

## **19. Data Cache Optimizations**

- **Locality Optimizations**

**Cluster accesses of data values both spatially (within a cache line) and temporally (for repeated use).**

*Loop interchange and loop tiling improve temporal locality.*

- **Conflict Optimizations**

**Adjust data locations so that data used consecutively and repeatedly don't share the same cache location.**

## **20. Instruction Cache Optimizations**

**Instructions that are repeatedly executed should be accessed from the instruction cache rather than the secondary cache or memory. Loops and “hot” instruction sequences should fit within the cache.**

**Temporally close instruction sequences should not map to conflicting cache**

# Basic Blocks

**A basic block is a linear sequence of instructions containing no branches except at the very end.**

**A basic block is always executed sequentially as a unit.**

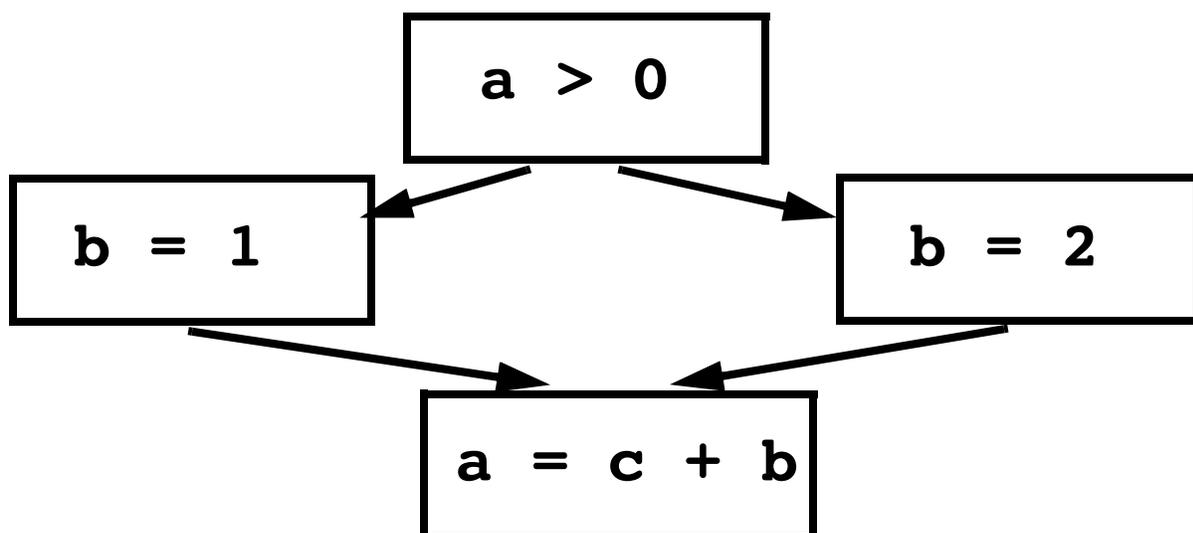
# Control Flow Graphs

**A Control Flow Graph (CFG) models possible execution paths through a program.**

**Nodes are basic blocks and arcs are potential transfers of control.**

**For example,**

```
if (a > 0)  
    b = 1;  
else b = 2;  
a = c + b;
```



**For a Basic Block  $b$ :**

**Let  $\text{Preds}(b)$  = the set of basic blocks that are Immediate Predecessors of  $b$  in the CFG.**

**Let  $\text{Succ}(b)$  = the set of basic blocks that are Immediate Successors to  $b$  in the CFG.**

# Data Flow Problems

**A data flow problem is a program analysis computed on a control flow graph.**

**A data flow problem may be *forward* (following a program's control flow) or *reverse* (opposite a program's control flow).**

**Informally, forward analyses “remember the past” while reverse analyses “predict the future.”**

**Some analyses determine that an event *may* have occurred, while others determine that an event *must* have occurred.**

**Some analyses compute a set of values, while others are Boolean-valued.**

**Two important data flow problems are *Reaching Definitions* and *Liveness*.**

**For a given use of a variable  $v$  reaching definitions tell us which assignments to  $v$  may reach (affect) the current value of  $v$ . Reaching definition analysis is useful in both optimization and debugging.**

**Liveness analysis tells us at a particular point in a program whether the current value of variable  $v$  will ever be used. A variable that is not live is dead. A dead value need not be kept in memory, or perhaps even be computed.**

# Reaching Definitions

**For a Basic Block  $b$  and Variable  $V$ :**

**Let  $\text{DefsIn}(b)$  = the set of basic blocks that contain definitions of  $V$  that reach (may be used in) the beginning of Basic Block  $b$ .**

**Let  $\text{DefsOut}(b)$  = the set of basic blocks that contain definitions of  $V$  that reach (may be used in) the end of Basic Block  $b$ .**

**The sets  $\text{Preds}$  and  $\text{Succ}$  are derived from the structure of the CFG.**

**They are given as part of the definition of the CFG.**

**DefsIn and DefsOut must be computed, using the following rules:**

**1. If Basic Block  $b$  contains a definition of  $V$  then**

$$\mathbf{DefsOut}(b) = \{b\}$$

**2. If there is no definition to  $V$  in  $b$  then**  
**DefsOut( $b$ ) = DefsIn( $b$ )**

**3. For the First Basic Block,  $b_0$ :**

$$\mathbf{DefsIn}(b_0) = \phi$$

**4. For all Other Basic Blocks**

$$\mathbf{DefsIn}(b) = \bigcup_{p \in \text{Preds}(b)} \mathbf{DefsOut}(p)$$

# Liveness Analysis

**For a Basic Block  $b$  and Variable  $V$ :**

**LiveIn( $b$ ) = true if  $V$  is Live (will be used before it is redefined) at the beginning of  $b$ .**

**LiveOut( $b$ ) = true if  $V$  is Live (will be used before it is redefined) at the end of  $b$ .**

**LiveIn and LiveOut are computed, using the following rules:**

**1. If Basic Block  $b$  has no successors then**

**LiveOut( $b$ ) = false**

**2. For all Other Basic Blocks**

**LiveOut( $b$ ) =  $\bigvee_{s \in \text{Succ}(b)} \text{LiveIn}(s)$**

**3. LiveIn(b) =**

**If V is used before it is defined in  
Basic Block b**

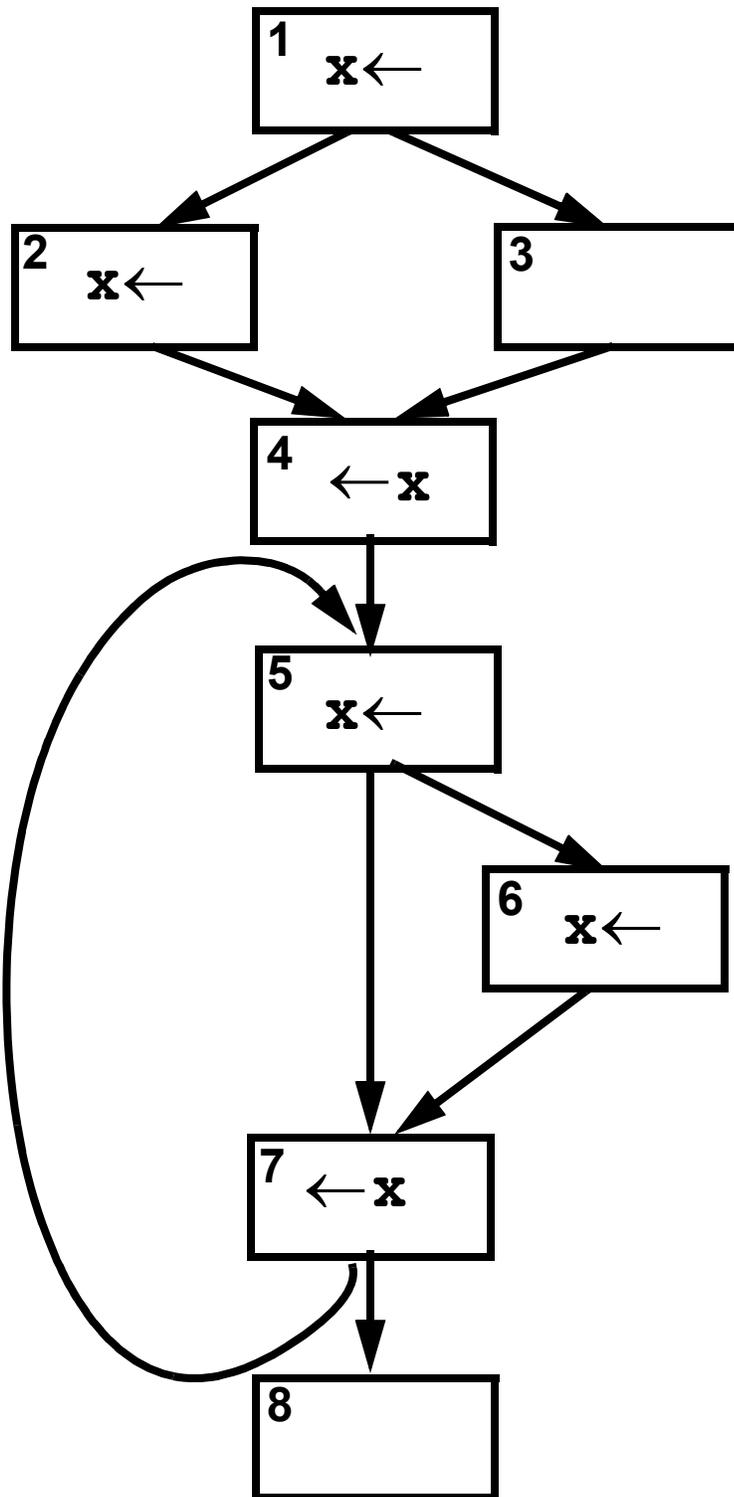
**Then true**

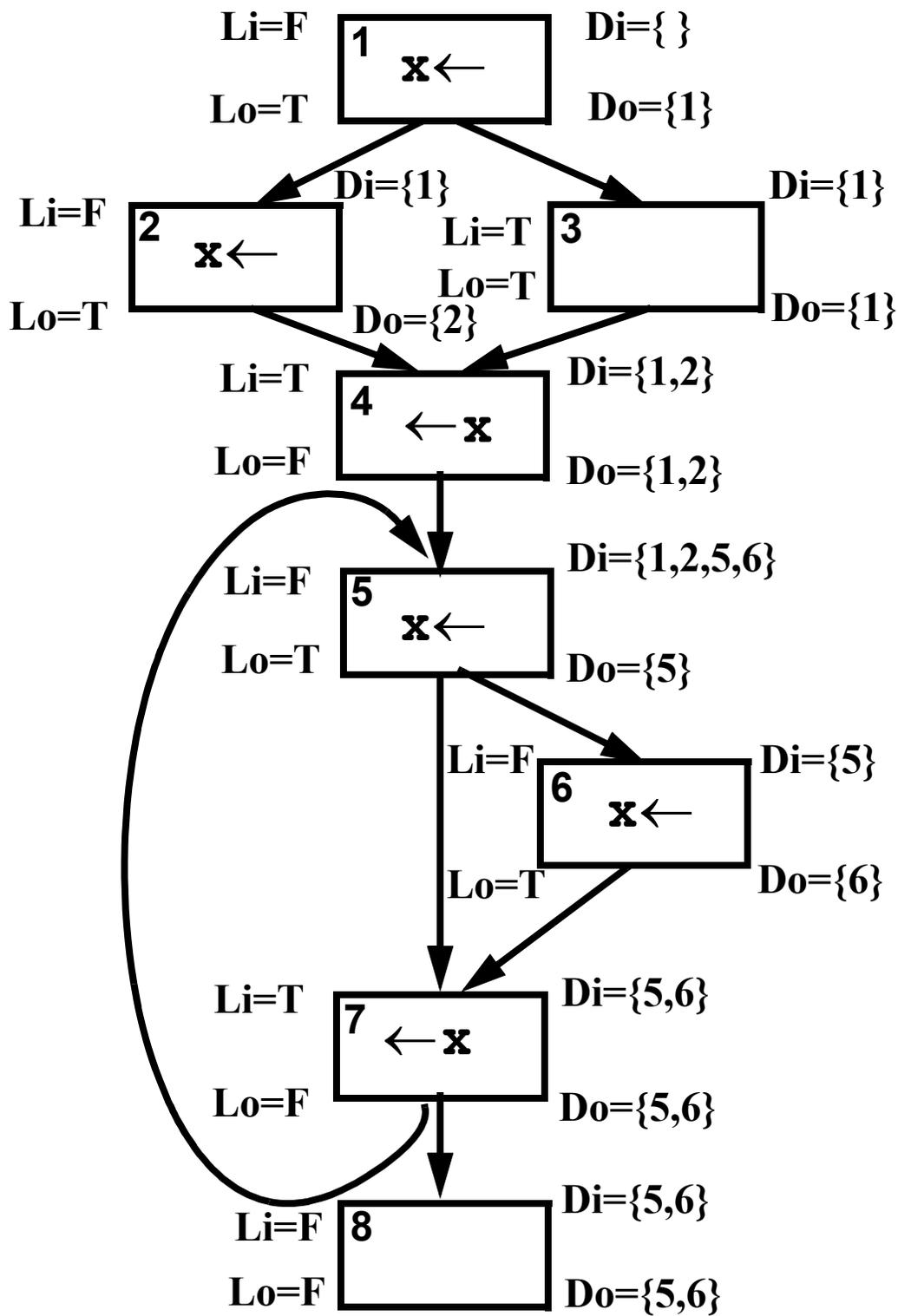
**Elsif V is defined before it is  
used in Basic Block b**

**Then false**

**Else LiveOut(b)**

# Example





# Reading Assignment

- **Section 14.3 - 14.4 of CaC**

# Data Flow Frameworks

- **Data Flow Graph:**

**Nodes of the graph are basic blocks or individual instructions.**

**Arcs represent flow of control.**

**Forward Analysis:**

**Information flow is the same direction as control flow.**

**Backward Analysis:**

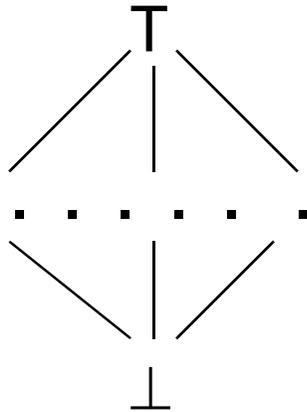
**Information flow is the opposite direction as control flow.**

**Bi-directional Analysis:**

**Information flow is in both directions. (Not too common.)**

- **Meet Lattice**

**Represents solution space for the data flow analysis.**



- **Meet operation**

**(And, Or, Union, Intersection, etc.)**

**Combines solutions from predecessors or successors in the control flow graph.**

- **Transfer Function**

**Maps a solution at the top of a node to a solution at the end of the node (forward flow)**

*or*

**Maps a solution at the end of a node to a solution at the top of the node (backward flow).**

# **Example: Available Expressions**

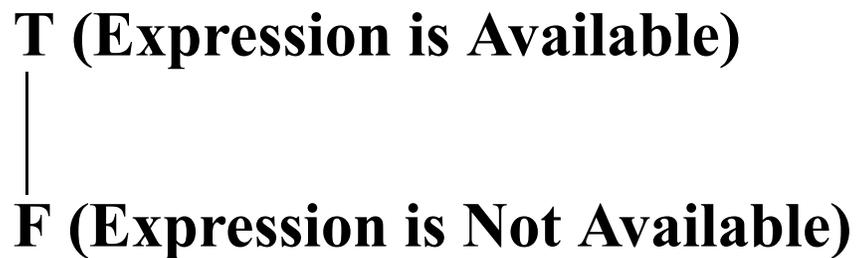
**This data flow analysis determines whether an expression that has been previously computed may be reused.**

**Available expression analysis is a forward flow problem—computed expression values flow forward to points of possible reuse.**

**The best solution is True—the expression may be reused.**

**The worst solution is False—the expression may not be reused.**

## The Meet Lattice is:



**As initial values, at the top of the start node, nothing is available.**

**Hence, for a given expression,**

$$\text{AvailIn}(b_0) = F$$

**We choose an expression, and consider all the variables that contribute to its evaluation.**

**Thus for  $e_1 = a + b - c$ ,  $a$ ,  $b$  and  $c$  are  $e_1$ 's operands.**

**The transfer function for  $e_1$  in block  $b$  is defined as:**

**If  $e_1$  is computed in  $b$  after any assignments to  $e_1$ 's operands in  $b$**

**Then  $\text{AvailOut}(b) = T$**

**Elsif any of  $e_1$ 's operands are changed**

**after the last computation of  $e_1$  or  $e_1$ 's operands are changed without any computation of  $e_1$**

**Then  $\text{AvailOut}(b) = F$**

**Else  $\text{AvailOut}(b) = \text{AvailIn}(b)$**

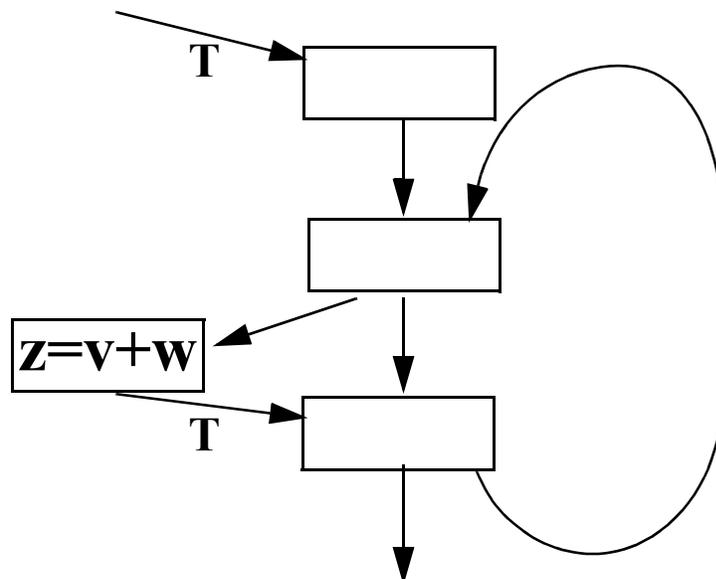
**The meet operation (to combine solutions) is:**

$$\text{AvailIn}(b) = \text{AND}_{p \in \text{Pred}(b)} \text{AvailOut}(p)$$



# Circularities Require Care

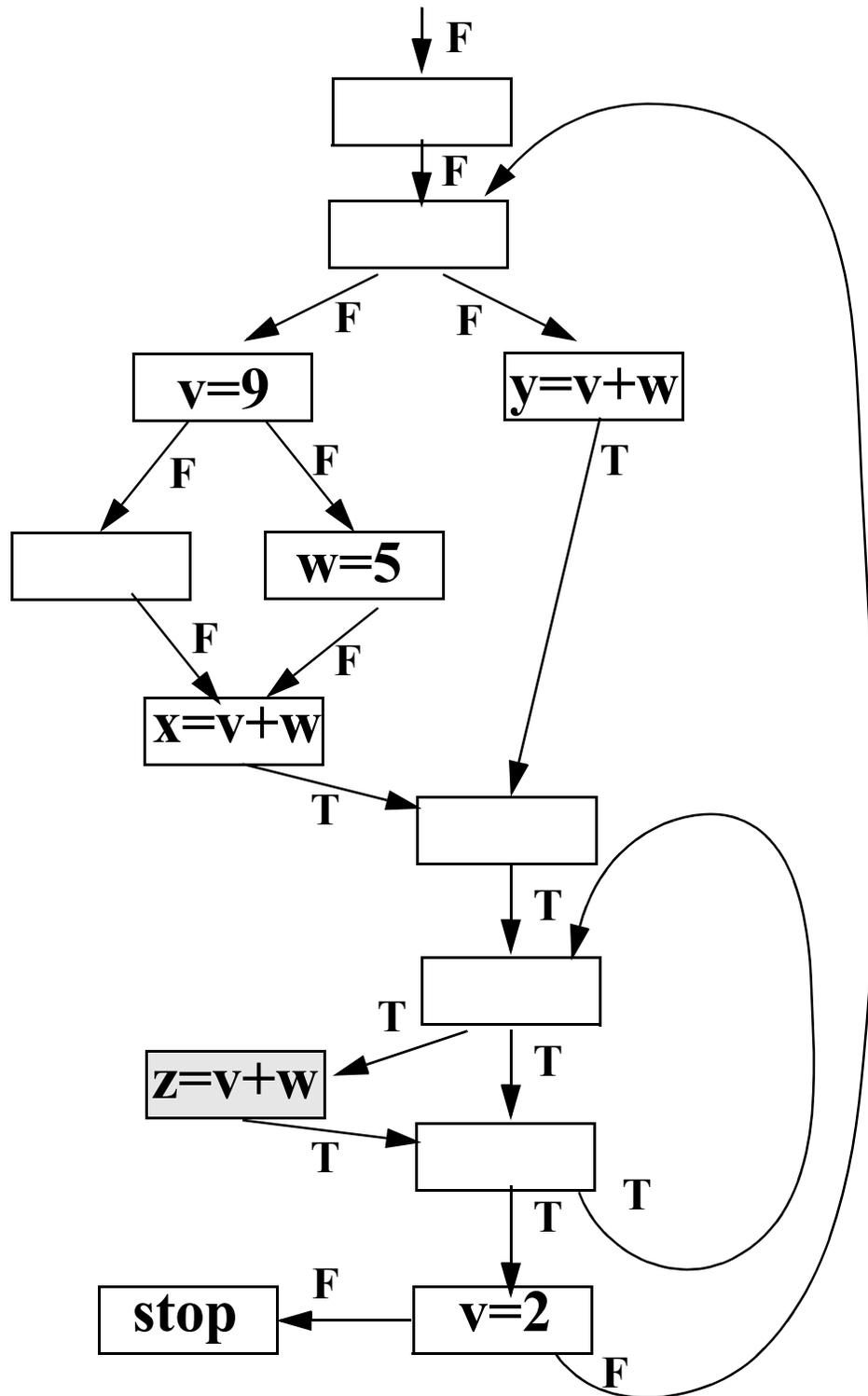
Since data flow values can depend on themselves (because of loops), care is required in assigning initial “guesses” to unknown values.



**Consider**

**If the flow value on the loop backedge is initially set to false, it can never become true. (Why?)**

**Instead we should use True, the *identity* for the AND operation.**



# Very Busy Expressions

**This is an interesting variant of available expression analysis.**

**An expression is *very busy* at a point if it is *guaranteed* that the expression will be computed at some time in the future.**

**Thus starting at the point in question, the expression must be reached before its value changes.**

**Very busy expression analysis is a backward flow analysis, since it propagates information about future evaluations backward to “earlier” points in the computation.**

**The meet lattice is:**

**T (Expression is Very Busy)**



**F (Expression is Not Very Busy)**

**As initial values, at the end of all exit nodes, nothing is very busy.**

**Hence, for a given expression,**

**$\text{VeryBusyOut}(b_{\text{last}}) = \mathbf{F}$**

**The transfer function for  $e_1$  in block  $b$  is defined as:**

**If  $e_1$  is computed in  $b$  before any of its operands**

**Then  $\text{VeryBusyIn}(b) = T$**

**Elsif any of  $e_1$ 's operands are changed**

**before  $e_1$  is computed**

**Then  $\text{VeryBusyIn}(b) = F$**

**Else  $\text{VeryBusyIn}(b) = \text{VeryBusyOut}(b)$**

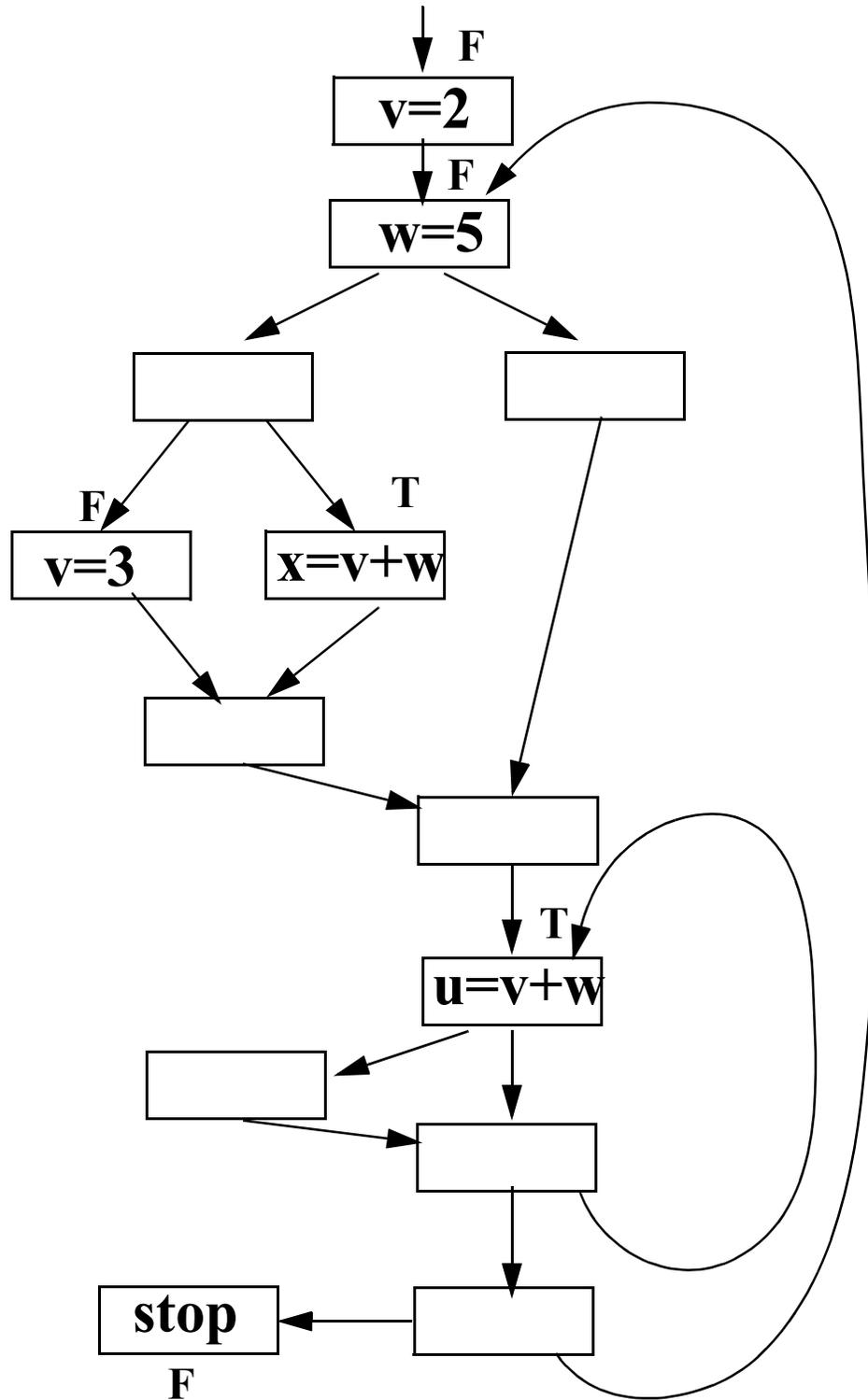
**The meet operation (to combine solutions) is:**

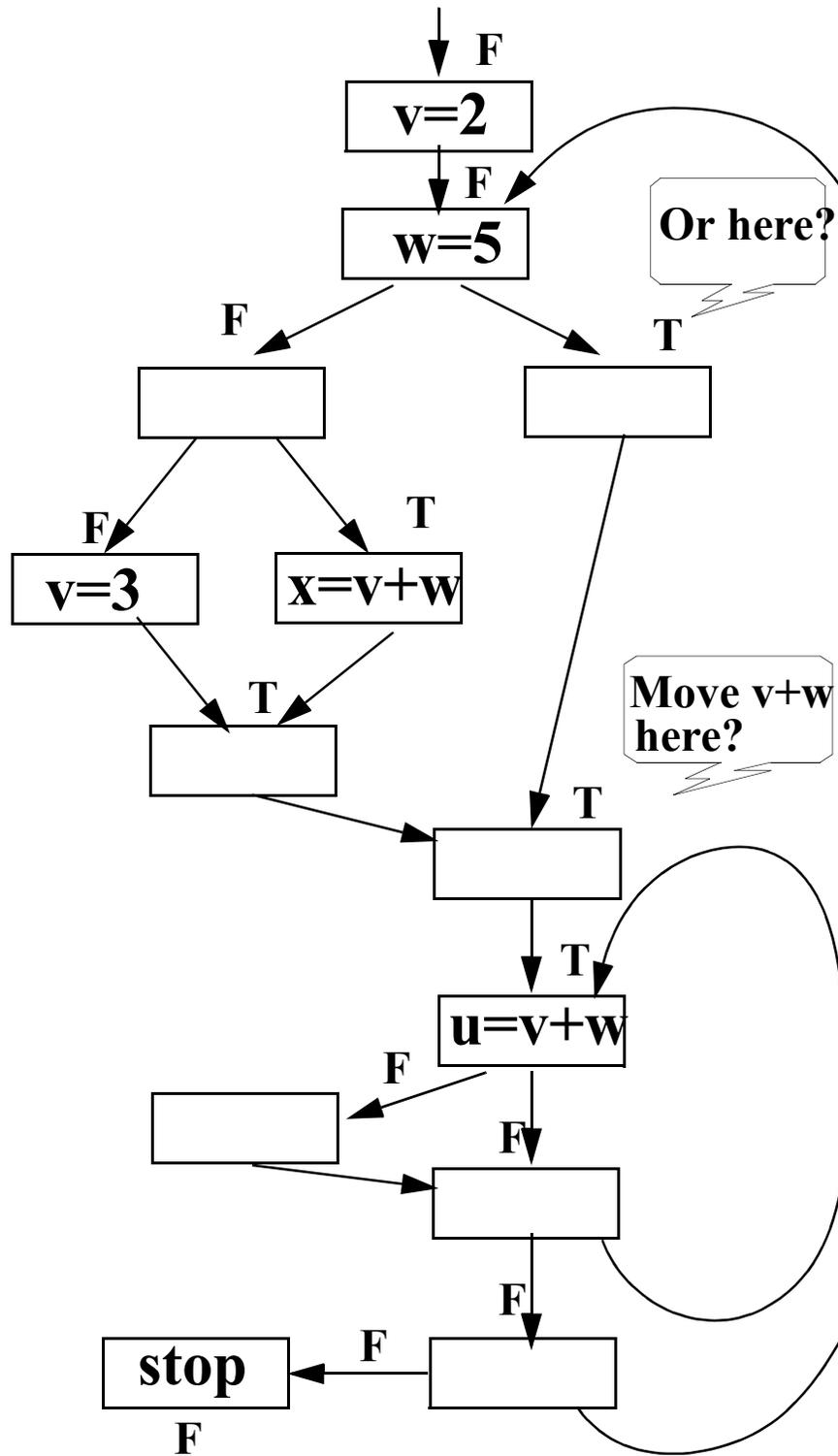
**$\text{VeryBusyOut}(b) =$**

**$\text{ANDVeryBusyIn}(s)$**

**$s \in \text{Succ}(b)$**

# Example: $e_1 = v + w$





# Identifying Identical Expressions

**We can hash expressions, based on hash values assigned to operands and operators. This makes recognizing potentially redundant expressions straightforward.**

**For example, if  $H(a) = 10$ ,  $H(b) = 21$  and  $H(+)$  = 5, then (using a simple product hash),  
 $H(a+b) = 10 \times 21 \times 5 \text{ Mod TableSize}$**

# Effects of Aliasing and Calls

**When looking for assignments to operands, we must consider the effects of pointers, formal parameters and calls.**

**An assignment through a pointer (e.g, `*p = val`) *kills* all expressions dependent on variables `p` might point too. Similarly, an assignment to a formal parameter kills all expressions dependent on variables the formal might be bound to.**

**A call kills all expressions dependent on a variable changeable during the call.**

**Lacking careful alias analysis, pointers, formal parameters and calls can kill all (or most) expressions.**

# **Very Busy Expressions and Loop Invariants**

**Very busy expressions are ideal candidates for invariant loop motion.**

**If an expression, invariant in a loop, is also very busy, we know it must be used in the future, and hence evaluation outside the loop must be worthwhile.**

```

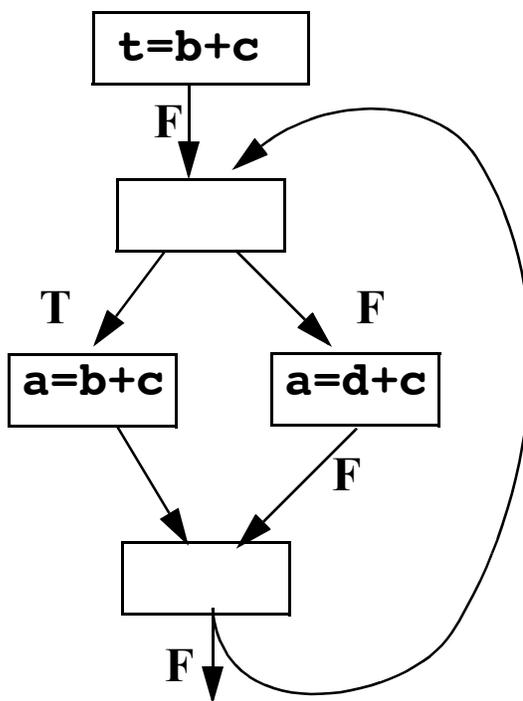
for (...) {
  if (...)
    a=b+c;
  else a=d+c;}

```

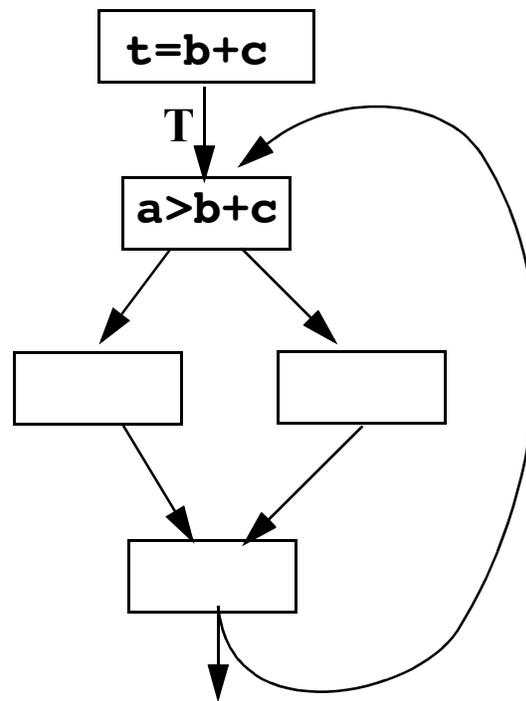
```

for (...) {
  if (a>b+c)
    x=1;
  else x=0;}

```



**b+c is not very busy  
at loop entrance**



**b+c is very busy  
at loop entrance**

# Reaching Definitions

**We have seen reaching definition analysis formulated as a set-valued problem. It can also be formulated on a per-definition basis.**

**That is, we ask “What blocks does a particular definition to  $v$  reach?”**

**This is a boolean-valued, forward flow data flow problem.**

**Initially,  $\text{DefIn}(b_0) = \text{false}$ .**

**For basic block  $b$ :**

**$\text{DefOut}(b) =$**

**If the definition being analyzed is  
the last definition to  $v$  in  $b$**

**Then True**

**Elsif any other definition to  $v$   
occurs**

**in  $b$**

**Then False**

**Else  $\text{DefIn}(b)$**

**The meet operation (to combine  
solutions) is:**

$$\text{DefIn}(b) = \text{OR}_{p \in \text{Pred}(b)} \text{DefOut}(p)$$

**To get all reaching definition, we do  
a series of single definition analyses.**

# Live Variable Analysis

This is a boolean-valued, backward flow data flow problem.

Initially,  $\text{LiveOut}(b_{\text{last}}) = \text{false}$ .

For basic block  $b$ :

$\text{LiveIn}(b) =$

If the variable is used before it is defined in  $b$

Then True

Elsif it is defined before it is used in  $b$

Then False

Else  $\text{LiveOut}(b)$

The meet operation (to combine solutions) is:

$$\text{LiveOut}(b) = \text{OR}_{s \in \text{Succ}(b)} \text{LiveIn}(s)$$

# Bit Vectoring Data Flow Problems

The four data flow problems we have just reviewed all fit within a *single* framework.

Their solution values are Booleans (bits).

The meet operation is And or OR.

The transfer function is of the general form

$$\text{Out}(b) = (\text{In}(b) - \text{Kill}_b) \cup \text{Gen}_b$$

or

$$\text{In}(b) = (\text{Out}(b) - \text{Kill}_b) \cup \text{Gen}_b$$

where  $\text{Kill}_b$  is true if a value is “killed” within  $b$  and  $\text{Gen}_b$  is true if a value is “generated” within  $b$ .

**In Boolean terms:**

**$\text{Out}(b) = (\text{In}(b) \text{ AND Not Kill}_b) \text{ OR Gen}_b$**

**or**

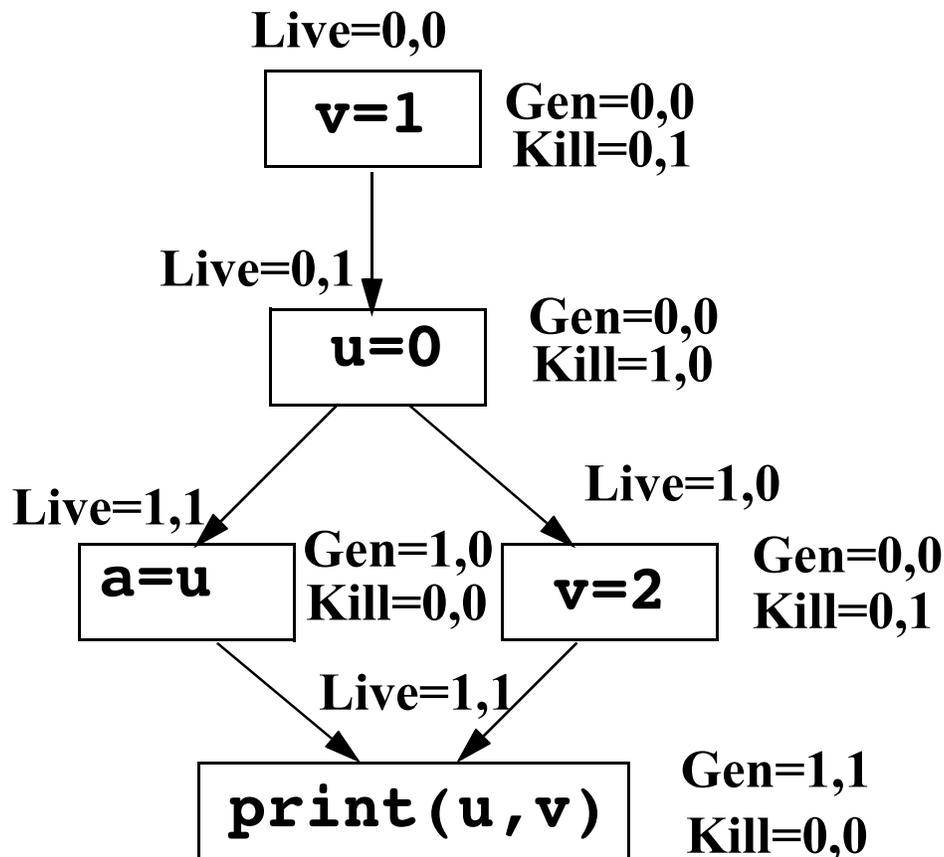
**$\text{In}(b) = (\text{Out}(b) \text{ AND Not Kill}_b) \text{ OR Gen}_b$**

**An advantage of a bit vectoring data flow problem is that we can do a series of data flow problems “in parallel” using a bit vector.**

**Hence using ordinary word-level ANDs, ORs, and NOTs, we can solve 32 (or 64) problems simultaneously.**

# Example

Do live variable analysis for  $u$  and  $v$ , using a 2 bit vector:



We expect *no variable* to be live at the start of  $b_0$ . (Why?)