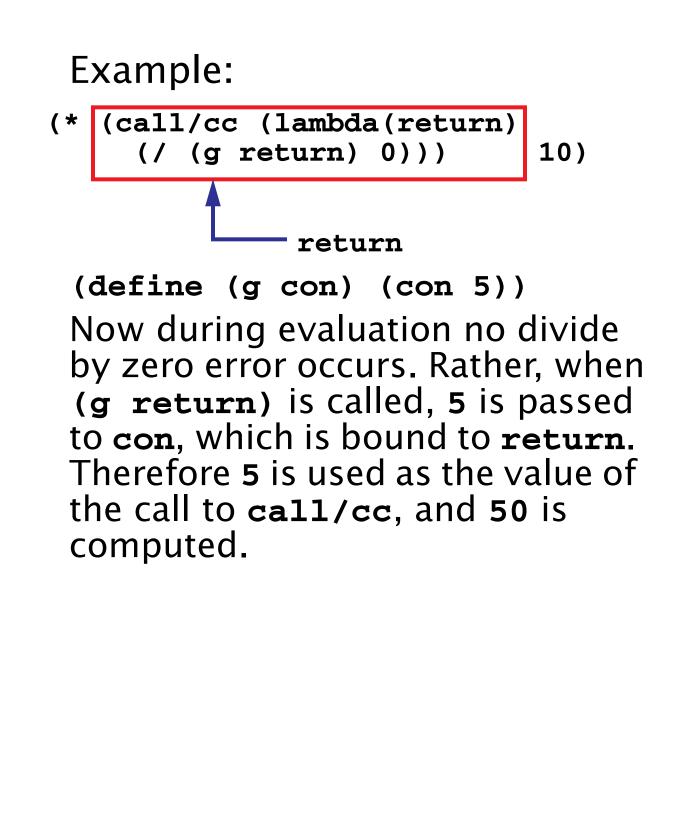
# **CURRENT CONTINUATIONS**

What is the current continuation? It is itself a function of one argument. The current continuation function represents the execution context within which the **call/cc** appears. The argument to the continuation is a value to be substituted as the return value of call/cc in that execution context. For example, given (+ (fct n) 3) the current continuation for (fct n) is (lambda (x) (+ x 3) Given (\* 2 (+ (fct z) 10)) the current continuation for (fct z) is (lambda (m) (\* 2 (+ m 10))

To use **call/cc** to grab a continuation in (say) (+ (fct n) 3) we make (fct n) the body of a function of one argument. Call that argument **return**. We therefore build (lambda (return) (fct n)) Then (call/cc (lambda (return) (fct n))) binds the current continuation to **return** and executes (fct n). We can ignore the current continuation bound to return and do a normal return OY we can use **return** to force a return to the calling context of the call/cc. The call (return value) forces **value** to be returned as the value

of call/cc in its context of call.



## **Continuations are Just Functions**

Continuations may be saved in variables or data structures and called in the future to "reactive" a completed or suspended computation.

```
(define CC ())
(define (F)
  (let (
      (v (call/cc
          (lambda(here)
              (set! CC here)
              1))))
      (display "The ans is: ")
      (display v)
      (newline)
) )
This displays The ans is: 1
At any time in the future, (cc 10)
will display The ans is: 10
```

# List Multiplication Revisited

```
We can use call/cc to
reimplement the original *list to
force an immediate return of 0
(much like a throw in Java):
(define (*listc L return)
  (cond
    ((null? L) 1)
    ((= 0 (car L)) (return 0))
    (else (* (car L)
        (*listc (cdr L) return)))
))
(define (*list L)
  (call/cc
   (lambda (return)
     (*listc L return)
  ))
)
```

A o in i forces a call of (return o) which makes o the value of call/cc.

#### INTERACTIVE REPLACEMENT OF Error Values

Using continuations, we can also redo **\*listE** so that zeroes can be replaced interactively! Multiple zeroes (in both original and replacement values) are correctly handled.

```
(define (*list L)
 (let (
    (V (call/cc
        (lambda (here)
            (*liste L here))))))
    (if (number? V)
        V
        (begin
        (display
        "Enter new value for 0")
        (newline) (newline)
        (V (read))
    )
    )
)
```

If a zero is seen, **\*liste** passes back to the caller (via **return**) a continuation that will set the next value of **value**. This value is checked, so if it is itself zero, a substitute is requested. Each occurrence of zero forces a return to the caller for a substitute value.

# Implementing Coroutines with call/cc

Coroutines are a very handy generalization of subroutines. A coroutine may *suspend* its execution and later *resume* from the point of suspension. Unlike subroutines, coroutines do no have to complete their execution before they return.

Coroutines are useful for computation of long or infinite streams of data, where we wish to compute some data, use it, compute additional data, use it, etc.

Subroutines aren't always able to handle this, as we may need to save a lot of internal state to resume with the correct next value.

#### Producer/Consumer using Coroutines

The example we will use is one of a consumer of a potentially infinite stream of data. The next integer in the stream (represented as an unbounded list) is read. Call this value n. Then the next n integers are read and summed together. The answer is printed, and the user is asked whether another sum is required. Since we don't know in advance how many integers will be needed, we'll use a coroutine to produce the data list in segments, requesting another segment as necessary.

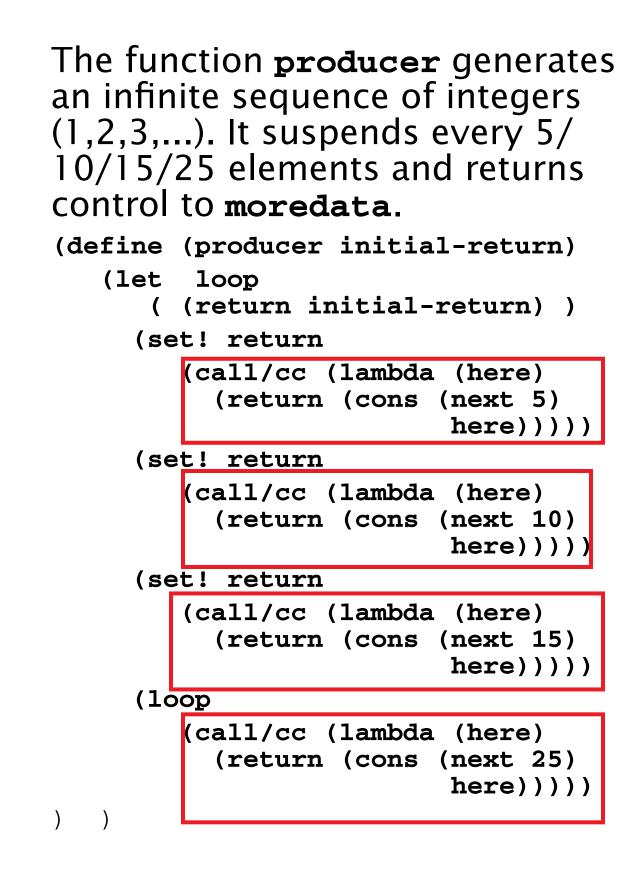
```
(define (consumer)
  (next 0); reset next function
  (let loop ((data (moredata)))
    (let (
     (sum+restoflist
       (sum-n-elems (car data)
           (cons 0 (cdr data)))))
      (display (car sum+restoflist))
      (newline)
      (display "more? ")
      (if (equal? (read) 'y)
        (if (= 1)
            (length sum+restoflist))
         (loop (moredata))
         (loop (cdr sum+restoflist))
        )
        #t ; Normal completion
      )
    )
 )
)
```

```
Next, we'll consider sum-n-
elems, which adds the first
element of list (a running sum) to
the next n elements on the list.
We'll use moredata to extend the
data list as needed.
(define (sum-n-elems n list)
  (cond
     ((= 0 n) list)
     ((null? (cdr list))
      (sum-n-elems n
       (cons (car list)(moredata))))
     (else
      (sum-n-elems (- n 1)
        (cons (+ (car list)
                 (cadr list))
              (cddr list))))
   )
)
```

The function moredata is called whenever we need more data. Initially a producer function is called to get the initial segment of data. producer actually returns the next data segment plus a continuation (stored in producer-cc) used to resume execution of producer when the next data segment is required.

```
(define moredata
 (let ( (producer-cc () ) )
   (lambda ()
     (let (
       (data+cont
         (if (null? producer-cc)
             (call/cc (lambda (here)
                (producer here)))
             (call/cc (lambda (here)
                (producer-cc here)))
         )
        ))
        (set! producer-cc
               (cdr data+cont))
        (car data+cont)
     )
   )
 )
)
```

```
Function (next z) returns the
next z integers in an infinite
sequence that starts at 1. A value
z=0 is a special flag indicating
that the sequence should be reset
to start at 1.
(define next
  (let ( (i 1))
    (lambda (z)
      (if (= 0 z))
        (set! i 1)
        (let loop
           ((cnt z) (val i) (ints () ))
              (if (> cnt 0)
                  (100p (- cnt 1))
                        (+ val 1)
                        (append ints
                         (list val)))
                  (begin
                     (set! i val)
                     ints
                  )
              )
        )
)))))
```



# **Reading Assignment**

 MULTILISP: a language for concurrent symbolic computation, by Robert H. Halstead (linked from class web page)

## LAZY EVALUATION

Lazy evaluation is sometimes called "call by need." We do an evaluation when a value is used; not when it is defined.

Scheme provides for lazy evaluation:

(delay expression)

Evaluation of **expression** is delayed. The call returns a "promise" that is essentially a lambda expression.

(force promise)

A promise, created by a call to **delay**, is evaluated. If the promise has already been evaluated, the value computed by the first call to **force** is reused.

```
Example:
Though and is predefined, writing
a correct implementation for it is
a bit tricky.
The obvious program
(define (and A B)
  (if A
      B
      #f
  )
)
is incorrect since в is always
evaluated whether it is needed or
not. In a call like
(and (not (= i 0)) (> (/ j i) 10))
unnecessary evaluation might be
fatal.
```

```
An argument to a function is strict
if it is always used. Non-strict
arguments may cause failure if
evaluated unnecessarily.
```

```
With lazy evaluation, we can define a more robust and function:
```

```
(define (and A B)
  (if A
      (force B)
      #f
    )
)
This is called as:
(and (not (= i 0))
    (delay (> (/ j i) 10)))
Note that making the programmer
remember to add a call to delay
is unappealing.
```

Delayed evaluation also allows us a neat implementation of suspensions.

The following definition of an infinite list of integers clearly fails:

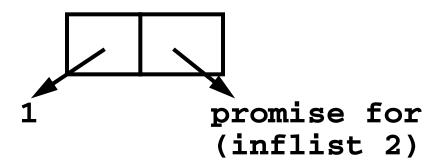
```
(define (inflist i)
```

(cons i (inflist (+ i 1))))
But with use of delays we get the
desired effect in finite time:

```
(define (inflist i)
```

(cons i

(delay (inflist (+ i 1)))))
Now a call like (inflist 1)
creates



#### We need to slightly modify how we explore suspended infinite lists. We can't redefine **car** and **cdr** as these are far too fundamental to tamper with. Instead we'll define **head** and **tail** to do much the same job: (**define head car**) (**define (tail L**)

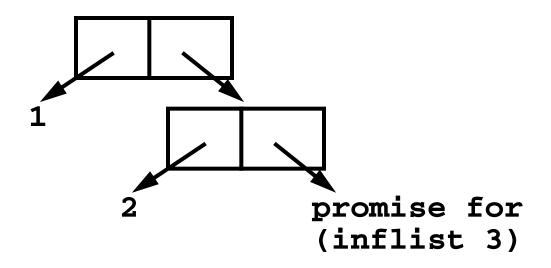
(force (cdr L)))

**head** looks at **car** values which are fully evaluated.

**tail** forces one level of evaluation of a delayed **cdr** and saves the evaluated value in place of the suspension (promise). Given

(define IL (inflist 1))

(head (tail IL)) returns 2 and expands IL into



# Exploiting Parallelism

Conventional procedural programming languages are difficult to compile for multiprocessors.

Frequent assignments make it difficult to find independent computations.

Consider (in Fortran):

```
do 10 I = 1,1000
X(I) = 0
A(I) = A(I+1)+1
B(I) = B(I-1)-1
C(I) = (C(I-2) + C(I+2))/2
10 continue
```

This loop defines 1000 values for arrays **x**, **A**, **B** and **C**.

Which computations can be done in parallel, partitioning parts of an array to several processors, each operating independently?

- x(I) = 0 Assignments to x can be readily parallelized.
- A(I) = A(I+1)+1
  Each update of A(I) uses an A(I+1)
  value that is not yet changed. Thus
  a whole array of new A values can
  be computed from an array of "old"
  A values in parallel.

B(I) = B(I-1)-1 This is less obvious. Each B(I) uses B(I-1) which is defined in terms of B(I-2), etc. Ultimately all new B values depend only on B(0) and I. That is, B(I) = B(0) - I. So this computation can be parallelized, but it takes a fair amount of insight to realize it. C(I) = (C(I-2) + C(I+2))/2 It is clear that even and odd elements of c don't interact. Hence two processors could compute even and odd elements of c in parallel. Beyond this, since both earlier and later c values are used in each computation of an element, no further means of parallel evaluation is evident. Serial evaluation will probably be needed for even or odd values.

## Exploiting Parallelism in Scheme

Assume we have a sharedmemory multiprocessor. We might be able to assign different processors to evaluate various independent subexpressions.

For example, consider

(map (lambda(x) (\* 2 x))

(1 2 3 4 5)) We might assign a processor to each list element and compute the lambda function on each concurrently:

