \hat{y}^2 - 2R^4 \hat{c}^2 \hat{z}^2 \hat{y}^4 + 2R^4 \hat{c}^2 \hat{y}^4 + \hat{c}^4 \hat{r}^4 - 6\hat{c}^4 \hat{r}^2 \\
 & + 4\hat{c}^4 \hat{r}^2 \hat{z}^2 + 2\hat{c}^4 \hat{r}^2 \hat{y}^2 + 15\hat{c}^4 \hat{r}^4 - 18\hat{c}^4 \hat{r}^2 \hat{z}^2 - 12\hat{c}^4 \hat{r}^2 \hat{y}^2 + 6\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 6\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + \hat{c}^4 \hat{r}^4 \\
 & - 20\hat{c}^4 \hat{r}^2 \hat{z}^2 + 32\hat{c}^4 \hat{r}^2 \hat{y}^2 + 28\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 18\hat{c}^4 \hat{r}^2 \hat{z}^4 - 22\hat{c}^4 \hat{r}^2 \hat{y}^4 - 8\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 4\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 \\
 & + 6\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 6\hat{c}^4 \hat{r}^2 \hat{z}^4 + 15\hat{c}^4 \hat{r}^2 \hat{y}^4 - 28\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 32\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 19\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + 32\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 \\
 & + 19\hat{c}^4 \hat{r}^2 \hat{y}^4 - 6\hat{c}^4 \hat{r}^2 \hat{z}^4 - 8\hat{c}^4 \hat{r}^2 \hat{y}^4 - 4\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 - 2\hat{c}^4 \hat{r}^2 \hat{z}^2 \hat{y}^2 + \hat{c}^4 \hat{z}^4 + 2\hat{c}^4 \hat{z}^2 \hat{y}^2 \\
 & + \hat{c}^4 \hat{y}^4 - 6\hat{c}^4 \hat{r}^4 + 12\hat{c}^4 \hat{z}^2 + 18\hat{c}^4 \hat{y}^2 - 8\hat{c}^4 \hat{z}^4 - 22\hat{c}^4 \hat{z}^2 \hat{y}^2 - 18\hat{c}^4 \hat{y}^4 + 2\hat{c}^4 \hat{z}^4 \\
 & + 4\hat{c}^4 \hat{z}^2 \hat{y}^2 + 8\hat{c}^4 \hat{z}^2 \hat{y}^4 + 6\hat{c}^4 \hat{z}^2 \hat{y}^2 + 2\hat{c}^4 \hat{z}^2 \hat{y}^4 + 4\hat{c}^4 \hat{z}^2 \hat{y}^2 + \hat{r}^4 - 2\hat{r}^4 \hat{z}^2 - 4\hat{r}^4 \hat{y}^2 \\
 & + \hat{r}^4 \hat{z}^4 + 6\hat{r}^4 \hat{z}^2 \hat{y}^2 + 6\hat{r}^4 \hat{y}^4 - 2\hat{r}^4 \hat{z}^4 \hat{y}^2 - 6\hat{r}^4 \hat{z}^2 \hat{y}^4 - 4\hat{r}^4 \hat{y}^4 + \hat{z}^4 \hat{y}^4 + 2\hat{z}^2 \hat{y}^4 + \hat{y}^4
 \end{aligned}$$

## METHOD 2: OBJECT DECOMPOSITION INTO PARTS (+ CORRESPONDENCE SPACE SEARCH)

- DECOMPOSE OBJECT INTO CONSTITUENT PARTS, WHERE EACH PART IS SIMPLE, GENERIC  
E.G., 1D CONTOURS — LINES, CORNERS, "CODONS"  
2D SURFACE PATCHES — HOLES  
3D VOLUMES — GENERALIZED CYLINDERS, "GEONS"
- DECOMPOSITION DONE INDEPENDENT OF VIEW POINT
- 1. SEGMENT IMAGE INTO PARTS  
2. CLASSIFY PARTS  
3. DESCRIBE OBJECT IN TERMS OF PARTS  
— SET OF FEATURES  
— SPATIAL RELATIONS BETWEEN PARTS
- EXAMPLES:  
PERCEPTION  
BOULES' LOCAL-FEATURE FOCUS METHOD

## Pose consistency

- Correspondences between image features and model features are not independent
- A small number of correspondences yields a camera --- the others must be consistent with this
- Strategy:
  - Generate hypotheses using small numbers of correspondences (e.g. triples of points for a calibrated perspective camera, etc., etc.)
  - Backproject and verify
- Notice that the main issue here is camera calibration
- Appropriate groups are “frame groups”

### BOLLES' LOCAL FEATURE FOCUS METHOD

- 2D LOCAL FEATURES: HOLES, CONVEX CORNERS, CONCAVE CORNERS
- DESCRIBE EACH OBJECT AS A ~~GRAPH~~ <sup>GRAPH</sup>
- FOREACH OCCURRENCE OF EACH FEATURE TYPE IN EACH MODEL,  
SELECT SUBGRAPH “CENTERED” AT NODE WHICH IS SUFFICIENT TO DISTINGUISH IT FROM ALL OTHERS
- COMPILE A TABLE FOREACH FEATURE TYPE WHICH SAYS WHERE TO LOOK FOR OTHER NEARBY FEATURES IN ORDER TO CONFIRM IT.



## Ex. Focus - Feature TABLE

"Focus" FEATURE: HOLE (i.e., CIRCLE)

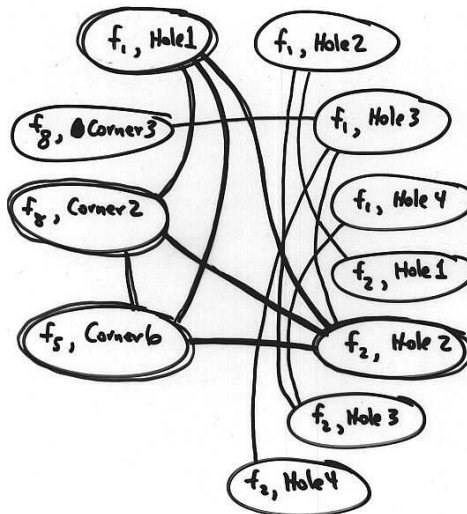
POSSIBLE OBJECT FEATURES: HOLE1 in OBJECT3  
HOLE4 in OBJECT5  
HOLE6 in OBJECT5  
:

NEARBY FEATURES:

|        |                       |                                                         |
|--------|-----------------------|---------------------------------------------------------|
| CORNER | DISTANCE, ORIENTATION | CORNER2<br>in OBJ2                                      |
| CORNER | DISTANCE, ORIENTATION | CORNER1<br>in OBJ5                                      |
| HOLE   | DISTANCE              | HOLE1<br>in OBJ2<br>OR<br>HOLE5<br>in OBJ4<br>OR<br>... |

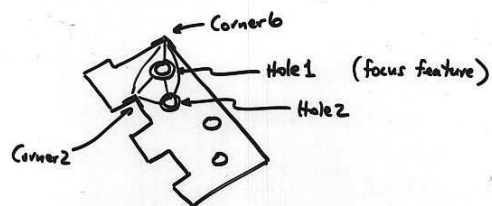
- BUILD A GRAPH FROM NODE-NODE MATCHES —  
 NODE = (MODEL NODE, IMAGE FEATURE)  
 PAIR  
 ARC = CONNECTS PAIRS OF NODES  
 WHICH ARE NEIGHBORS IN  
 MODEL AND IMAGE FEATURES  
 ARE DISTINCT  
 (⇒ LOCALLY CONSISTENT  
 (PAIRWISE) ASSIGNMENT)
- FIND MAXIMAL CLIQUE —  
 LARGEST CONNECTED SUBGRAPH  
 = LARGEST CLUSTER OF MUTUALLY-  
 CONSISTENT MATCHES
- VERIFY MATCH BY COMPARING  
 COMPLETE MODEL w/ IMAGE

Graph of pairwise-consistent feature matches



- MAXIMAL CLIQUE IN RED.
- EXAMPLE OF SEARCHING THE "CORRESPONDENCE SPACE"

### Hypothesized Solution :



### Verification :

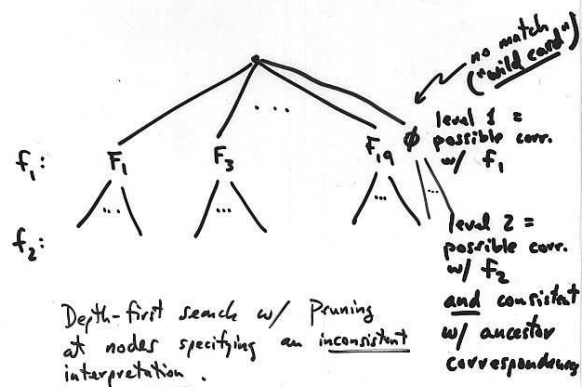
1. Compute pose
2. Project model to image space
3. Cross-correlation



## Interpretation Trees

Using geometric constraints to  
limit search of Correspondence Space

Given: Image features  $f_1, \dots, f_n$   
Model features  $F_1, \dots, F_m$



Size of Correspondence Space =

$$(m+1)^n$$

Height of Interpretation Tree =  $n$

Goal: find path from root to leaf  
such that all  $n$  correspondences  
are consistent w/ a single model

Approach: Use 1st and 2nd order  
geometric constraints to  
prune interpretation tree as  
we traverse it.

Possible  
Constraints: Unary Constraints: properties of  
 $f_i$  and  $F_i$  must be similar  
(i.e. match)

Ex. length of edge  
corner angle  
color  
texture

Binary Constraints: consistency constraints  
between  $(f_{i_1}, F_{j_1})$  and  
 $(f_{i_2}, F_{j_2})$  pairings.

Ex: Relative angle between 2 edges  
Range of distances between  
2 edges

Range of directions from  
 $f_{i_1}$  to  $f_{i_2}$

etc.

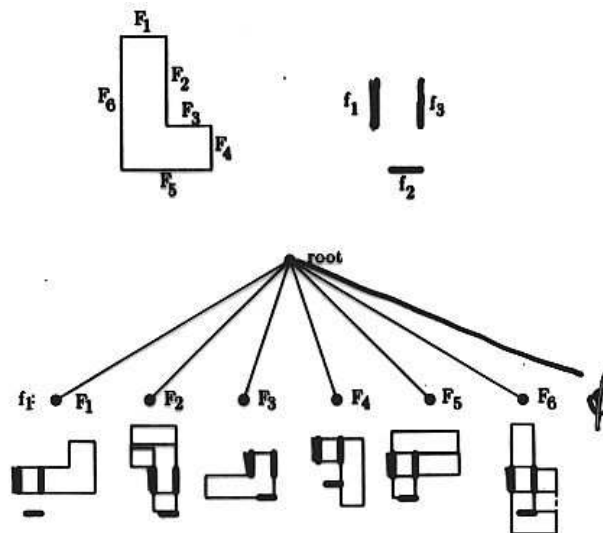


Figure 3.1

We can build a tree of possible interpretations, by first considering all the ways of matching the first data feature,  $f_1$ , to each of the model features,  $F_j, j = 1, \dots, m$ . In the bottom part of the figure, we show an example of these pairings for the model and data shown at the top. In some cases, due to occlusion of the data features, a range of possible poses is given.

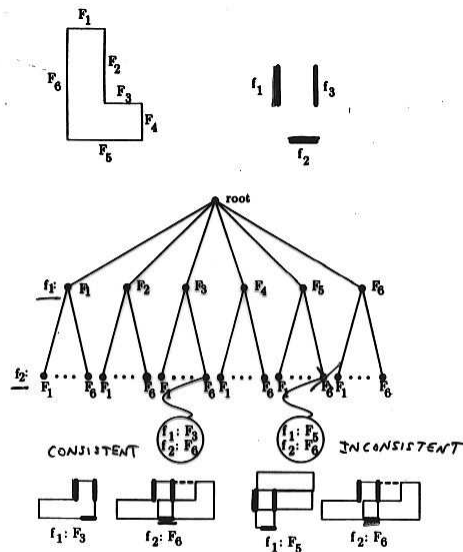


Figure 3.2  
For each pairing of the first data feature with a model feature, we can consider matchings for the second data feature with each of the model features. Thus, each node in the second level of the tree defines a pairing for the first two data features, found by tracing up the tree to the root. Two examples are shown. The example on the left is consistent with a single rigid transformation, as shown by the fact that the two ranges of poses specified by each of the data-model feature pairings have a common pose. The example on the right is not consistent with a single transformation, as its two ranges of poses do not have a common pose.

## Interpretation Tree Search Algorithm

- Depth-First search with pruning (cut-offs)
- At each node, test all unary & binary constraints. If all are satisfied, continue. Otherwise, backtrack
- At leaf node have an hypothesis for a feasible interpretation. Verify by solving for pose given correspondences, and compare projected model w/ data.

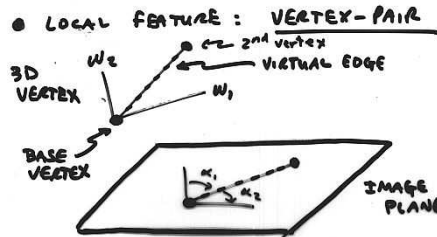


- METHOD <sup>3</sup>: COMBINING LOCAL EVIDENCE  
+ POSE SPACE SEARCH
- FIRST MATCH, THEN FIND BEST VIEWING TRANSFORMATION
  - DEFINE 6D PARAMETER SPACE - <sup>POSE</sup>SPACE  
OF ALL POSSIBLE (DISCRETELY SAMPLED) VIEWING TRANSFORMATIONS
  - 1. FOR EACH MATCHING (IMAGE FEATURE, MODEL FORT.) PAIR, "VOTE" IN PARAMETER SPACE FOR ALL TRANSFORMATIONS THEY DESCRIBE.  
2. FIND "PEAK" IN PARAMETER SPACE.
  - EXAMPLES :  
GENERALIZED HOUGH TRANSFORM  
THOMPSON & MUNDY, 1987  
HINTON, 1981

## Voting on Pose

- Each model leads to many correct sets of correspondences, each of which has the same pose
  - Vote on pose, in an accumulator array
  - This is a Hough transform, with all its issues

# THOMPSON & MUNDY'S ALGORITHM



EACH VERTEX = INTERSECTION OF 2 EDGES

GIVEN IMAGE w/  $n$  VERTICES,  
 $\Rightarrow 2n^2$  VERTEX-PAIRS

- GIVEN ~~AND~~ A CORRESPONDENCE BETWEEN MODEL & IMAGE VERTICES & EDGES, THERE IS A UNIQUE TRANSFORMATION (AFFINE) WHICH MAPS IMAGE VERTEX-PAIR TO MODEL VERTEX-PAIR  
 $\Rightarrow$  MODELS WEAK PERSPECTIVE PROJECTION

## ALGORITHM

```

FOR EACH IMAGE VERTEX-PAIR DO
  FOR EACH MODEL VERTEX-PAIR DO
    COMPUTE 6-ELEMENT TRANSFORMATION
      T THAT MAPS ONE TO OTHER
    VOTE (INCREMENT "BIN") FOR 1
      POINT IN 6D TRANSFORM PARAM.
      SPACE CORRESPONDING TO T.
  FIND "CLUSTERS" OF VOTES (PEAK FINDING)
  VERIFY PROJECTED MODEL w/ IMAGE
  
```

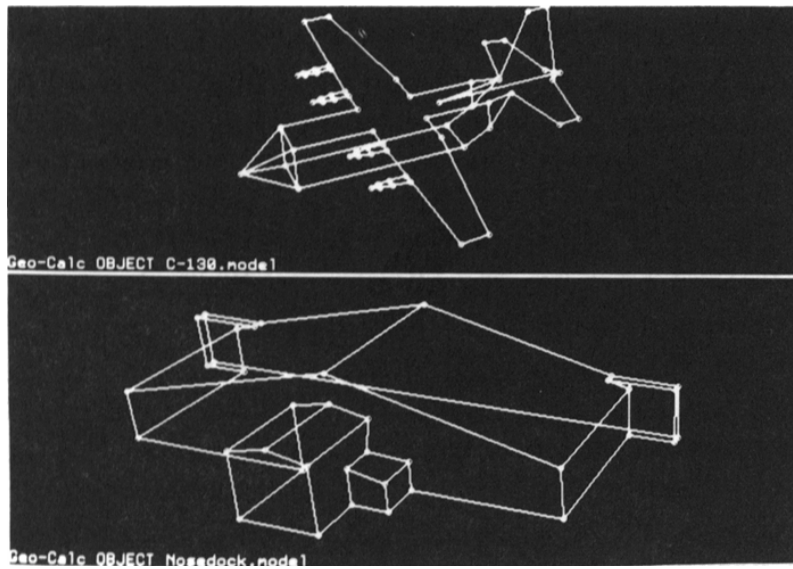
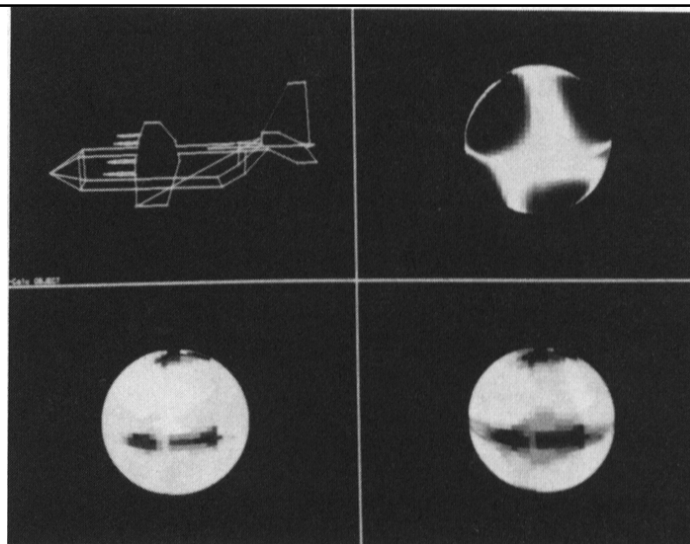


Figure from "The evolution and testing of a model-based object recognition system", J.L. Mundy and A. Heller, Proc. Int. Conf. Computer Vision, 1990  
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From "The evolution and testing of a model-based object recognition system", J.L. Mundy and A. Heller, Proc. ICCV, 1990

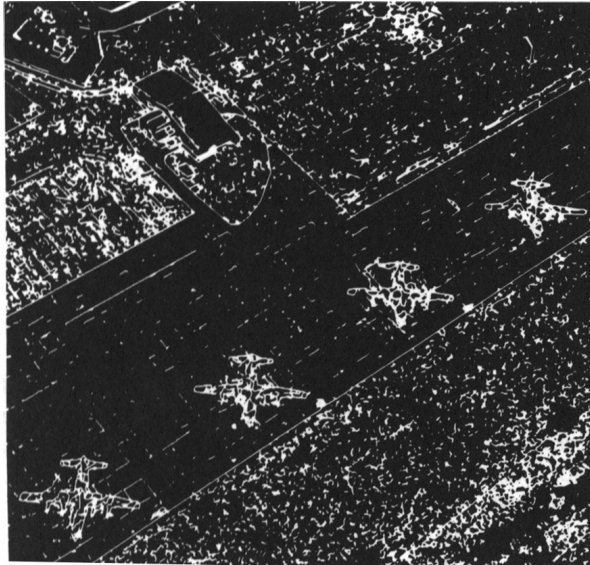


Figure from "The evolution and testing of a model-based object recognition system", J.L. Mundy and A. Heller, Proc. Int. Conf. Computer Vision, 1990  
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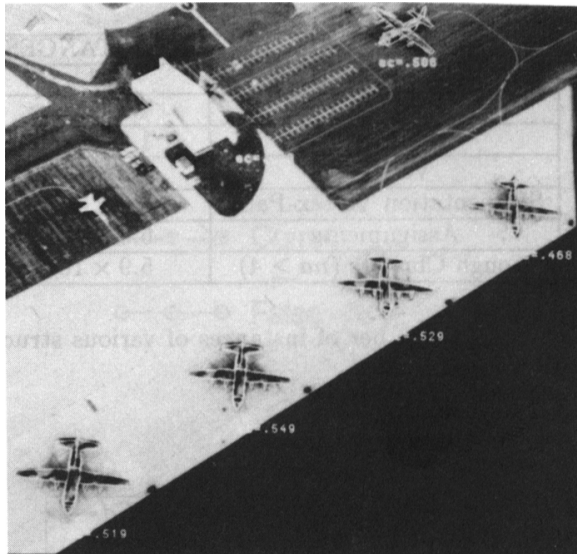


Figure from "The evolution and testing of a model-based object recognition system", J.L. Mundy and A. Heller, Proc. Int. Conf. Computer Vision, 1990  
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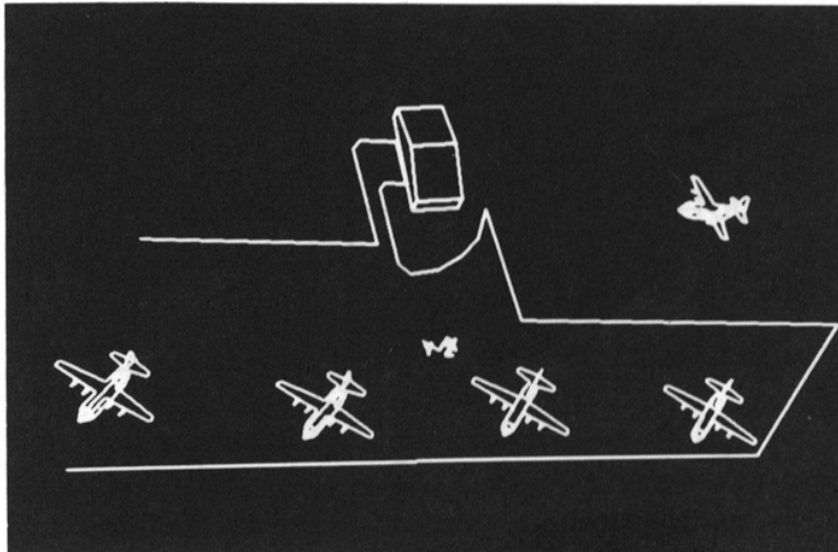


Figure from "The evolution and testing of a model-based object recognition system", J.L. Mundy and A. Heller, Proc. Int. Conf. Computer Vision, 1990  
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### GEOMETRIC HASHING

- Wolfson, Lamdan et al. 1988
- PLANAR, RIGID objects
- Affine camera model
- Property: An affine transform of a planar rigid body is uniquely defined by the transformation of 3 ordered, non-collinear pts [e.g., Klein, 1925]

⇒ Pick 3 non-collinear model pts  $B_0, B_1, B_2$  as affine basis

Any pt  $p$  represented by the affine coords  $(\alpha, \beta)$  where

$$p = \alpha(B_1 - B_0) + \beta(B_2 - B_0) + B_0$$

$(\alpha, \beta)$  invariant under affine transf.  $T$

$$Tp = \alpha(TB_1 - TB_0) + \beta(TB_2 - TB_0) + TB_0$$

## Invariants

- There are geometric properties that are invariant to camera transformations
- Easiest case: view a plane object in weak perspective
- Assume we have three base points  $P_i$  on the object
  - then any other point on the object can be written as
- Now image points are obtained by multiplying by a plane affine transformation, so

$$\begin{aligned}
 p_k &= AP_k \\
 &= A(P_1 + \mu_{ka}(P_2 - P_1) + \mu_{kb}(P_3 - P_1)) \\
 &= p_1 + \mu_{ka}(p_2 - p_1) + \mu_{kb}(p_3 - p_1)
 \end{aligned}$$

$$P_k = P_1 + \mu_{ka}(P_2 - P_1) + \mu_{kb}(P_3 - P_1)$$

## Invariants

- This means that, if I know the base points in the image, I can read off the  $\mu$  values for the object
  - they're the same in object and in image --- **invariant**
- Suggests a strategy rather like the Hough transform
  - search correspondences, form  $\mu$ 's and vote

## Geometric Hashing

- Vote on identity and correspondence using invariants
  - Take hypotheses with large enough votes
- Fill up a table, indexed by  $\mu$ 's, with
  - the base points and fourth point that yield those  $\mu$ 's
  - the object identity

### Offline Modeling/Learning Phase

1. Select  $m$  feature pts on planar model( $s$ ).
2. foreach ordered, non-collinear triple of model pts do  
    Compute coords of other  $(m-3)$  pts  
    foreach coord  $(\alpha, \beta)$  store  
        Hash  $(\alpha, \beta) = (\text{object}, \text{basis})$

$O(m^4)$  time and space.

**Algorithm 18.3:** Geometric hashing: voting on identity and point labels

```
For all groups of three image points  $T(I)$ 
  For every other image point  $p$ 
    Compute the  $\mu$ 's from  $p$  and  $T(I)$ 
    Obtain the table entry at these values
      if there is one, it will label the three points in  $T(I)$ 
      with the name of the object
      and the names of these particular points.
    Cluster these labels;
      if there are enough labels, backproject and verify
    end
  end
end
```

Online Matching Phase

1. Feature Detection:  
Extract  $n$  interest pts from image
2. Choose Basis:  
Pick 3 non-collinear pts.  
Compute affine coords of other  
( $n-3$ ) pts.
3. For each affine coord,  
vote for all (model, basis) pairs  
in entry in hash table.
4. Find Peaks in Object-Basis space  
If none, goto step 2.
5. ~~From~~ (model pt, image pt) pairs in Peaks  
compute best-fit affine transform  
(least squares)
6. Verify complete transformed model  
w/ image
7. If no peak verified, goto step 2  
 $O(n')$  time

### ALIGNMENT METHOD

- HUTTENLOCHER AND ULLMAN, 1987
- ARBITRARY (NON-PLANAR) objects defined by points and edge contours
- Weak-perspective camera model

$$\underset{\substack{\uparrow \\ 2D}}{x'} = \Pi \left( \underset{\substack{\uparrow \\ 3D}}{sRx} + b \right)$$

where  $\Pi$  = orthographic proj  
 $s$  = scale  
 $R$  = 3D rotation  
 $b$  = 2D translation } 6 params.

- Type of Affine transformation  
 $x' = Lx + b$  where  $L$  is  $2 \times 2$
- OK when object far from camera  
and object depth small relative to distance from camera

### Main Idea:

Separate problem of finding best model from problem of finding best transformation (3D  $\rightarrow$  2D determined by viewpoint) of model to image

1. Hypothesize viewpoint for each model  
 $\Rightarrow$  solve for viewing transformation  
"normalization" step
2. Select best model by matching "normalized" model w/ image

### EX. CHARACTER RECOGNITION

- FOR EACH LETTER, STORE ITS DESCRIPTION IN SOME CANONICAL POSITION, ORIENTATION & SIZE
- GIVEN "VIEWED" LETTER, "UNDO" SHIFT, ROTATION AND SCALE:
  - + SHIFT CENTER-OF-MASS TO FIXED LOCATION (ORIGIN)
  - + SCALE CONVEX HULL TO FIXED SIZE
  - + ROTATE MAJOR AXIS TO FIXED ORIENTATION  
(OR DETECT ORIENTATIONS OF KEY FEATURES & ORIENT THESE — E.G.,  $\text{D}$ ,  $\text{L}$ )
- MATCH "NORMALIZED" INPUT w/ EACH MODEL AND SELECT BEST MATCH.

## Recognizing Human Actions

- Movement and posture change
  - run, walk, crawl, jump, hop, swim, skate, sit, stand, kneel, lie, dance (various), ...
- Object manipulation
  - pick, carry, hold, lift, throw, catch, push, pull, write, type, touch, hit, press, stroke, shake, stir, turn, eat, drink, cut, stab, kick, point, drive, bike, insert, extract, juggle, play musical instrument (various)...
- Conversational gesture
  - point, ...
- Sign Language

## Activities and Situation Assessment

- Example: Withdrawing money from an ATM
- Activities constructed by composing actions. Partial order plans may be a good model.
- Activities may involve multiple agents
- Detecting unusual situations or activity patterns is facilitated by the video activity transform

### Objects in Space

- Segment/Region-of-interest
- Features (points, curves, wavelet coefficients..)
- Correspondence and deform into alignment
- Recover parameters of generative model
- Discriminative classifier

### Actions in Space-Time

- Segment/volume-of-interest
- Features (points, curves, wavelets, motion vectors..)
- Correspondence and deform into alignment
- Recover parameters of generative model
- Discriminative classifier

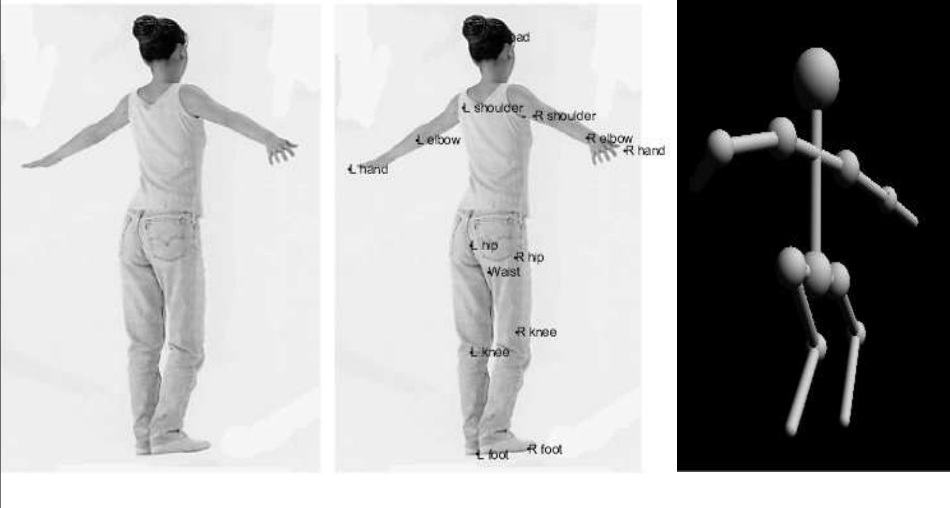
## Key Cues for Action Recognition

- “Morpho-kinesics” of action (shape and movement of the body)
- Identity of the object/s
- Activity context

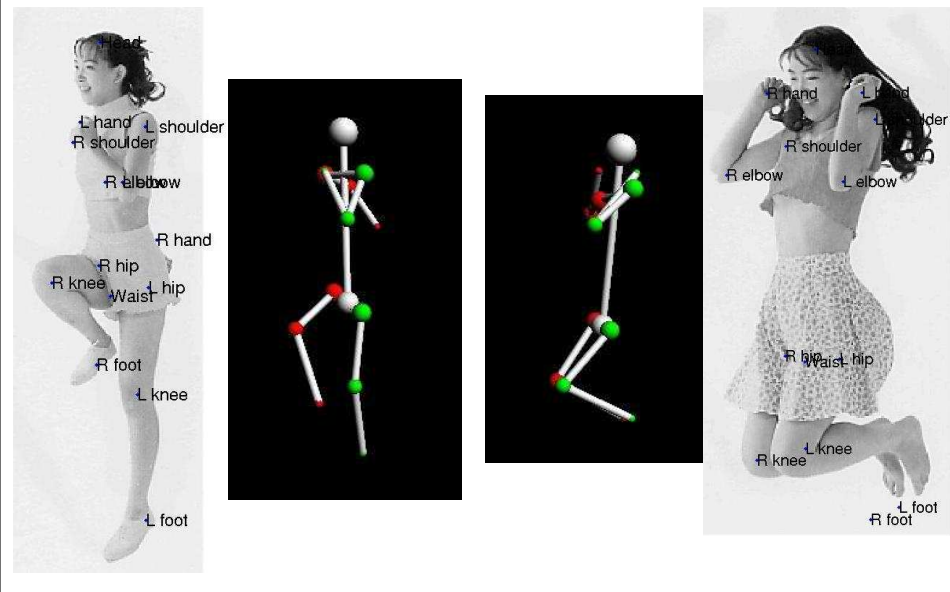
## Image/Video      Stick figure Action

- Stick figures can be specified in a variety of ways or at various resolutions (degrees of freedom)
  - 2D joint positions
  - 3D joint positions
  - Joint angles
- Complete representation
- Evidence that it is effectively computable

# Human Body Configurations



# Human Body Configurations



## Mathematical Challenges

- Modeling shape variation
- Nearest neighbor search in high dimensions
- Combining statistical optimality with computational efficiency
- Reconstruction algorithms for novel sensing modalities