

CS559: Computer Graphics

Lecture 12: OpenGL - Transformation

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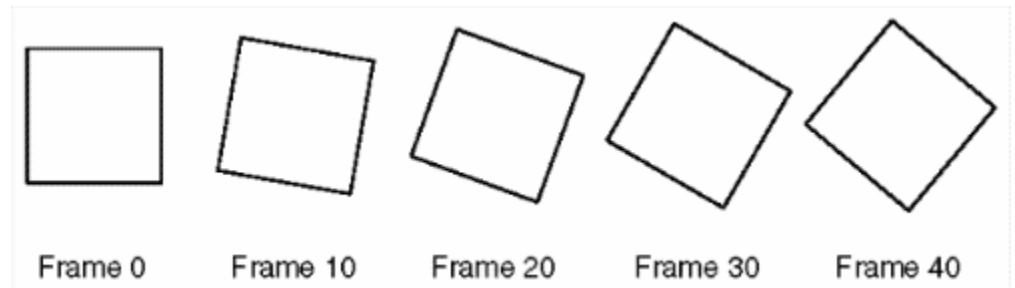
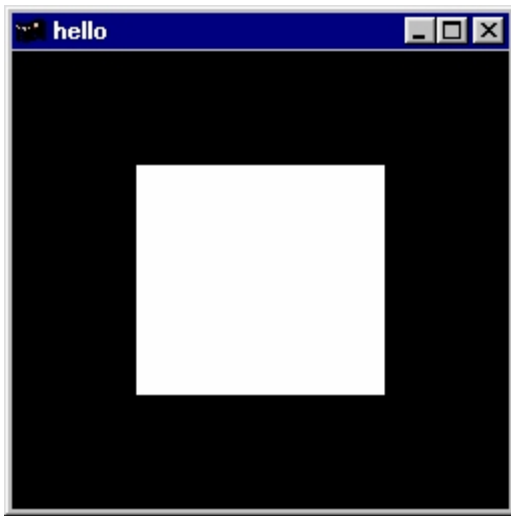
Spring 2008

Today

- Transformation in OpenGL

- Reading
 - Chapter 3

Last time

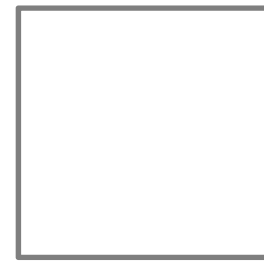


Primitive Details

- `glPolygonMode(GLenum face, GLenum mode);`
 - face: `GL_FRONT`, `GL_BACK`
 - mode: `GL_POINT`, `GL_LINE`, `GL_FILL`



```
glPolygonMode(GL_FRONT, GL_FILL);  
glRectf(0, 0, 100, 100);
```



```
glPolygonMode(GL_BACK, GL_LINE);  
glRectf(0, 0, 100, 100);
```

Primitive Details

- Determine Polygon Orientation

$$\text{area}(P_1P_2P_3P_4)$$

$$= \text{area}(P_1P_2Q_2Q_1) + \text{area}(P_2P_3Q_3Q_2)$$

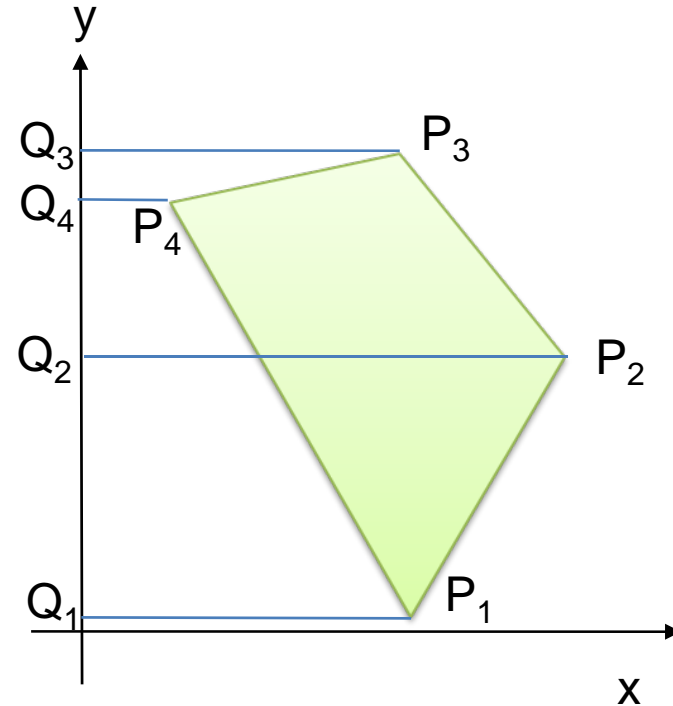
$$- \text{area}(P_3P_4Q_4Q_3) - \text{area}(P_4P_1Q_4Q_1)$$

$$\text{area} = \sum_{n=1}^N \frac{1}{2} (x_n + x_{n+1})(y_{n+1} - y_n)$$

$$= \frac{1}{2} \left(\sum_{n=1}^N x_n y_{n+1} - \sum_{n=1}^N x_n y_n + \sum_{n=1}^N x_{n+1} y_{n+1} - \sum_{n=1}^N x_{n+1} y_n \right)$$

$$= \frac{1}{2} \sum_{n=1}^N (x_n y_{n+1} - x_{n+1} y_n)$$

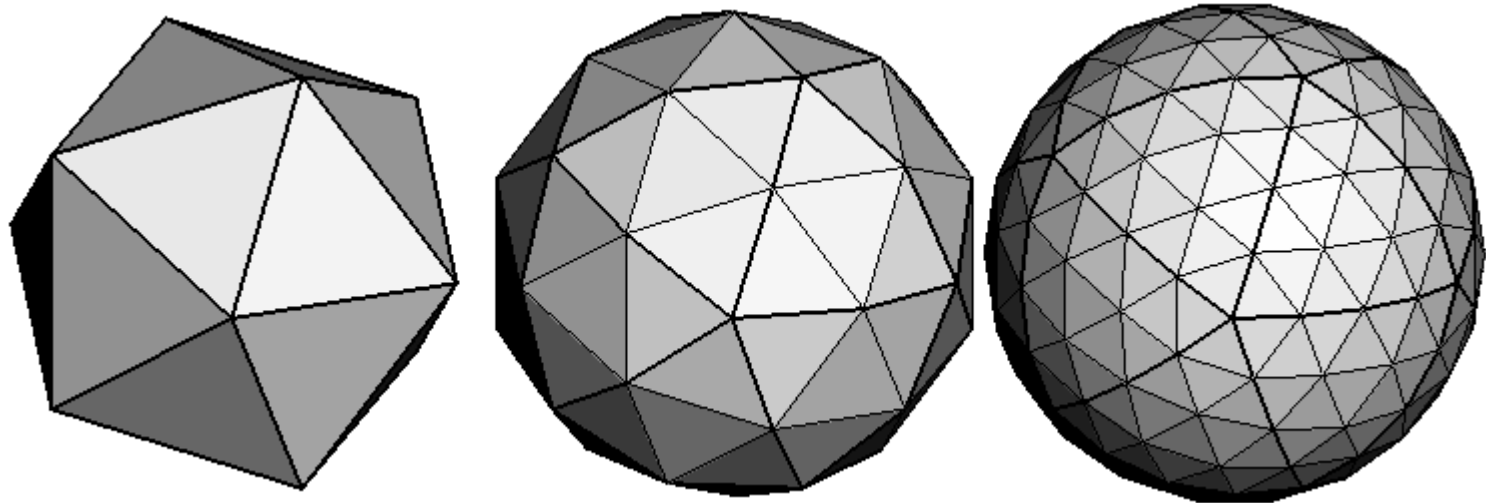
Orientation == sign of the area



Stokes' Theorem

$$\iint_R dx dy = \oint_{\partial R} x dy$$

Icosahedron



Icosahedron

```
//initial icosahedron
Static float t[20][3][3] = {...};

void display(void)
{

}
}
```

Icosahedron

```
//initial icosahedron
Static float t[20][3][3] = {...};

void display(void)
{
    //clear buffer
    //set up viewport and frustum

    if (animation) angle+=0.3;
    if (angle>360) angle-=360.0;

    glLoadIdentity();
    glRotatef(angle,1,0,1);

}
```


Icosahedron

```
//initial icosahedron
Static float t[20][3][3] = {...};

void display(void)
{
    //clear buffer
    //set up viewport and frustum

    if (animation) angle+=0.3;
    if (angle>360) angle-=360.0;

    glLoadIdentity();
    glRotatef(angle,1,0,1);

    // subdivide each face of the triangle
    for (int i = 0; i < 20; i++)
    {
        Subdivide(t[i][0], t[i][1], t[i][2], subdiv);
    }
}
```

Icosahedron

```
//initial icosahedron
Static float t[20][3][3] = {...};

void display(void)
{
    //clear buffer
    //set up viewport and frustum

    if (animation) angle+=0.3;
    if (angle>360) angle-=360.0;

    glLoadIdentity ();
    glRotatef(angle,1,0,1);

    // subdivide each face of the triangle
    for (int i = 0; i < 20; i++)
    {
        Subdivide(t[i][0], t[i][1], t[i][2], subdiv);
    }

    glFlush();
    glutSwapBuffers();
}
```

Icosahedron

```
void Subdivide(GLfloat v1[3], GLfloat v2[3], GLfloat v3[3], int depth)
{
}
}
```

Icosahedron

```
void Subdivide(GLfloat v1[3], GLfloat v2[3], GLfloat v3[3], int depth)
{
    if (depth == 0) {
        glColor3f(0.5,0.5,0.5);
        glBegin(GL_TRIANGLES);
        glVertex3fv(v1);  glVertex3fv(v2);  glVertex3fv(v3);
        glEnd();
    }
}
```

Icosahedron

```
void Subdivide(GLfloat v1[3], GLfloat v2[3], GLfloat v3[3], int depth)
{
    if (depth == 0) {
        glColor3f(0.5,0.5,0.5);
        glBegin(GL_TRIANGLES);
        glVertex3fv(v1); glVertex3fv(v2); glVertex3fv(v3);
        glEnd();
    }
    else
    {
        GLfloat v12[3], v23[3], v31[3];
        for (int i = 0; i < 3; i++) {
            v12[i] = (v1[i]+v2[i])/2.0;
            v23[i] = (v2[i]+v3[i])/2.0;
            v31[i] = (v3[i]+v1[i])/2.0;
        }
        Normalize(v12); Normalize(v23); Normalize(v31);
    }
}
```

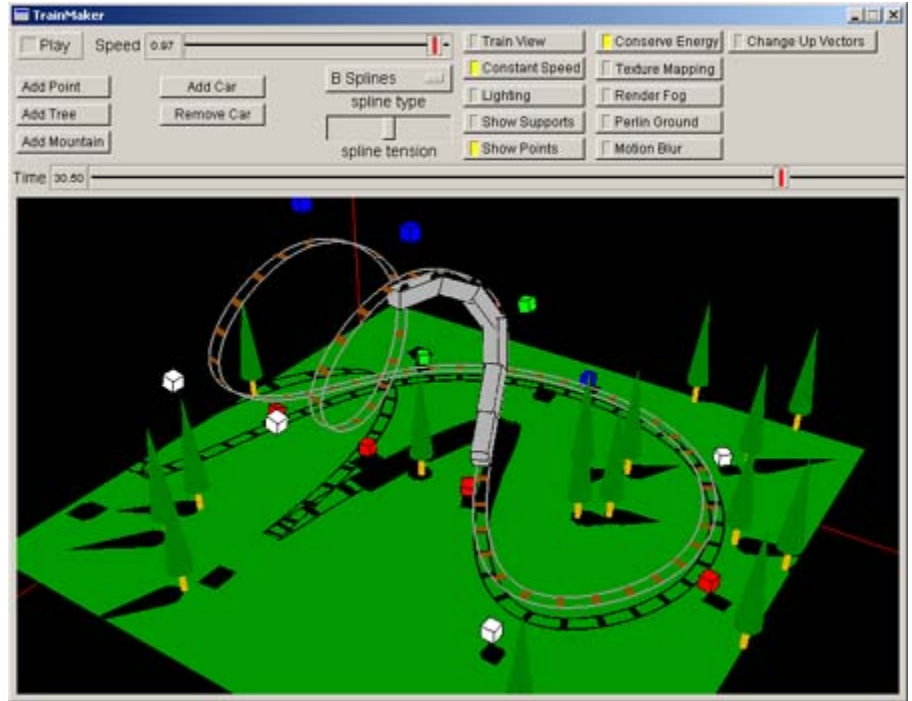
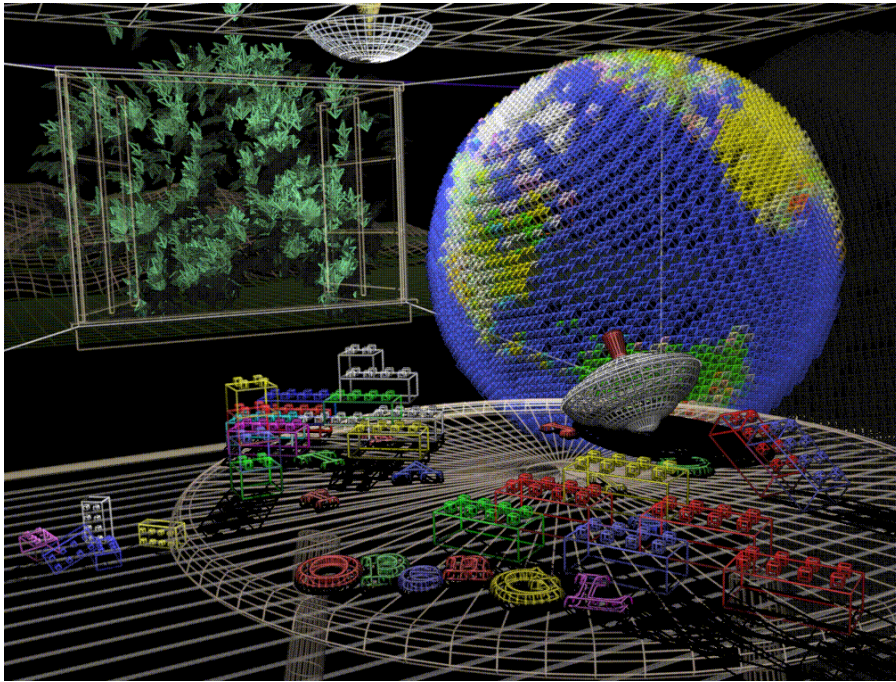
Icosahedron

```
void Subdivide(GLfloat v1[3], GLfloat v2[3], GLfloat v3[3], int depth)
{
    if (depth == 0) {
        glColor3f(0.5,0.5,0.5);
        glBegin(GL_TRIANGLES);
        glVertex3fv(v1); glVertex3fv(v2); glVertex3fv(v3);
        glEnd();
    }
    else
    {
        GLfloat v12[3], v23[3], v31[3];
        for (int i = 0; i < 3; i++) {
            v12[i] = (v1[i]+v2[i])/2.0;
            v23[i] = (v2[i]+v3[i])/2.0;
            v31[i] = (v3[i]+v1[i])/2.0;
        }
        Normalize(v12); Normalize(v23); Normalize(v31);
        Subdivide(v1, v12, v31, depth-1);
        Subdivide(v2, v23, v12, depth-1);
        Subdivide(v3, v31, v23, depth-1);
        Subdivide(v12, v23, v31, depth-1);
    }
}
```

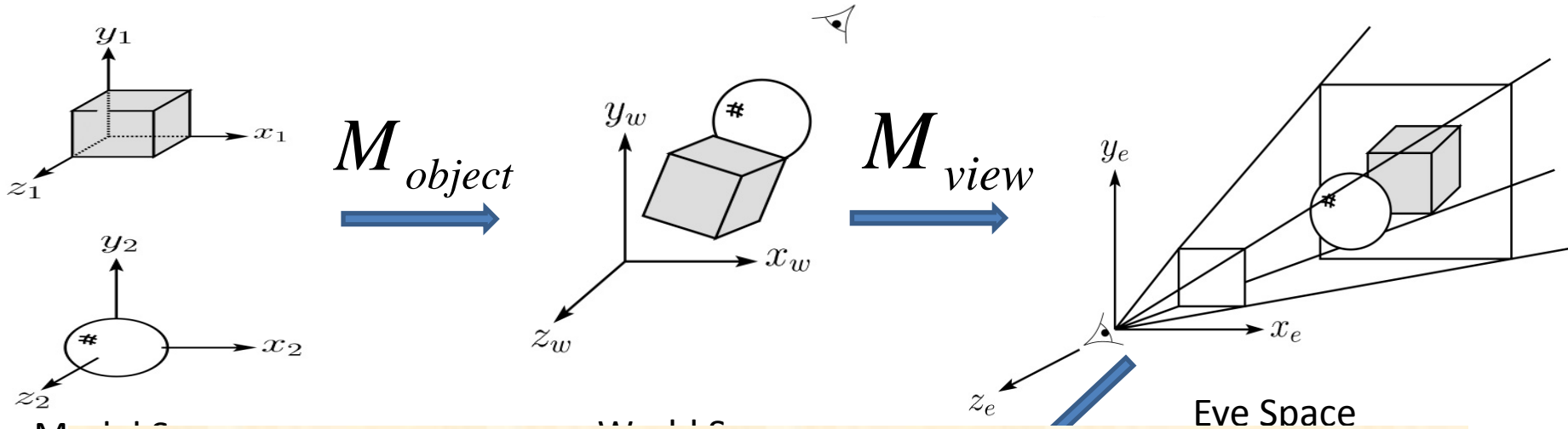
So far

- Fixed Camera location
 - => Change Camera location
- Single object
 - => Multiple objects

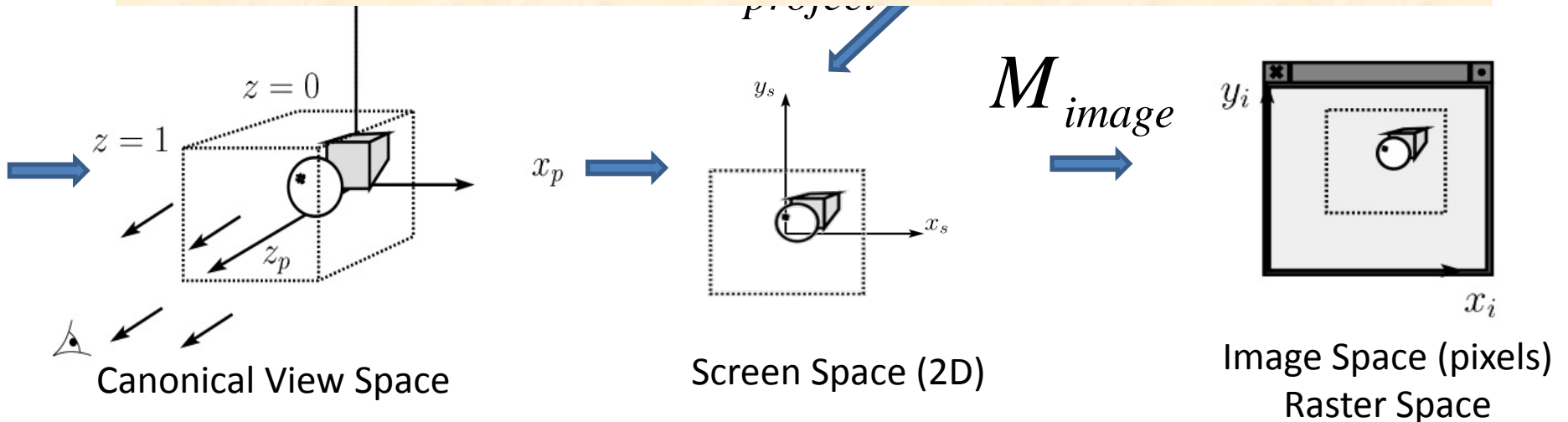
Examples of multiple objects



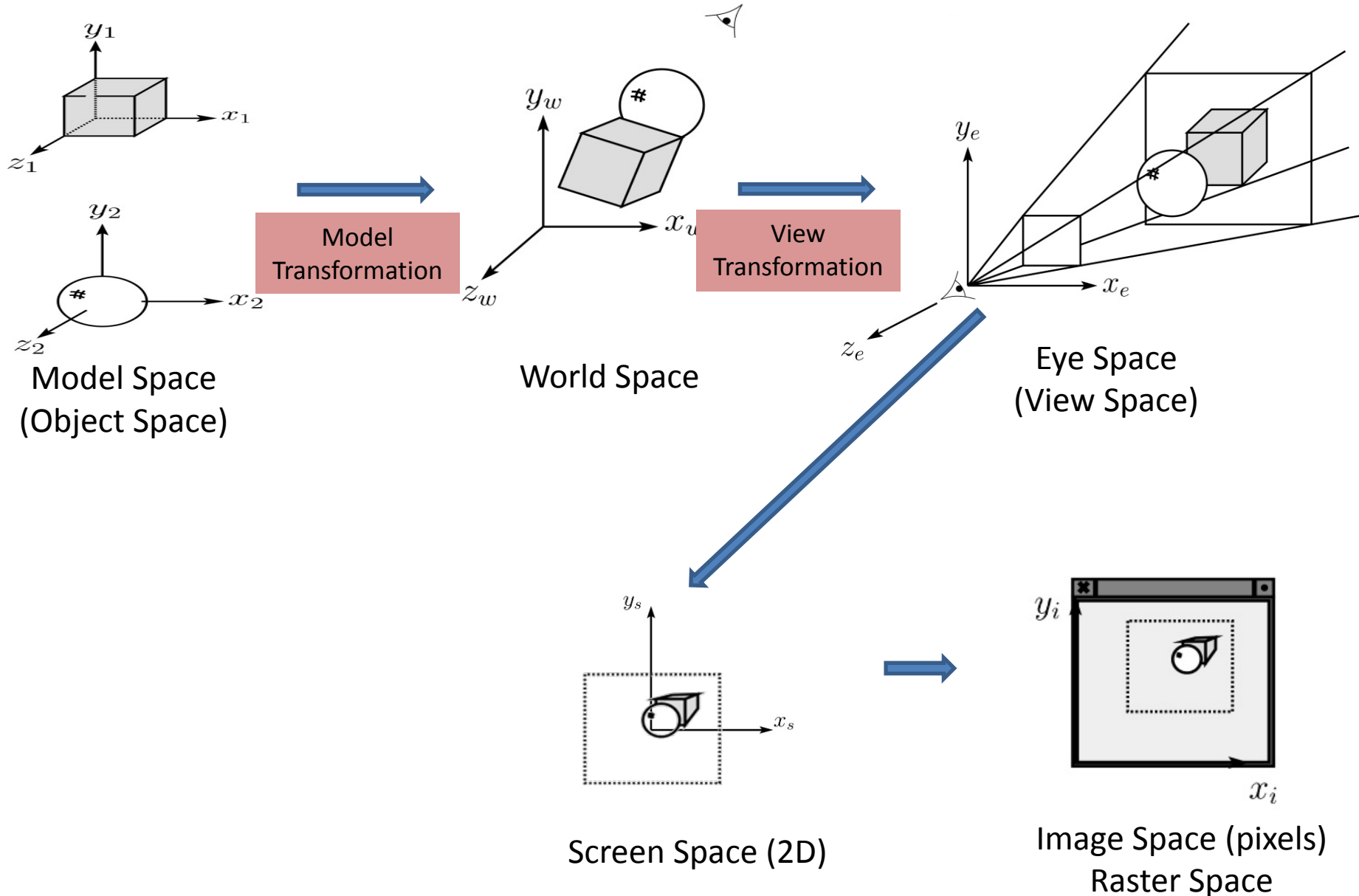
3D Geometry Pipeline



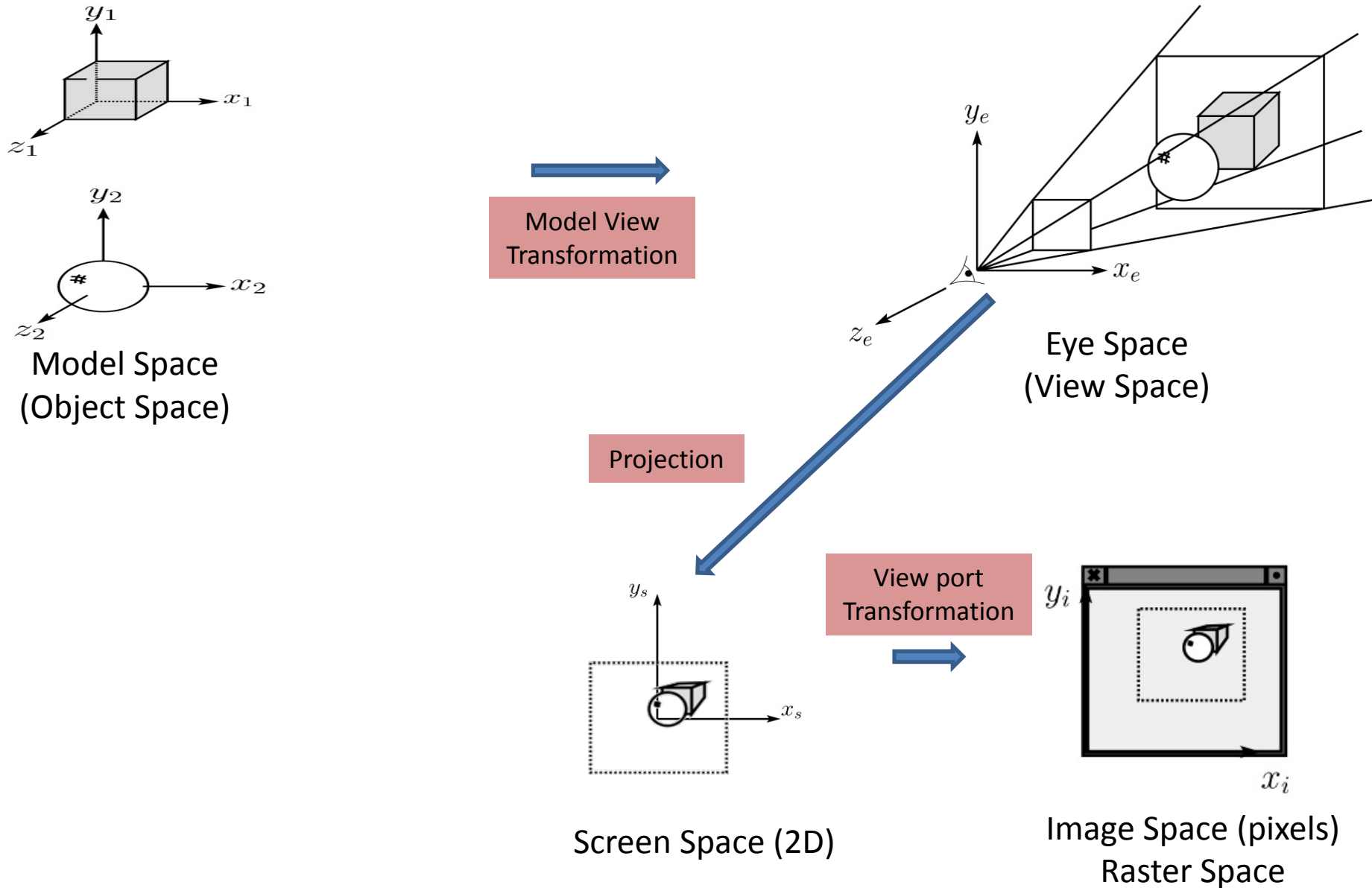
$$\mathbf{y} = M_{image} M_{project} M_{view} M_{object} \mathbf{x}$$



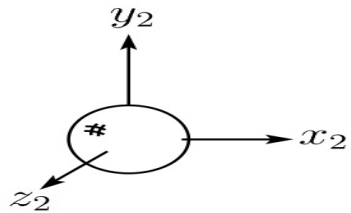
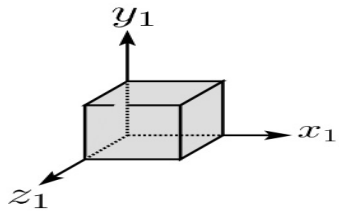
3D Geometry Pipeline



3D Geometry Pipeline



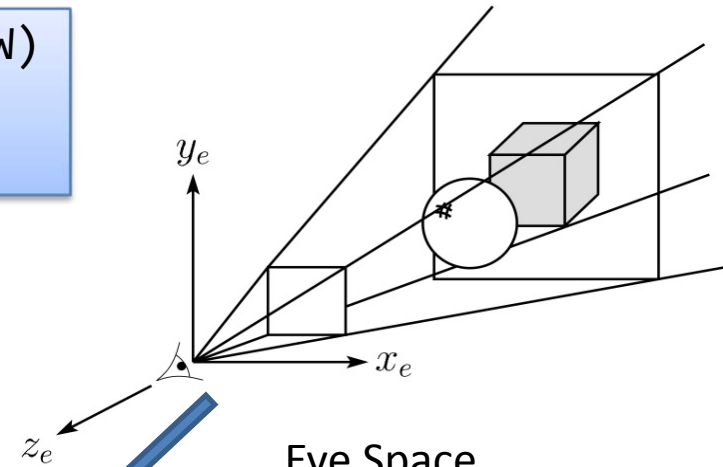
3D Geometry Pipeline



Model Space
(Object Space)

```
glMatrixMode(GL_MODELVIEW)  
glLoadIdentity();  
glRotate(...);
```

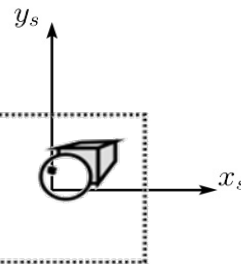
Model View
Transformation



Eye Space
(View Space)

```
glMatrixMode(GL_Projection)  
glLoadIdentity();  
glFrustum(...);
```

Projection



Screen Space (2D)

```
glViewport(...);
```

View port
Transformation

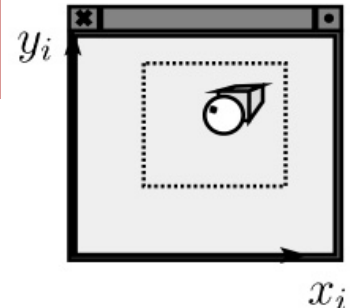
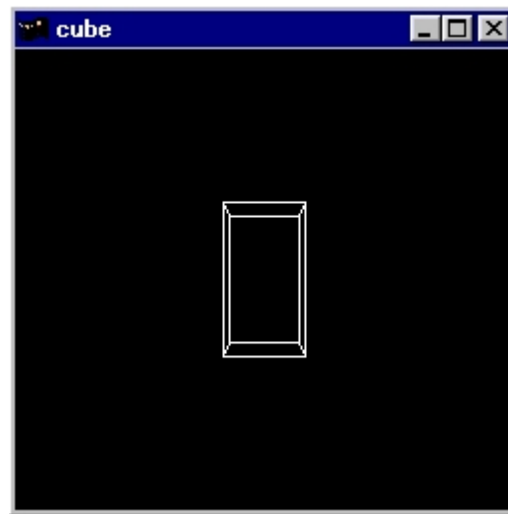


Image Space (pixels)
Raster Space

Cube.cpp



Cube.cpp

- Event-Driven Programming



Cube.cpp

```
int main(int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);
    glutInitWindowSize (500, 500);
    glutInitWindowPosition (100, 100);
    glutCreateWindow (argv[0]);
    init ();
    glutDisplayFunc(display);
    glutReshapeFunc(reshape);
    glutKeyboardFunc(keyboard);
    glutMainLoop();
    return 0;
}
```

```
void keyboard(unsigned char key, int x, int y) {
    switch (key) {
        case 27: //correspond to ESC
            exit(0);
            break;
    }
}
```

Cube.cpp

```
int main(int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);
    glutInitWindowSize (500, 500);
    glutInitWindowPosition (100, 100);
    glutCreateWindow (argv[0]);
    init ();
    glutDisplayFunc(display);
    glutReshapeFunc(reshape);
    glutKeyboardFunc(keyboard);
    glutMainLoop();
    return 0;
}
```

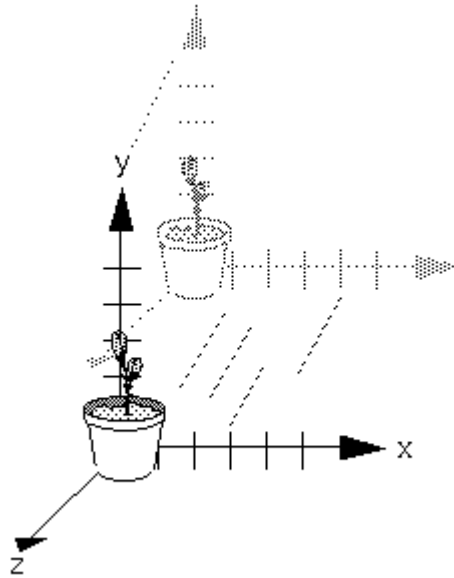
```
void reshape (int w, int h) {
    glViewport(0, 0, w, h);
    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();
    glFrustum(-1.0, 1.0, -1.0, 1.0, 1.5, 20.0);
}
```


Cube.cpp

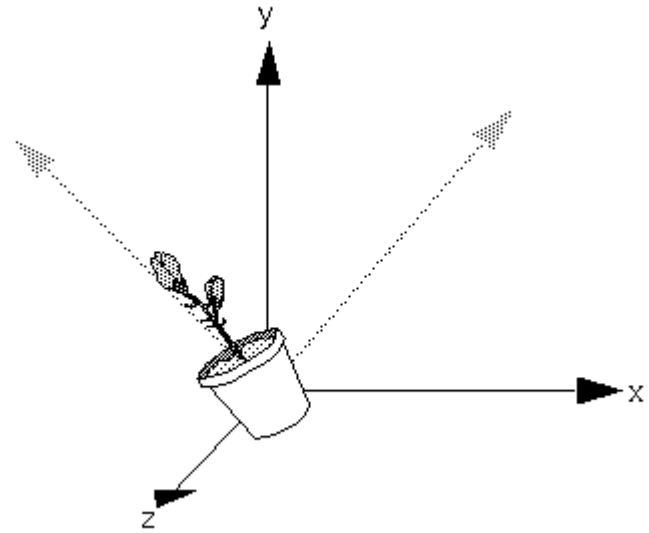
```
int main(int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);
    glutInitWindowSize (500, 500);
    glutInitWindowPosition (100, 100);
    glutCreateWindow (argv[0]);
    init ();
    glutDisplayFunc(display);
    glutReshapeFunc(reshape);
    glutKeyboardFunc(keyboard);
    glutMainLoop();
}
```

```
void display(void) {
    glClear(GL_COLOR_BUFFER_BIT);
    glColor3f(1.0, 1.0, 1.0);
    glMatrixMode(GL_MODELVIEW);
    glLoadIdentity();          /* clear the matrix */
        /* viewing transformation */
    gluLookAt(0.0, 0.0, 5.0, 0.0, 0.0, 0.0, 1.0, 0.0);
    glScalef(1.0, 2.0, 1.0);   /* modeling transformation */
    glutWireCube(1.0);
    glFlush();
}
```

Modeling Transformation



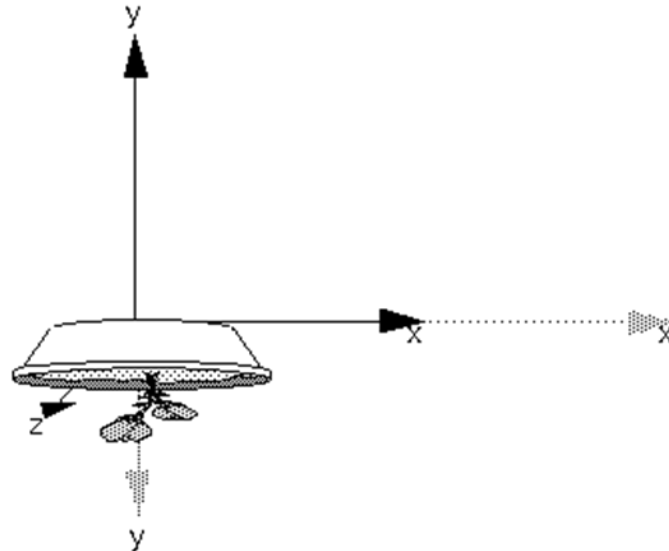
```
glTranslatef(float x, float y, float z)
```



```
glRotatef(float angle, float x, float y, float z)
```

```
glScalef(float x, float y, float z)
```

```
glScalef(2.0, -0.5, 1.0)
```



General Modeling Transform

```
glLoadIdentity()
```

```
glLoadMatrixf(float *M)
```

```
glMultiMatrixf(float *M)
```

$$\mathbf{M} = \begin{bmatrix} m_1 & m_5 & m_9 & m_{13} \\ m_2 & m_6 & m_{10} & m_{14} \\ m_3 & m_7 & m_{11} & m_{15} \\ m_4 & m_8 & m_{12} & m_{16} \end{bmatrix}$$

```
double M[4][4];
```

```
M[2][1] corresponds to???
```

```
M[10]
```

Matrix Chain

```
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
glMultMatrixf(N);           /* apply transformation N */
glMultMatrixf(M);           /* apply transformation M */
glMultMatrixf(L);           /* apply transformation L */
glBegin(GL_POINTS);
glVertex3f(v);              /* draw transformed vertex v */
glEnd();                    /* which is (N*(M*(L*v))) */
```

Matrix Chain

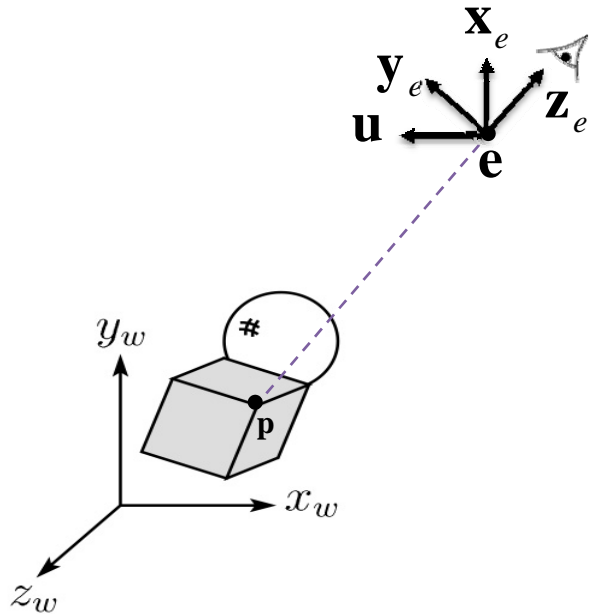
```
glMatrixMode(GL_MODELVIEW);  
glLoadIdentity();  
  
glMultMatrixf(V);  
  
glMultMatrixf(R);  
  
glMultMatrixf(T);  
  
glBegin(GL_POINTS);  
glVertex3f(v);  
glEnd();
```



```
glMatrixMode(GL_MODELVIEW);  
glLoadIdentity();  
  
gluLookat(...);  
  
glRotatef(...);  
  
glTranslatef(...);  
  
glBegin(GL_POINTS);  
glVertex3f(v);  
glEnd();
```

gluLookAt

```
gluLookAt(  
    float eyex, float eyey, float eyez,  
    float px, float py, float pz,  
    float upx, float upy, float upz )
```



1. Give eye location e
2. Give target position p
3. Give upward direction u

$$\mathbf{z}_e = -\frac{\mathbf{p} - \mathbf{e}}{|\mathbf{p} - \mathbf{e}|}$$

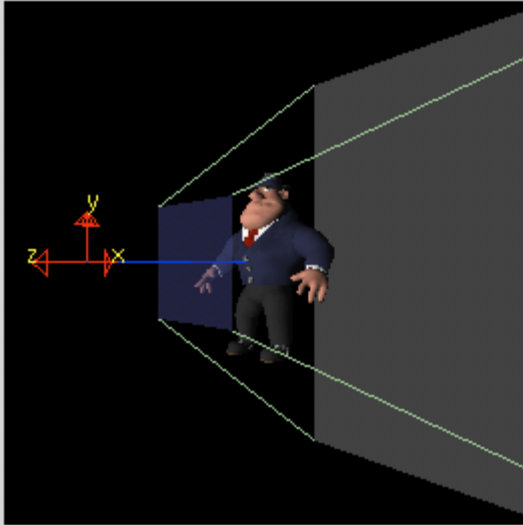
$$\mathbf{x}_e = \frac{\mathbf{u} \times \mathbf{z}_e}{|\mathbf{u} \times \mathbf{z}_e|}$$

$$\mathbf{y}_e = \frac{\mathbf{z}_e \times \mathbf{x}_e}{|\mathbf{z}_e \times \mathbf{x}_e|}$$

$$\mathbf{M}_v = \begin{bmatrix} -\mathbf{x}_e^T & -\mathbf{y}_e^T & -\mathbf{z}_e^T & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & | & 0 \\ 0 & 1 & 0 & | & -\mathbf{e} \\ 0 & 0 & 1 & | & 0 \\ 0 & 0 & 0 & | & 1 \end{bmatrix}$$

gluLookAt

World-space view



Screen-space view



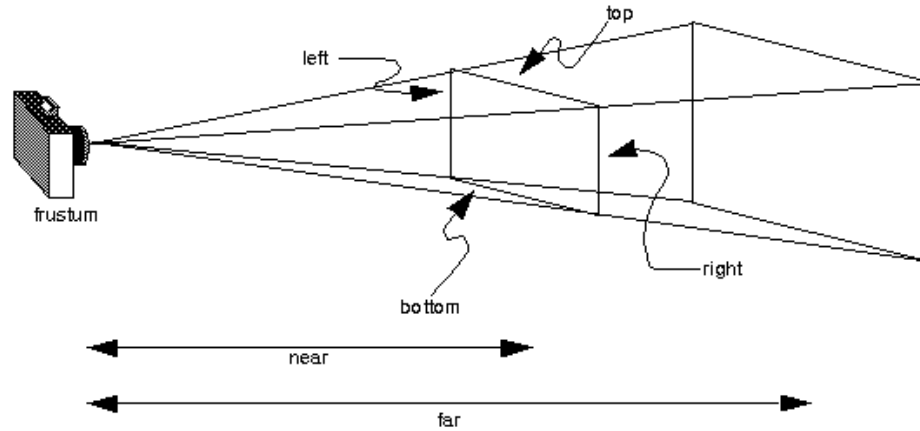
Command manipulation window

```
          fovy aspect zNear zFar
gluPerspective( 60.0 , 1.00 , 1.0 , 10.0 );
          gluLookAt( 0.00 , 0.00 , 2.00 ,  <- eye
                    0.00 , 0.00 , 0.00 ,  <- center
                    0.00 , 1.00 , 0.00 ); <- up
```

Click on the arguments and move the mouse to modify values.

glFrustum

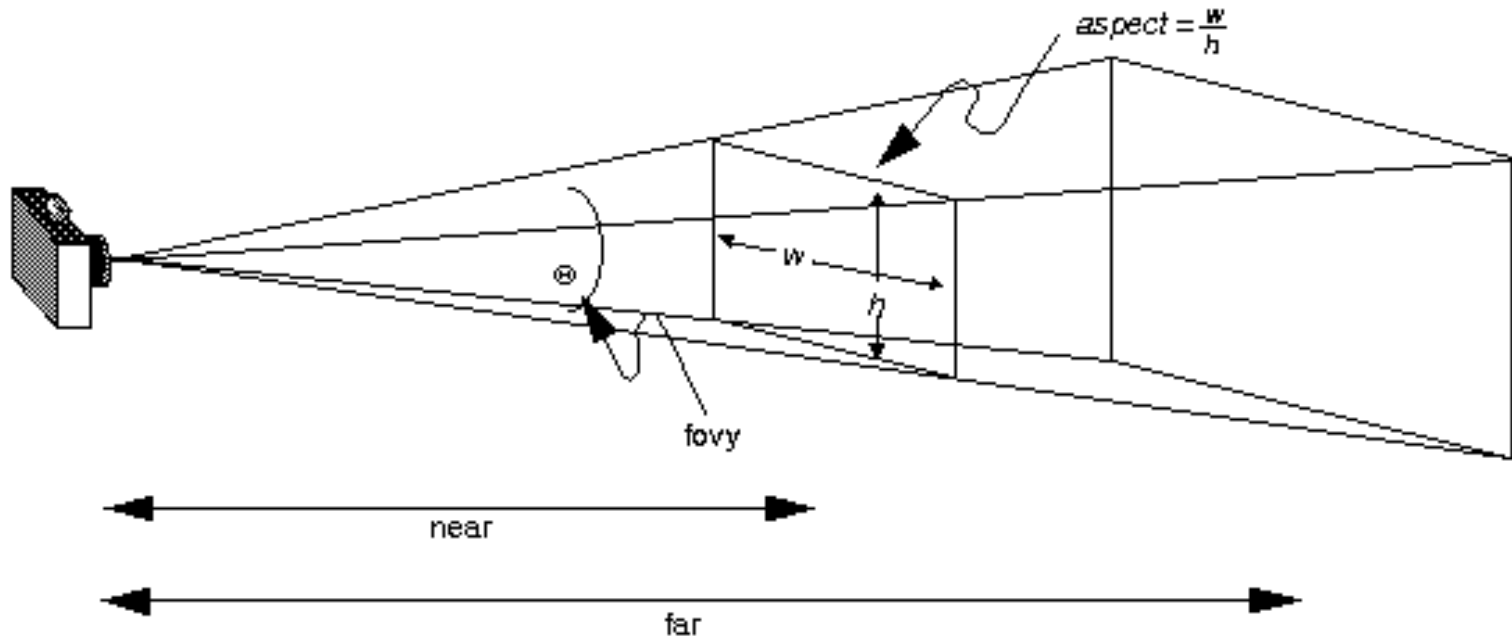
`glFrustum(double left, double right, double bottom, double top, double near, double far)`



$$\mathbf{M}_{view \rightarrow canonical} = \mathbf{M}_O \mathbf{M}_P = \begin{bmatrix} \frac{2}{(r-l)} & 0 & 0 & \frac{-(r+l)}{(r-l)} \\ 0 & \frac{2}{(t-b)} & 0 & \frac{-(t+b)}{(t-b)} \\ 0 & 0 & \frac{2}{(n-f)} & \frac{-(n+f)}{(n-f)} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} n & 0 & 0 & 0 \\ 0 & n & 0 & 0 \\ 0 & 0 & (n+f) & -nf \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

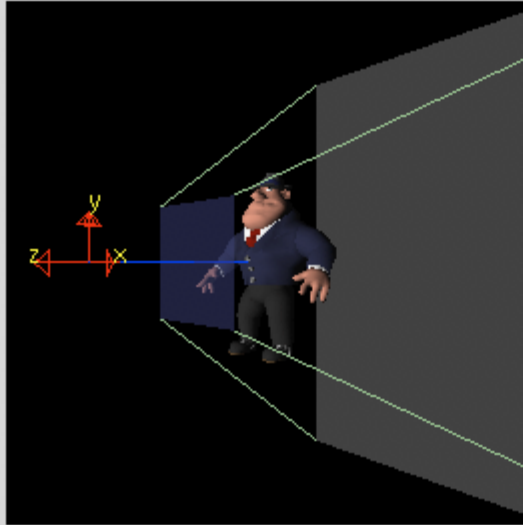
gluPerspective

```
gluPerspective(double fovy, double aspect, double zNear, double zFar)
```



gluPerspective

World-space view



Screen-space view



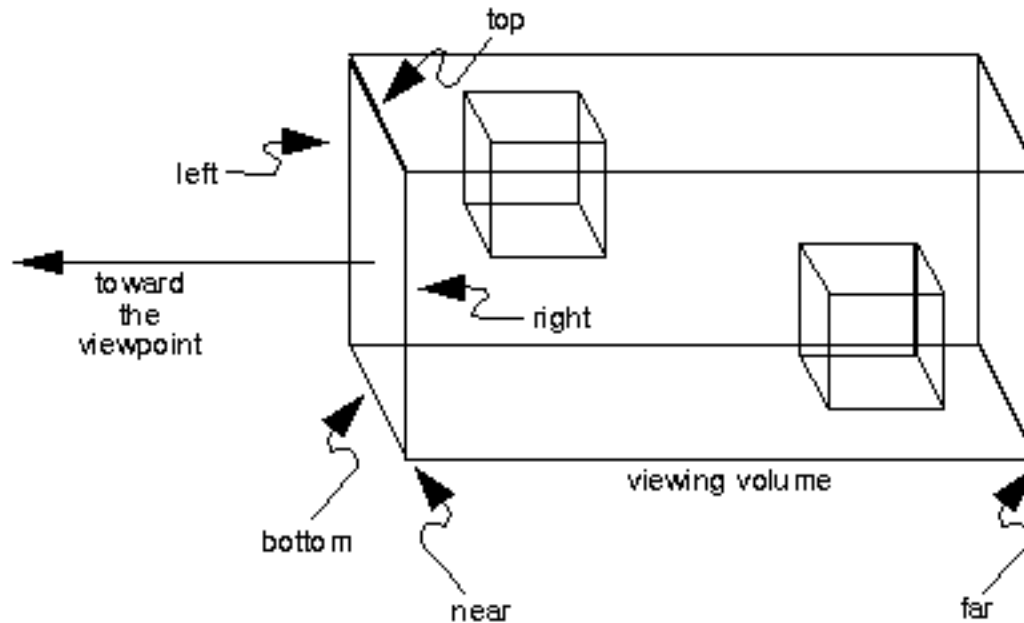
Command manipulation window

```
gluPerspective( fovy aspect zNear zFar  
gluPerspective( 60.0 , 1.00 , 1.0 , 10.0 );  
gluLookAt( 0.00 , 0.00 , 2.00 , <- eye  
           0.00 , 0.00 , 0.00 , <- center  
           0.00 , 1.00 , 0.00 ); <- up
```

Click on the arguments and move the mouse to modify values.

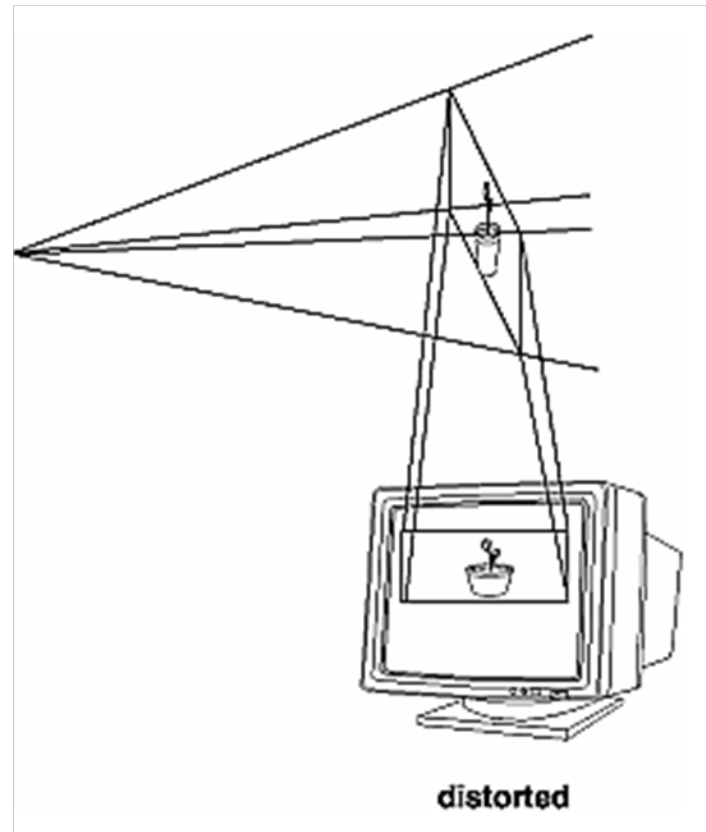
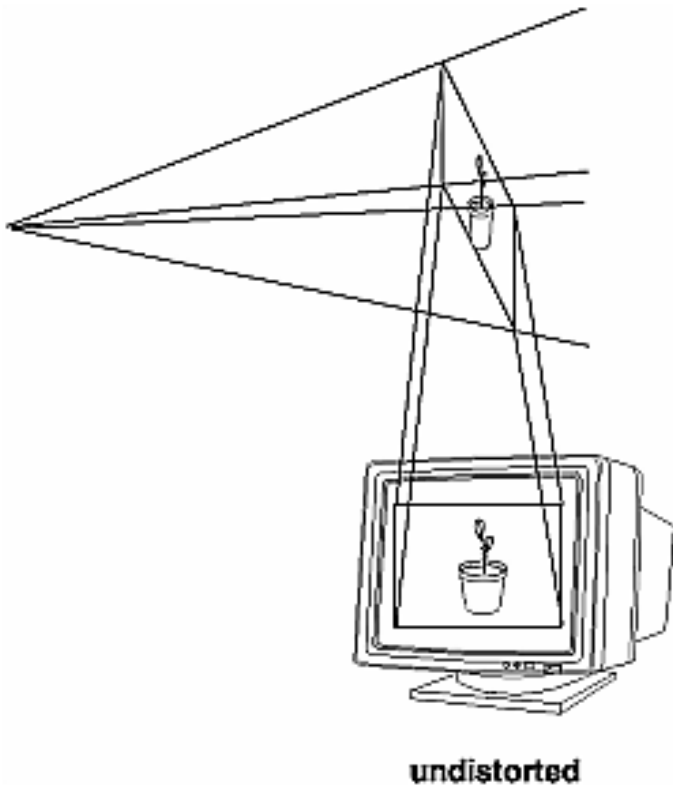
Orthographic Projection

```
glOrtho(double left, double right, double bottom,  
double top, double near, double far);
```



Viewport Transformation

```
glViewport(int x, int y, int width, int height);
```



```
glFrustum(double left, double right, double bottom, double top, double near, double far)  
gluPerspective(double fovy, double aspect, double zNear, double zFar)
```

Revisit cube.cpp

```
int main(int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode (GLUT_SINGLE | GLUT_RGB);
    glutInitWindowSize (500, 500);
    glutInitWindowPosition (100, 100);
    glutCreateWindow (argv[0]);
    init ();
    glutDisplayFunc(display);
    glutReshapeFunc(reshape);
    glutKeyboardFunc(keyboard);
    glutMainLoop();
    return 0;
}
```

```
void reshape (int w, int h) {
    glViewport(0, 0, w, h);
    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();
    glFrustum(-1.0, 1.0, -1.0, 1.0, 1.5, 20.0);
}
```

```
void display(void) {
    glClear(GL_COLOR_BUFFER_BIT);
    glColor3f(1.0, 1.0, 1.0);
    glMatrixMode(GL_MODELVIEW);
    glLoadIdentity();          /* clear the matrix */
    /* viewing transformation */
    gluLookAt(0.0, 0.0, 5.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0);
    glScalef(1.0, 2.0, 1.0);   /* modeling transformation */
    glutWireCube(1.0);
    glFlush();
}
```