

Spring 2017

# **SCHEMA REFINEMENT AND NORMAL FORMS**

**[CH 19]**

# Database Design: The Story so Far

- Requirements Analysis
  - Data stored, operations, apps, ...
- Conceptual Database Design
  - Model high-level description of the data, constraints, ER model
- Logical Database Design
  - Choose a DBMS and design a database schema
- Schema Refinement
  - Normalize relations, avoid redundancy, anomalies ...
- Physical Database Design
  - Examine physical database structures like indices, restructure ...
- Security Design

# Normalization

What is a good relational schema? How can we improve it?

- e.g.: Suppliers (name, item, desc, addr, price)

## Redundancy Problems:

1. A supplier supplies two items: **Redundant Storage**
2. Change address of a supplier: **Update Anomaly**
3. Insert a supplier: **Insertion Anomaly**
  - What if the supplier does not supply any items (nulls?)
  - **Record desc for an item that is not supplied by any supplier**
4. Delete the only supplier tuple: **Delete Anomaly**
  - Use nulls?
  - **Delete the last item tuple. Can't make name null. Why?**

Alternative:

# Dealing with Redundancy

- Identify “bad” schemas
  - functional dependencies
- Main refinement technique: decomposition
  - replacing larger relation with smaller ones
- Decomposition should be used judiciously:
  - Is there a reason to decompose a relation?
    - Normal forms: guarantees against (some) redundancy
  - Does decomposition cause any problems?
    - Lossless join
    - Dependency preservation
    - Performance (must join decomposed relations)

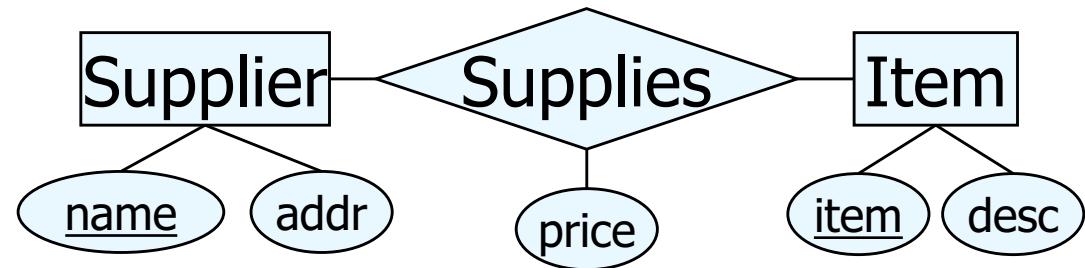
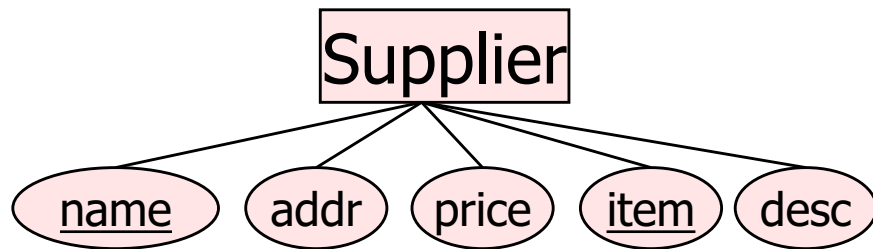
# Functional Dependencies (FDs)

- A form of IC
- $D: X \rightarrow Y$        $X$  and  $Y$  subsets of relation  $R$ 's attributes  
 $t1 \in r, t2 \in r, \Pi_X(t1) = \Pi_X(t2) \Rightarrow \Pi_Y(t1) = \Pi_Y(t2)$
- An FD is a statement about all allowable relations.
  - Based only on application semantics, can't deduce from instances
  - Can simply check if an instance violates FD (and other ICs)
- Consider,  $(X,Y) \rightarrow Z$ . Does this imply  $(X,Y)$  is a key?

X	Y	Z	K
1	1	11	A
1	2	12	A
2	2	22	A
2	2	22	B

Primary Key IC is a special case of FD

# Example: Constraints on Entity Set



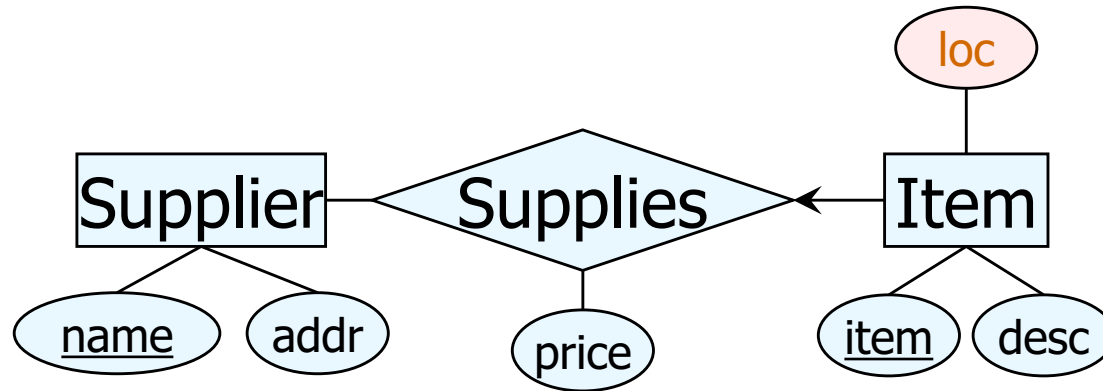
- $S(\underline{\text{name}}, \underline{\text{item}}, \text{desc}, \text{addr}, \text{price})$
- FD:  $\{n, i\} \rightarrow \{n, i, d, a, p\}$
- FD:  $\{n\} \rightarrow \{a\}$
- FD:  $\{i\} \rightarrow \{d\}$
- Decompose to:  $\underline{\text{NA}}, \underline{\text{ID}}, \underline{\text{INP}}$

- $\text{Spl}(\underline{\text{name}}, \underline{\text{item}}, \text{price})$ 
  - FD:  $\{n, i\} \rightarrow \{n, i, p\}$
- $\text{Sup}(\text{name}, \text{addr})$ 
  - FD:  $\{n\} \rightarrow \{n, a\}$
- $\text{Item}(\underline{\text{item}}, \text{desc})$ 
  - FD:  $\{i\} \rightarrow \{i, d\}$

ER design is subjective and can have many E + Rs  
FDs: sanity checks + deeper understanding of schema

Same situation could happen with a relationship set

# Refining an ER Diagram



- IS (item, name, desc, loc, price)  
S (name, addr)
- A supplier keeps all items in the same location  
FD: name → loc
- Solution:

# Inferring FD

- $\text{ename} \rightarrow \text{ejob}, \text{ejob} \rightarrow \text{esal}; \Rightarrow \text{ename} \rightarrow \text{esal}$
- Armstrong's Axioms ( $X, Y, Z$  are sets of attributes):
  - **Reflexivity**: If  $Y \subseteq X$ , then  $X \rightarrow Y$
  - **Augmentation**: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$
  - **Transitivity**: If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- Additional rules (derivable):
  - **Union**: If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
  - **Decomposition**: If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$
- Set of all FD = closure of  $F$ , denoted as  $F^+$
- AA sound: only generates FD in  $F^+$
- AA complete: repeated application generates all FD in  $F^+$



# Decomposition

- Replace a relation with two or more relations
- Problems with decomposition
  1. Some queries become more expensive. (more joins)
  2. **Lossless Join**: Can we reconstruct the original relation from instances of the decomposed relations?
  3. **Dependency Preservation**: Checking some dependencies may require joining the instances of the decomposed relations.

# Lossless Join Decompositions

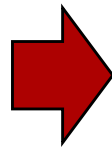
- Relation R, FDs F: Decomposed to X, Y

- Lossless-Join decomposition if:

$$\Pi_X(r) \bowtie \Pi_Y(r) = r \quad \text{for every instance } r \text{ of } R$$

- Note,  $r \subseteq \Pi_X(r) \bowtie \Pi_Y(r)$  is always true, not vice versa, unless the join is lossless
- Can generalize to three more relations

A	B	C
1	2	3
4	5	6
7	2	8



A	B
1	2
4	5
7	2

B	C
2	3
5	6
2	8



A	B	C
1	2	3
4	5	6
7	2	8
1	2	8
7	2	3

# Lossless Join ...

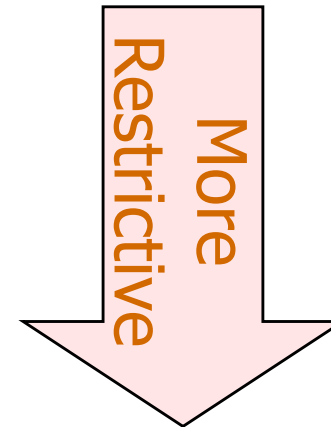
- Relation R, FDs F: Decomposed to X, Y
  - Test: lossless-join w.r.t. F if and only if the closure of F contains:
    - $X \cap Y \rightarrow X$ , or
    - $X \cap Y \rightarrow Y$
  - i.e. attributes common to X and Y contain a key for either X or Y
  - Also, given FD:  $X \rightarrow Y$  and  $X \cap Y = \emptyset$ , the decomposition into R-Y and XY is lossless
    - **X is a key in XY, and appears in both**

# Dependency Preserving Decomposition

- $R(\text{sailor, boat, date}) \quad \{D \rightarrow S, D \rightarrow B\}$   
     $\rightarrow X(\text{sailor, boat})$   
     $Y(\text{boat, date}) \quad \{D \rightarrow B\}$
- To check  $D \rightarrow S$  need to join  $R_1$  and  $R_2$  (expensive)
- Dependency preserving:
  - $R \rightarrow X, Y \quad F^+ = (F_x \cup F_y)^+$ 
    - Note:  $F$  not necessarily  $= F_x \cup F_y$

# Normal Forms

- Is any refinement is needed!
- Normal Forms: guarantees that certain kinds of problems won't occur
  - 1 NF : Atomic values
  - 2 NF : Historical
  - 3 NF : ...
  - BCNF : Boyce-Codd Normal Form
- Role of FDs in detecting redundancy:
  - Relation R with 3 attributes, ABC.
    - No ICs (FDs) hold  $\Rightarrow$  no redundancy.
    - $A \rightarrow B \Rightarrow$  2 or more tuples with the same A value, redundantly have the same B value!



# Boyce-Codd Normal Form (BCNF)

- Reln R with FDs F is in **BCNF** if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (**trivial** FD), or
  - X is a super key
- i.e. all non-trivial FDs over R are key constraints.
- **No redundancy in R** (at least none that FDs detect)
- Most desirable normal form

- Consider a relation in BCNF and FD:  $X \rightarrow A$ , two tuples have the same X value
  - Can the A values be the same (i.e. redundant)?
  - **NO!** X is a key,  $\Rightarrow y1 = y2$ . Not a set!

X	Y	A
x	y1	a
x	y2	?

# 3NF

- Relation R with FDs F is in **3NF** if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  or
  - X is a super key or
  - A is part of some key for R (**prime attribute**)
    - Minimality of a key (not superkey) is crucial!
- BCNF implies 3NF
- e.g.: Sailor (Sailor, Boat, Date, CreditCrd)
  - SBD  $\rightarrow$  SBDC, S  $\rightarrow$  C (**not 3NF**)
  - If C  $\rightarrow$  S, then CBD  $\rightarrow$  SBDC (i.e. CBD is also a key). Now in 3NF!
  - Note redundancy in (S, C); 3NF permits this
  - Compromise used when BCNF not achievable, or perf. Consideration
- Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.