



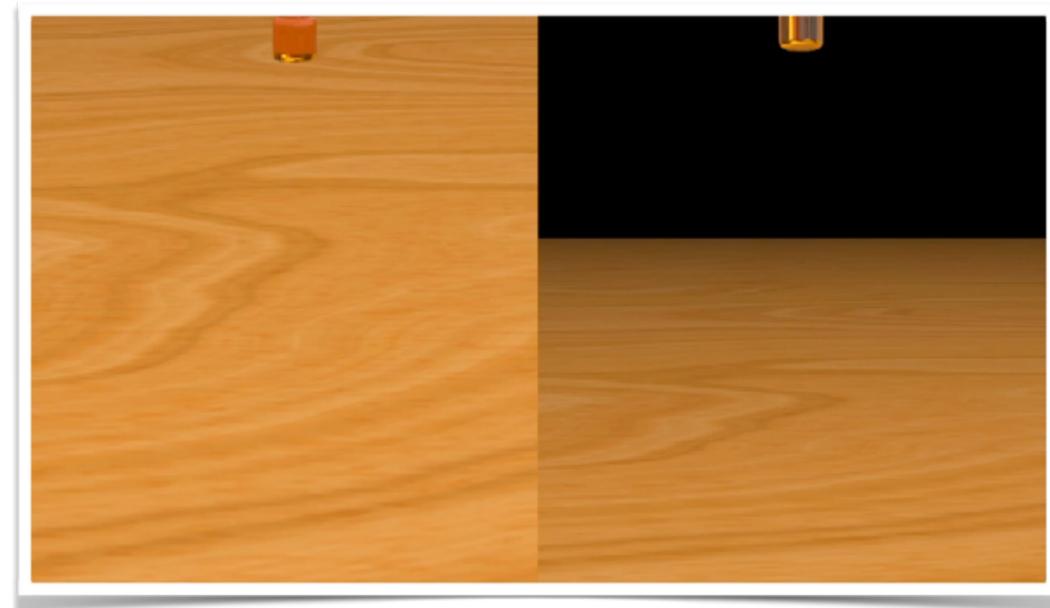
# Sparse Paged Grid and its Applications to Adaptivity and **Material Point Method**

Ming Gao

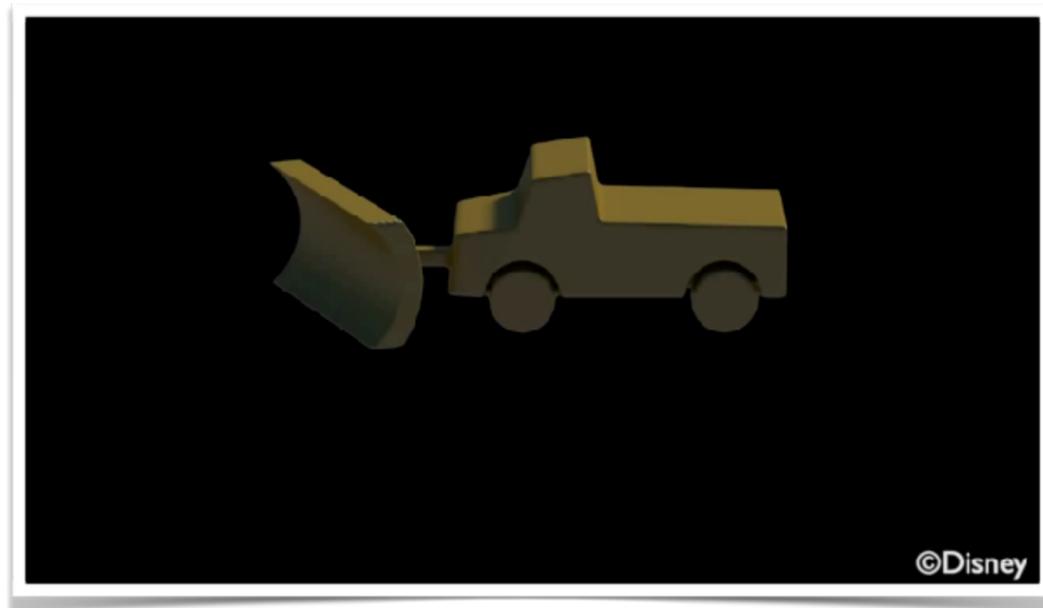
# Motivation - expanding feature set



Wet cloth - [Fei et al. 18]



Viscous fluid - [Larionov et al. 17]

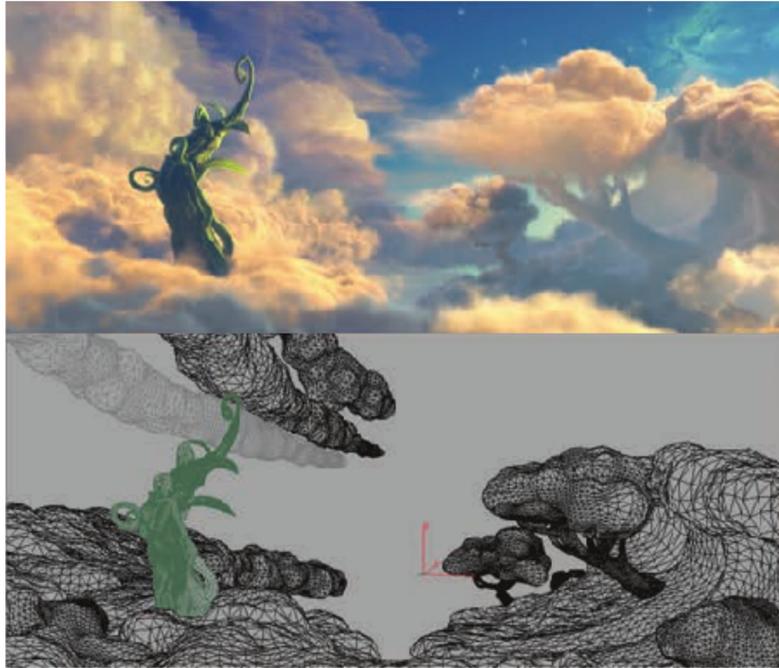


Snow - [Stomakhin et al. 13]



Melting - [Stomakhin et al. 14]

# Motivation - accelerating performance



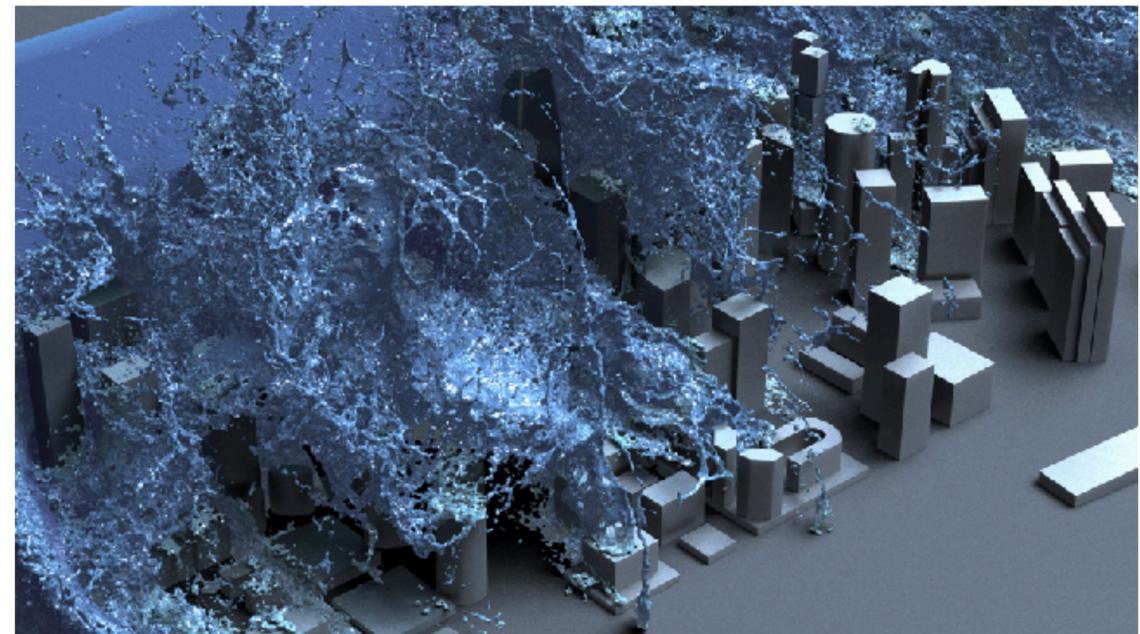
OpenVDB - [Museth et al. 13]



PhysGrid - [Milne et al. 16]



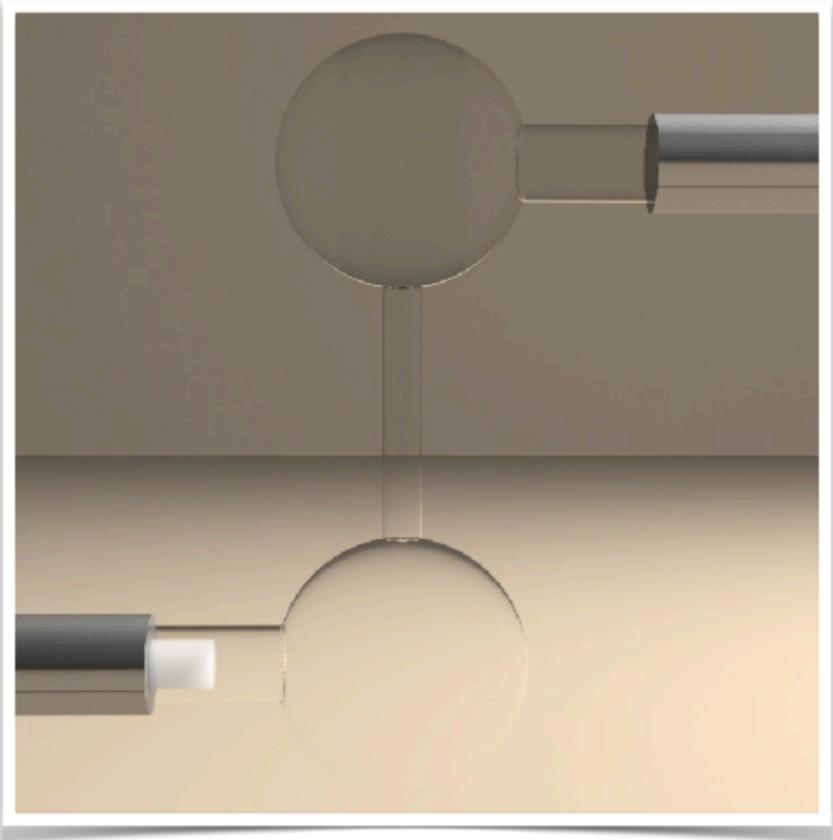
Cloth - [Tang et al. 16]



Fluid - [Wu et al. 18]

# Feature breadth vs. optimal performance

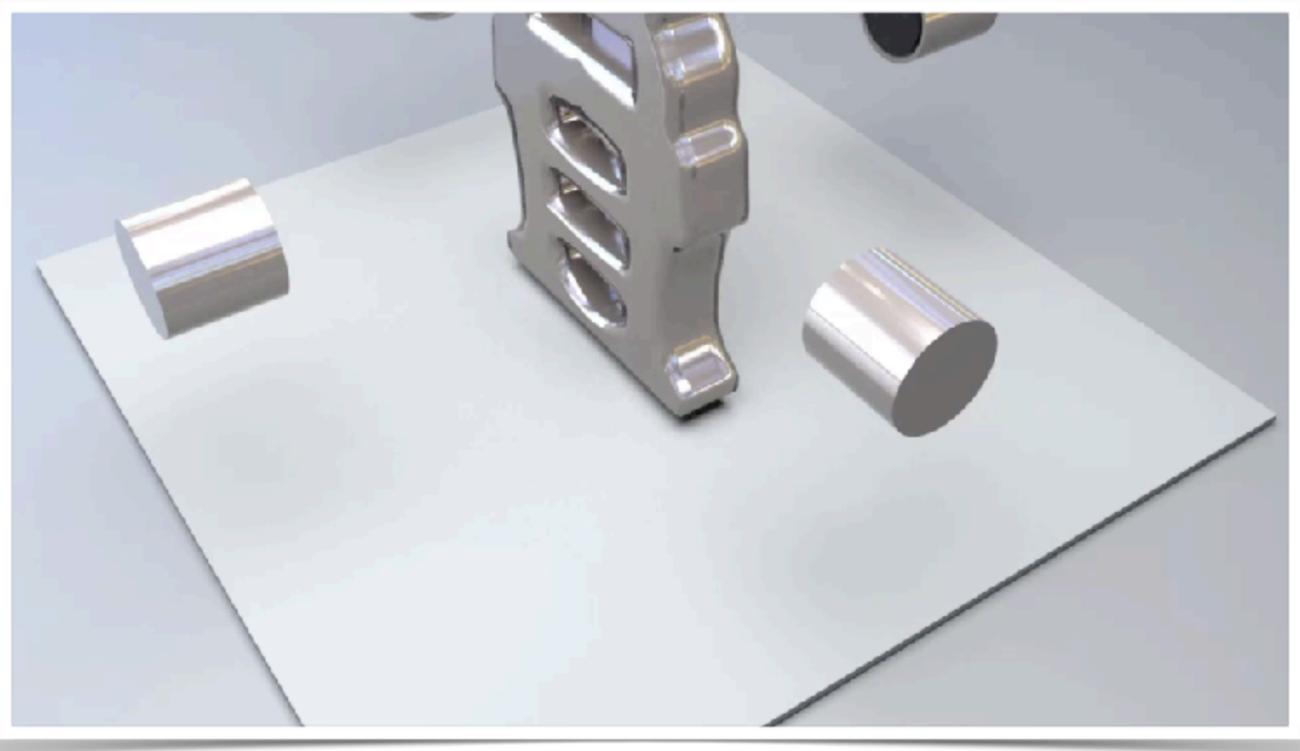




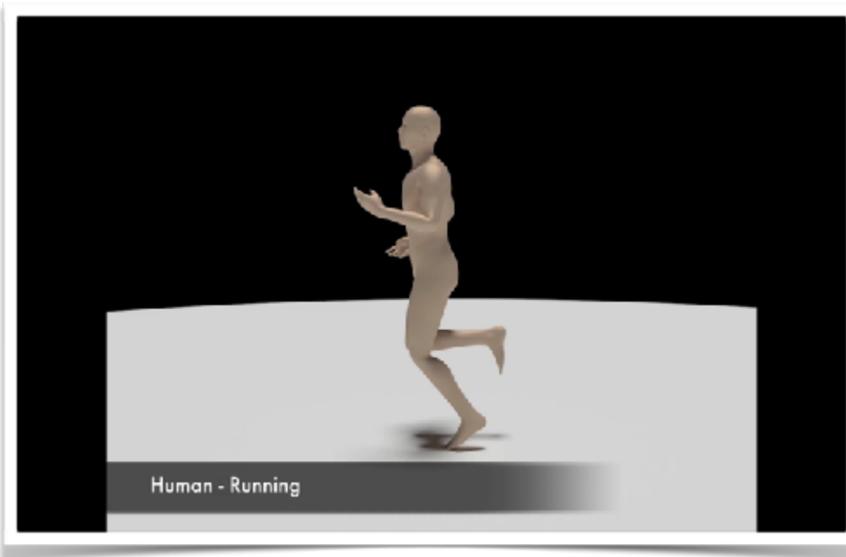
Sparse paged grid



Material point method



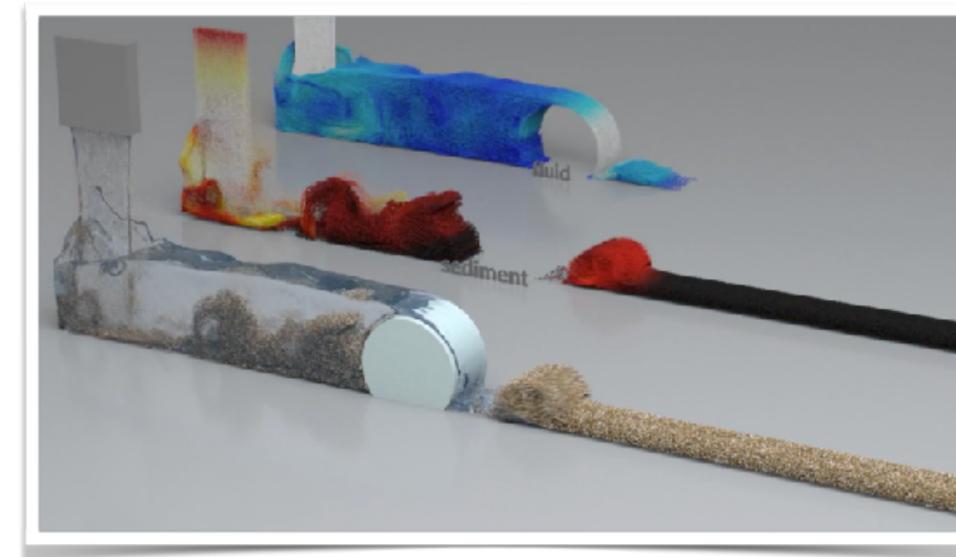
Adaptivity



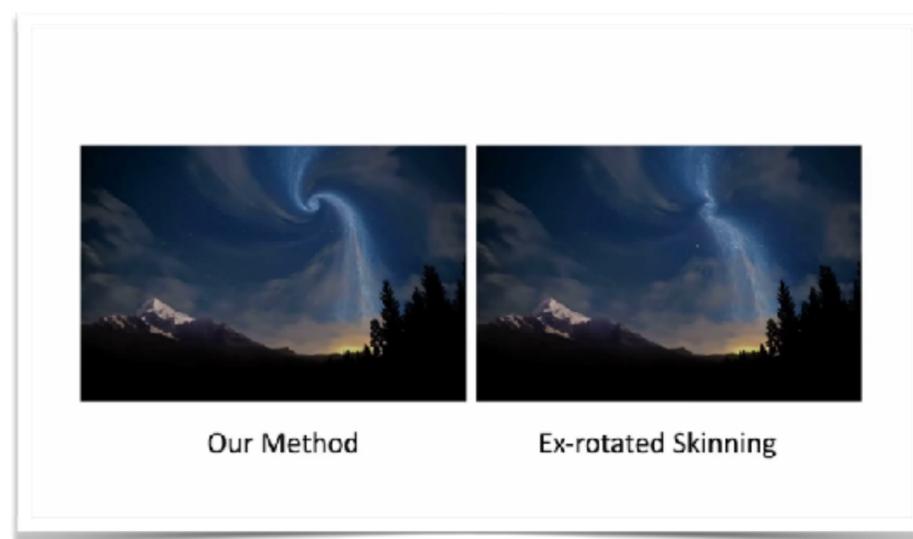
SCA 14



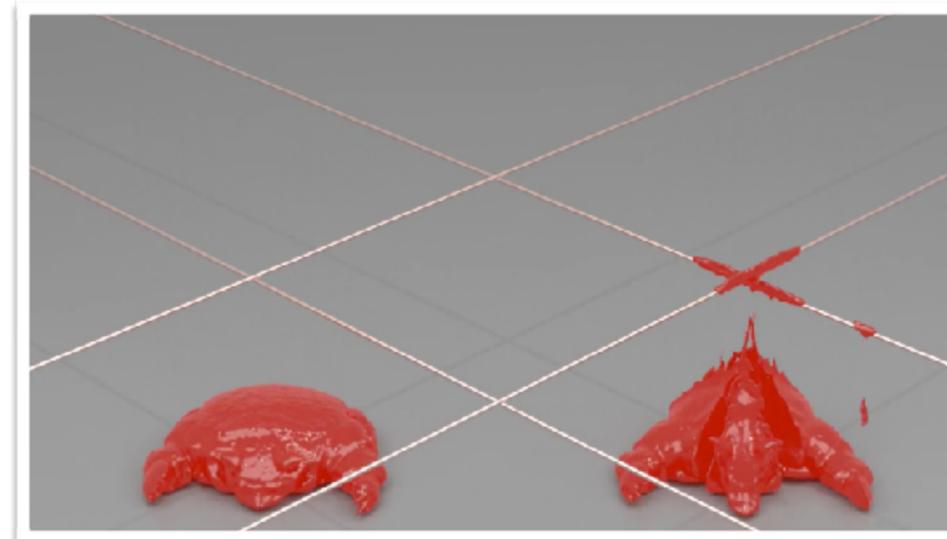
SIGGRAPH 17



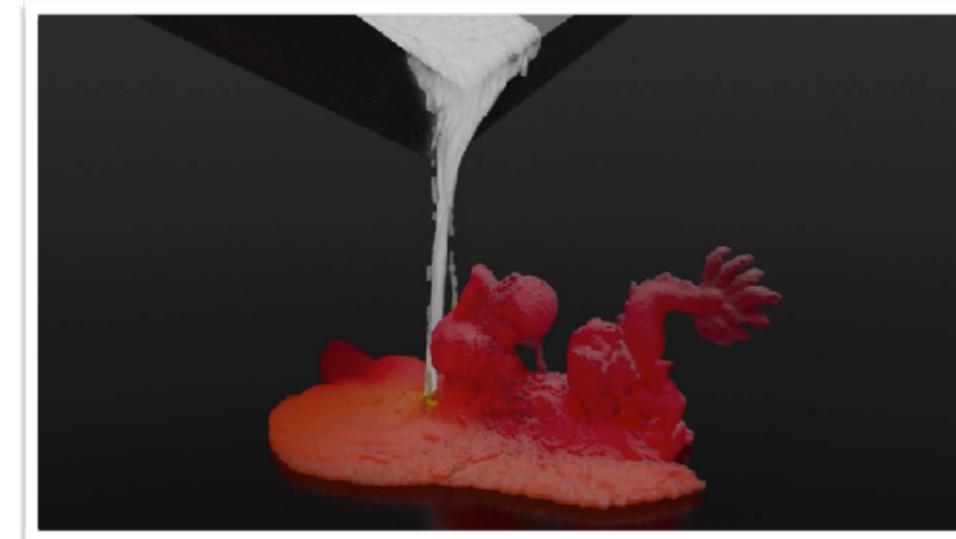
SIGGRAPH 18



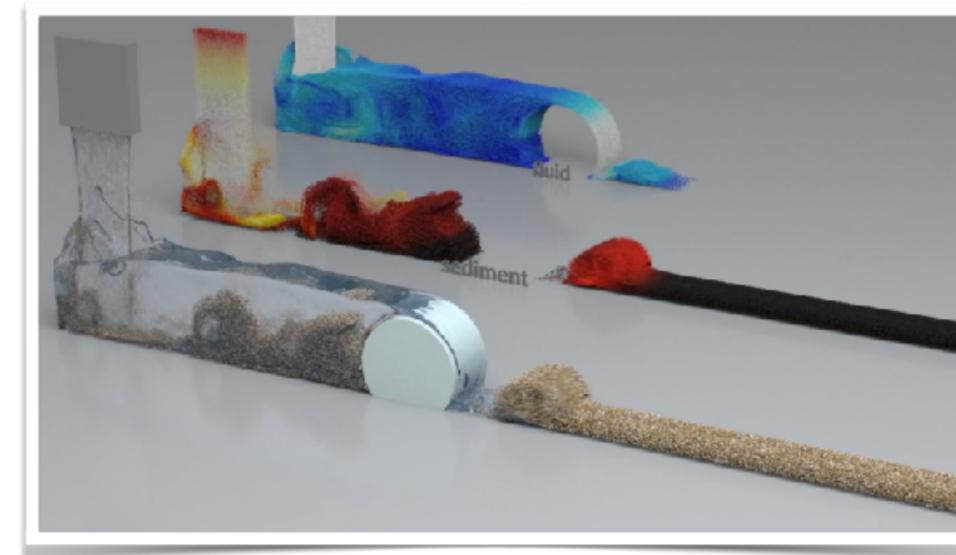
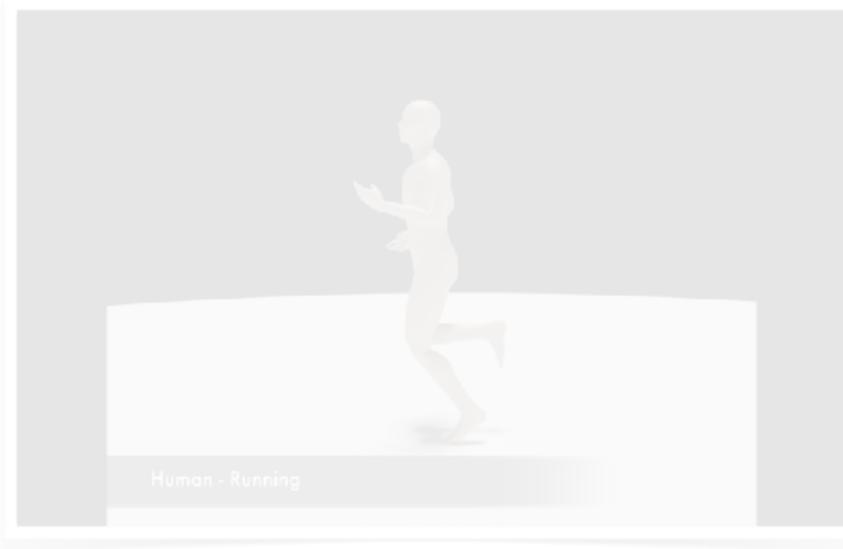
Eurographics 16



SIGGRAPH Asia 17

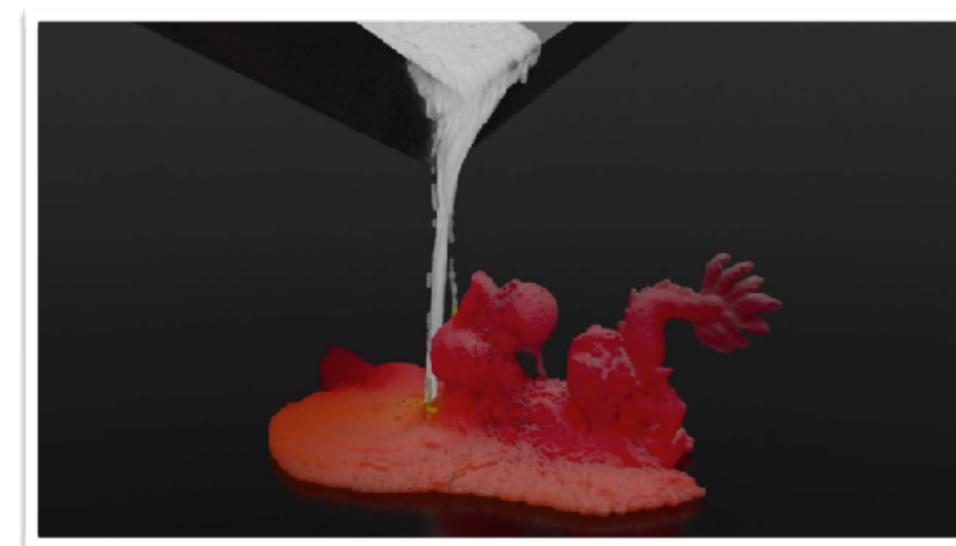
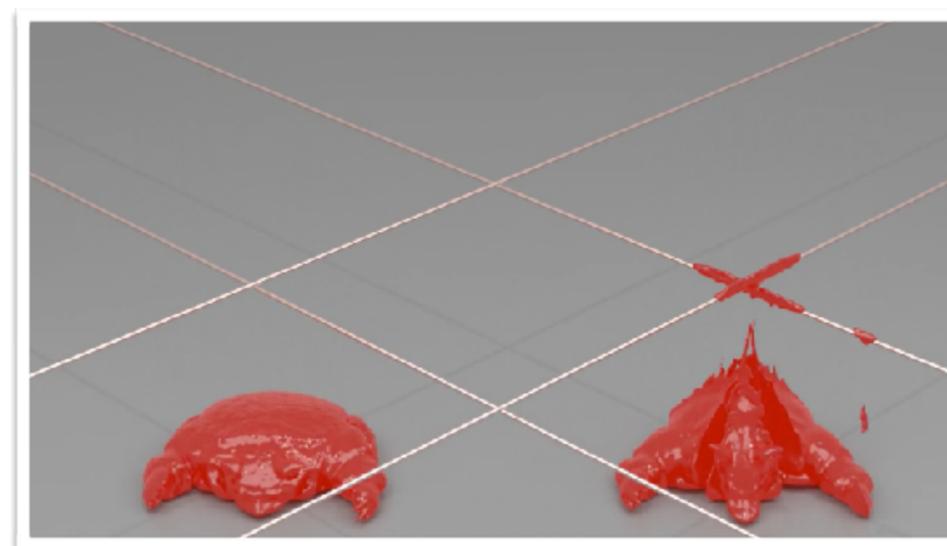
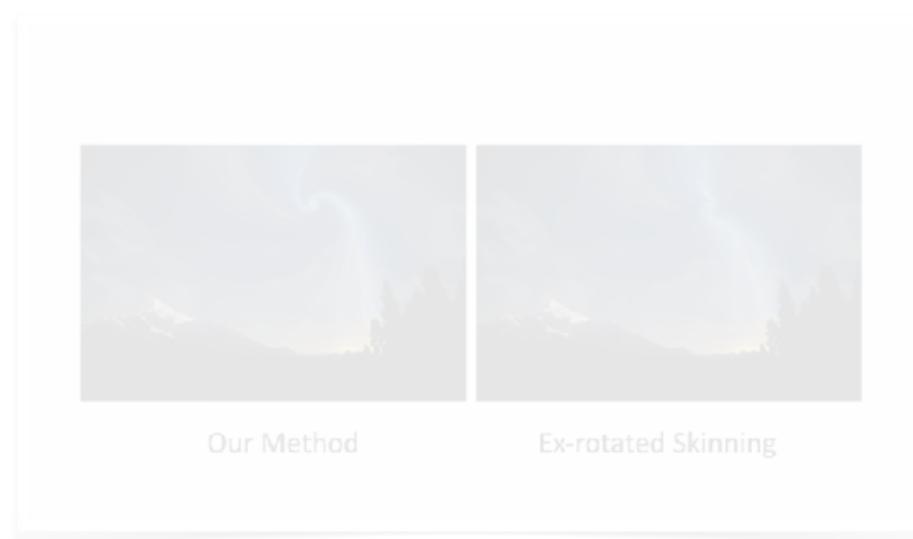


SIGGRAPH Asia 18  
(under review)



SPGrid / Adaptivity

SPGrid / MPM

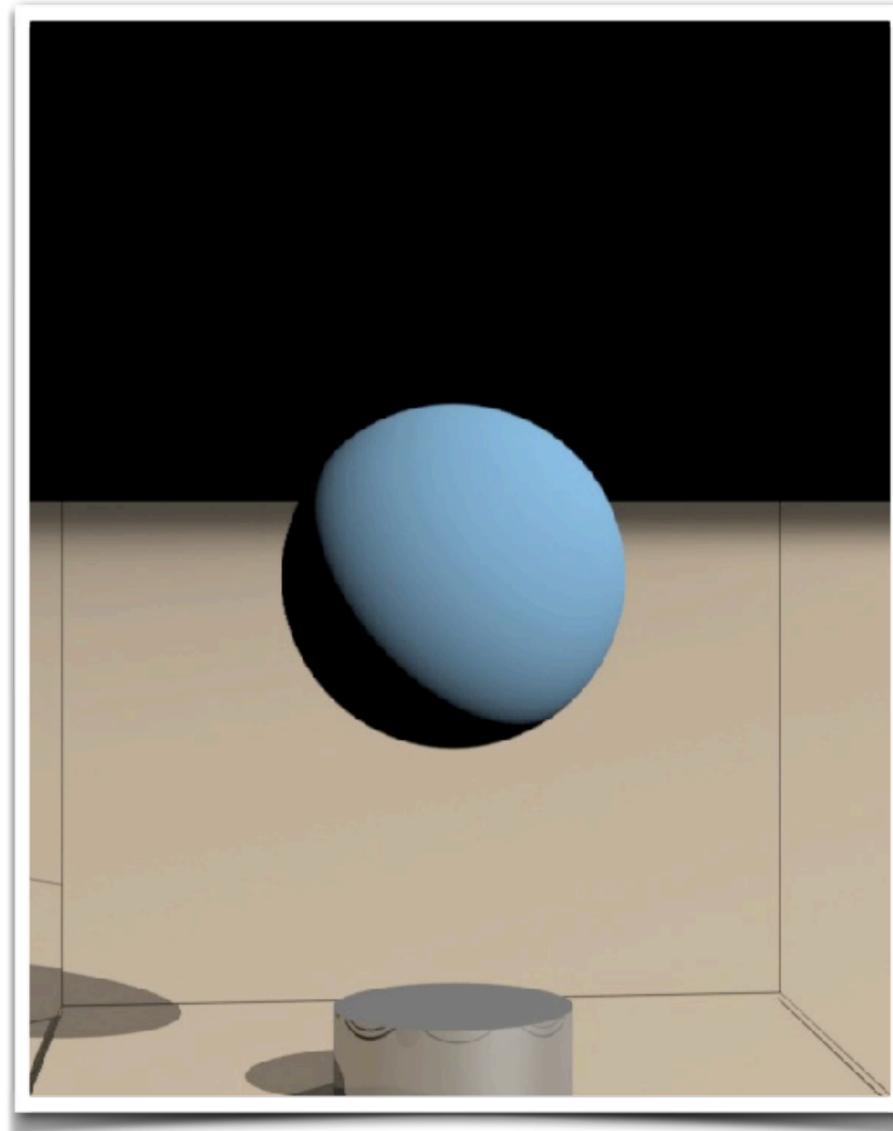


SPGrid / MPM / Adaptivity

SPGrid / MPM / GPU

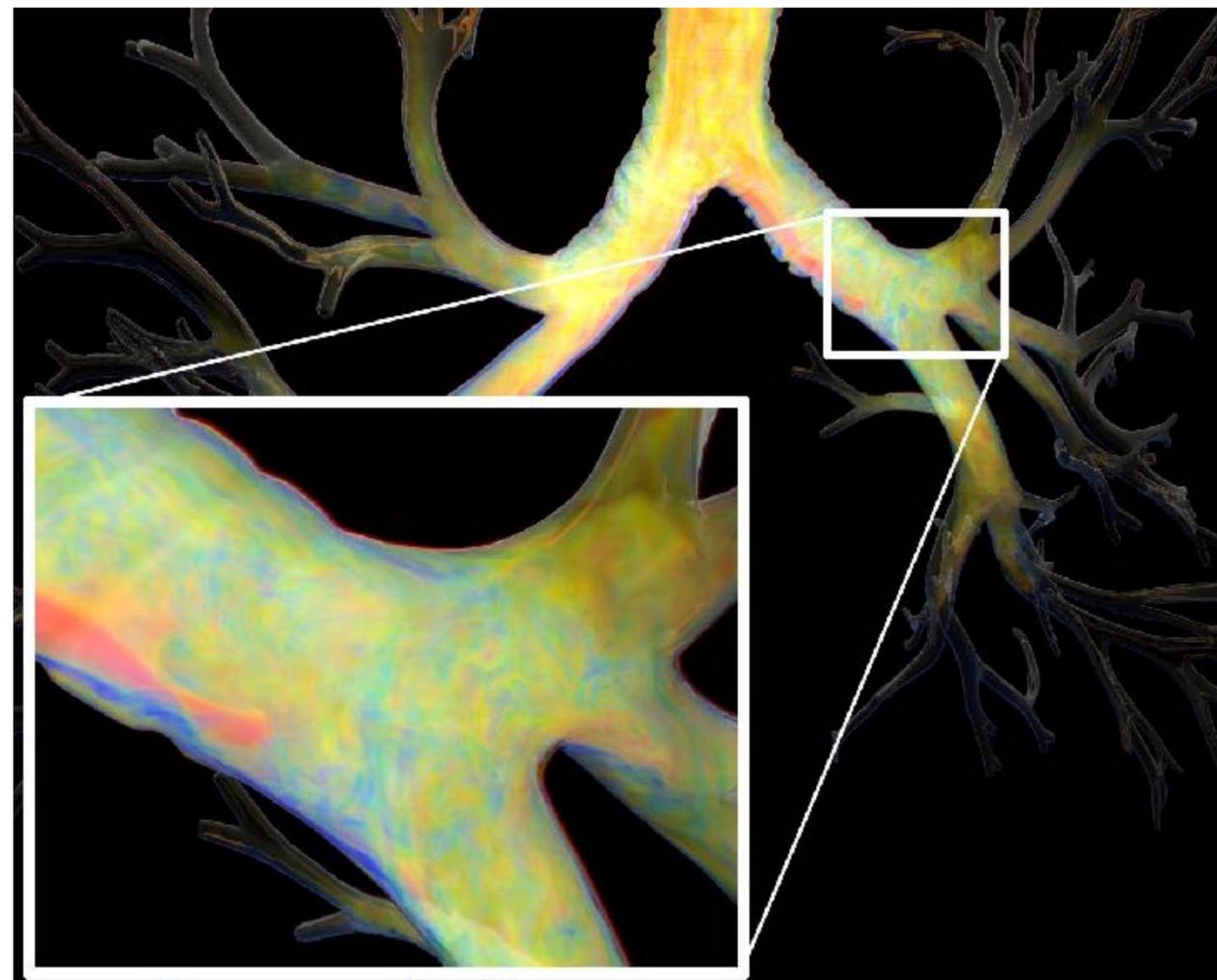
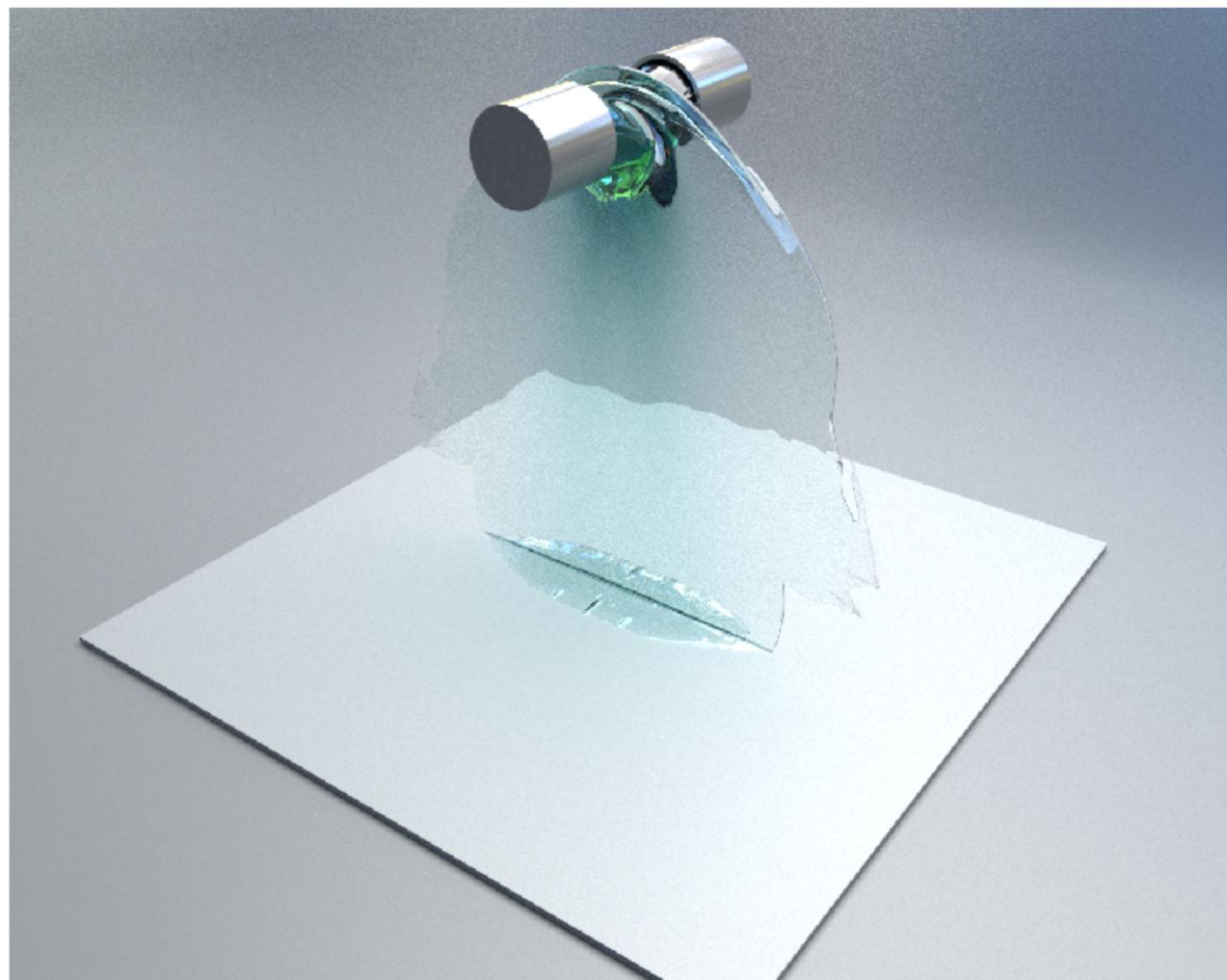
# Sparse paged grid (SPGrid)

135M voxels  
23GB



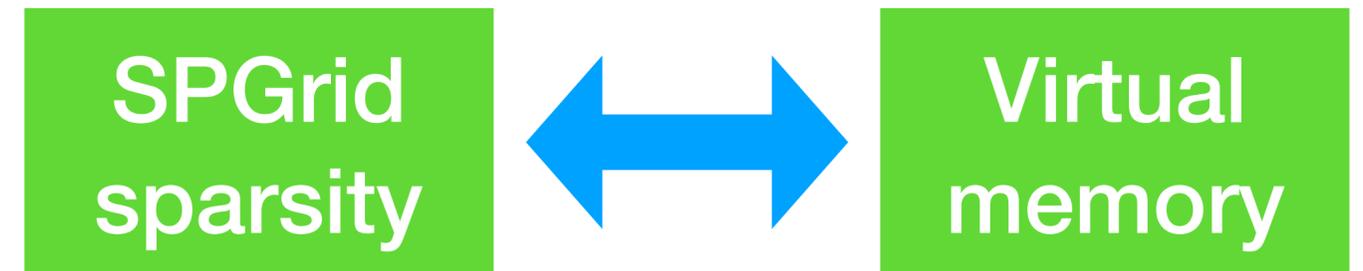
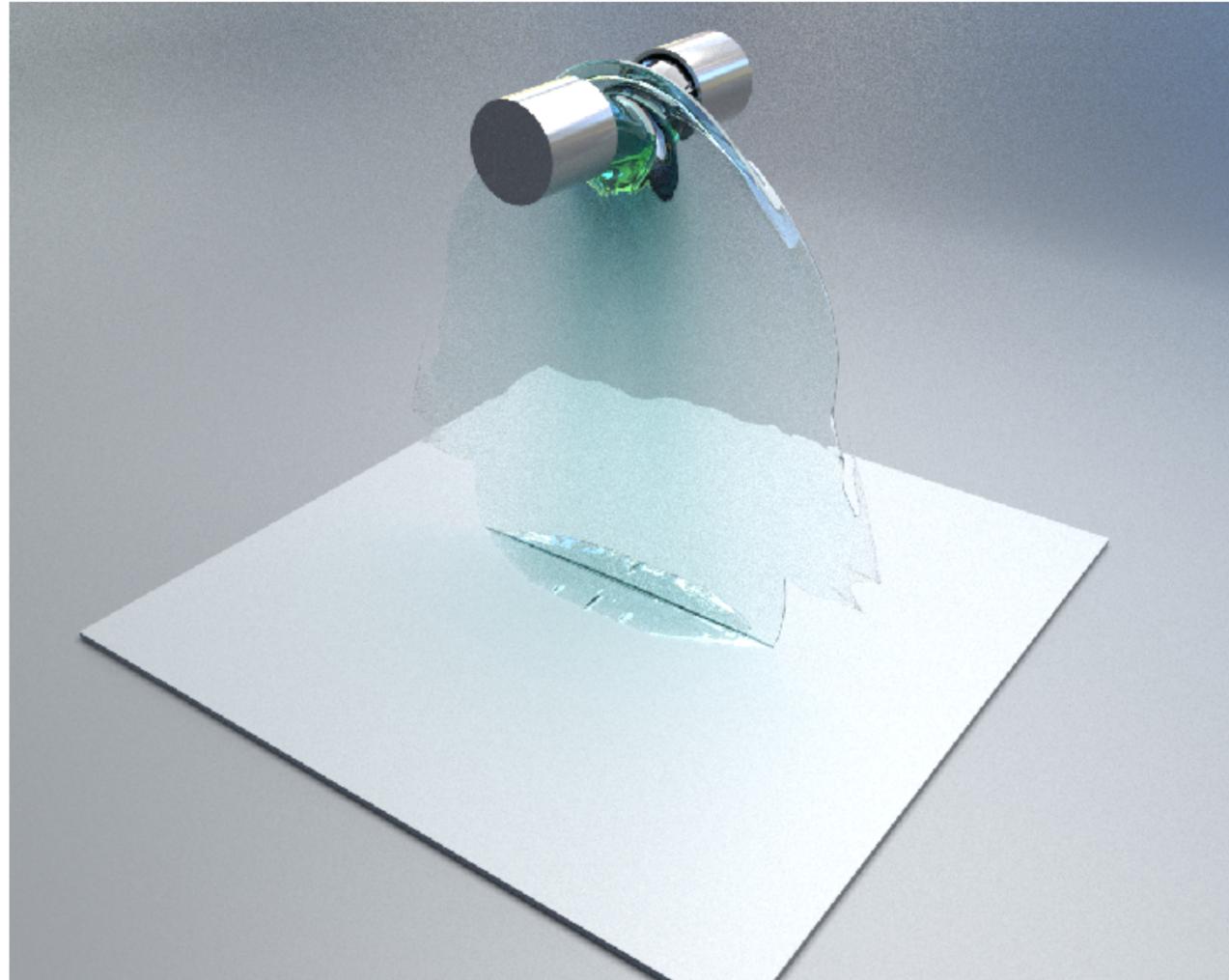
# Sparsity

Liu et al. 16



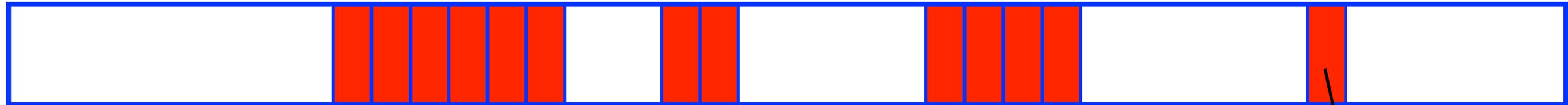
Resolution:  $8192 \times 8192 \times 4096$

# Sparsity

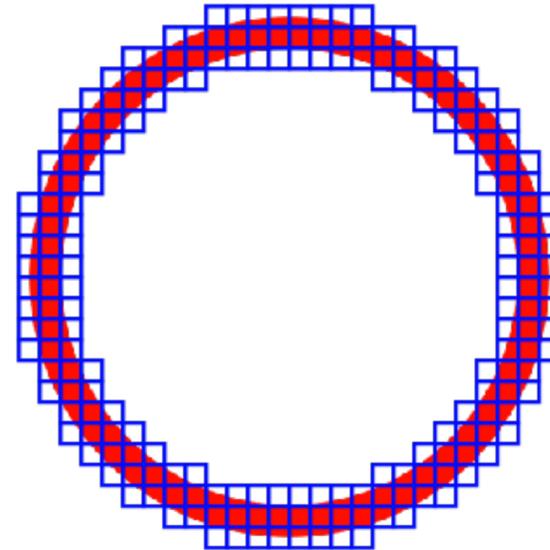
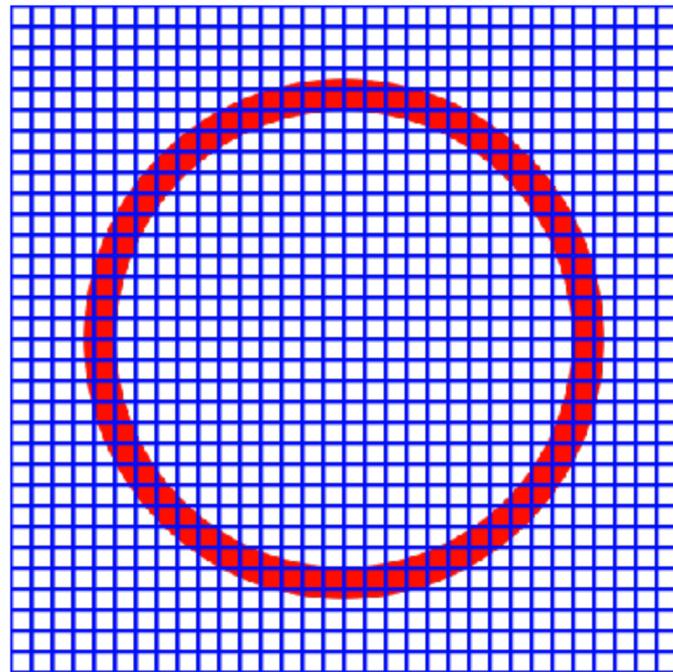


# Virtual memory

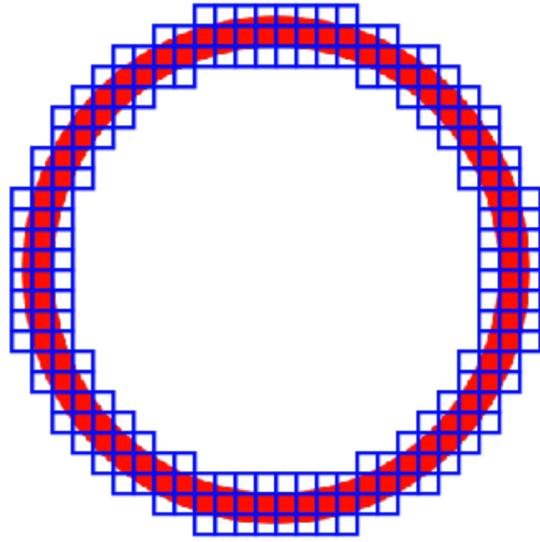
128 TB



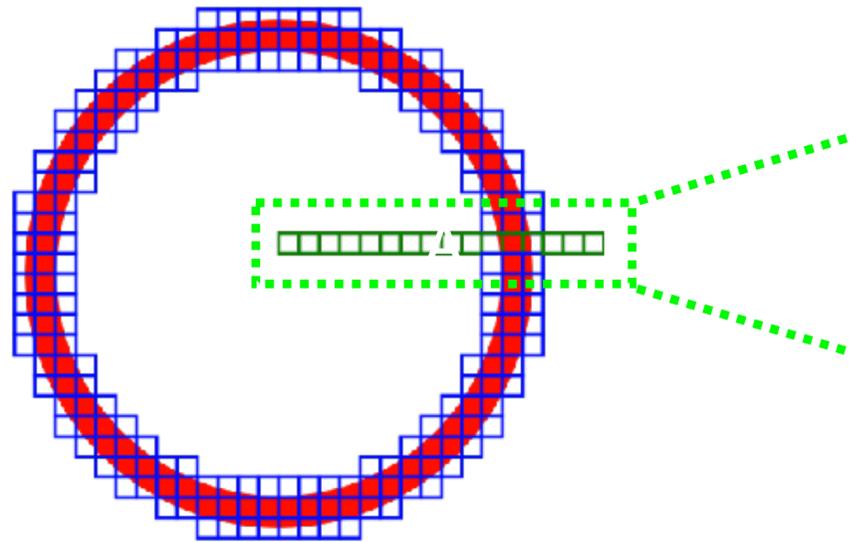
4 KB



# Cell ordering



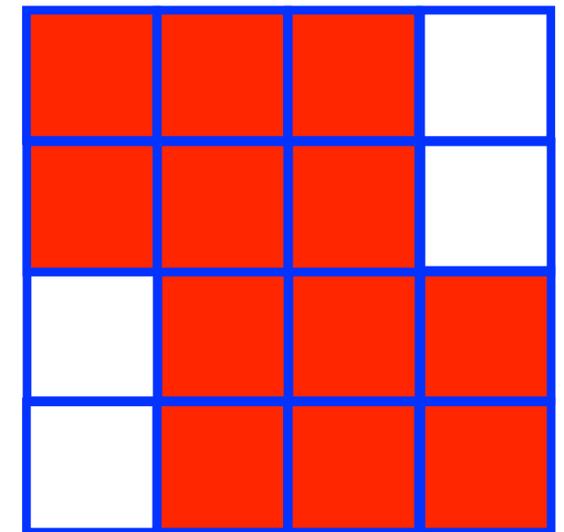
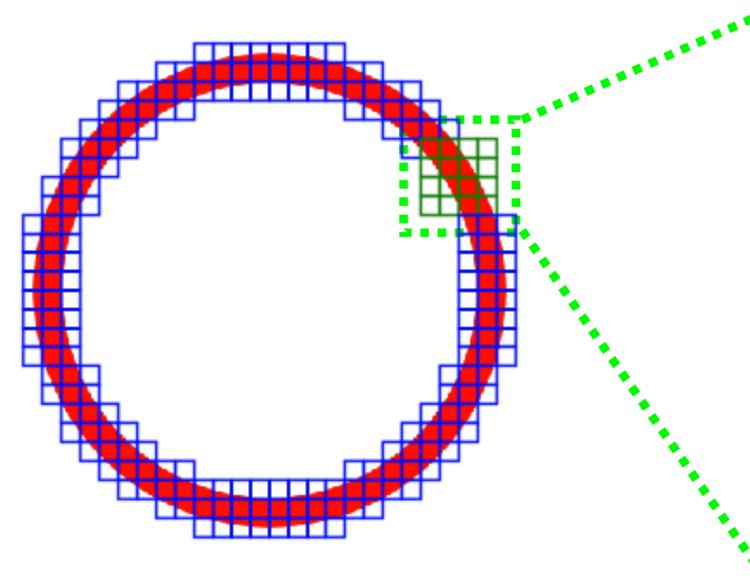
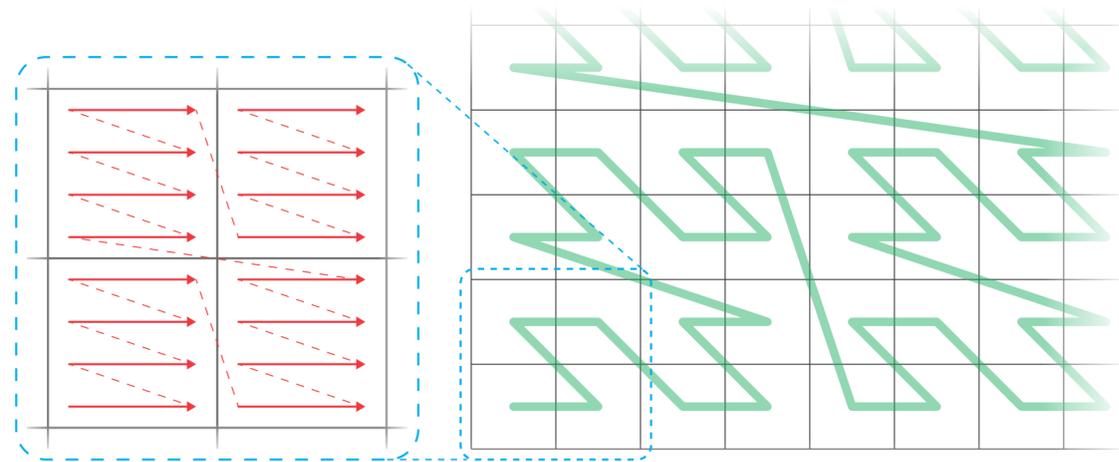
# Cell ordering



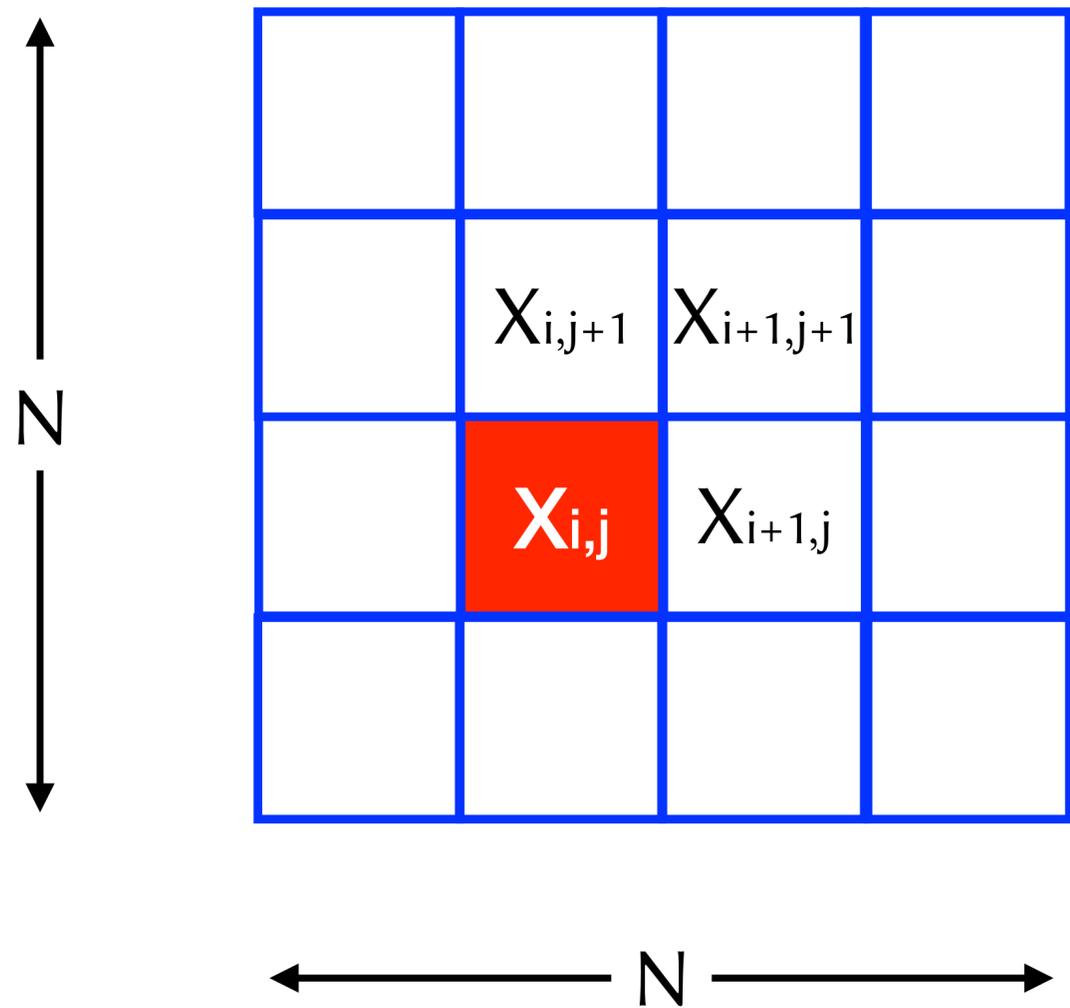
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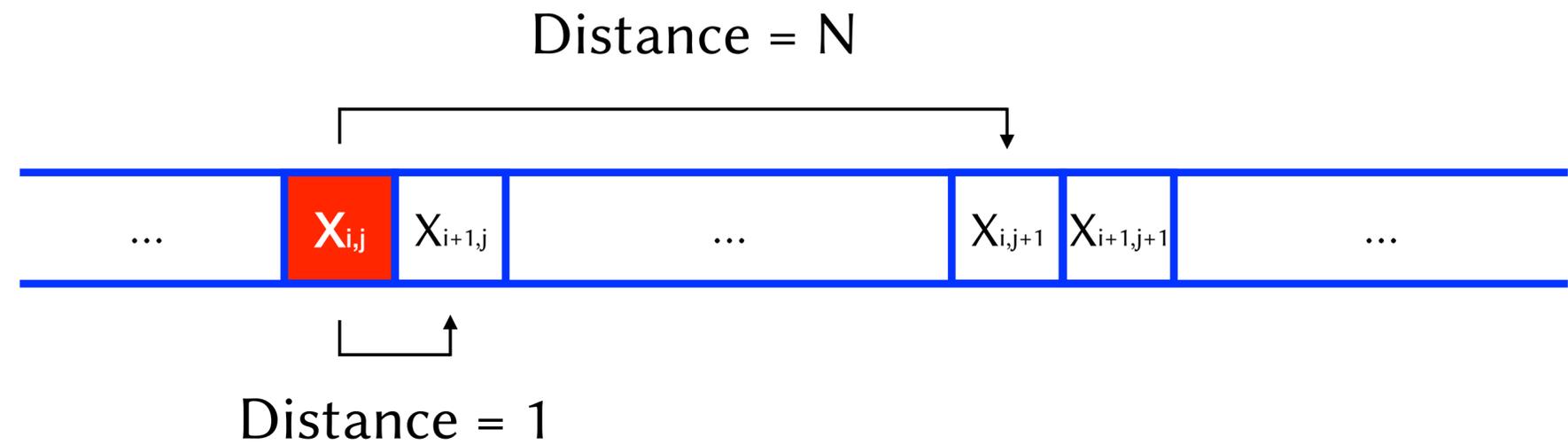
4 KB



# Stencil operations

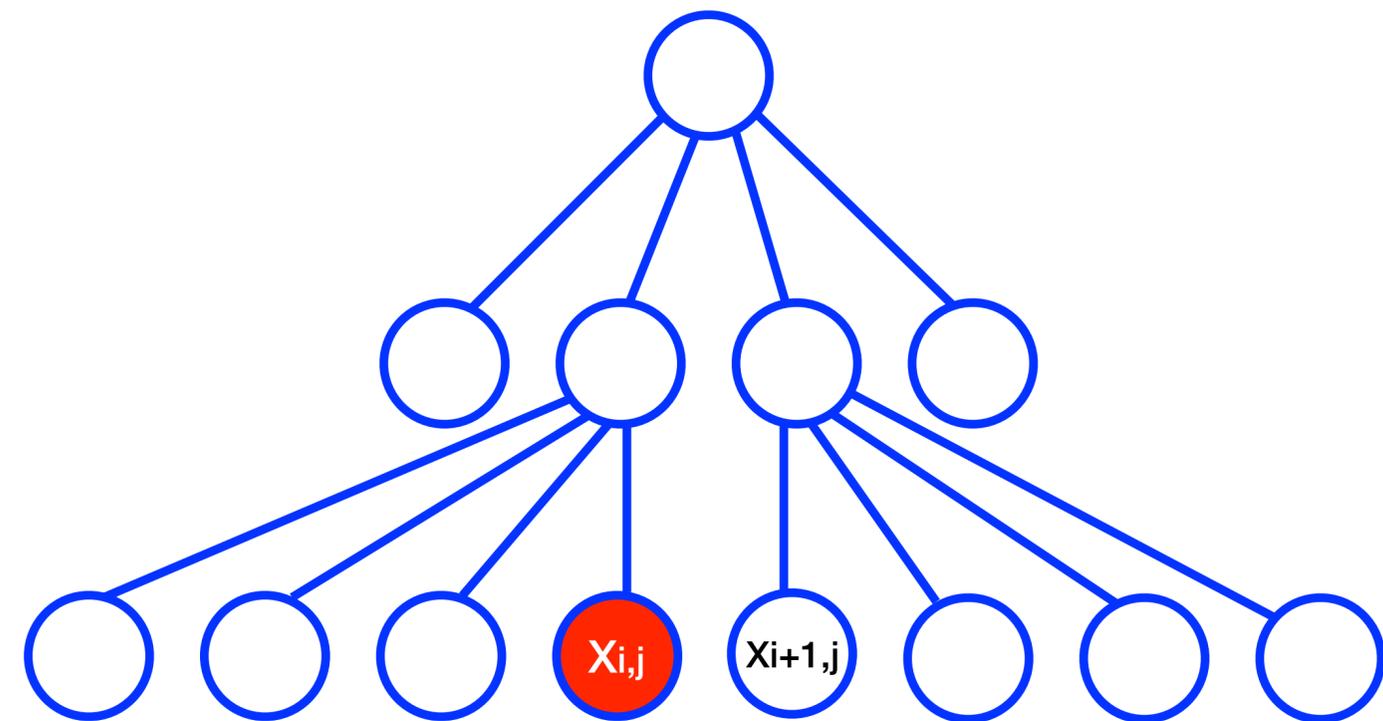
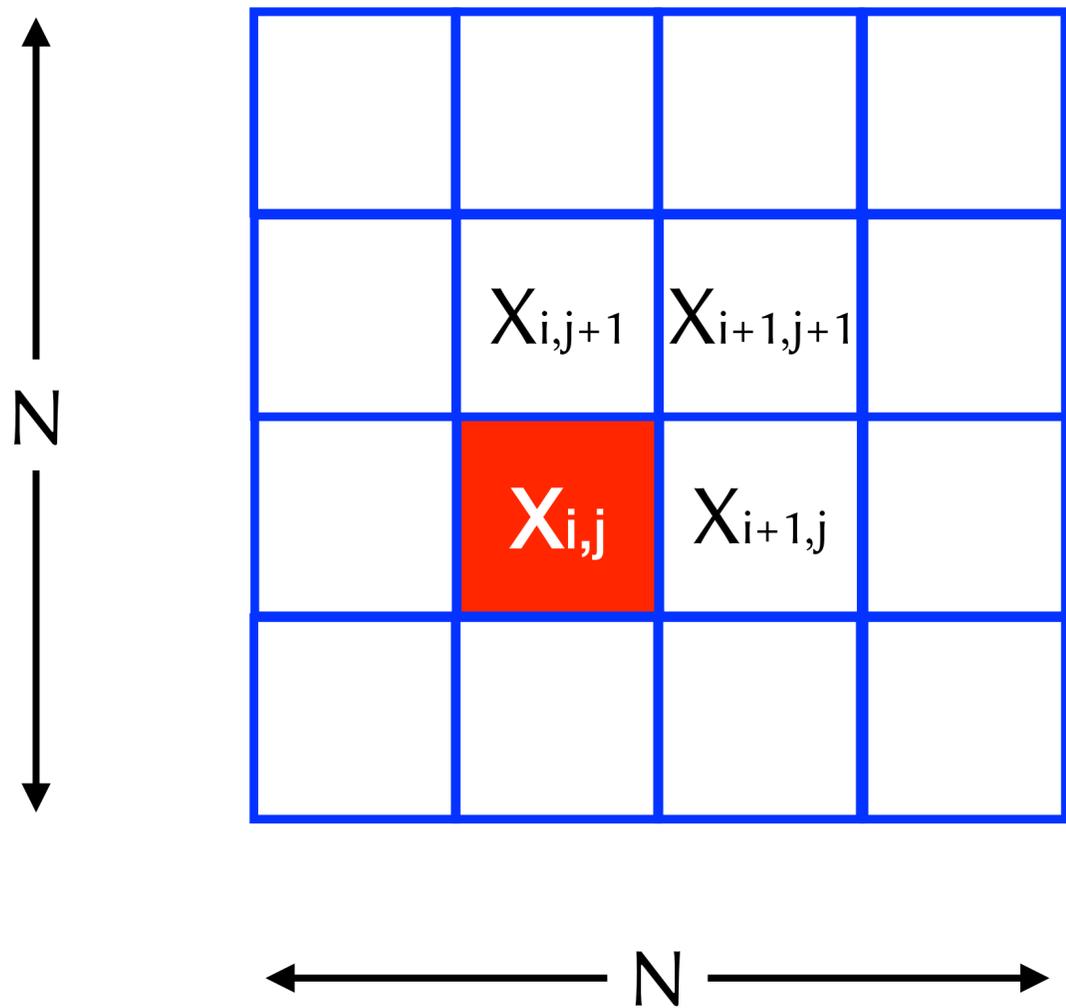


Memory



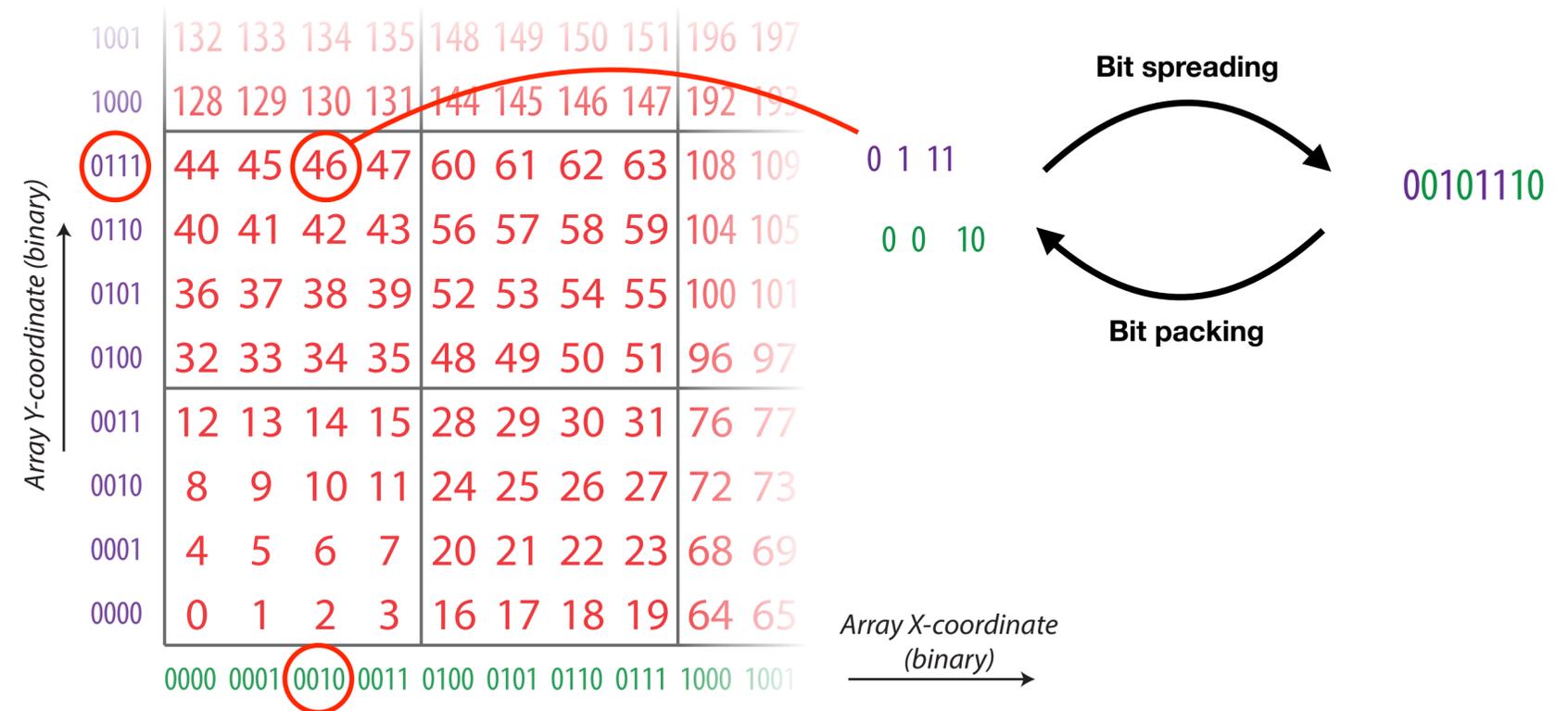
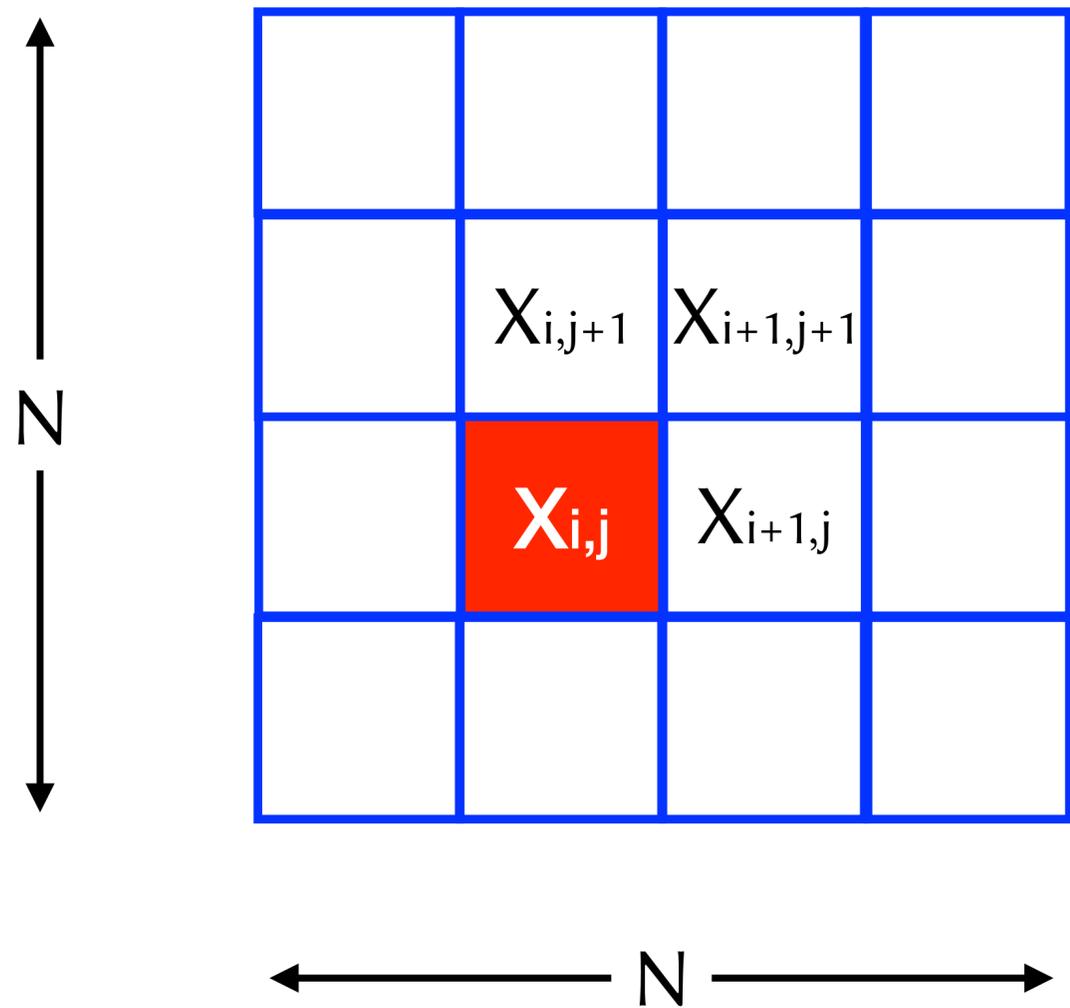
Dense array

# Stencil operations



Octree

# Stencil operations



SPGrid

# Material point method (MPM)

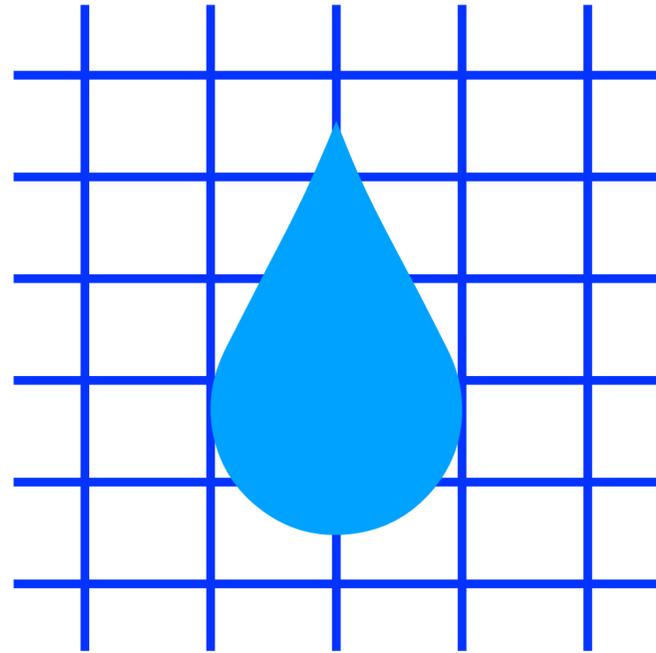


Stomakhin et al. 13



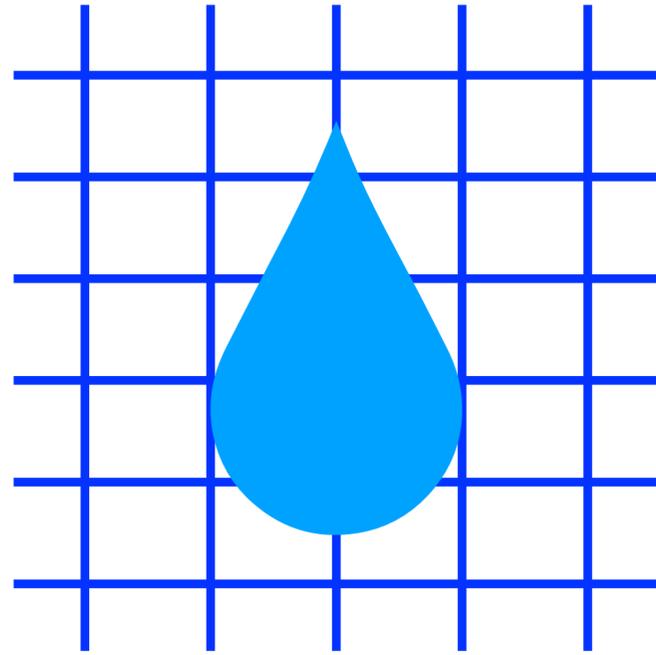
Gao et al. 18

# Discretization schemes

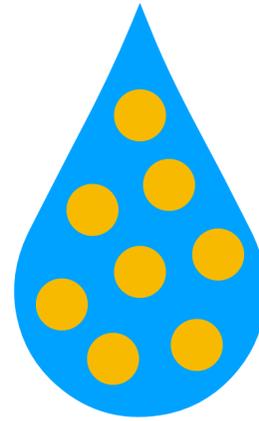


Grid

# Discretization schemes

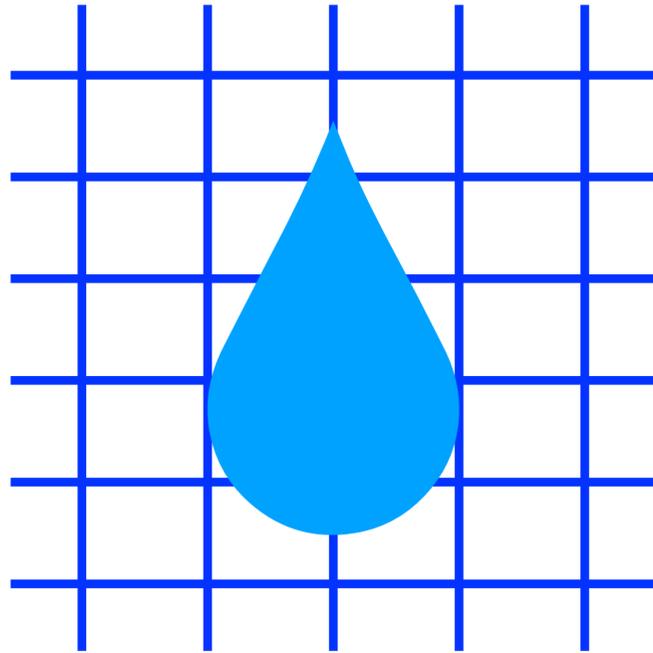


Grid

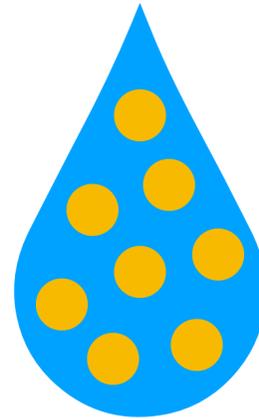


Particle

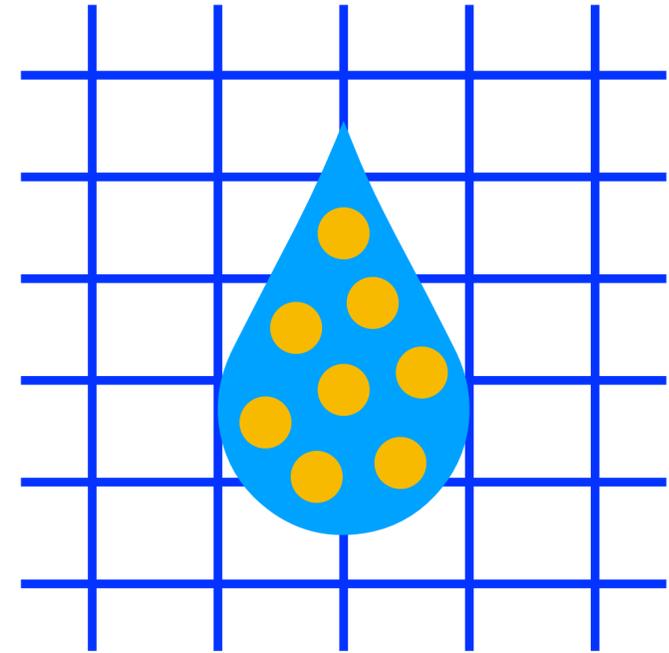
# Discretization schemes



Grid

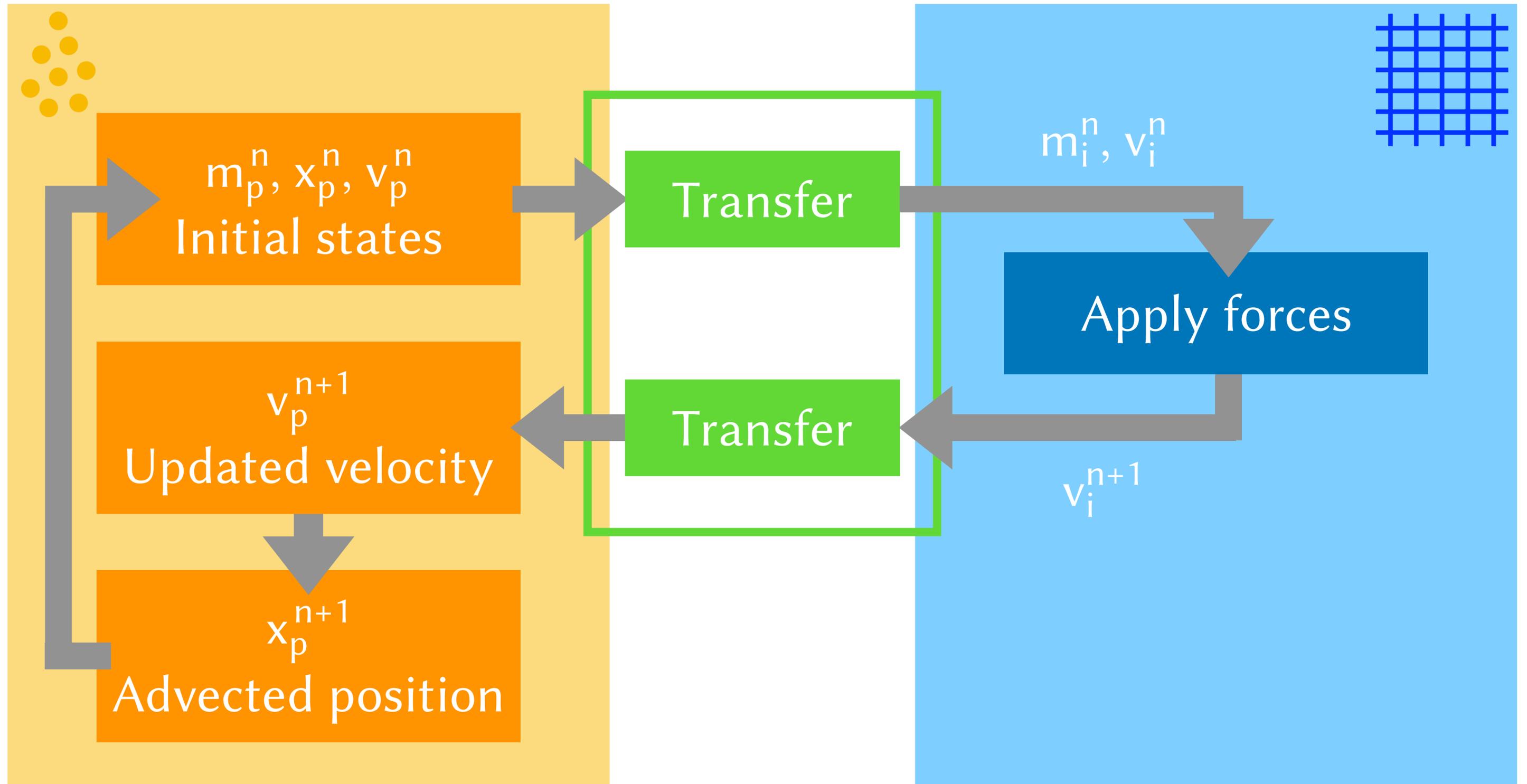


Particle

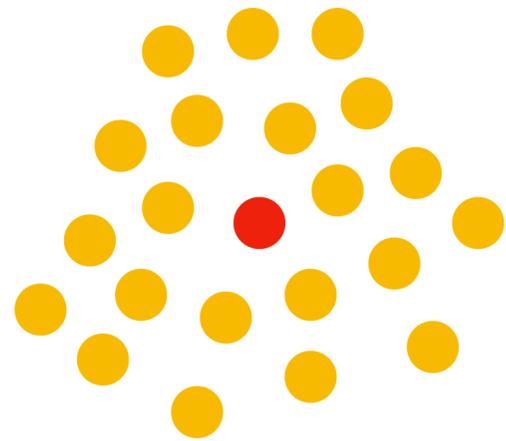


Hybrid

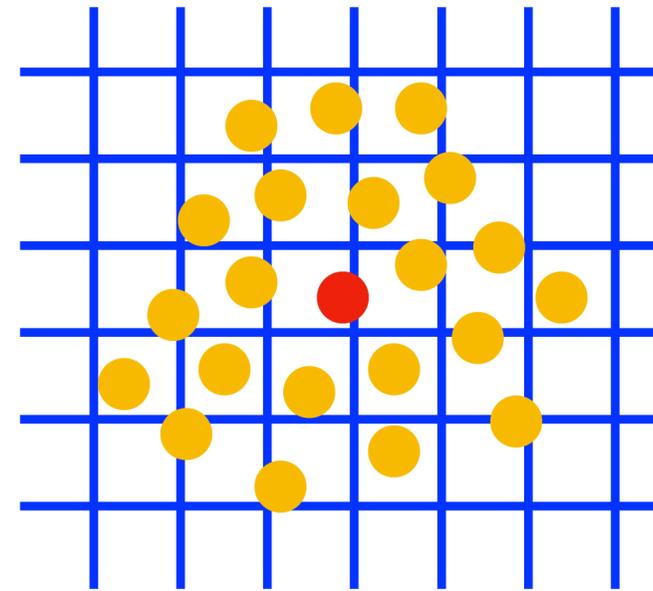
# Data flow



# Particle communication

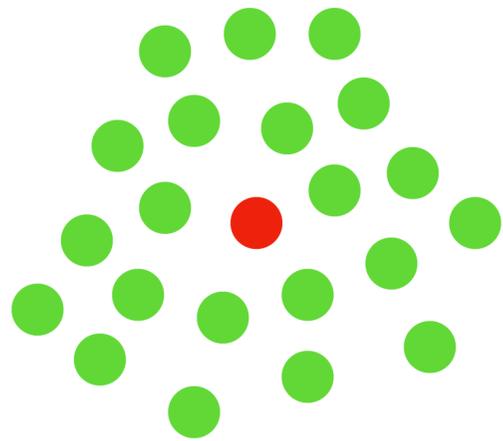


SPH

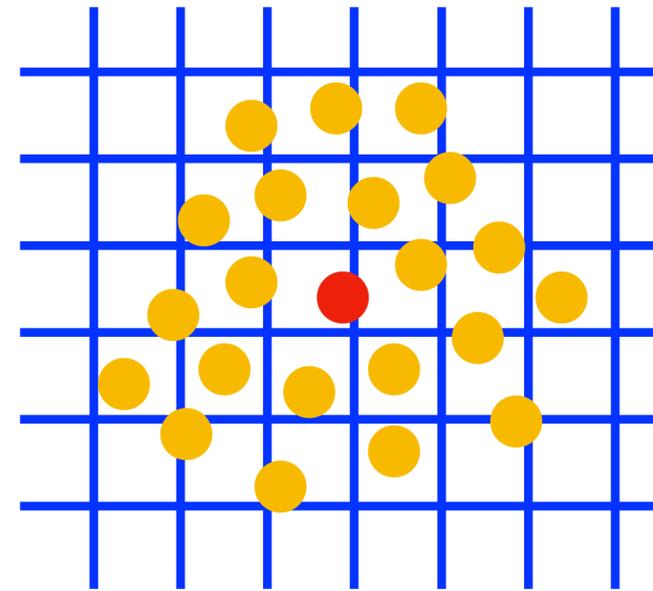


MPM

# Particle communication

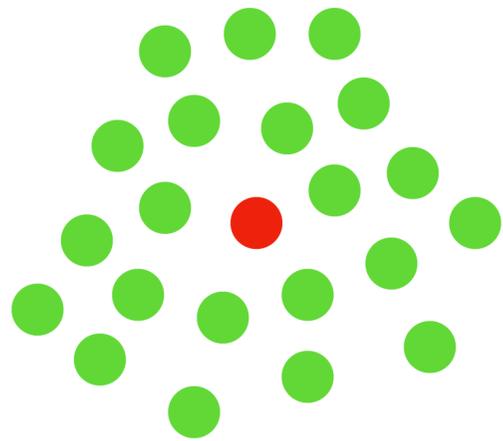


SPH

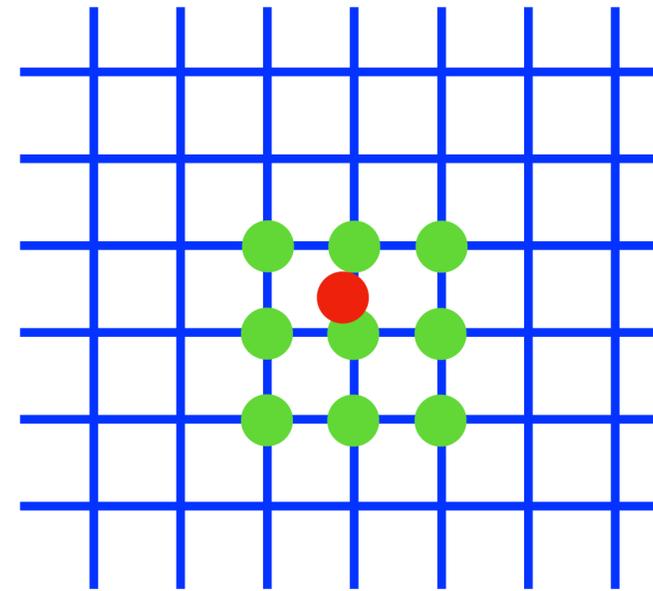


MPM

# Particle communication

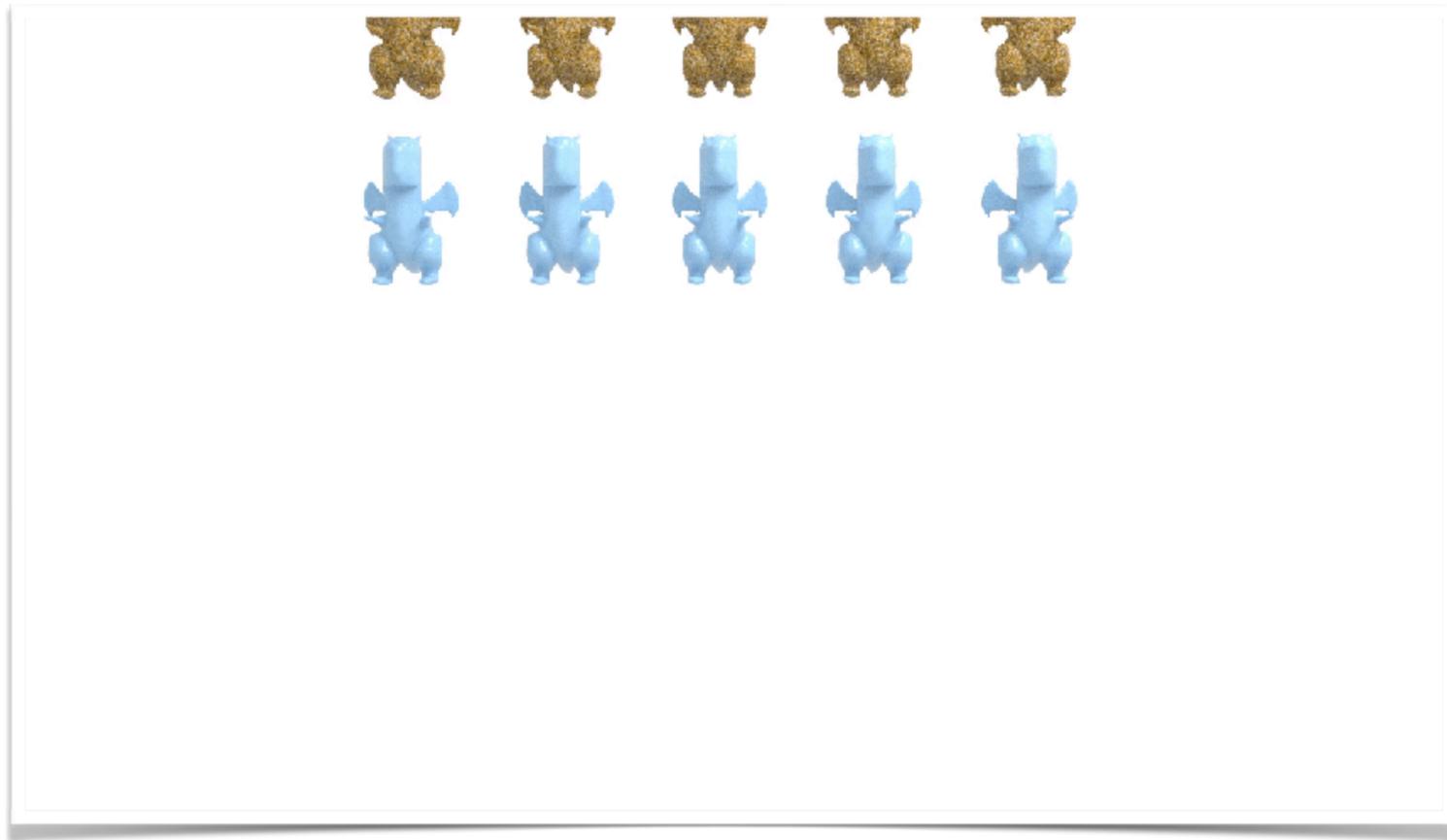


SPH

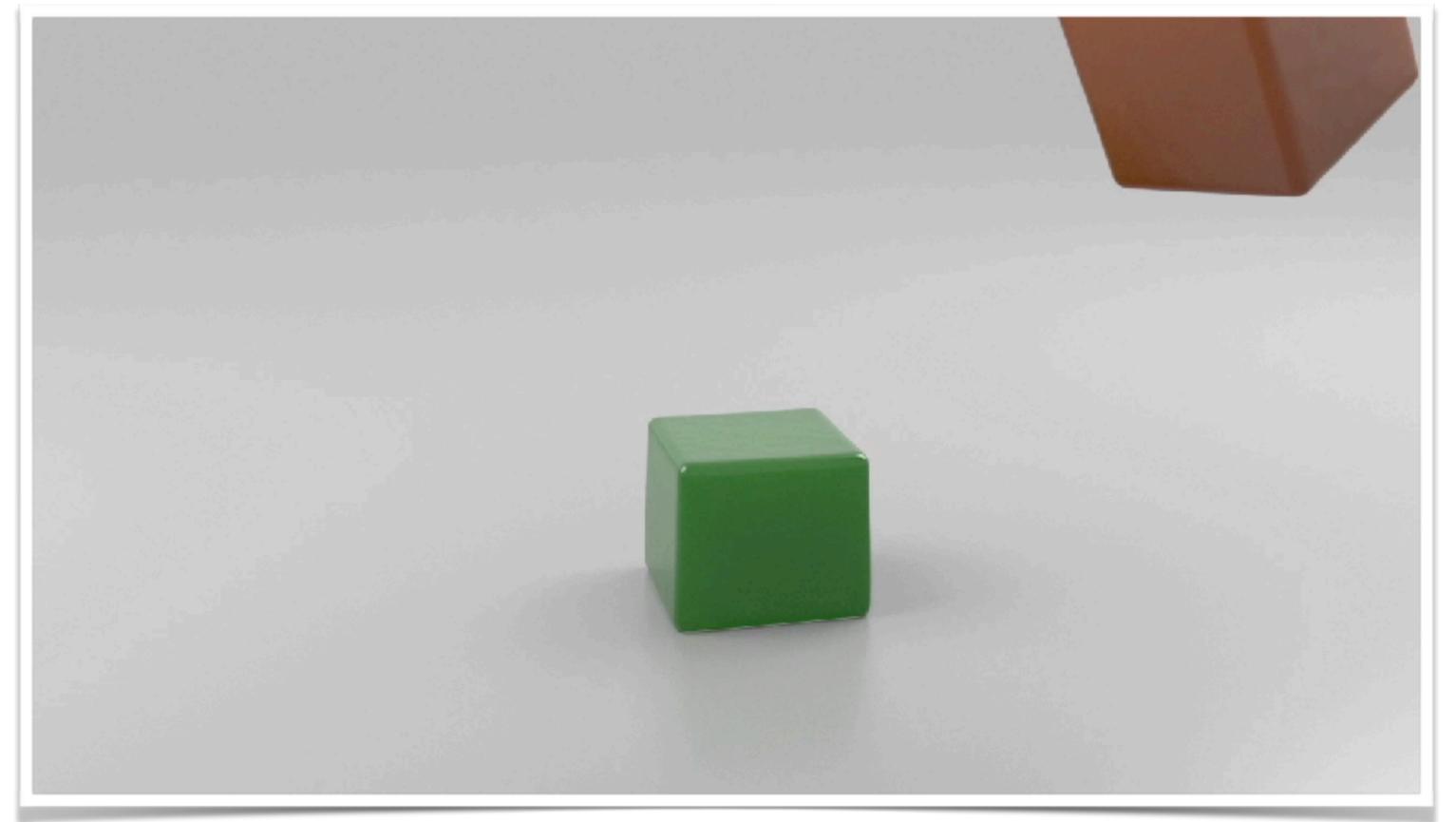


MPM

# Sparsity



Gao et al. 18



Gao et al. 17

# Power Diagrams and Sparse Paged Grids for High Resolution Adaptive Liquids

## Power Diagrams and Sparse Paged Grids for High Resolution Adaptive Liquids

MRIDUL AANJANEYA<sup>†\*</sup>, Rutgers University  
MING GAO<sup>†</sup> and HAIXIANG LIU, University of Wisconsin - Madison  
CHRISTOPHER BATTY, University of Waterloo  
EFTYCHIOS SIFAKIS, University of Wisconsin - Madison

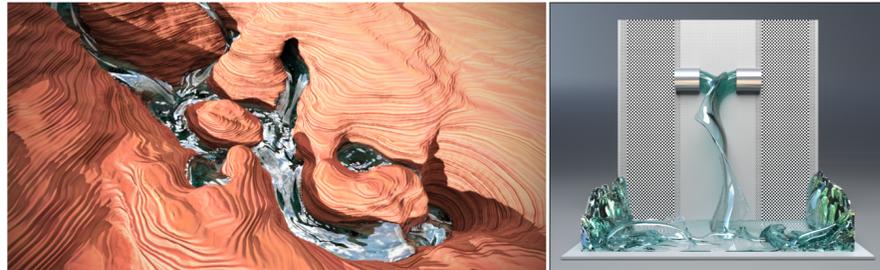


Fig. 1. (Left) Water filling a river bed surrounded by a canyon, with effective resolution  $512^2 \times 1024$ . Three refinement levels are used, based on proximity to the terrain. (Right) Sources inject water into a container and collide to form a thin sheet, with effective resolution  $512^3$ . Adaptivity pattern shown on background.

We present an efficient and scalable octree-inspired fluid simulation framework with the flexibility to leverage adaptivity in any part of the computational domain, even when resolution transitions reach the free surface. Our methodology ensures symmetry, definiteness and second order accuracy of the discrete Poisson operator, and eliminates numerical and visual artifacts of prior octree schemes. This is achieved by adapting the operators acting on the octree's simulation variables to reflect the structure and connectivity of a *power diagram*, which recovers primal-dual mesh orthogonality and eliminates problematic T-junction configurations. We show how such operators can be efficiently implemented using a pyramid of sparsely populated uniform grids, enhancing the regularity of operations and facilitating parallelization. A novel scheme is proposed for encoding the topology of the power diagram in the neighborhood of each octree cell, allowing us to locally reconstruct it on the fly via a lookup table, rather than resorting to costly explicit meshing. The pressure Poisson equation is solved via a highly efficient, matrix-free multigrid preconditioner for Conjugate Gradient, adapted to the power diagram discretization. We use another sparsely

populated uniform grid for high resolution interface tracking with a narrow band level set representation. Using the recently introduced SPGrid data structure, sparse uniform grids in both the power diagram discretization and our narrow band level set can be compactly stored and efficiently updated via streaming operations. Additionally, we present enhancements to adaptive level set advection, velocity extrapolation, and the fast marching method for redistancing. Our overall framework gracefully accommodates the task of dynamically adapting the octree topology during simulation. We demonstrate end-to-end simulations of complex adaptive flows in irregularly shaped domains, with tens of millions of degrees of freedom.

CCS Concepts: • **Computing methodologies** → **Physical simulation**;

Additional Key Words and Phrases: Power diagrams, Octrees, Adaptivity

### ACM Reference format:

Mridul Aanjaneya, Ming Gao, Haixiang Liu, Christopher Batty, and Eftychios Sifakis. 2017. Power Diagrams and Sparse Paged Grids for High Resolution Adaptive Liquids. *ACM Trans. Graph.* 36, 4, Article 140 (July 2017), 12 pages. DOI: <http://dx.doi.org/10.1145/3072959.3073625>

## 1 INTRODUCTION

Liquids exhibit complex and detailed motion across a vast range of scales, from tiny ripples to huge waves; this fact motivates the desire for liquid simulation tools that can handle ever increasing levels of resolution. While a key avenue towards this goal is the development of more efficient numerical methods on regular uniform grids that conserve mass with large time steps [Chentanez and Müller 2012; Lentine et al. 2011, 2012] and allow for fast pressure projection [Ando et al. 2015; Dick et al. 2016; Lentine et al. 2010; Liu

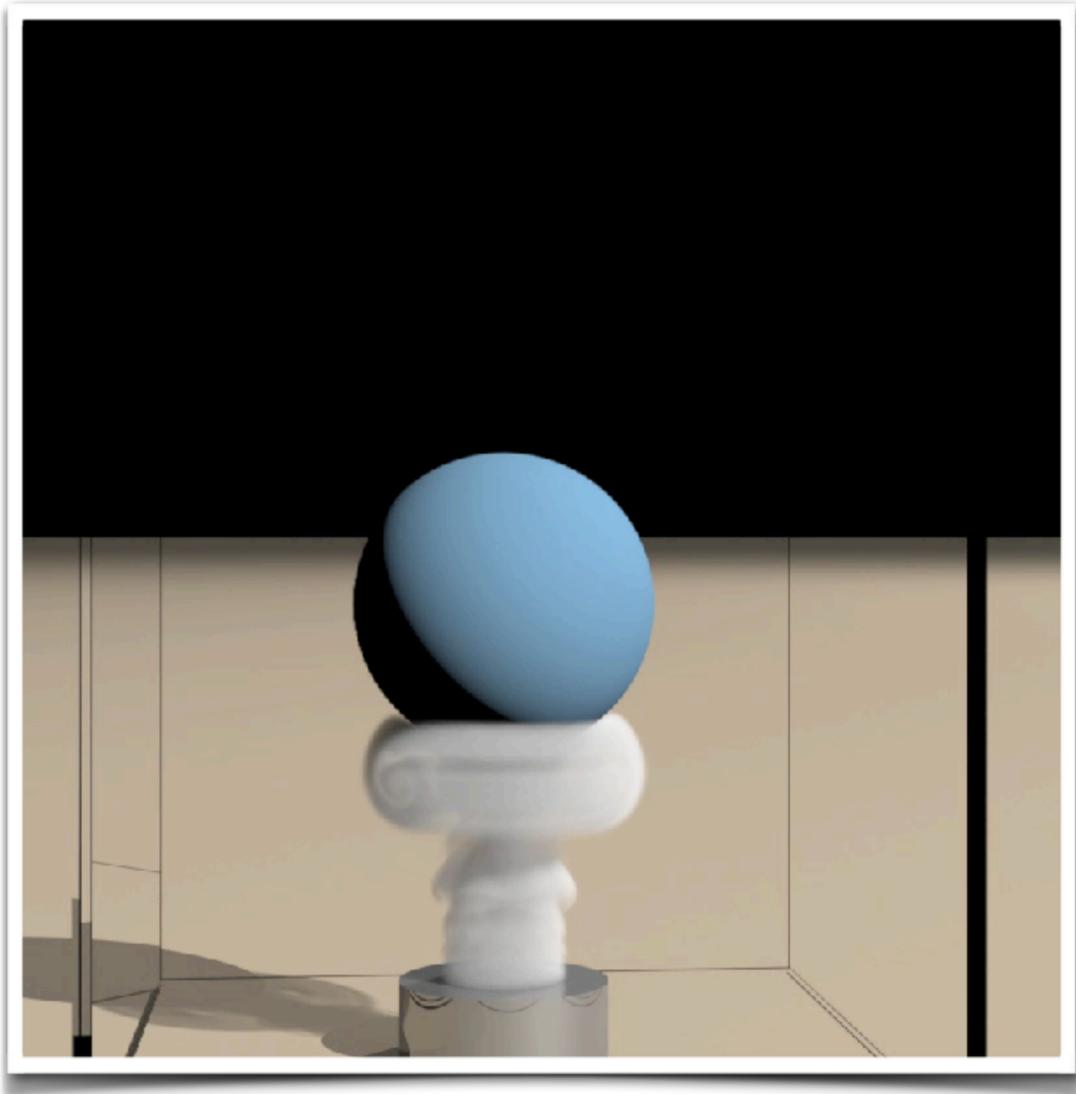
M. Aanjaneya\*, M. Gao\* (joint first authors), H. Liu, C. Batty, E. Safaris  
ACM Transactions on Graphics (Proceedings of ACM SIGGRAPH), 2017

30 JULY – 3 AUGUST *Los Angeles*  
**SIGGRAPH2017**



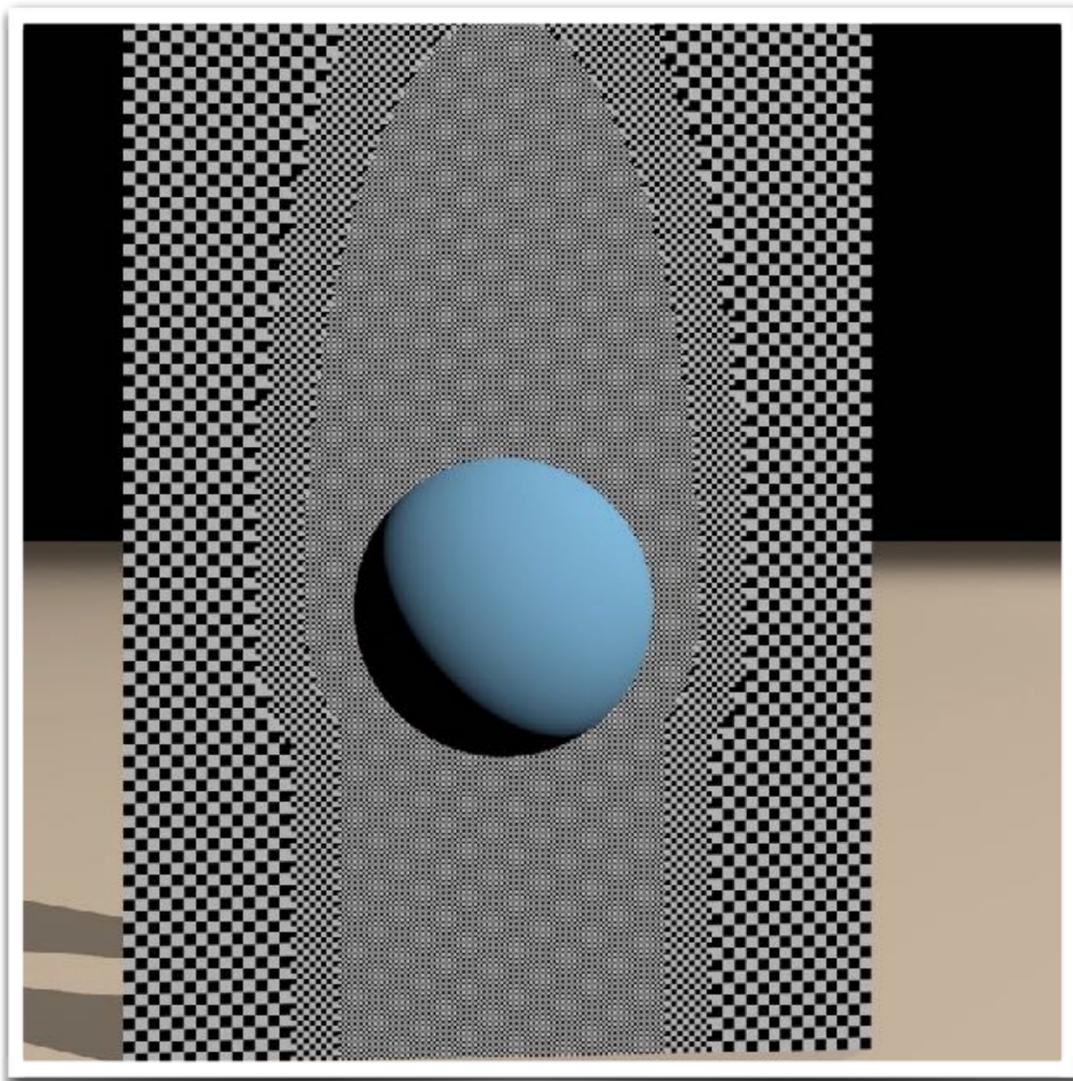
<sup>†</sup> M. Aanjaneya and M. Gao are joint first authors.  
<sup>\*</sup> M. Aanjaneya was with the University of Wisconsin - Madison during this work. This work was supported in part by National Science Foundation grants IIS-1253598, CCF-1423064, CCF-1533885 and by the Natural Sciences and Engineering Research Council of Canada under grant RGPIN-04360-2014. The authors are grateful to Nathan Mitchell for his indispensable help with modeling and rendering of examples. C. Batty would like to thank Ted Ying for carrying out preliminary explorations on quad-trees. Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from [permissions@acm.org](mailto:permissions@acm.org).  
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DOI: <http://dx.doi.org/10.1145/3072959.3073625>

# Previous work

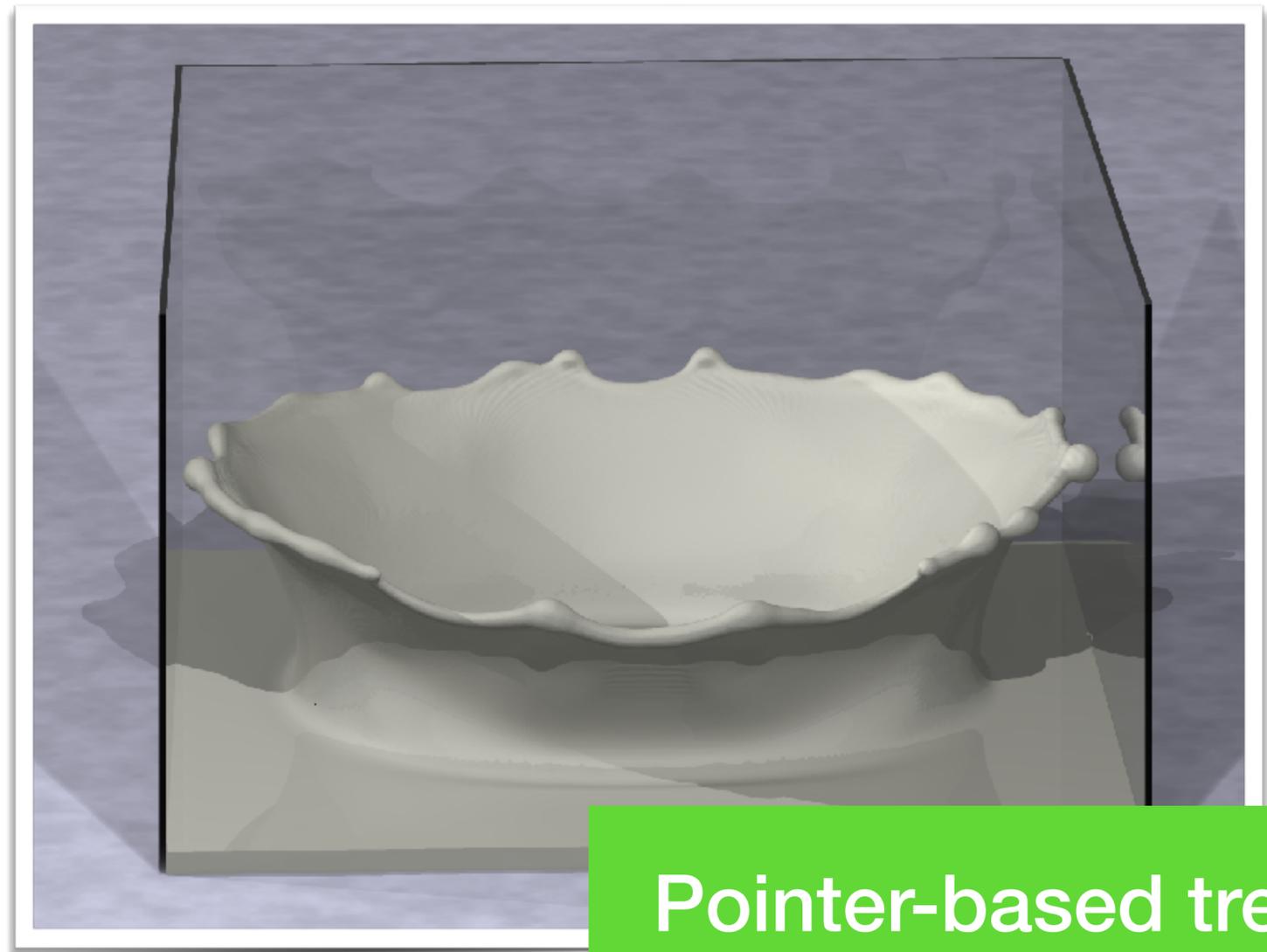


Setaluri et al. 14

# Previous work



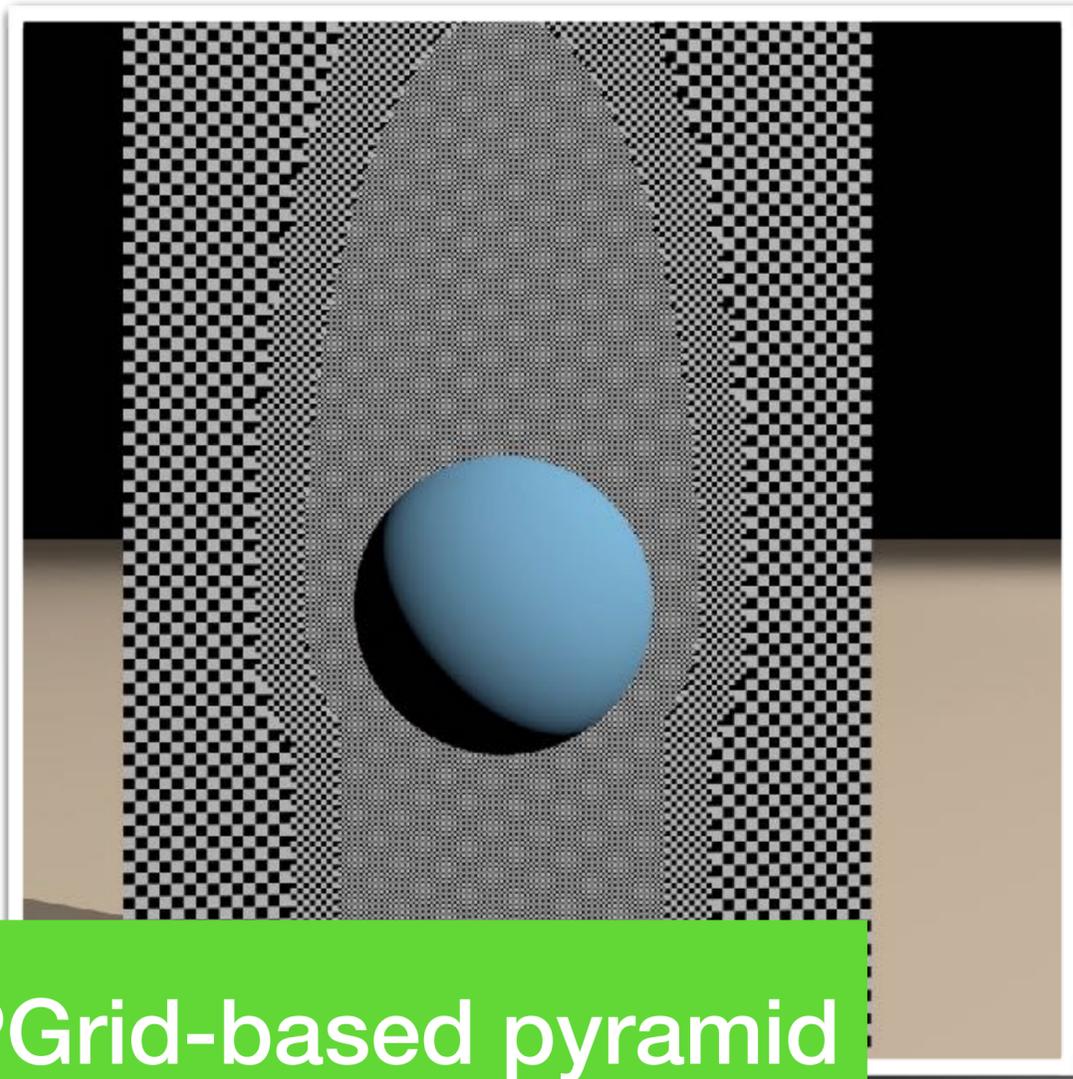
Setaluri et al. 14



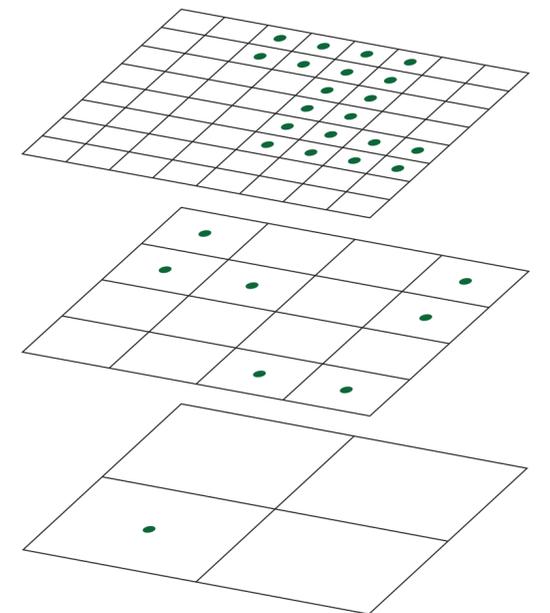
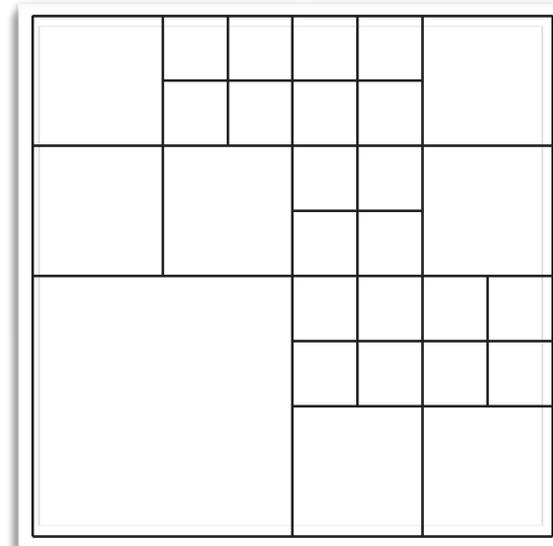
Pointer-based tree

Losasso et al. 04

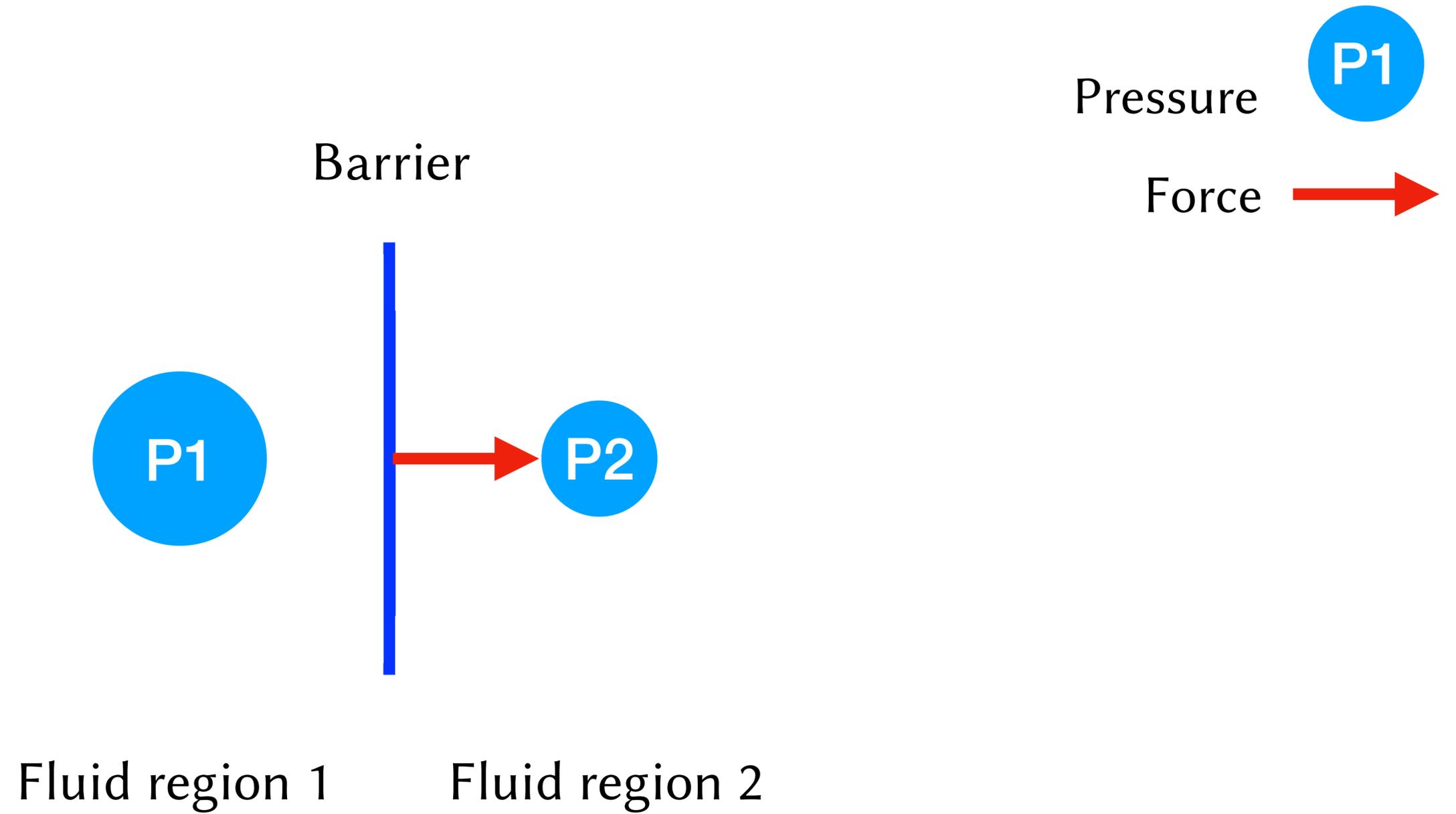
# Previous work



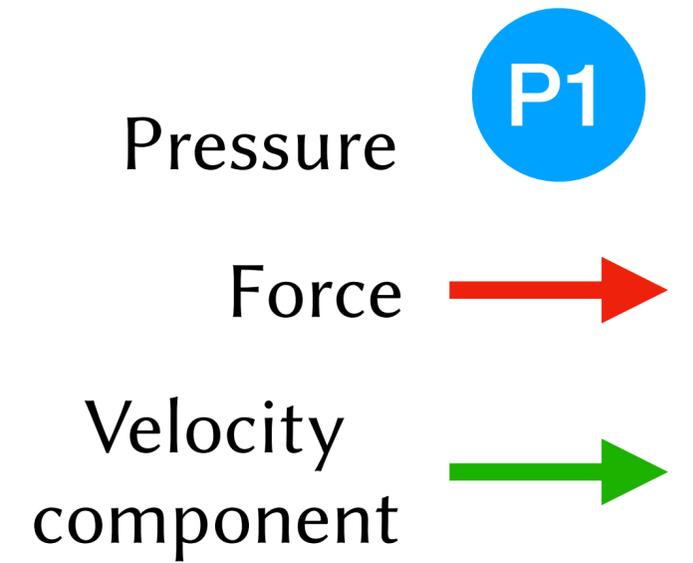
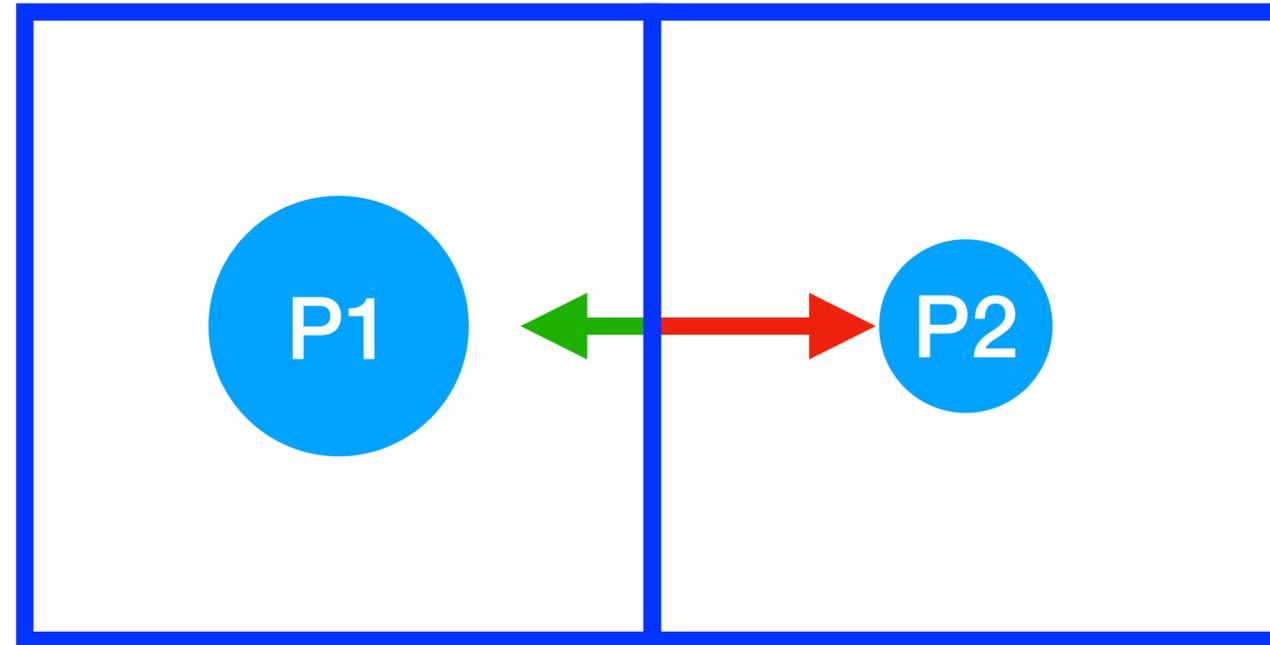
SPGrid-based pyramid



# Loss of orthogonality

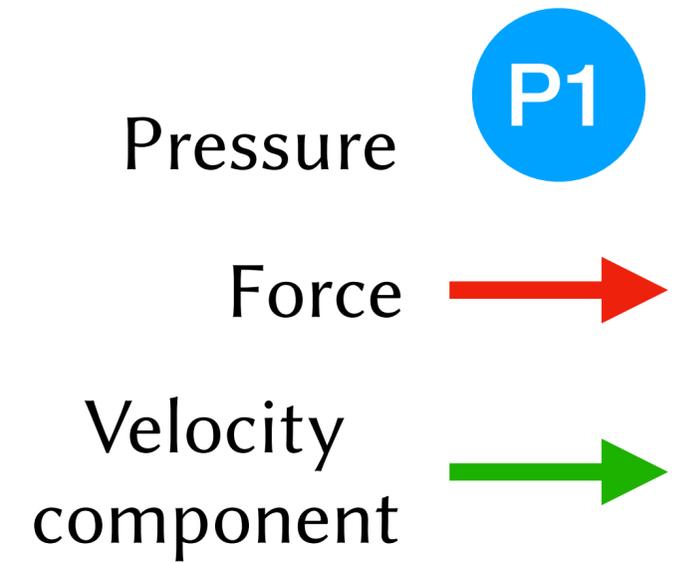
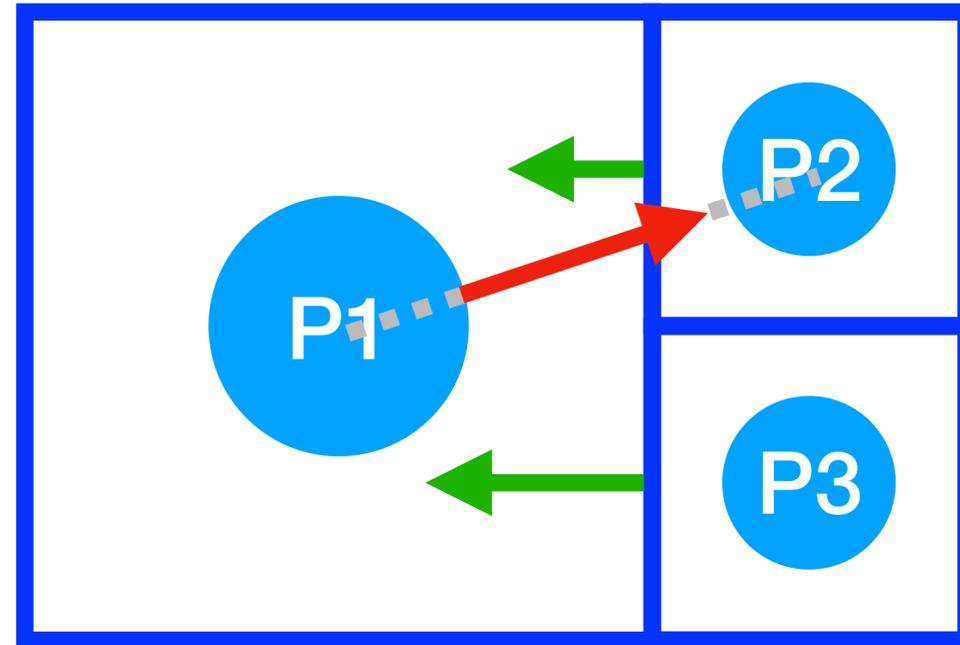


# Loss of orthogonality

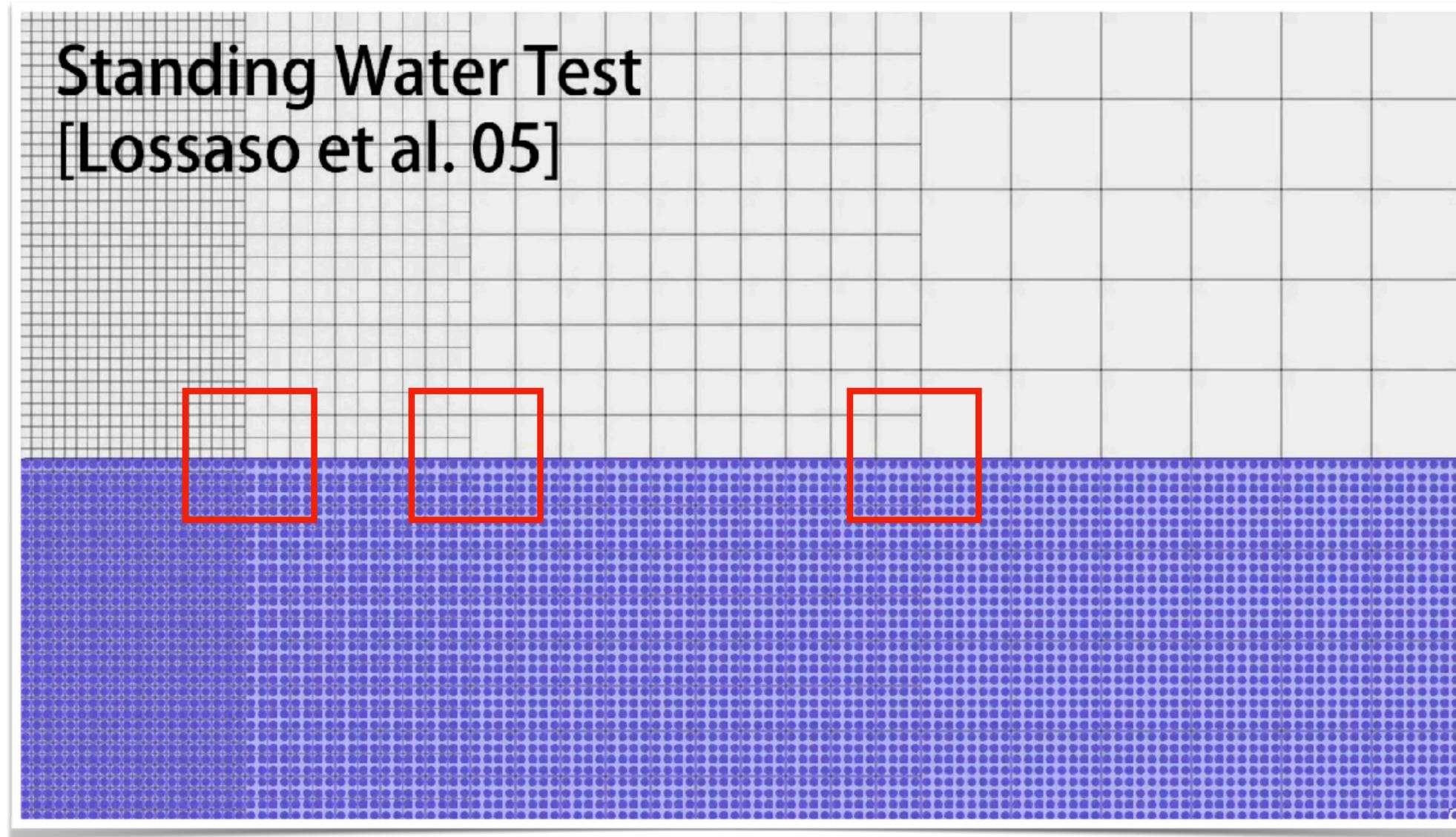


Staggered grid

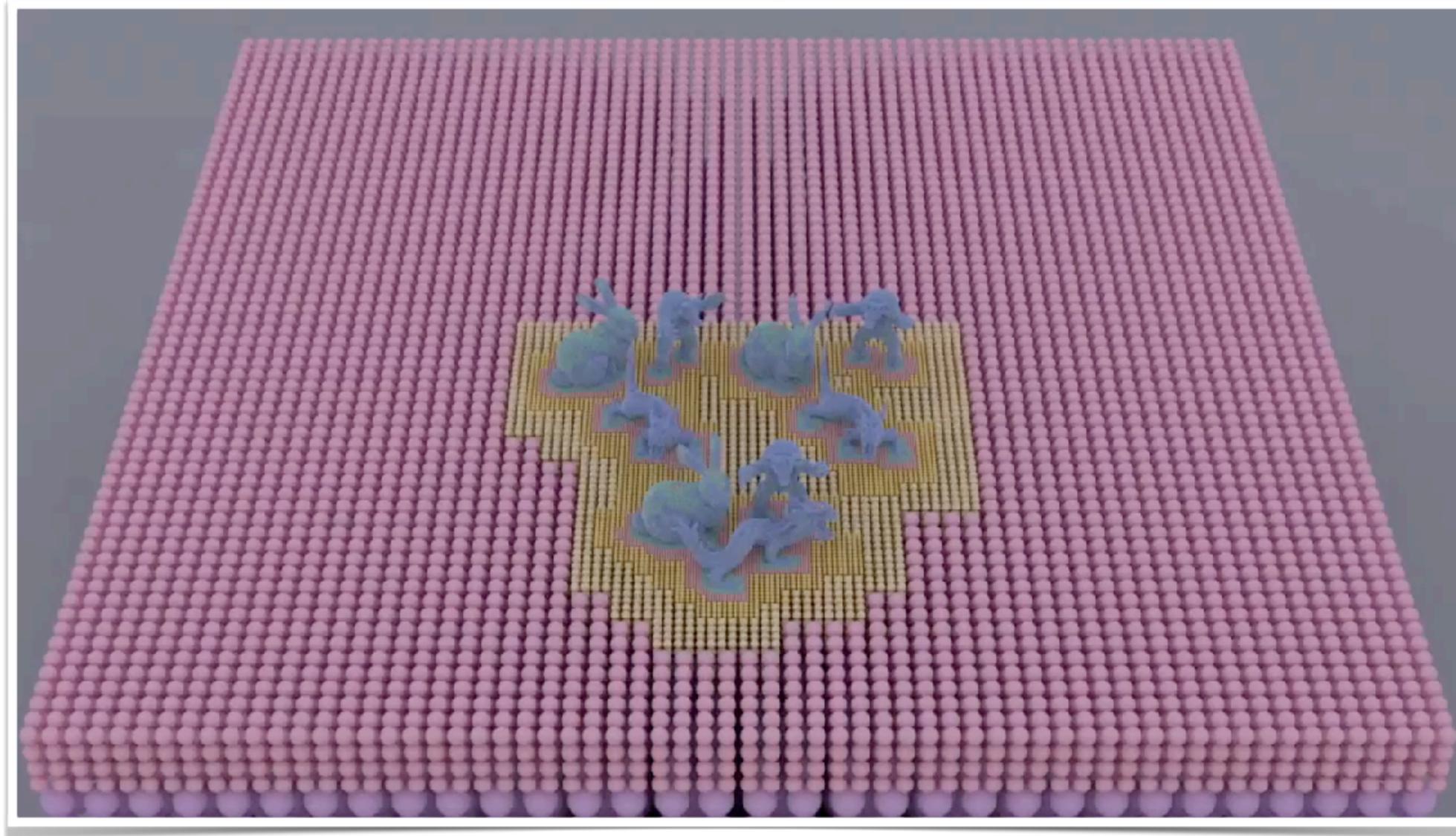
# Loss of orthogonality



# Spurious motions

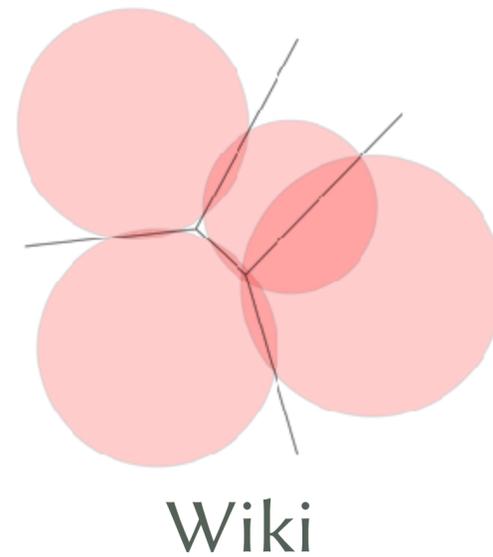
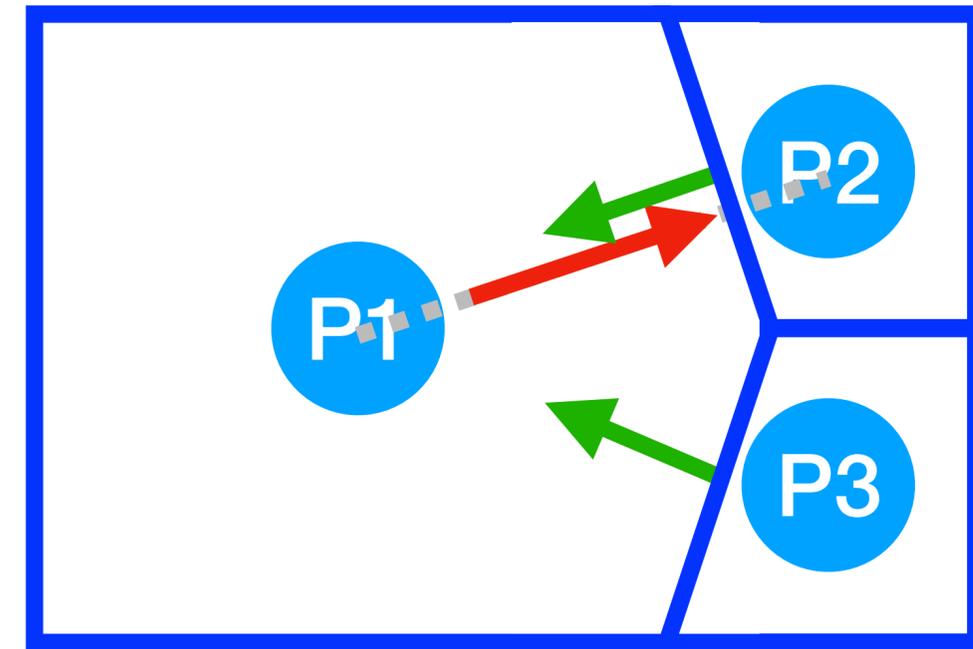
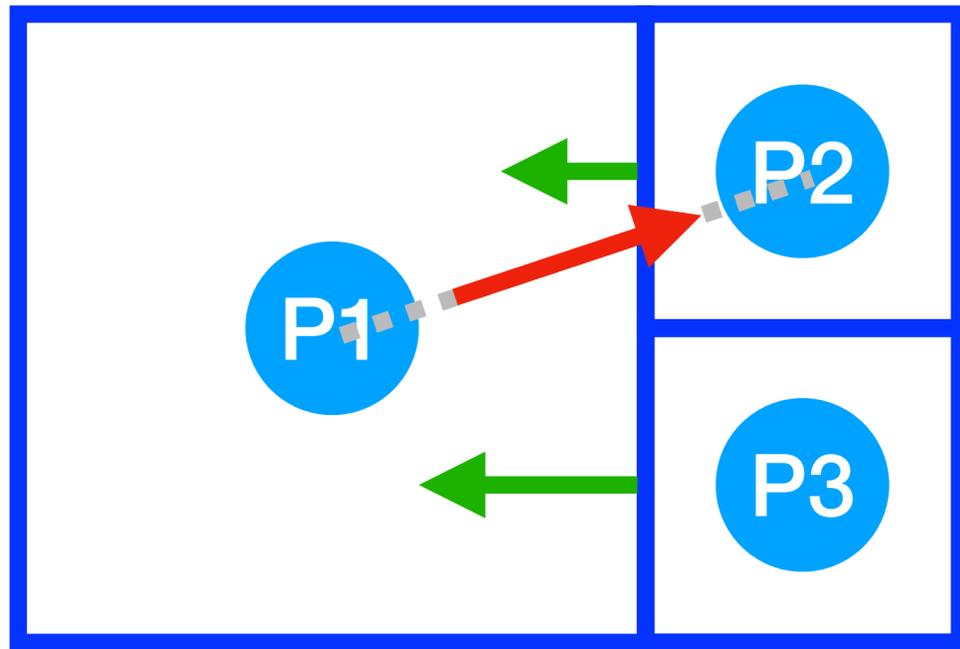


# Unstructured mesh



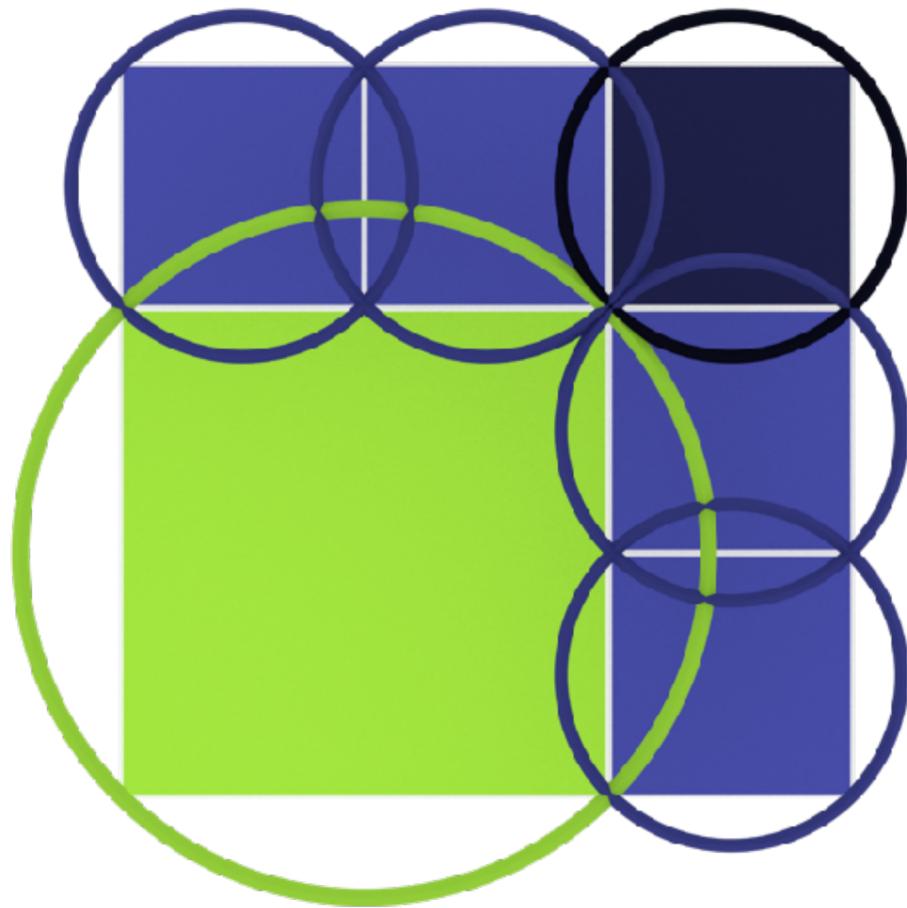
Ando et al. 13

# Our solution: power diagram

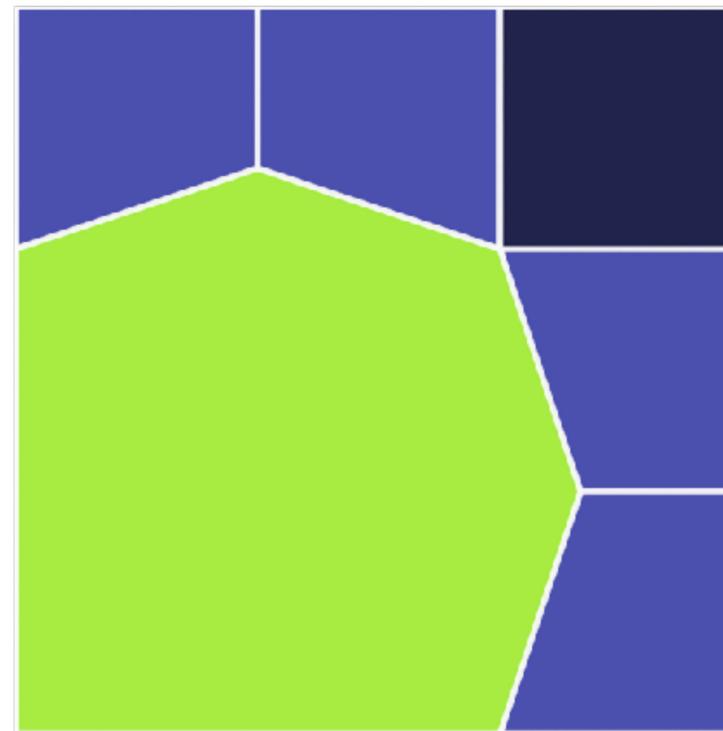


# Comparison

Original topology

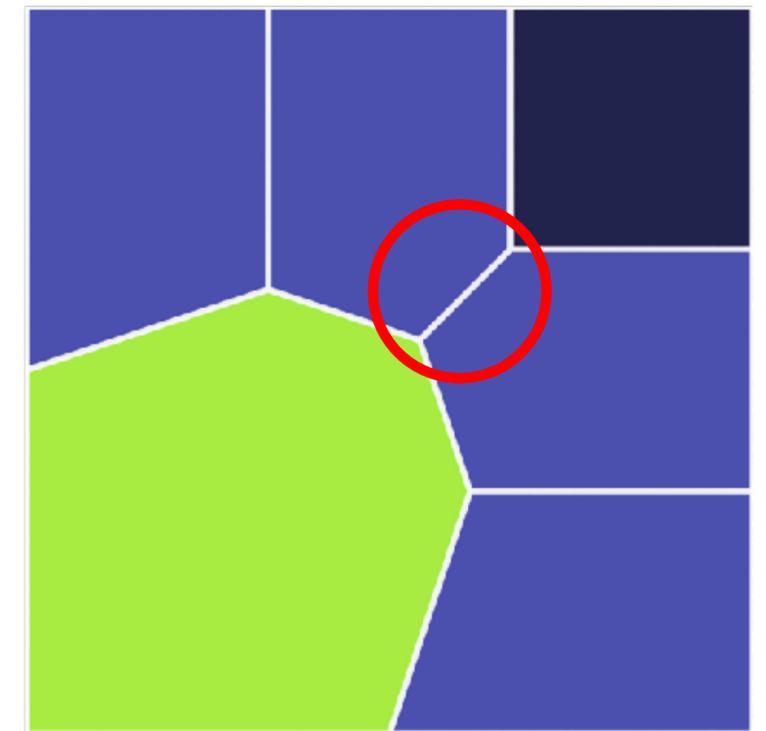


Power diagram



$$d^2 - r^2$$

Voronoi diagram



$$d^2$$

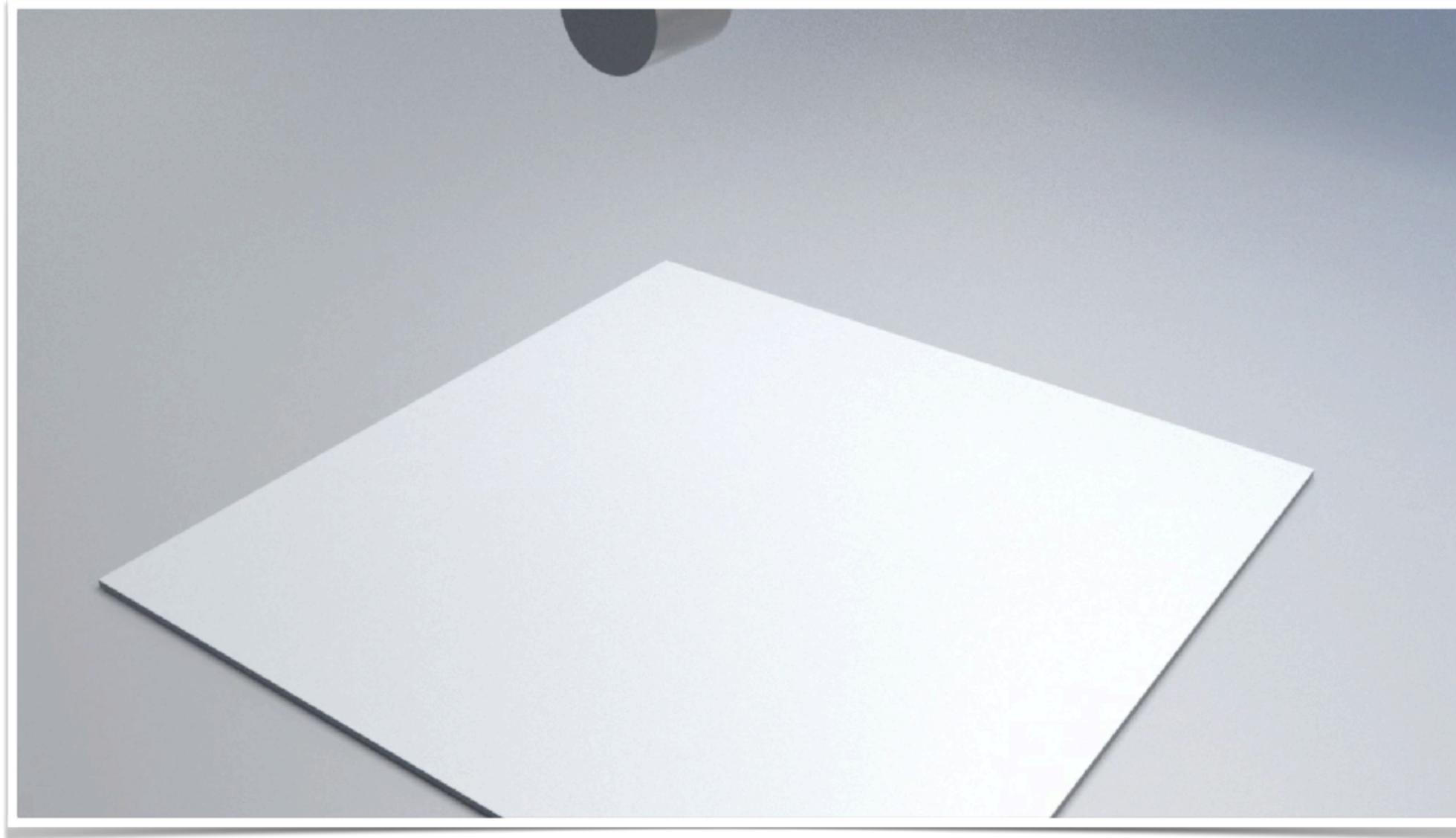
# Opportunities

- Power diagram ensures orthogonality
- Can still use octree for storage
- Accelerate via SPGrid

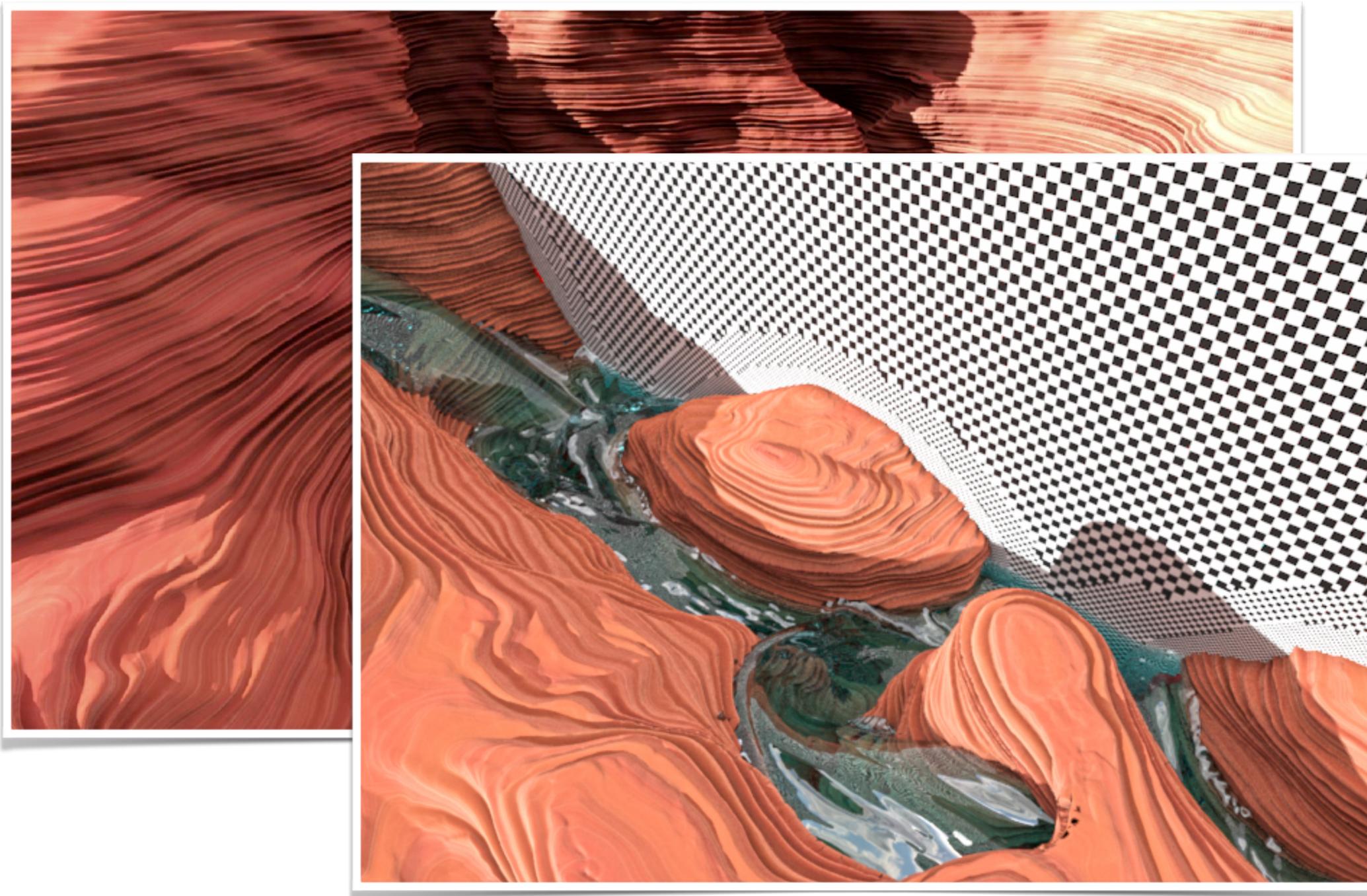
# Further technicalities (see thesis)

- Minor topological complications (3D)
- Velocity interpolation
- Retrieval of Poisson equation stencils

# Results



# Results



# An Adaptive Generalized Interpolation Material Point Method for Simulating Elastoplastic Materials

An Adaptive Generalized Interpolation Material Point Method for Simulating Elastoplastic Materials

MING GAO, University of Wisconsin Madison  
ANDRE PRADHANA TAMPUBOLON, University of Pennsylvania  
CHENFANFU JIANG, University of Pennsylvania  
EFTYCHIOS SIFAKIS, University of Wisconsin Madison

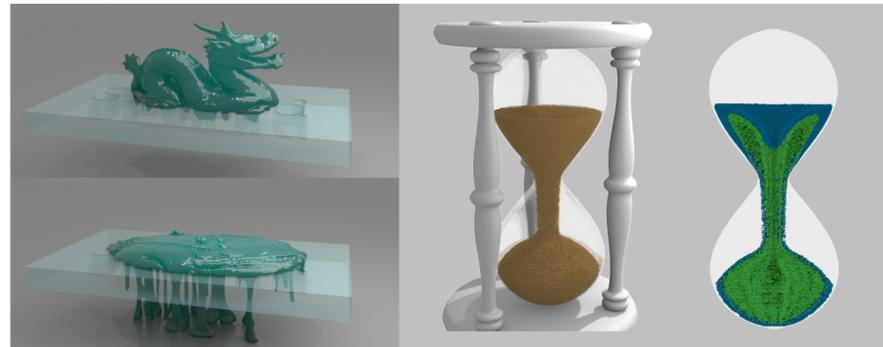


Fig. 1. Left: An elastoplastic model is dropped into a plane with a thin perforation pattern; our adaptive discretization allows the material to drip through. Right: Adaptive sand simulation with a visualization of the underlying grid refinement. We color refined particles with blue and coarse ones with green.

We present an adaptive Generalized Interpolation Material Point (GIMP) method for simulating elastoplastic materials. Our approach allows adaptive refining and coarsening of different regions of the material, leading to an efficient MPM solver that concentrates most of the computation resources in specific regions of interest. We propose a  $C^1$  continuous adaptive basis function that satisfies the partition of unity property and remains non-negative throughout the computational domain. We develop a practical strategy for particle-grid transfers that leverages the recently introduced SPGrid data structure for storing sparse multi-layered grids. We demonstrate the robustness and efficiency of our method on the simulation of various elastic and plastic materials. We also compare key kernel components to uniform grid MPM solvers to highlight performance benefits of our method.

CCS Concepts: • **Computing methodologies** → **Physical simulation**;

Additional Key Words and Phrases: Material Point Method (MPM), Generalized Interpolation Material Point (GIMP), Adaptive grids, Elastoplasticity

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DOI: 10.1145/3130800.3130879

**ACM Reference format:**  
Ming Gao, Andre Pradhana Tampubolon, Chenfanfu Jiang, and Eftychios Sifakis. 2017. An Adaptive Generalized Interpolation Material Point Method for Simulating Elastoplastic Materials. *ACM Trans. Graph.* 36, 6, Article 223 (November 2017), 12 pages.  
DOI: 10.1145/3130800.3130879

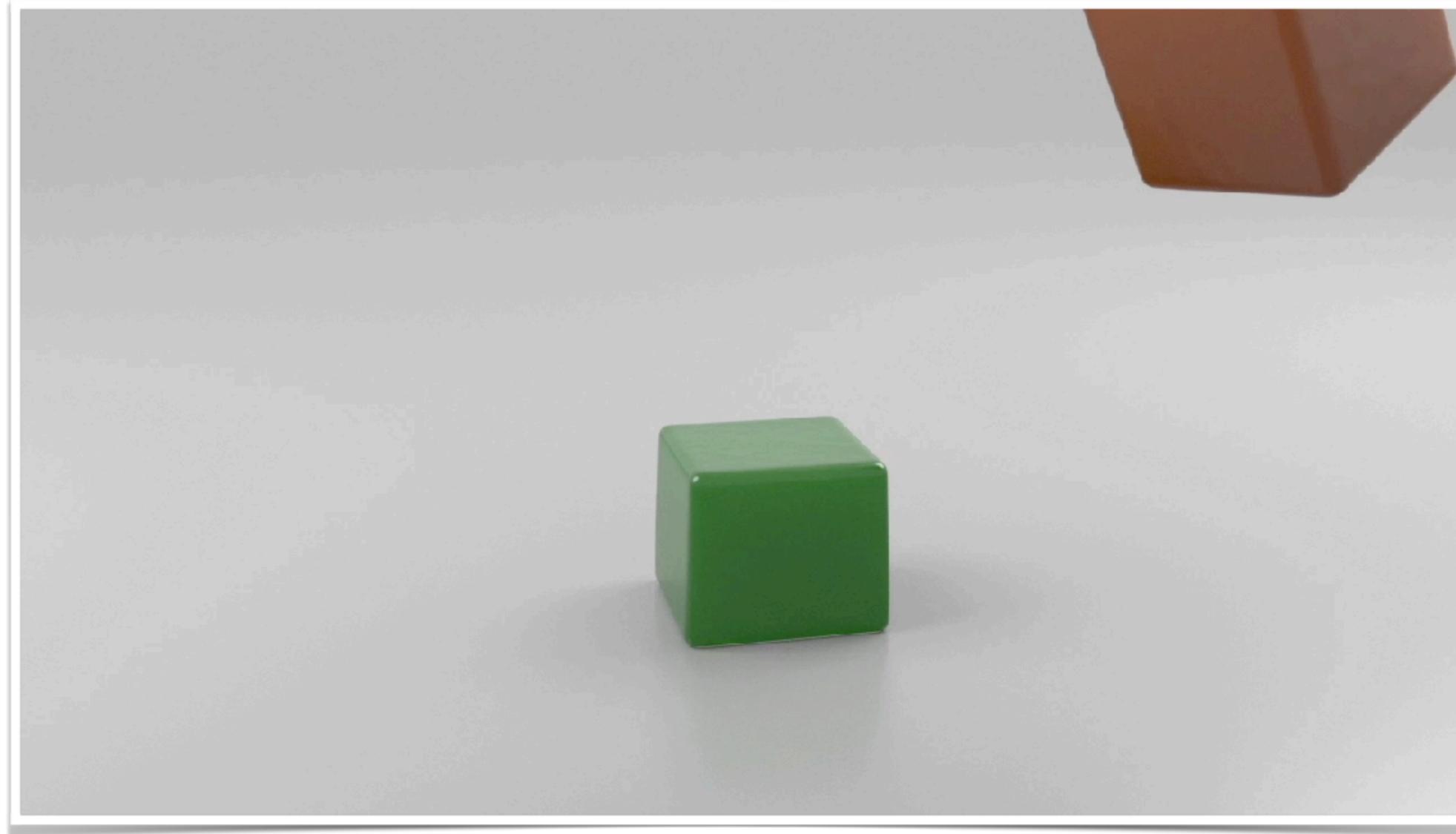
## 1 INTRODUCTION

The Material Point Method (MPM) has been attracting considerable interest since it was introduced to the field of computer graphics by Stomakhin et al. [2013]. Combining advantages from both Lagrangian particle representation and Eulerian grid representation, MPM proves to be especially effective for animating elastoplastic materials undergoing large deformation or topology change [Jiang et al. 2016]. Despite its physical realism and geometrical convenience, a traditional MPM solver has several disadvantages. First, it is more computationally expensive than mesh-based Lagrangian approaches such as those based on Finite Element Methods (FEM) [Sifakis and Barbic 2012]. The bottleneck of MPM is usually the costly transfer operations between the particles and the grid. The cost of such transfer operations is particularly evident when we realize that MPM has to maintain the same grid resolution and a sufficient particle count throughout the simulation domain. The overhead of this process is highlighted in scenarios such as the example of drawing in a

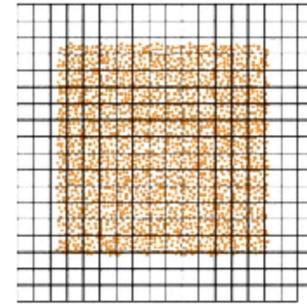
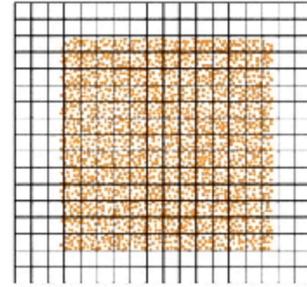
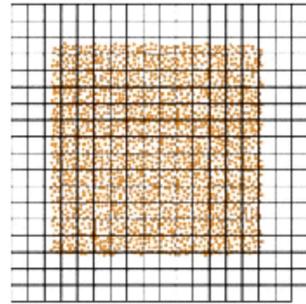
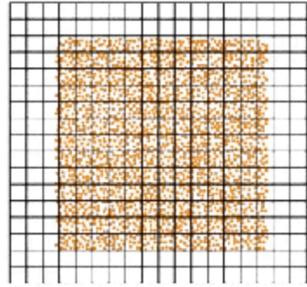
**M. Gao, A. Tampubolon, C. Jiang, E. Sifakis**  
ACM Transactions on Graphics (Proceedings of  
ACM SIGGRAPH Asia), 2017



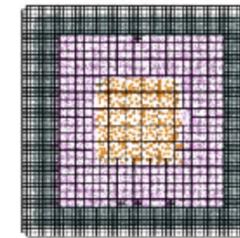
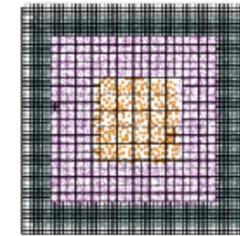
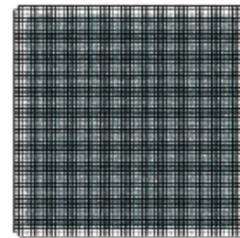
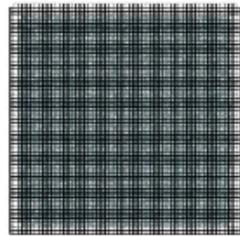
# Motivation



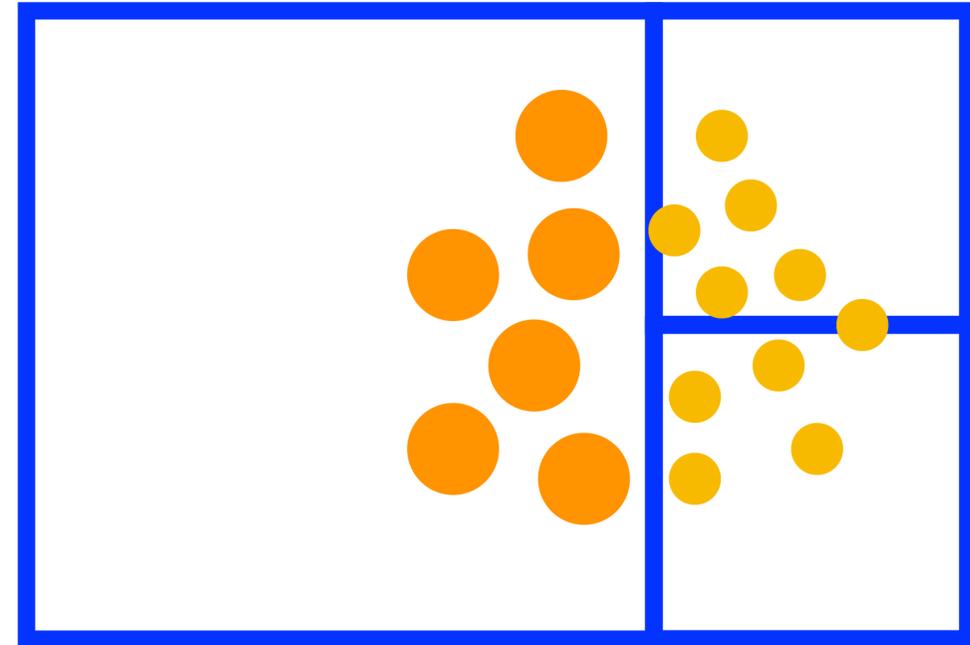
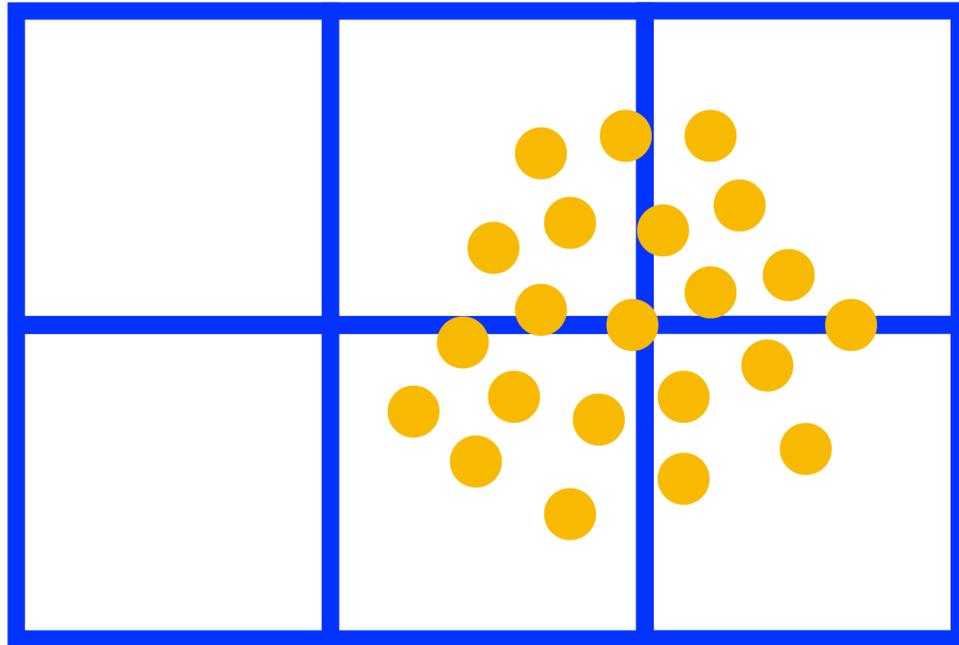
# Motivation



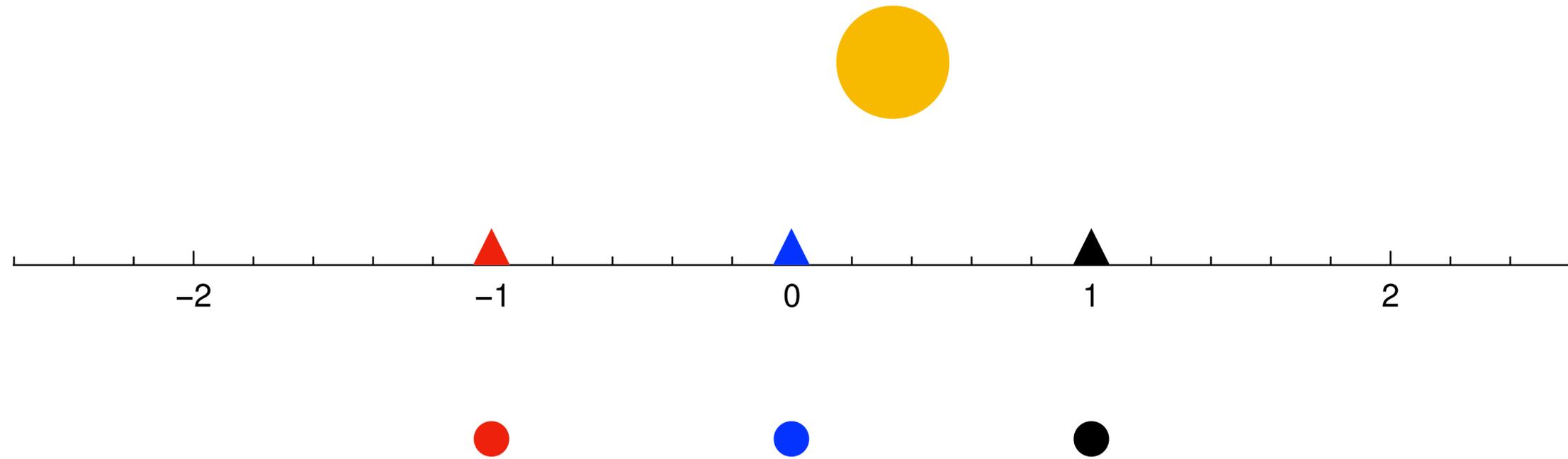
# Motivation



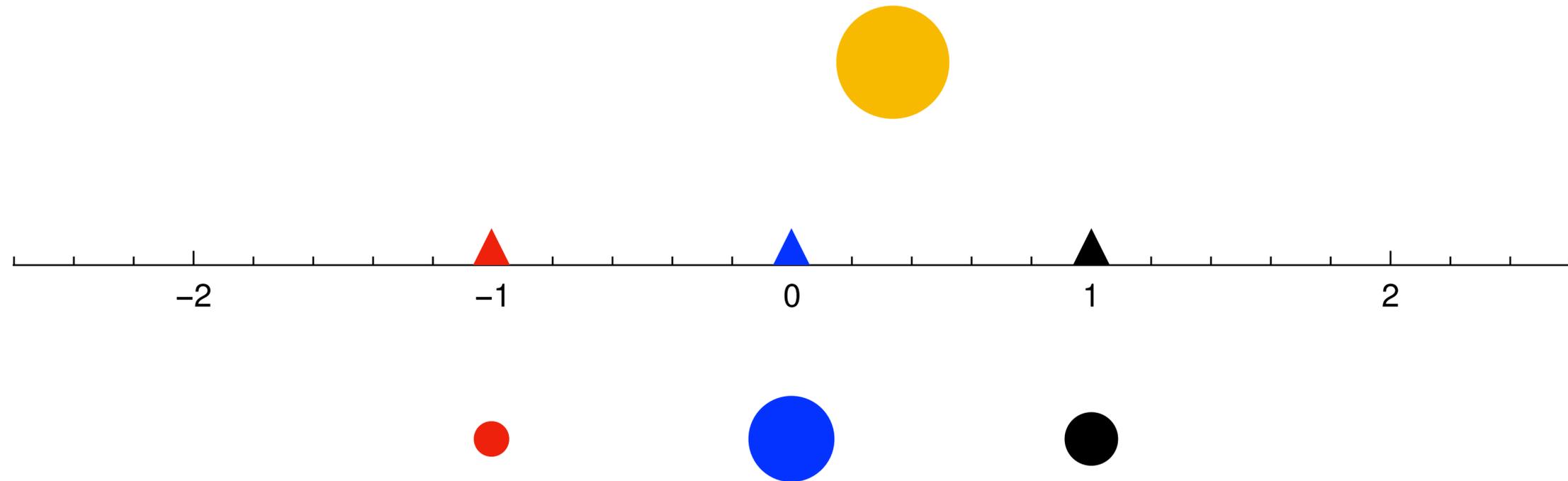
# MPM adaptivity



# Transfer of mass



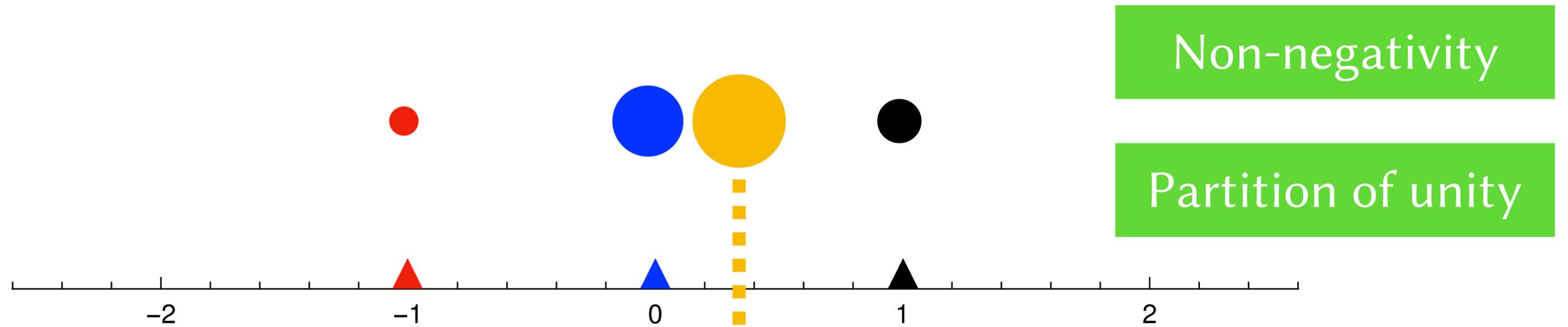
# Transfer of mass



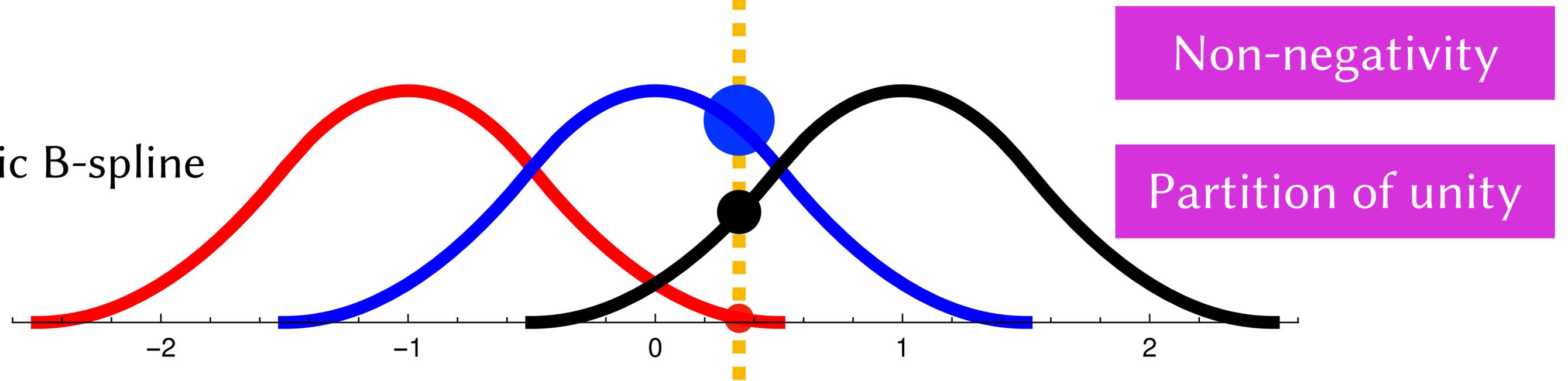
Non-negativity

Partition of unity

# Transfer of mass

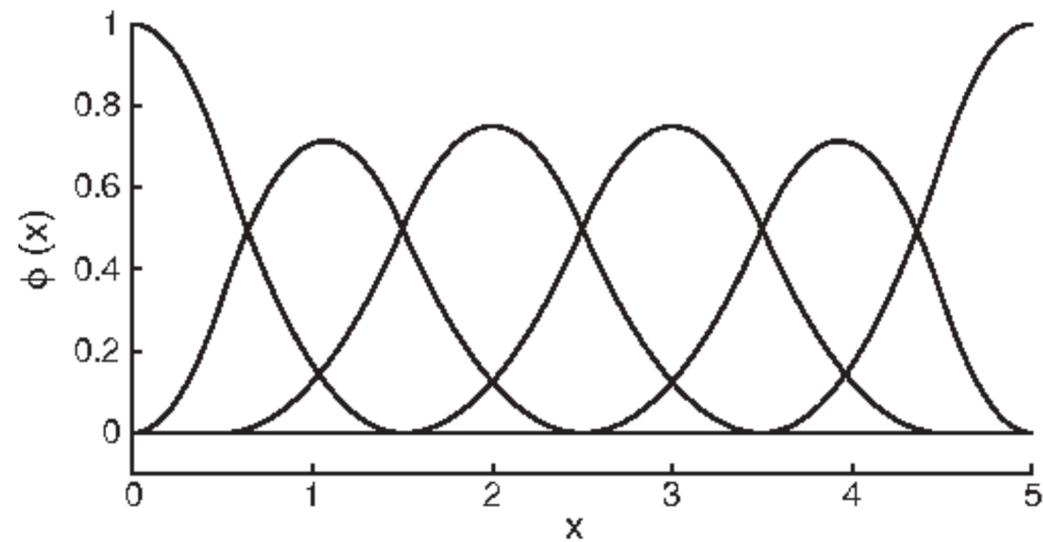


Quadratic B-spline

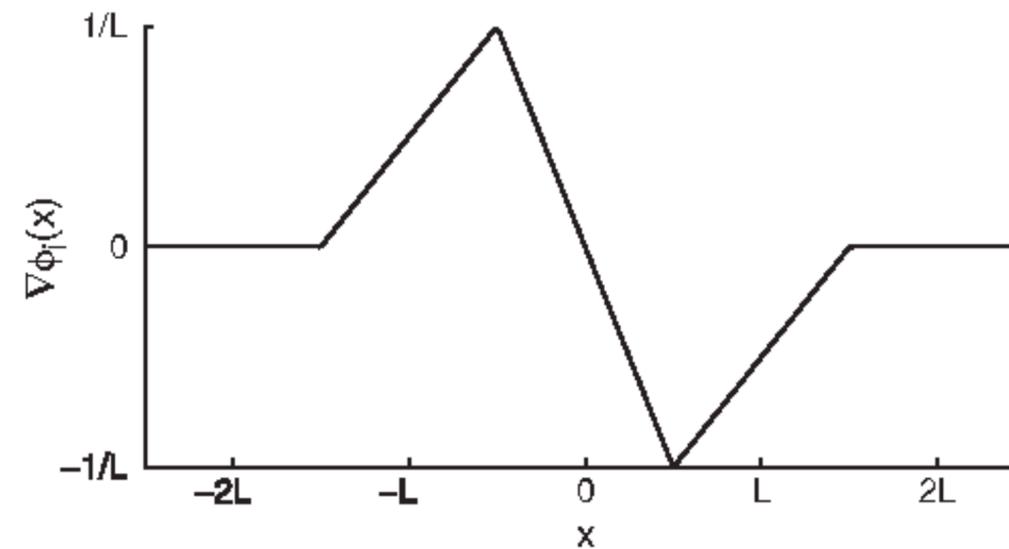


# $C^1$ continuity

Weight / mass



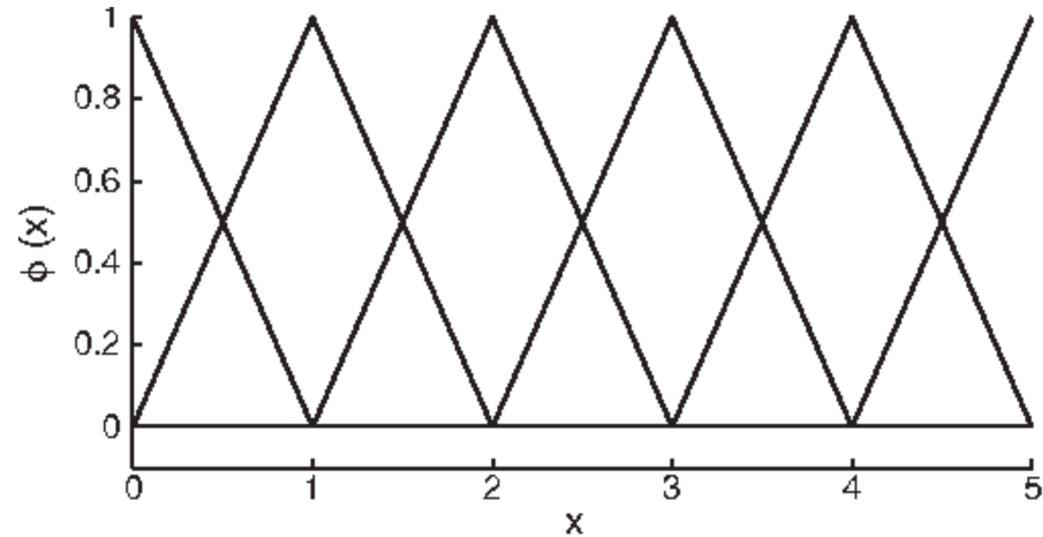
Weight gradient / force



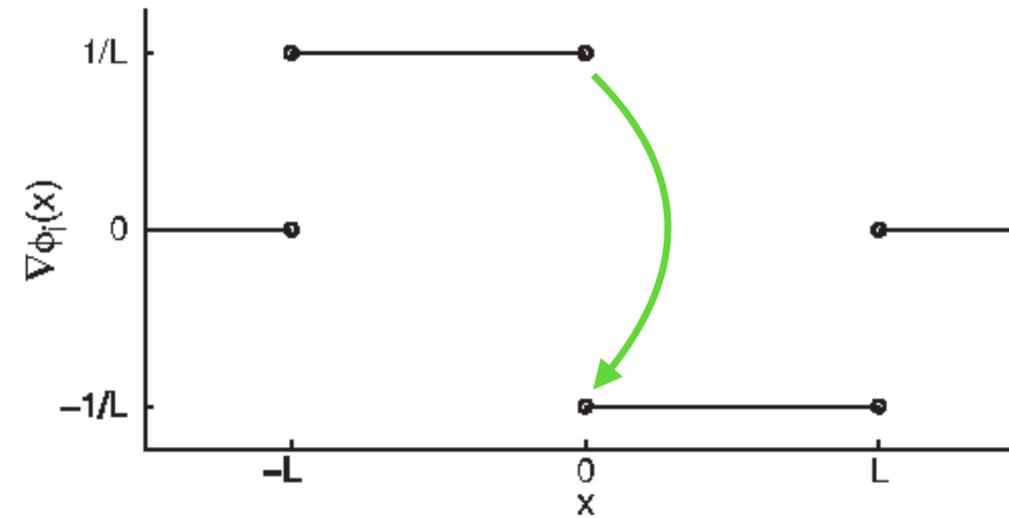
Steffen et al. 08

# $C^0$ continuity

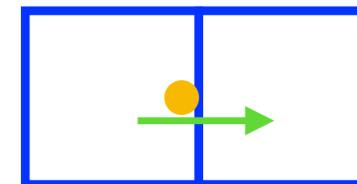
Weight / mass



Weight gradient / force

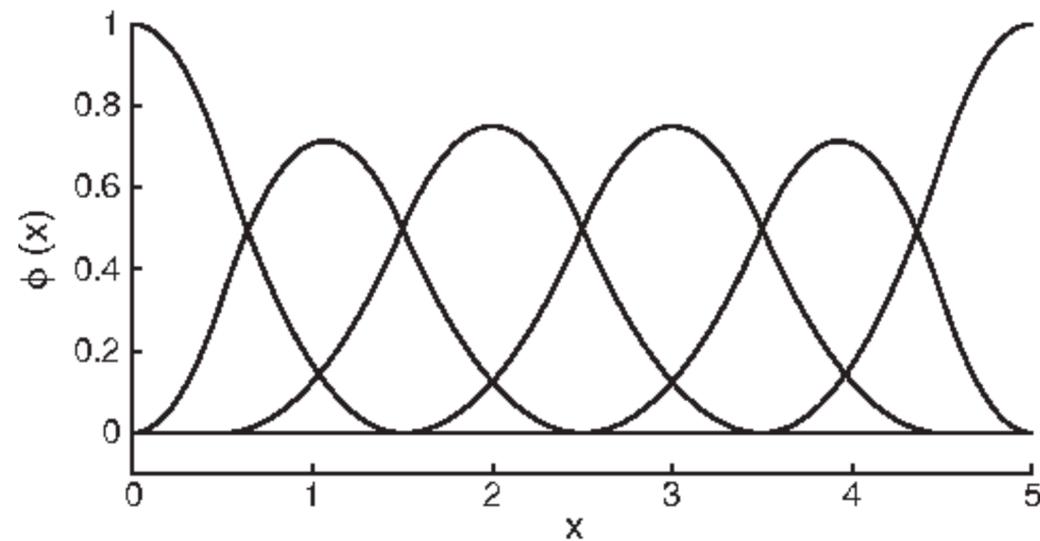


Steffen et al. 08

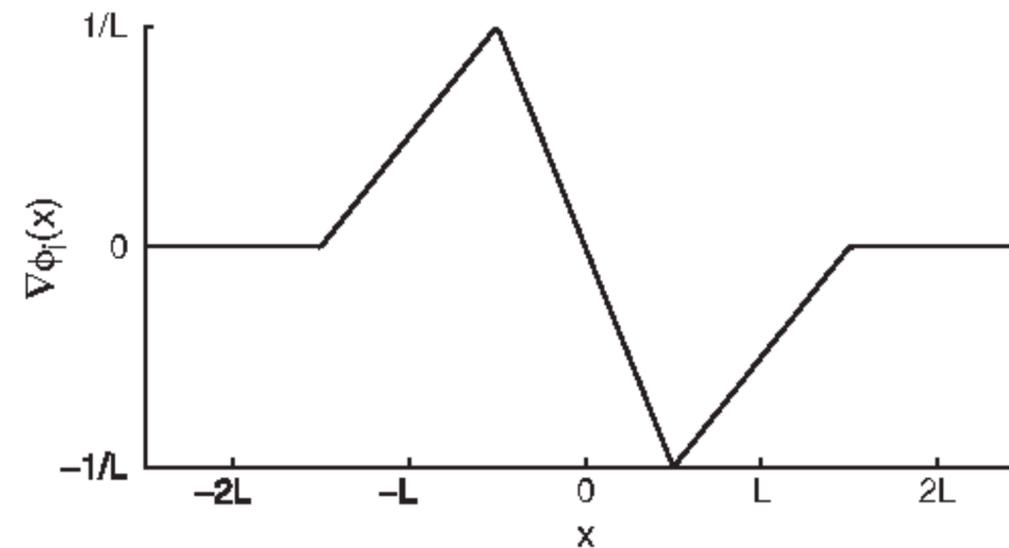


# $C^1$ continuity in octree ?

Weight / mass



Weight gradient / force



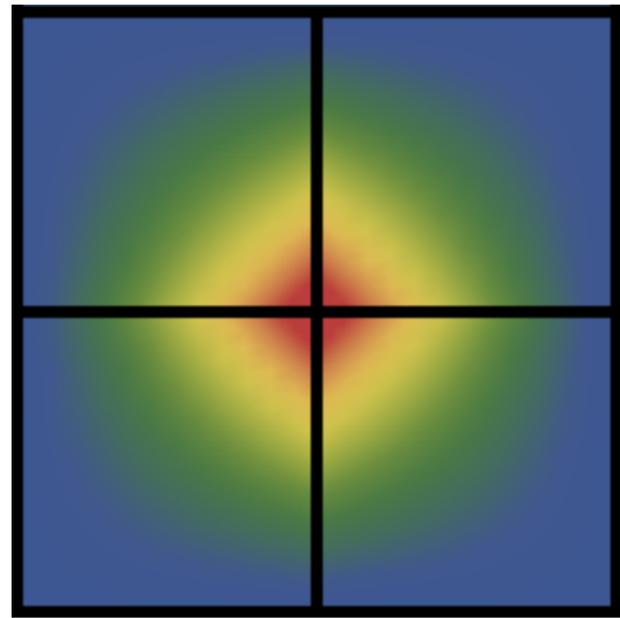
Steffen et al. 08

$C^0$

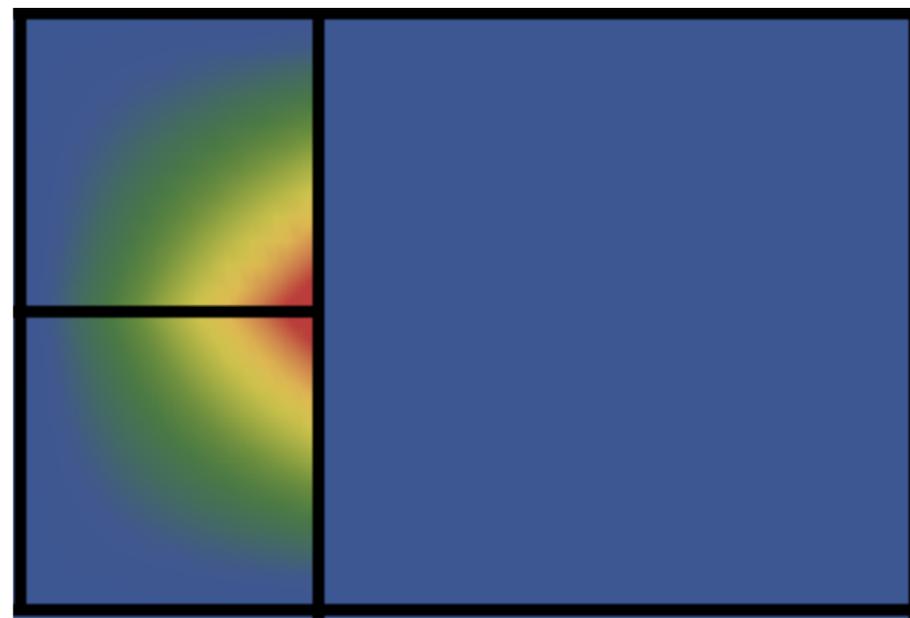


$C^1$

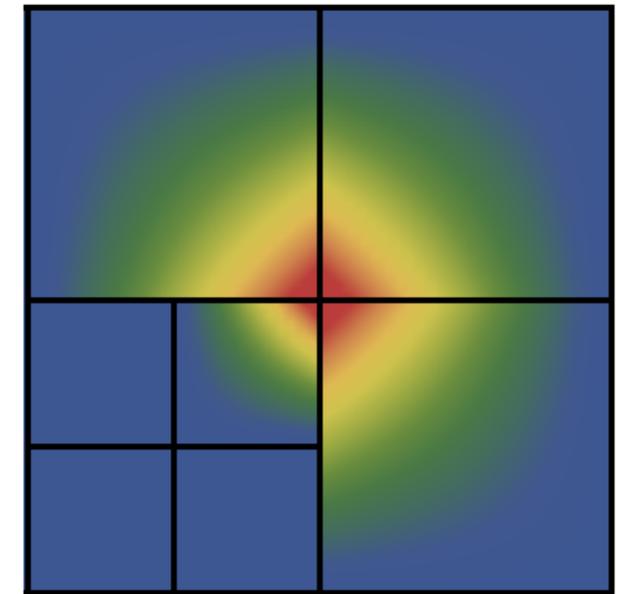
# $C^0$ from uniform to quadtree



Uniform

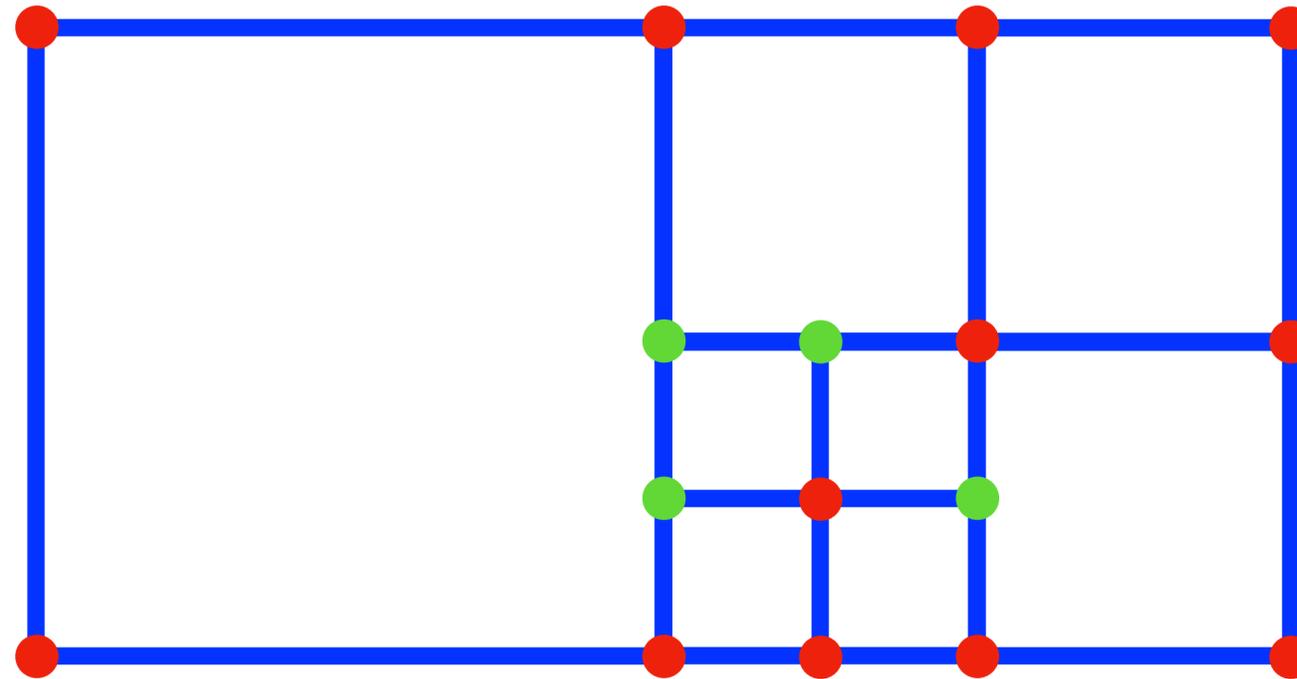


Quadtree



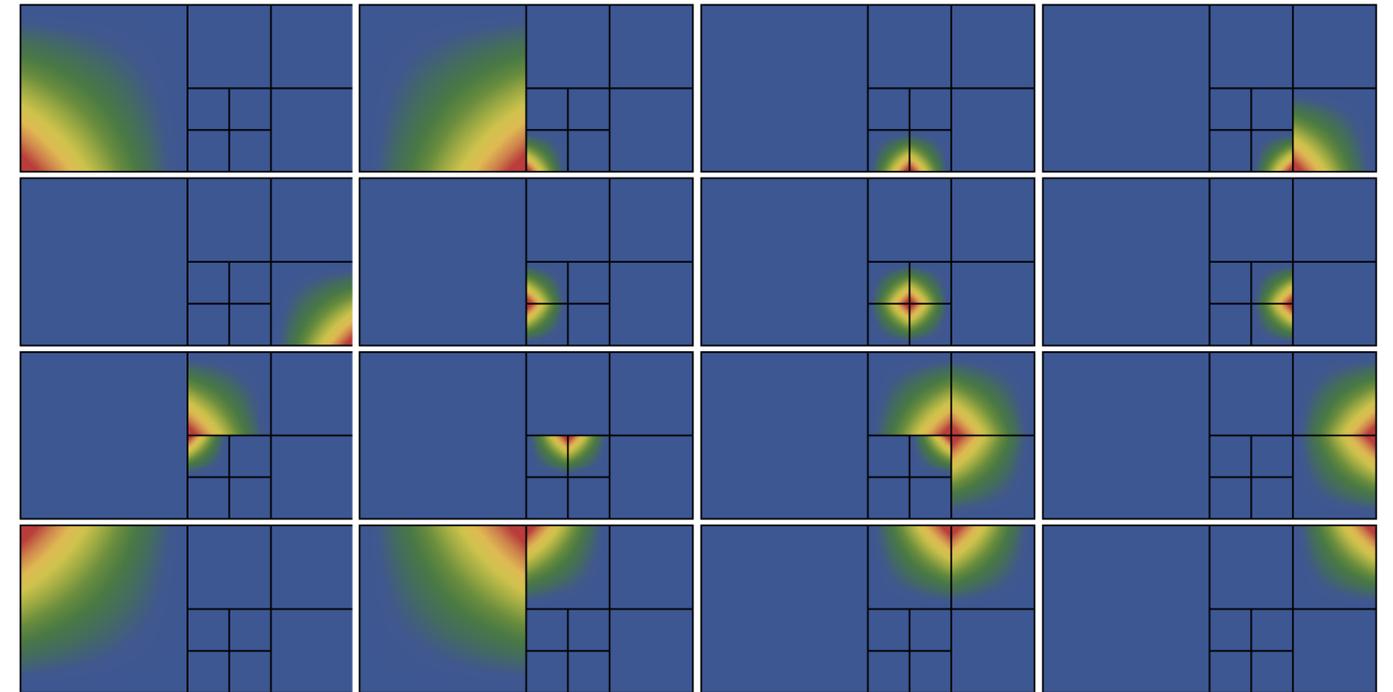
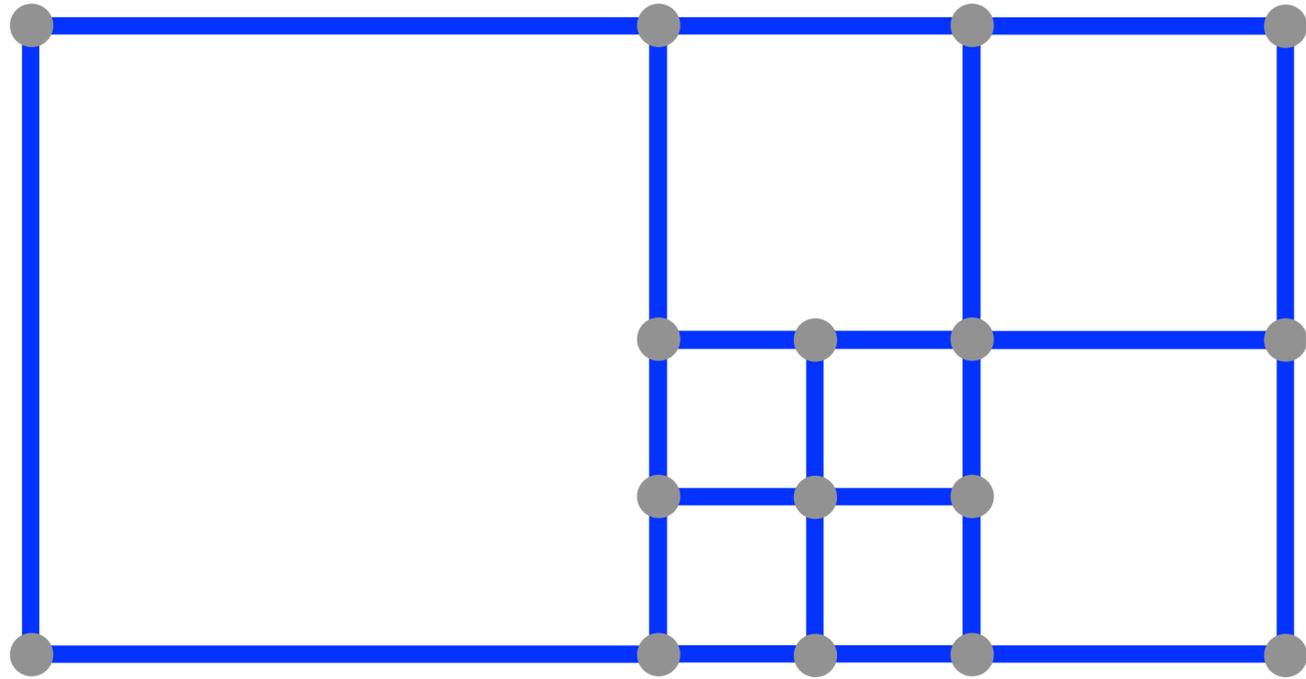
# Embedding T-junctions

- DOF node
- Embedded node / T-junction node



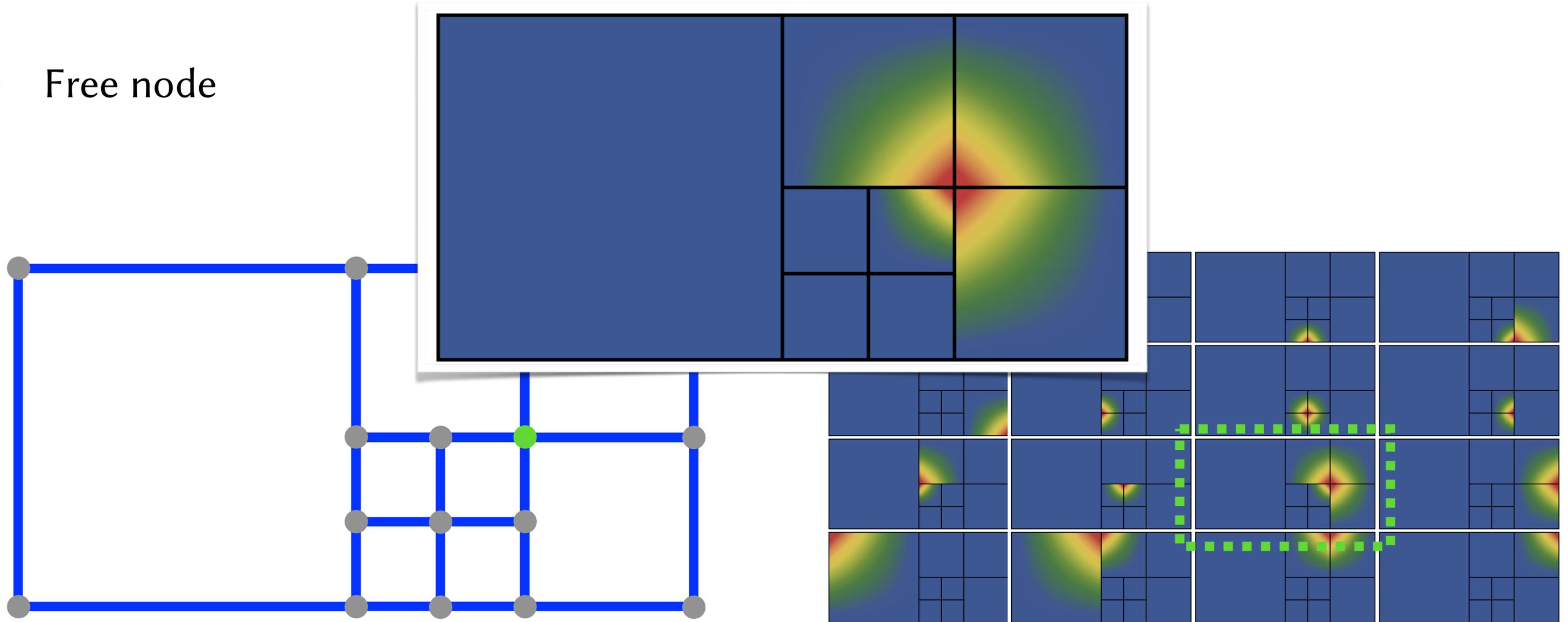
# Step 1 - set all nodes free

- Free node



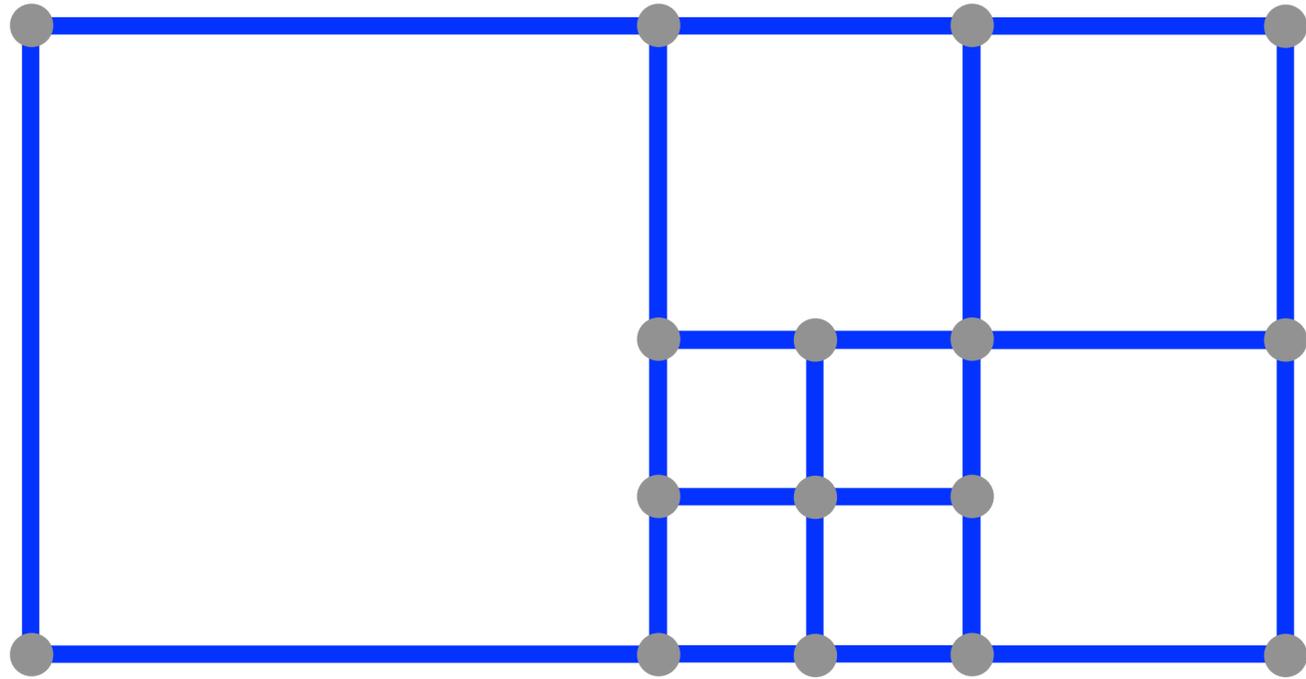
# Step 1 - set all nodes free

● Free node



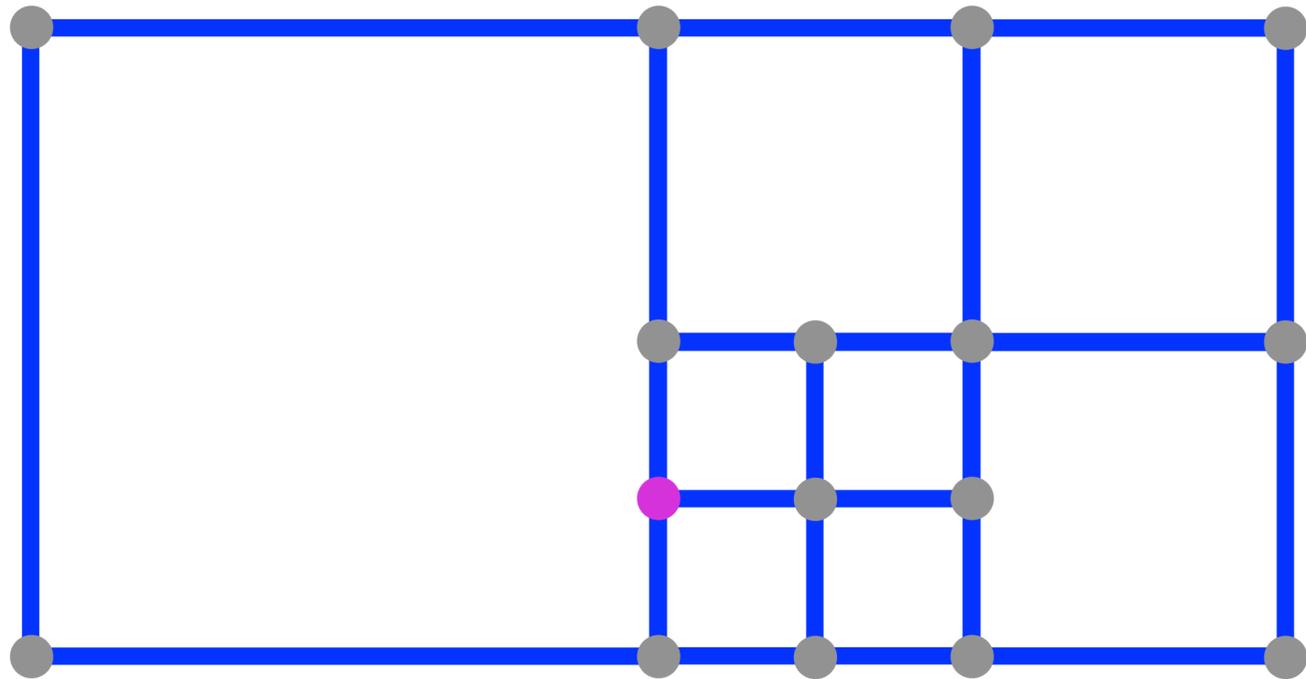
# Step 2 - constrain T-junctions

- Free node



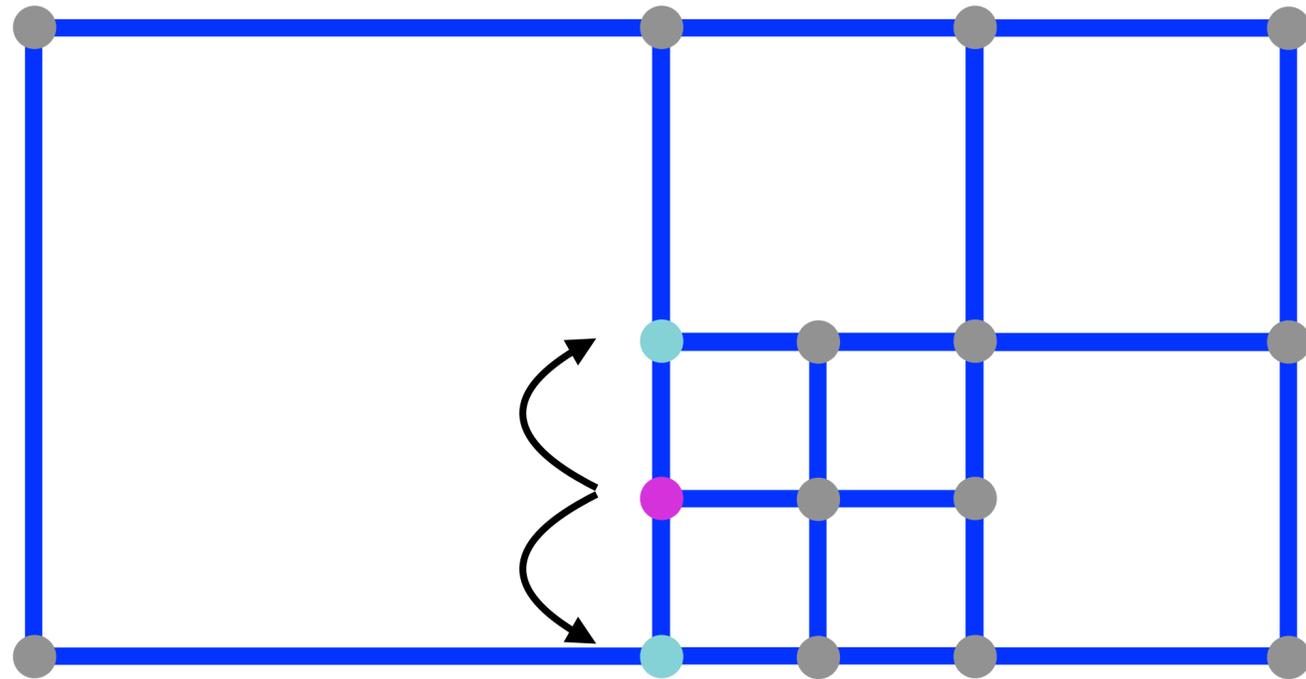
# Step 2 - constrain T-junctions

- Free node
- T-junction node



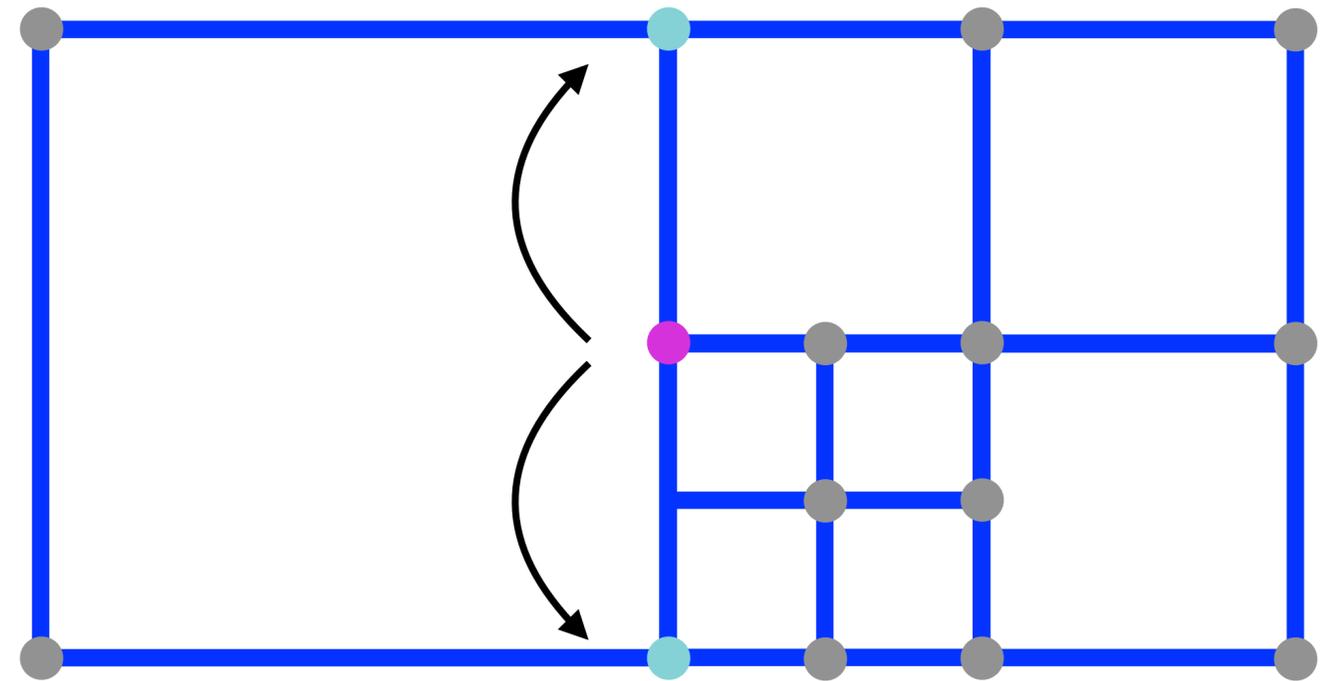
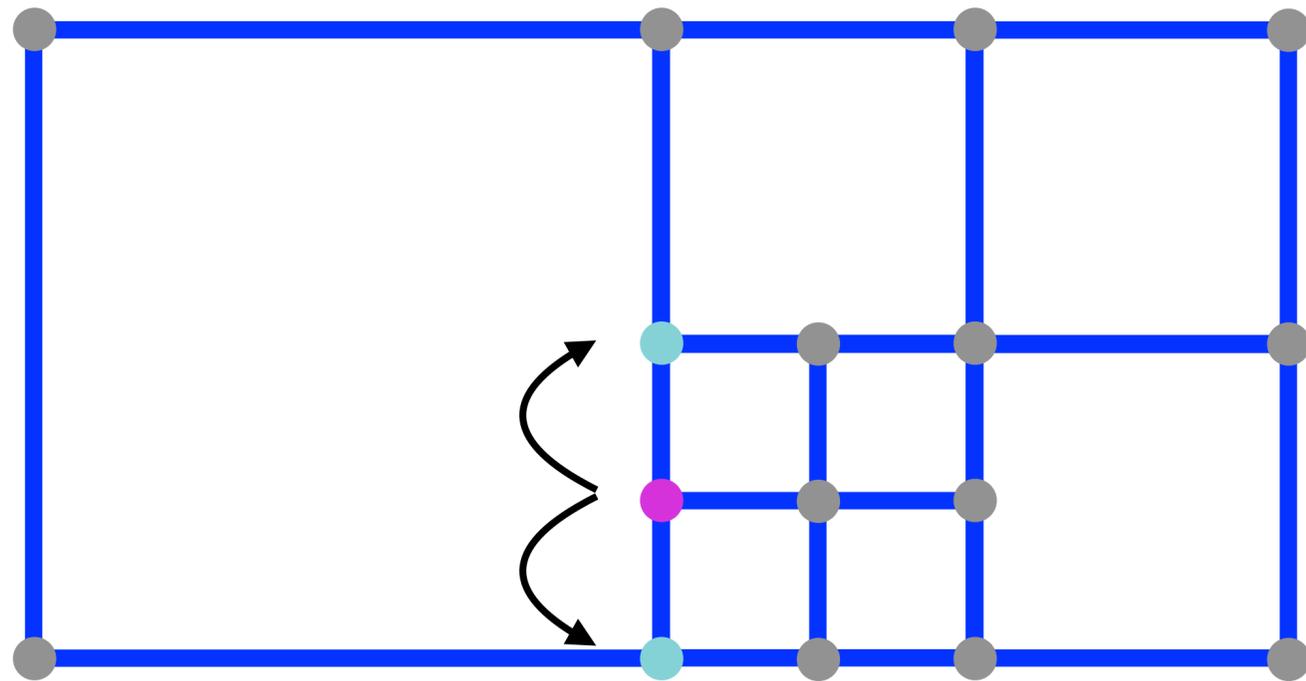
# Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



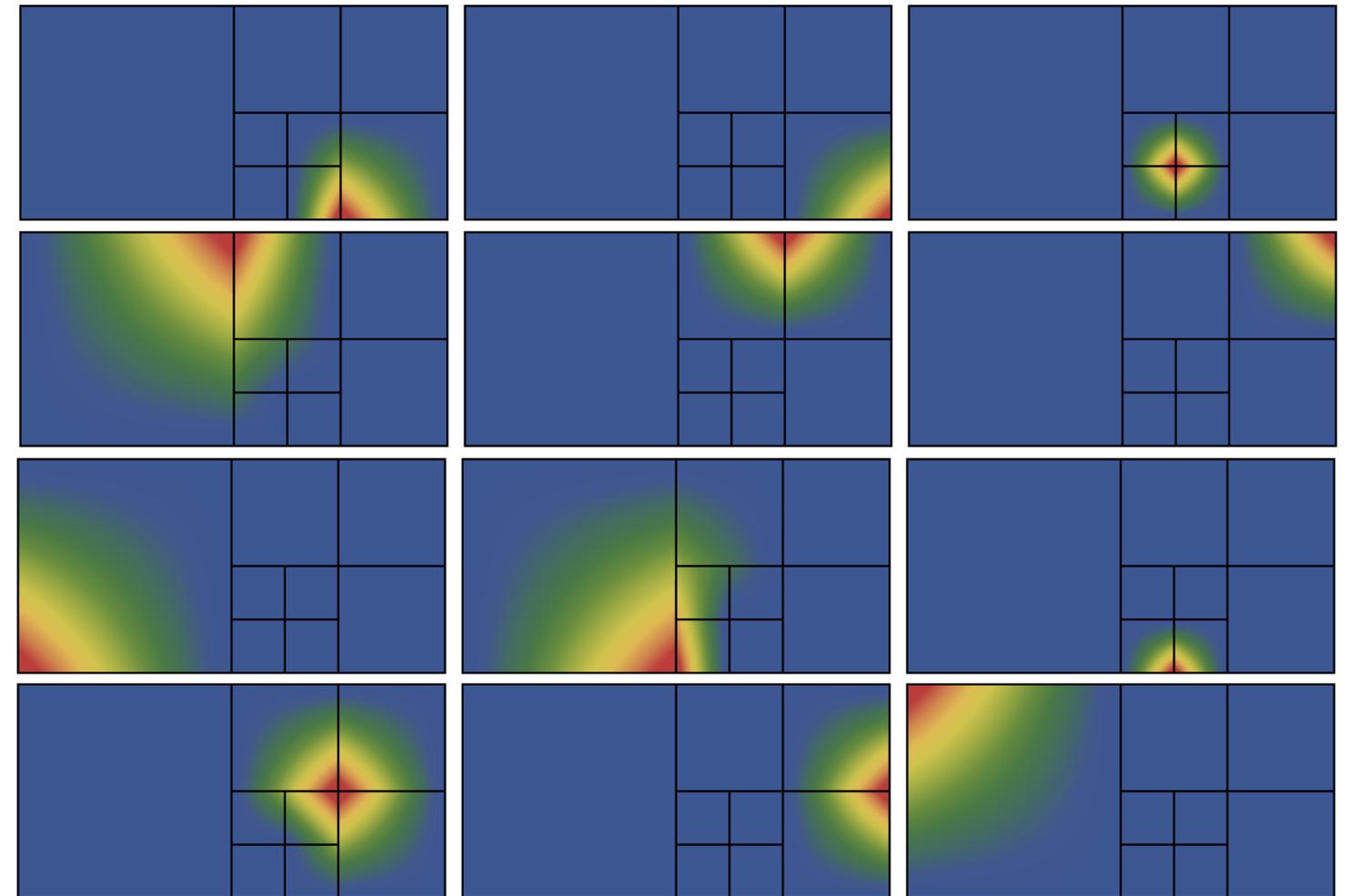
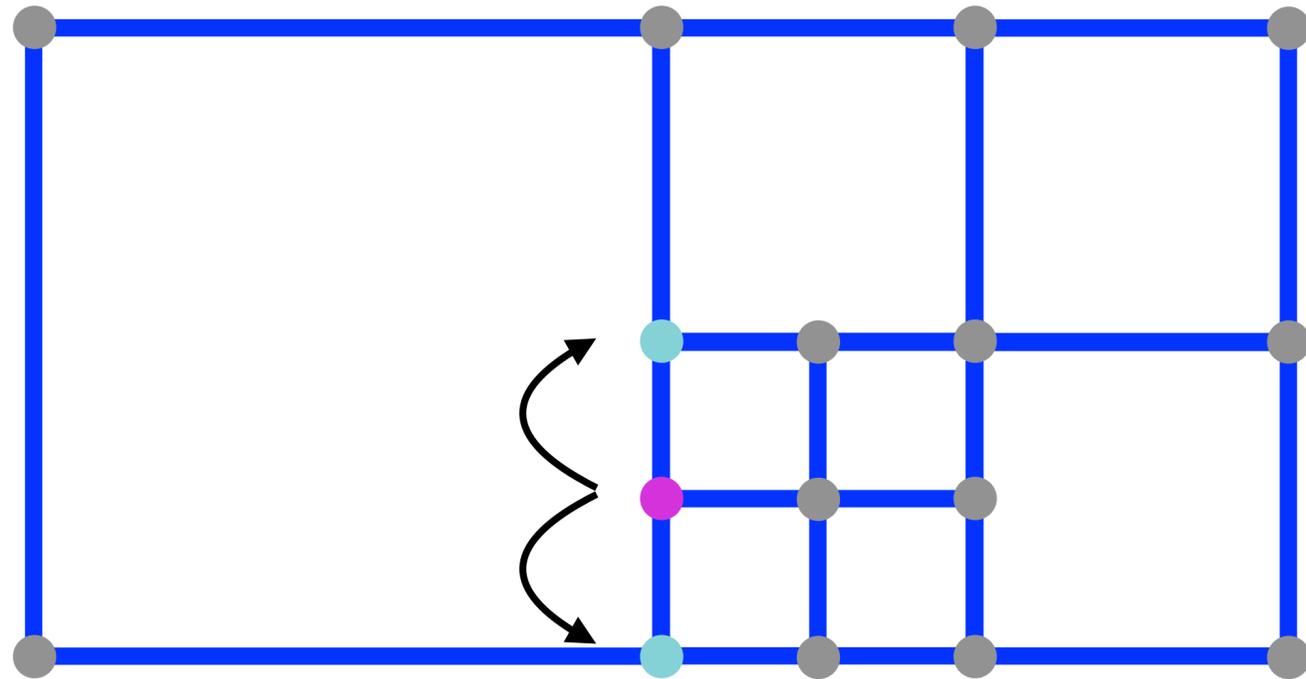
# Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



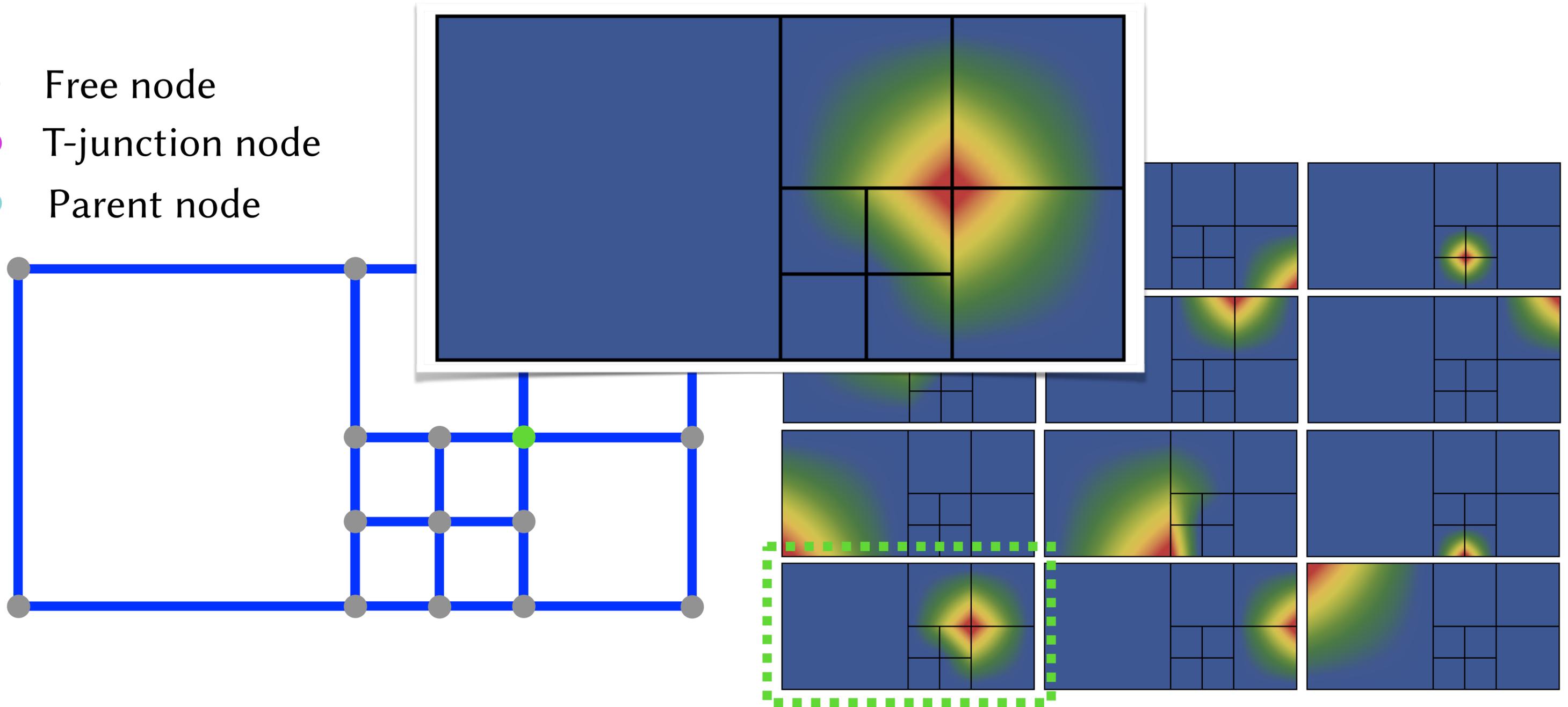
# Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node

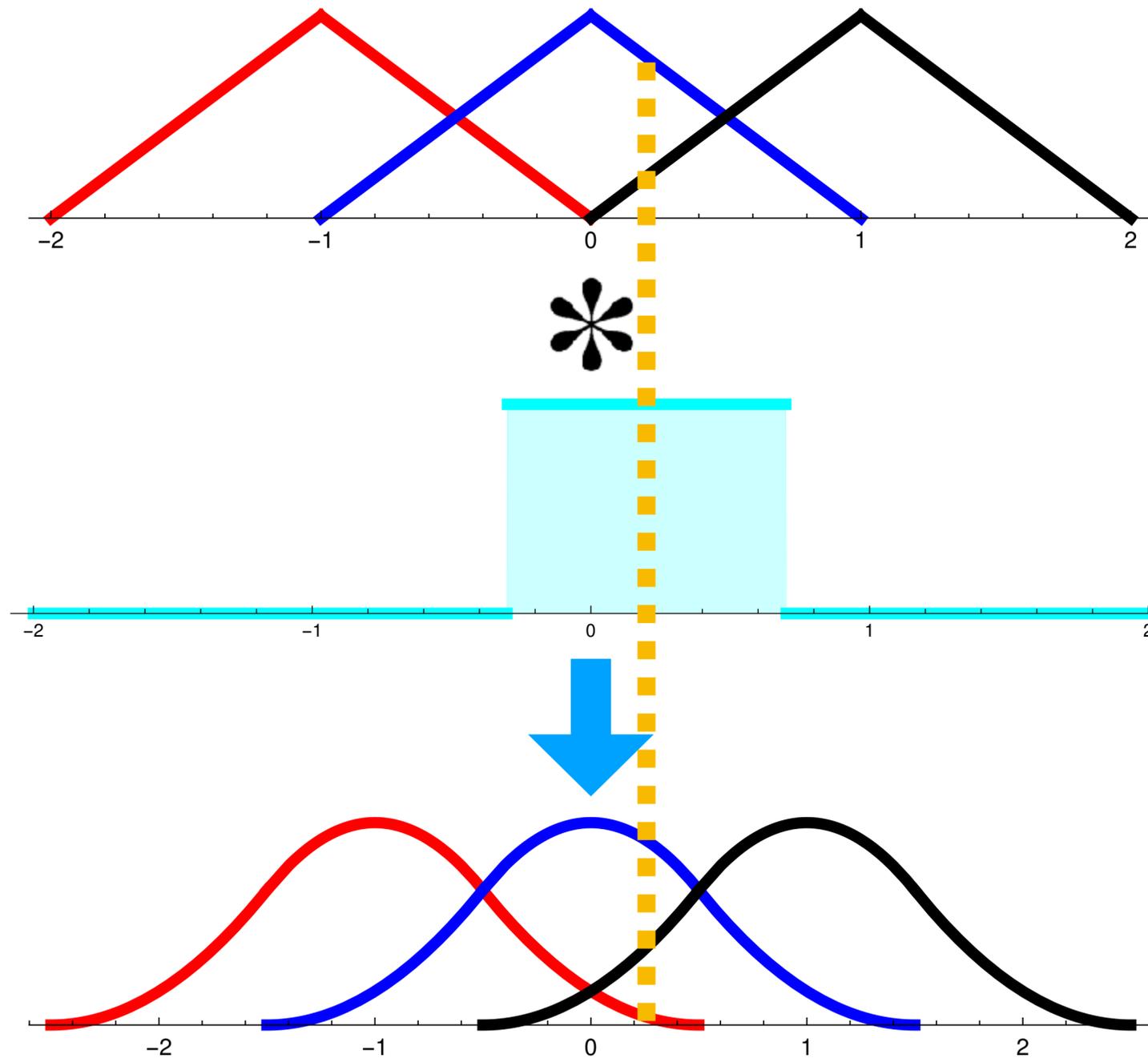


# Step 2 - constrain T-junctions

- Free node
- T-junction node
- Parent node



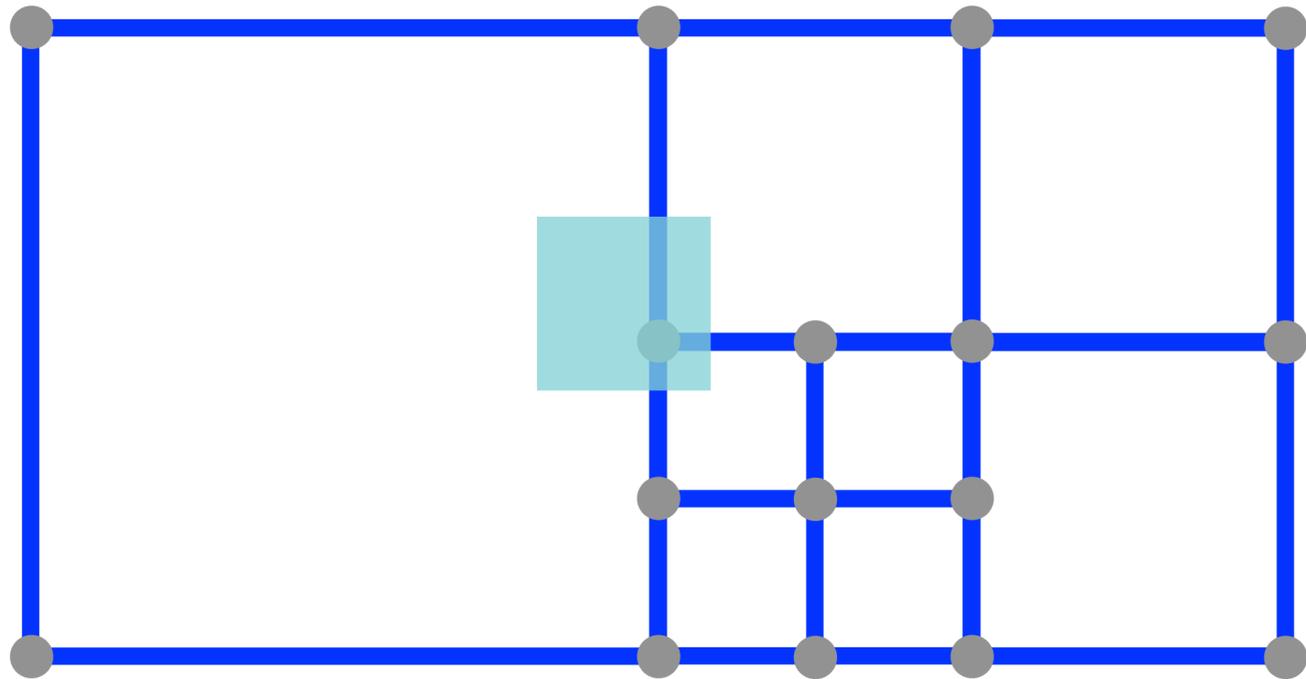
# Step 3 - upgrade to $C^1$ continuity



GIMP

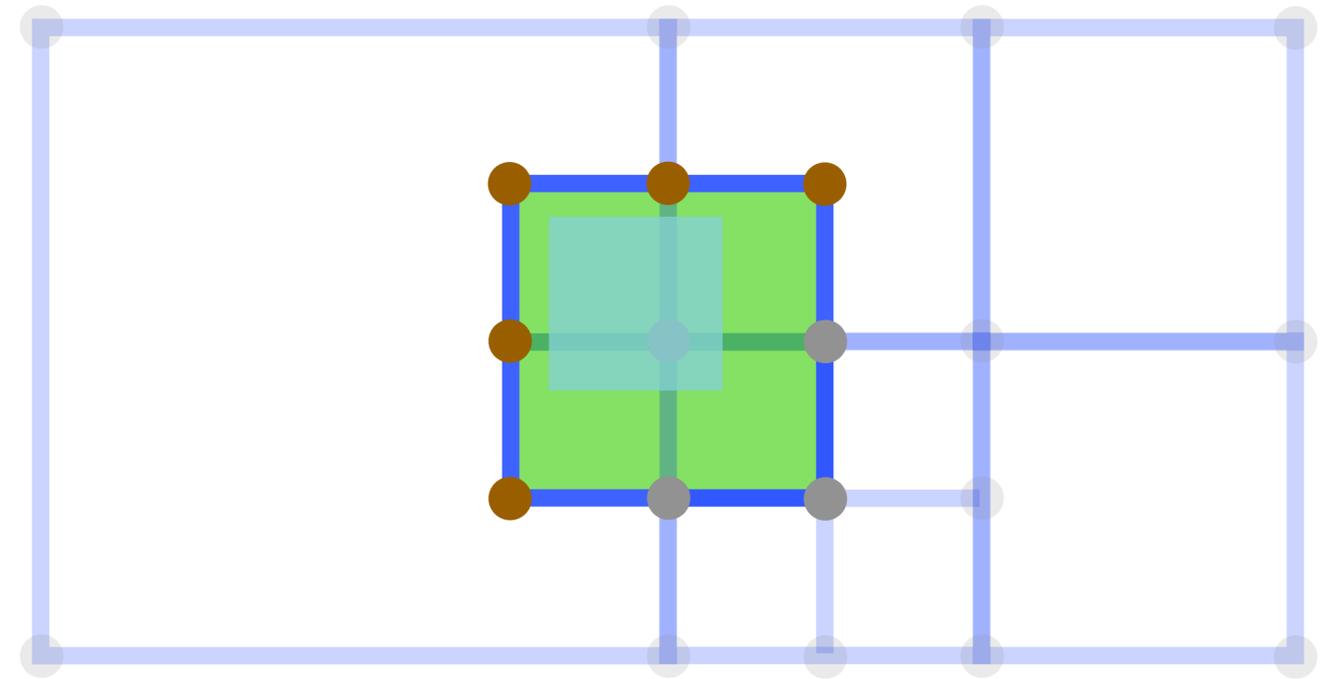
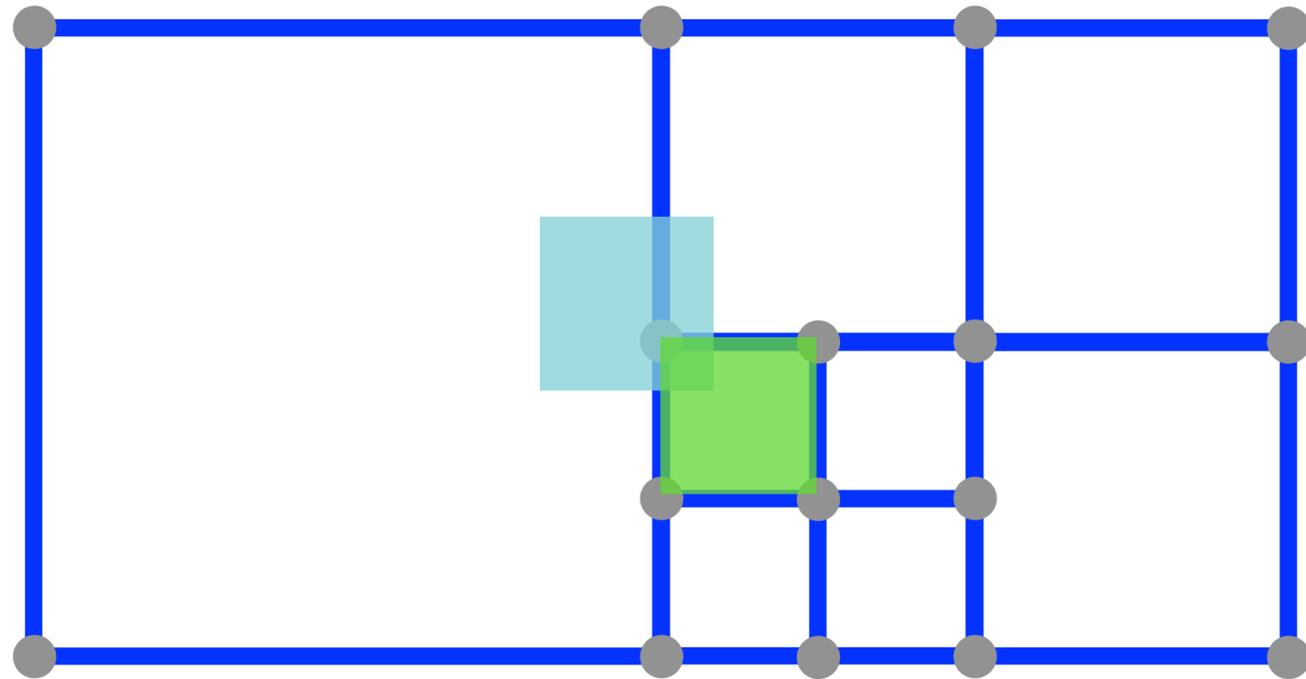
# Step 3 - upgrade to $C^1$ continuity

- Free node



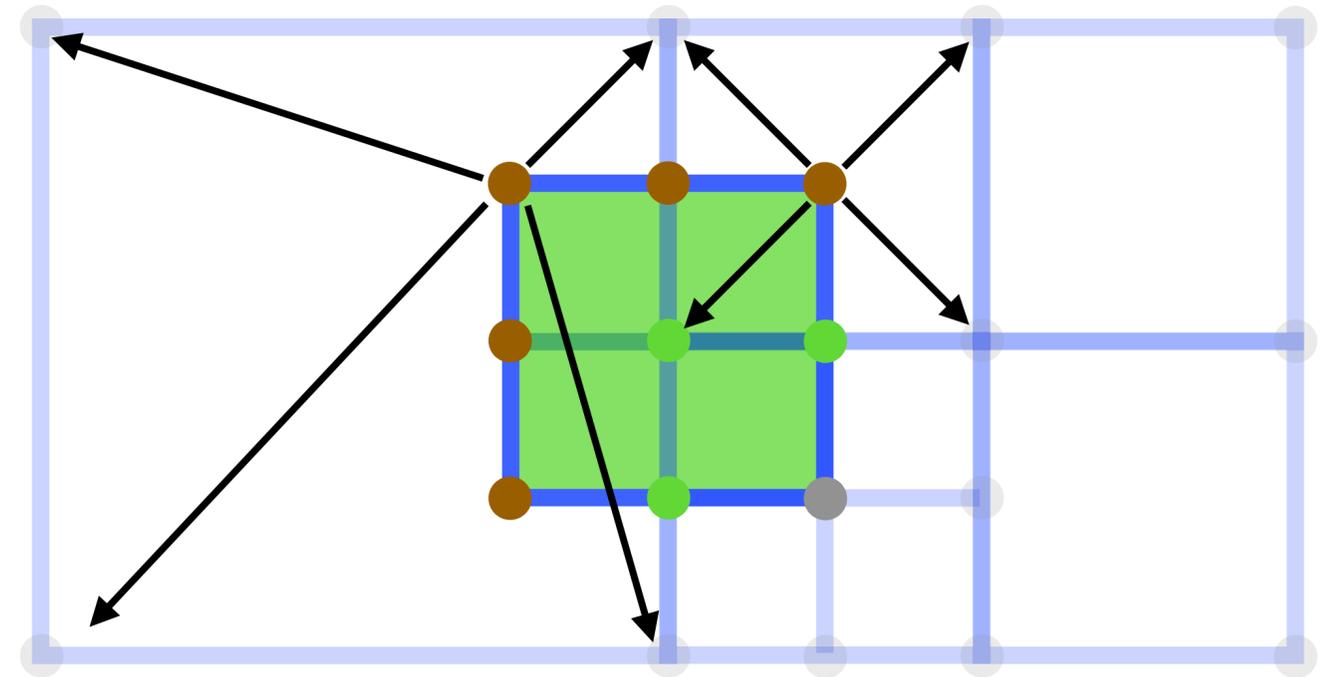
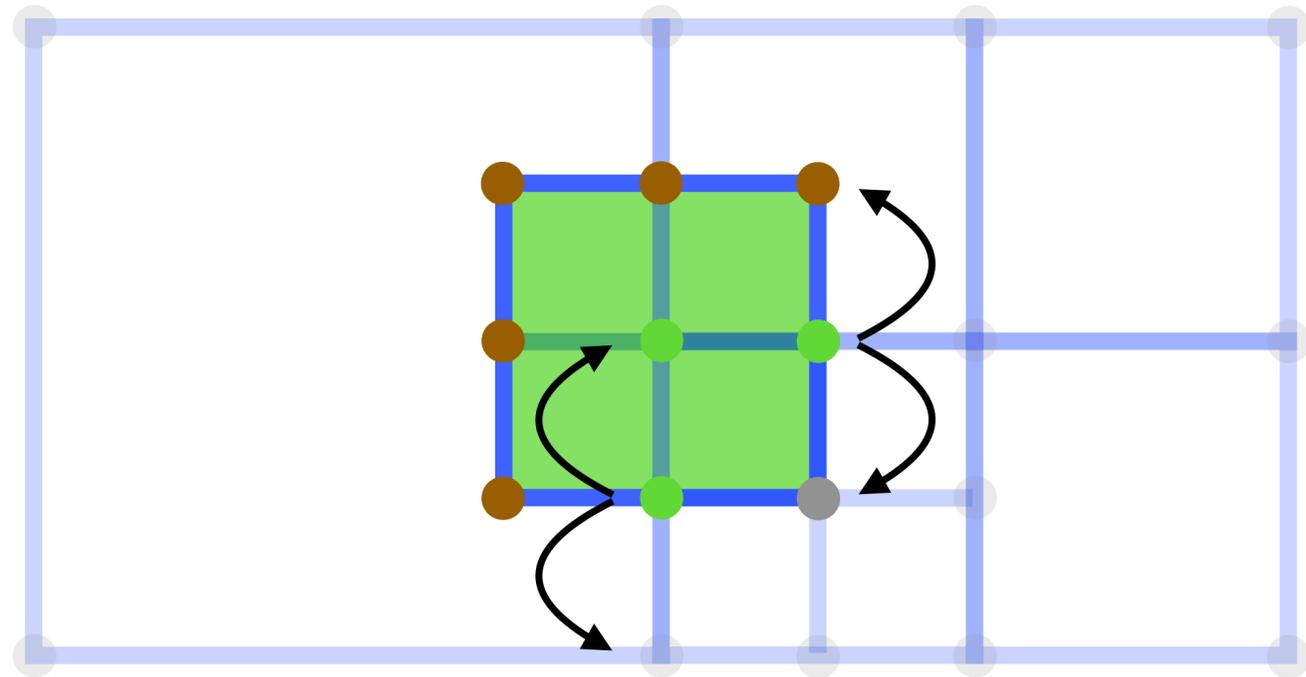
# Parallelism optimization

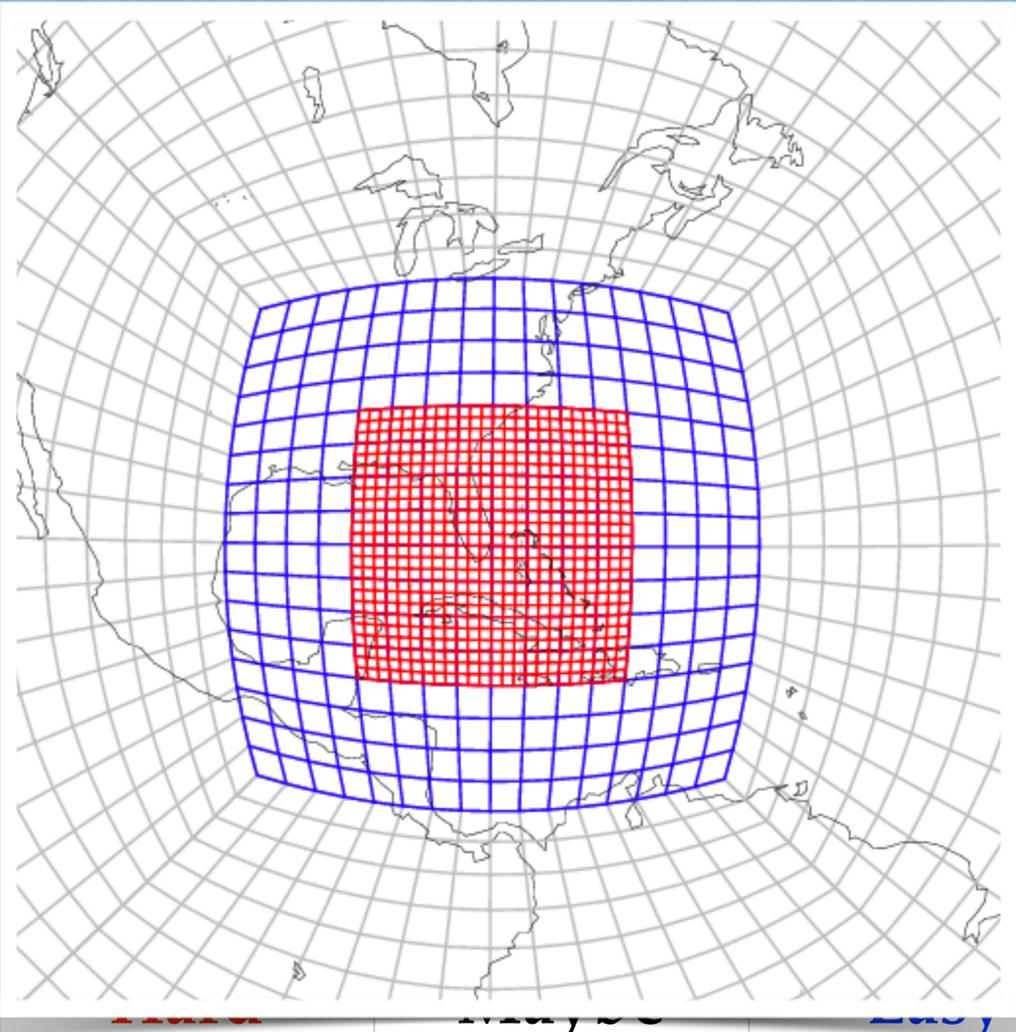
- Free node
- Ghost node



# Parallelism optimization

- Free node
- Ghost node
- T-junction node



	Tan 02	Ma 05	Lian 14	Lian 15	Our
C1 continuity	No	Yes			
Partition of unity	Yes	Yes			
Non-negativity	Yes	Yes			
Arbitrary octree	Yes	No			
Ease of parallelism	Hard	Maybe			

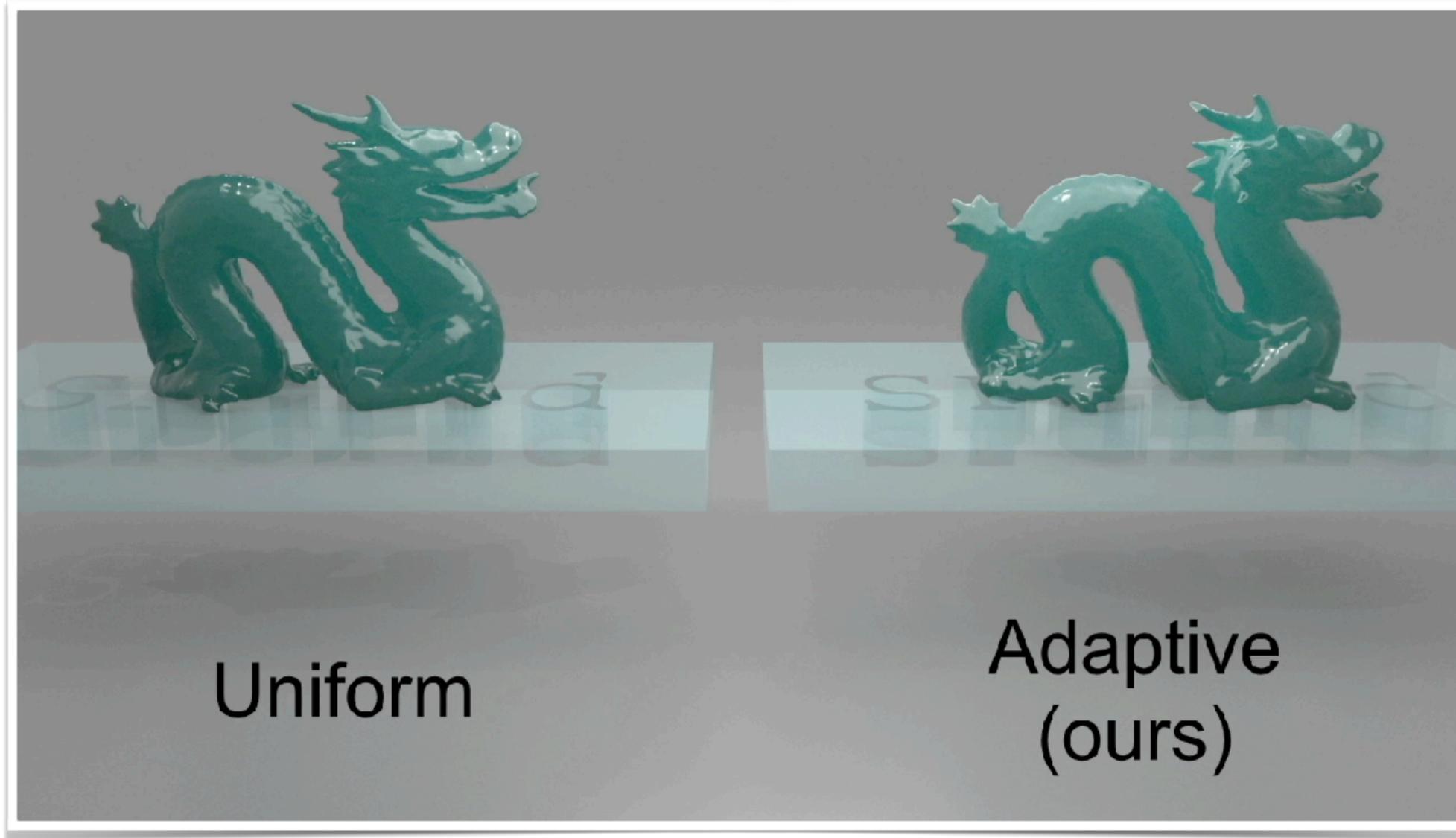
H. Tan and J. A. Nairn. 2002. **Hierarchical, adaptive, material point method for dynamic energy release rate calculations.**

J. Ma, H. Lu, B. Wang, S. Roy, R. Hornung, A. Wissink, and R. Komanduri. 2005. **Multiscale simulations using generalized interpolation material point (GIMP) method and SAMRAI parallel processing.** *Comp Model Eng & Sci* 8, 2 (2005), 135–152.

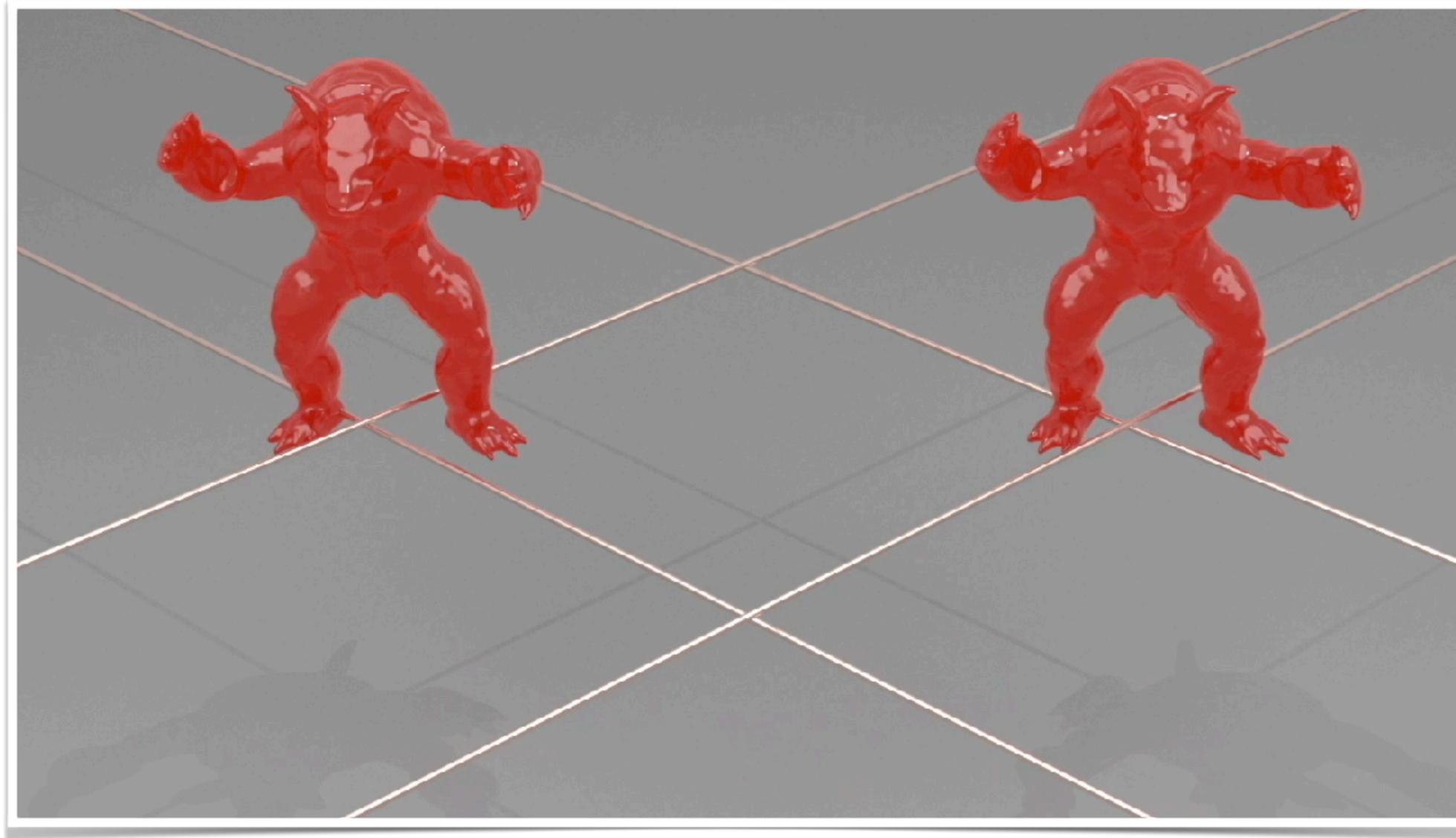
Y. Lian, X. Zhang, F. Zhang, and X. Cui. 2014. **Tied interface grid material point method for problems with localized extreme deformation.** *Int J Imp Eng* 70 (2014), 50–61.

Y.P. Lian, P.F. Yang, X. Zhang, F. Zhang, Y. Liu, and P. Huang. 2015. **A mesh-grading material point method and its parallelization for problems with localized extreme deformation.** *Comp Meth App Mech Eng* 289 (2015), 291 – 315.

# Results



# Results



# Animating Fluid Sediment Mixture in Particle-Laden Flows

## Animating Fluid Sediment Mixture in Particle-Laden Flows

MING GAO, University of Wisconsin, Madison  
ANDRE PRADHANA, University of Pennsylvania  
XUCHEN HAN, University of California, Los Angeles  
QI GUO, University of California, Los Angeles  
GRANT KOT, Phosphorus  
EFTYCHIOS SIFAKIS, University of Wisconsin, Madison  
CHENFANFU JIANG, University of Pennsylvania



Fig. 1. **Sediment transport:** Our method can animate intricate two-way coupled particle-laden flows such as sediment transport in liquid.

In this paper, we present a mixed explicit and semi-implicit Material Point Method for simulating particle-laden flows. We develop a Multigrid Preconditioned fluid solver for the Locally Averaged Navier Stokes equation. This is discretized purely on a semi-staggered standard MPM grid. Sedimentation is modeled with the Drucker-Prager elastoplasticity flow rule, enhanced by a novel particle density estimation method for converting particles between representations of either continuum or discrete points. Fluid and sediment are two-way coupled through a momentum exchange force that can be easily resolved with two MPM background grids. We present various results to demonstrate the efficacy of our method.

CCS Concepts: • **Computing methodologies** → **Physical simulation**;

Additional Key Words and Phrases: Material Point Method (MPM), particle-fluid interaction, multiphase, sedimentation, sediment transport

### ACM Reference format:

Ming Gao, Andre Pradhana, Xuchen Han, Qi Guo, Grant Kot, Eftychios Sifakis, and Chenfanfu Jiang. 2018. Animating Fluid Sediment Mixture in Particle-Laden Flows. *ACM Trans. Graph.* 37, 4, Article 1 (August 2018), 11 pages.  
DOI: 10.1145/3197517.3201309

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DOI: 10.1145/3197517.3201309

## 1 INTRODUCTION

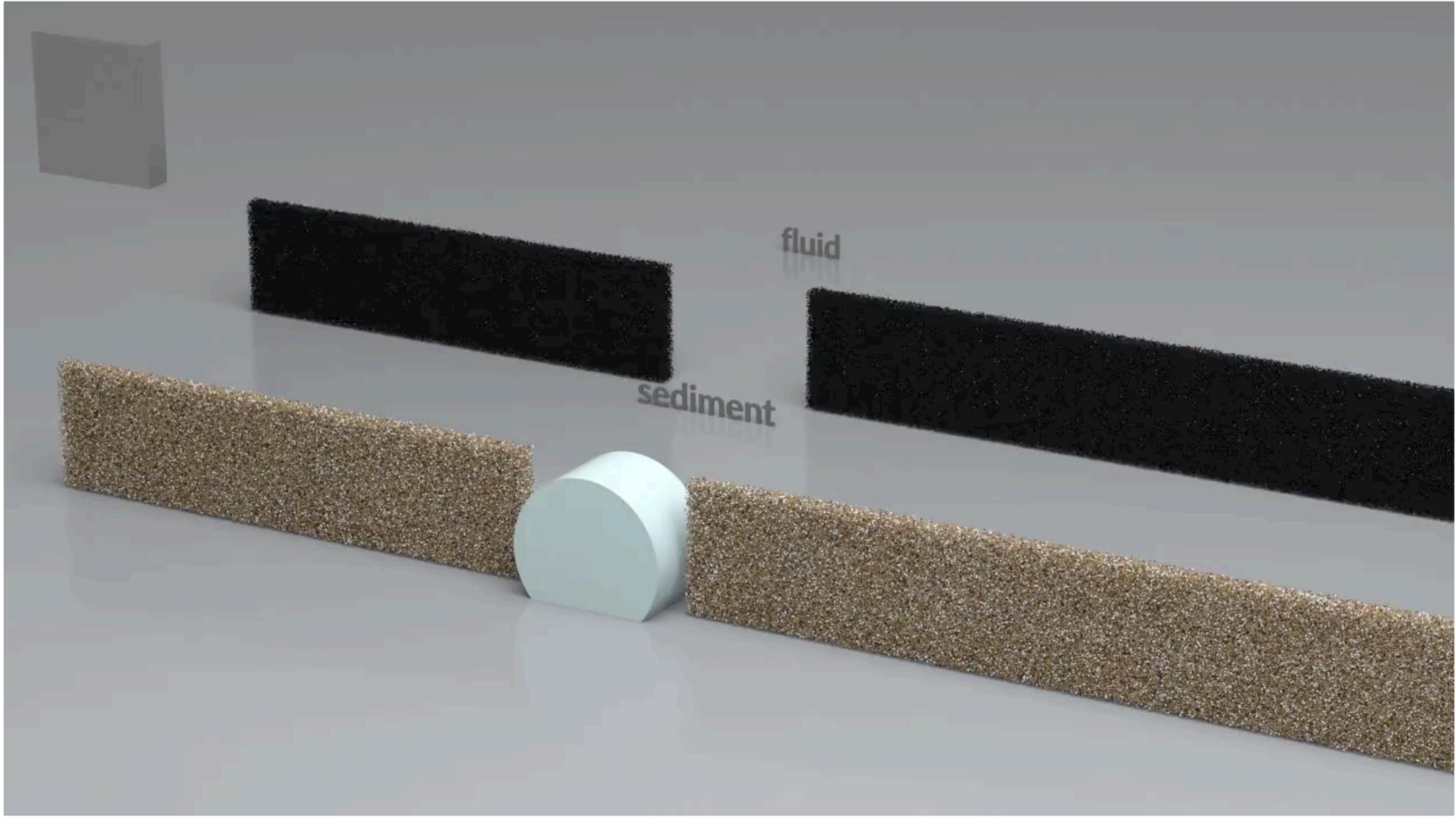
Recently, multi-phase multi-material simulations are increasingly gaining attention from computer graphics researchers. Simulating various phases or materials in a unified framework is particularly favored. Existing work includes coupled Lagrangian particle simulation with Position Based Dynamics (PBD) [Macklin et al. 2014], water-gas mixtures [Nielsen and Østerby 2013] with an Eulerian method, solid-fluid phase-change [Stomakhin et al. 2014] and porous granular media [Pradhana-Tampubolon et al. 2017] with Material Point Method (MPM), as well as interactive solids and fluids based on the mixture model with Smoothed Particle Hydrodynamics (SPH) [Yan et al. 2016].

Most of the existing approaches are based on *continuum* mixture theory [Manninen et al. 1996]. The continuum assumption for each material phase is essential for simulations of macroscopic porous media (e.g., landslides and liquid blending). However, it may fail to capture the correct behavior of particle-laden flows where the solid phase is on a relatively small scale. Note that particle-laden sediment flow is ubiquitous in natural systems. Typical examples include sediment transport, sedimentation, volcano eruption, dune migration by erosion with ripples, and dust storms. The significance of understanding and simulating these phenomena is also recognized in many engineering applications, such as granular material fluidization [van der Hoef et al. 2006] and coastal erosion prediction [Sun and Xiao 2016a].

**M. Gao, A. Tampubolon, X. Han, Q. Guo, G. Kot, E. Sifakis, C. Jiang**  
ACM Transactions on Graphics (Proceedings of ACM SIGGRAPH), 2018



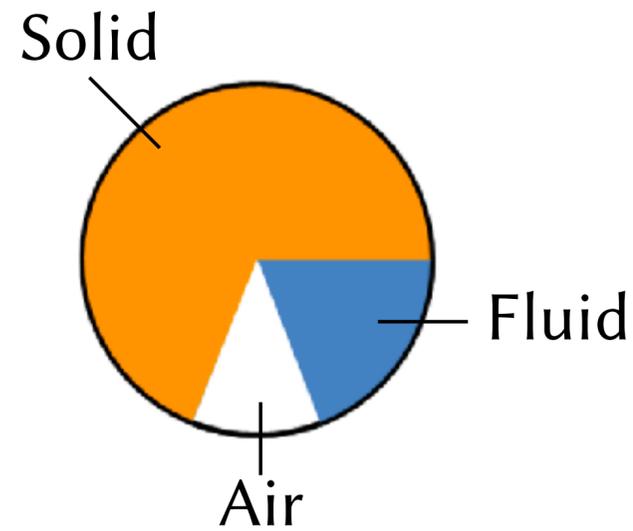
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**SIGGRAPH2018**



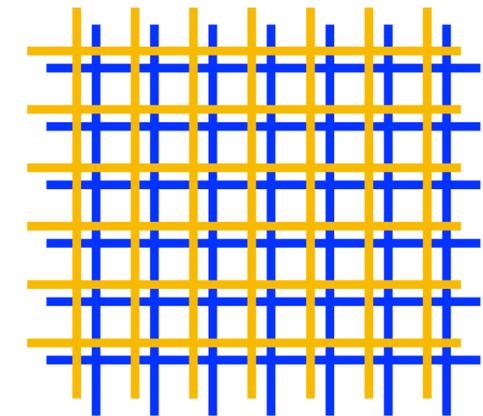
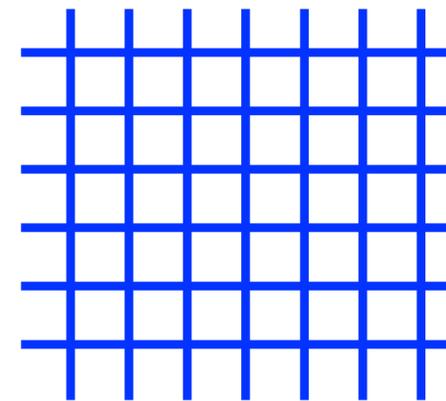
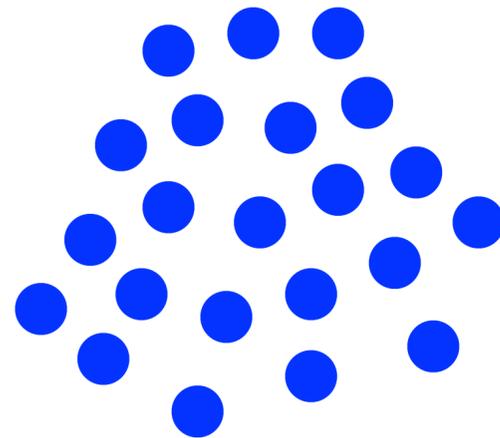
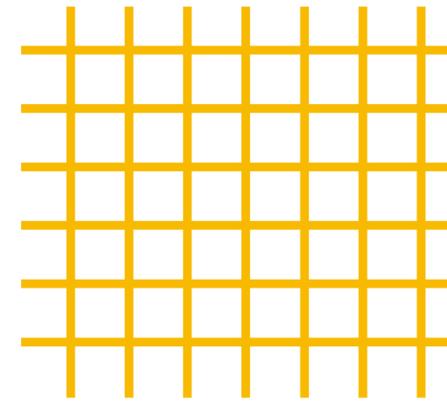
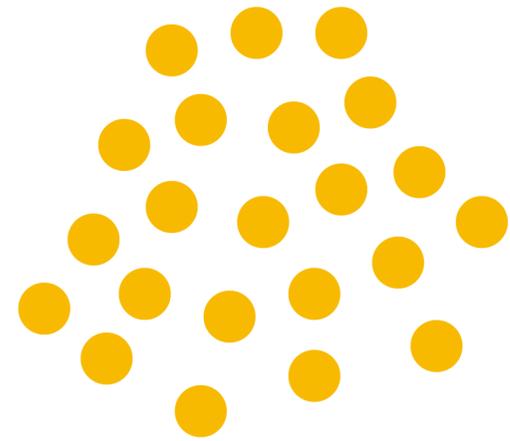
fluid

sediment

# Approach: mixture in particles vs. grid



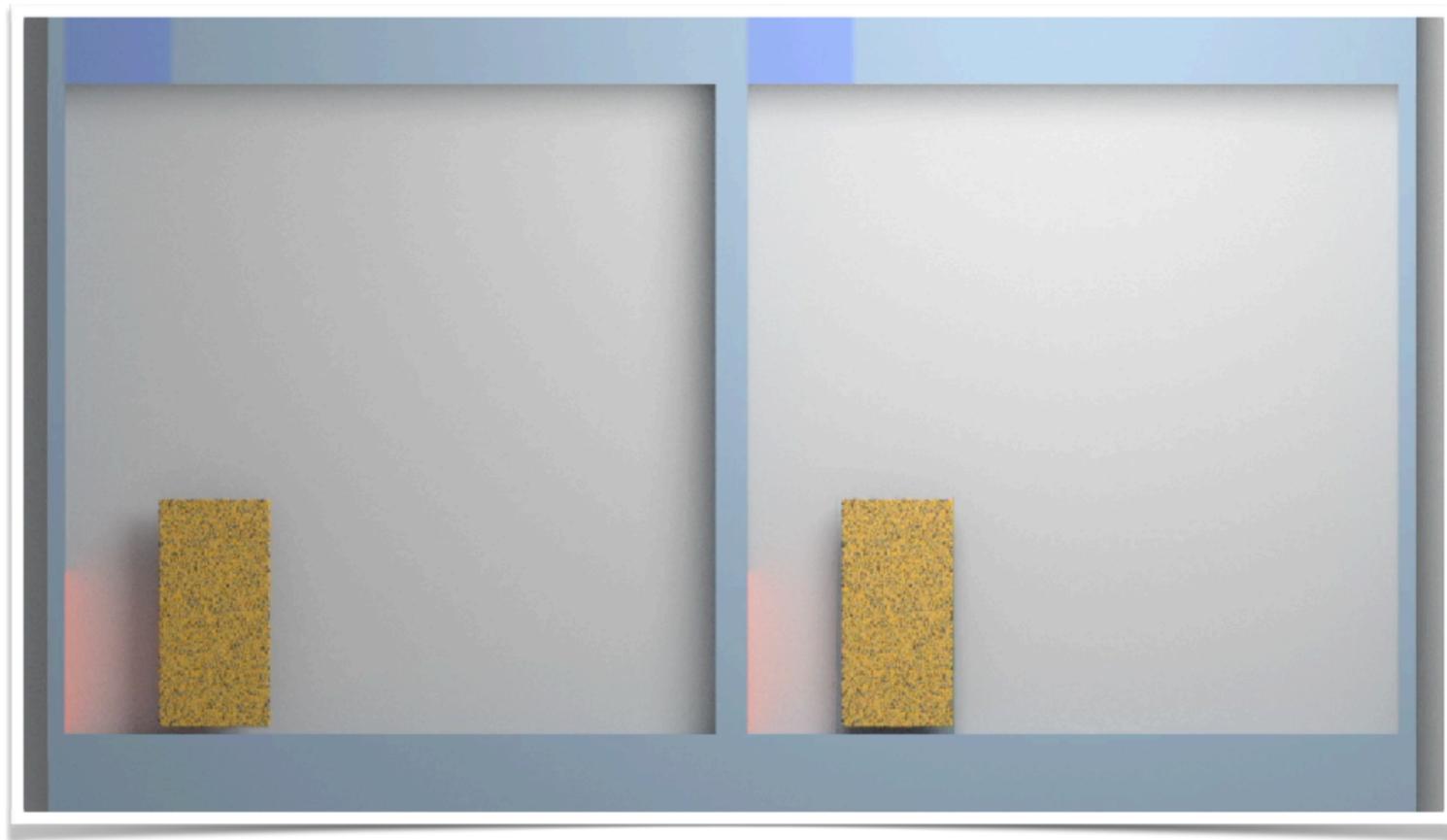
Colom et al. 15



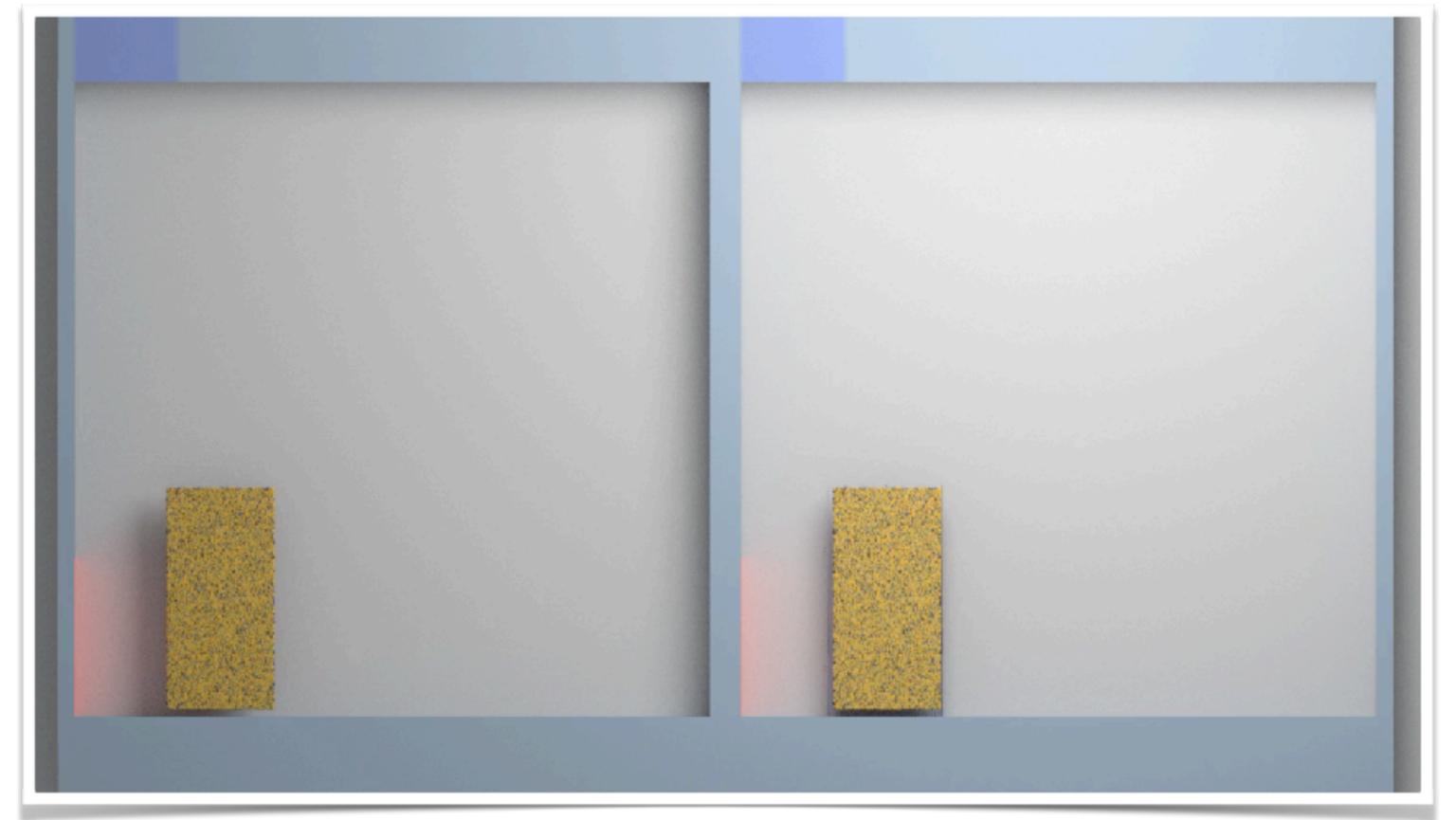
3 phases 1 point

2 phases 2 point

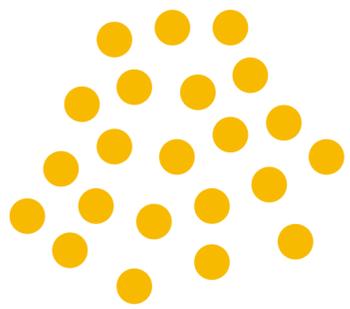
# Approach: one-way coupling vs. two-way



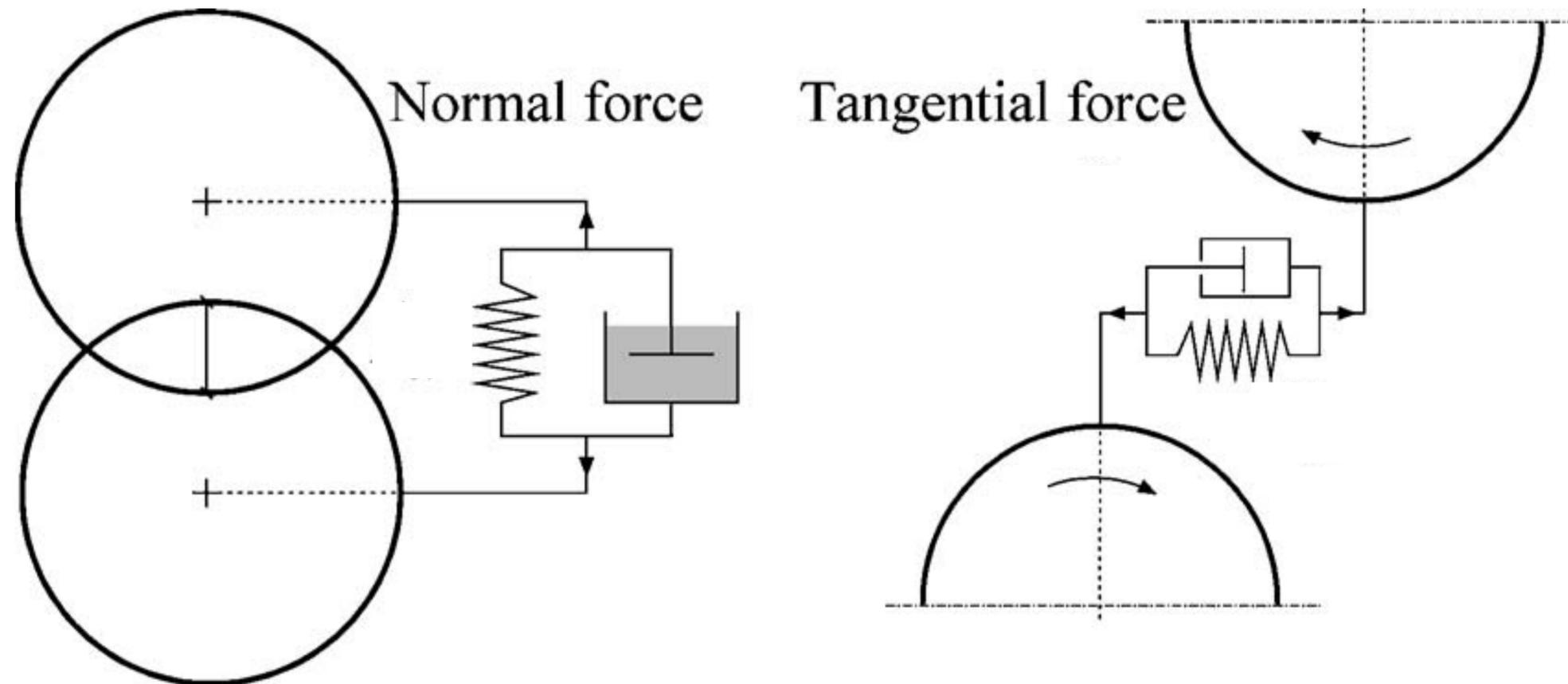
One way coupling



Two way coupling



# Approach: DEM vs. MPM

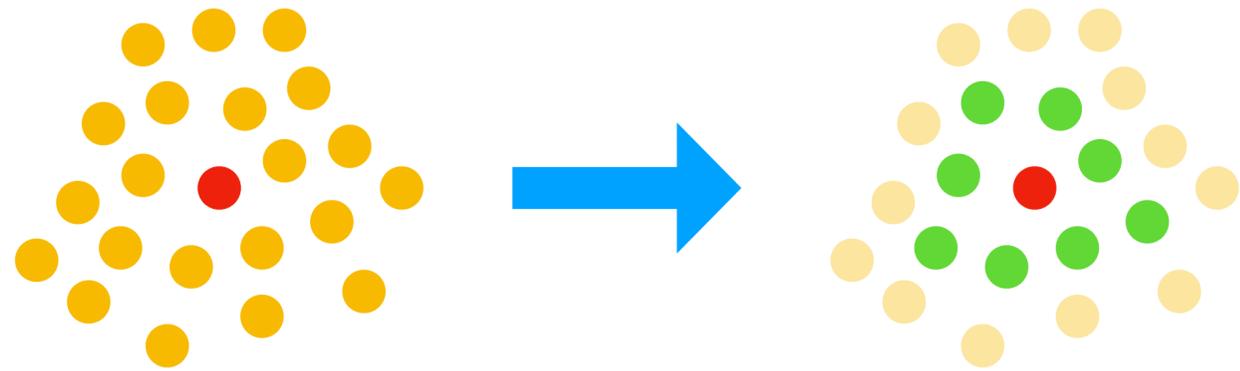


Krugger-Emden et al. 05

Translational interaction

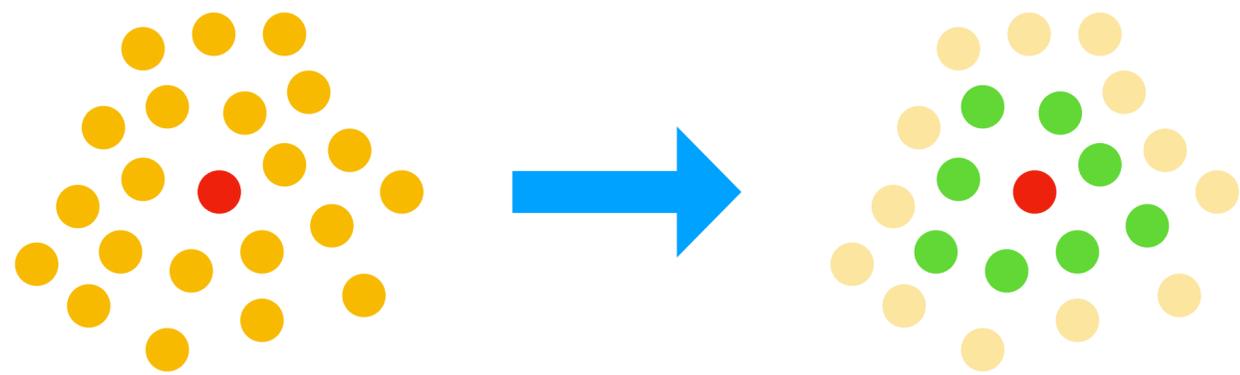
Rotational interaction

# Approach: DEM vs. MPM

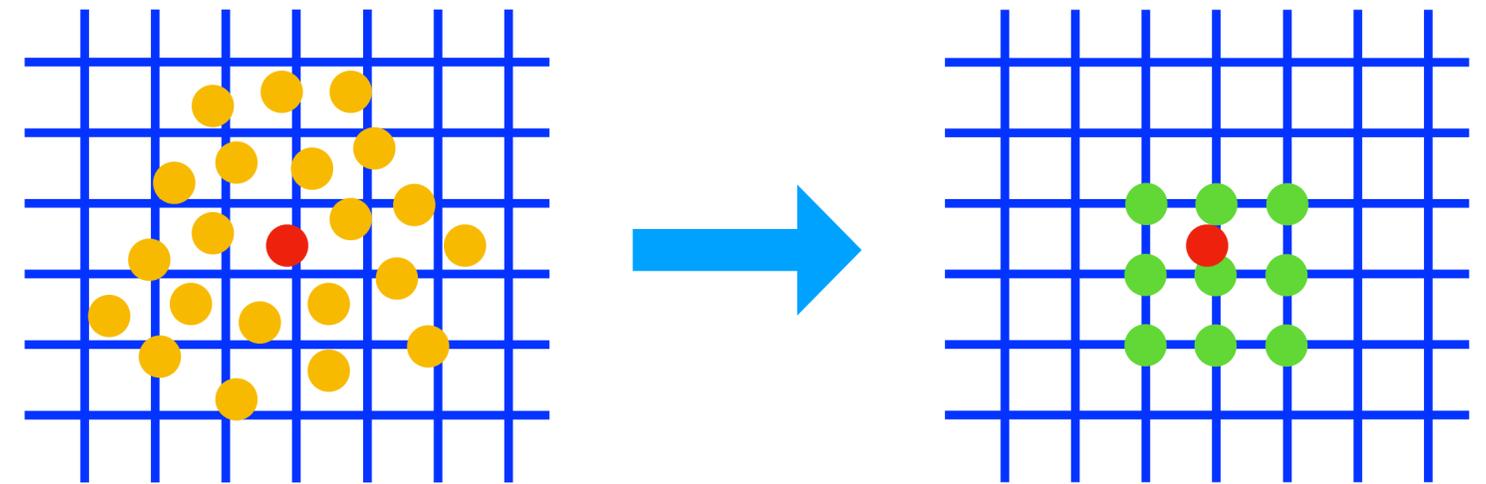


DEM - discrete view

# Approach: DEM vs. MPM

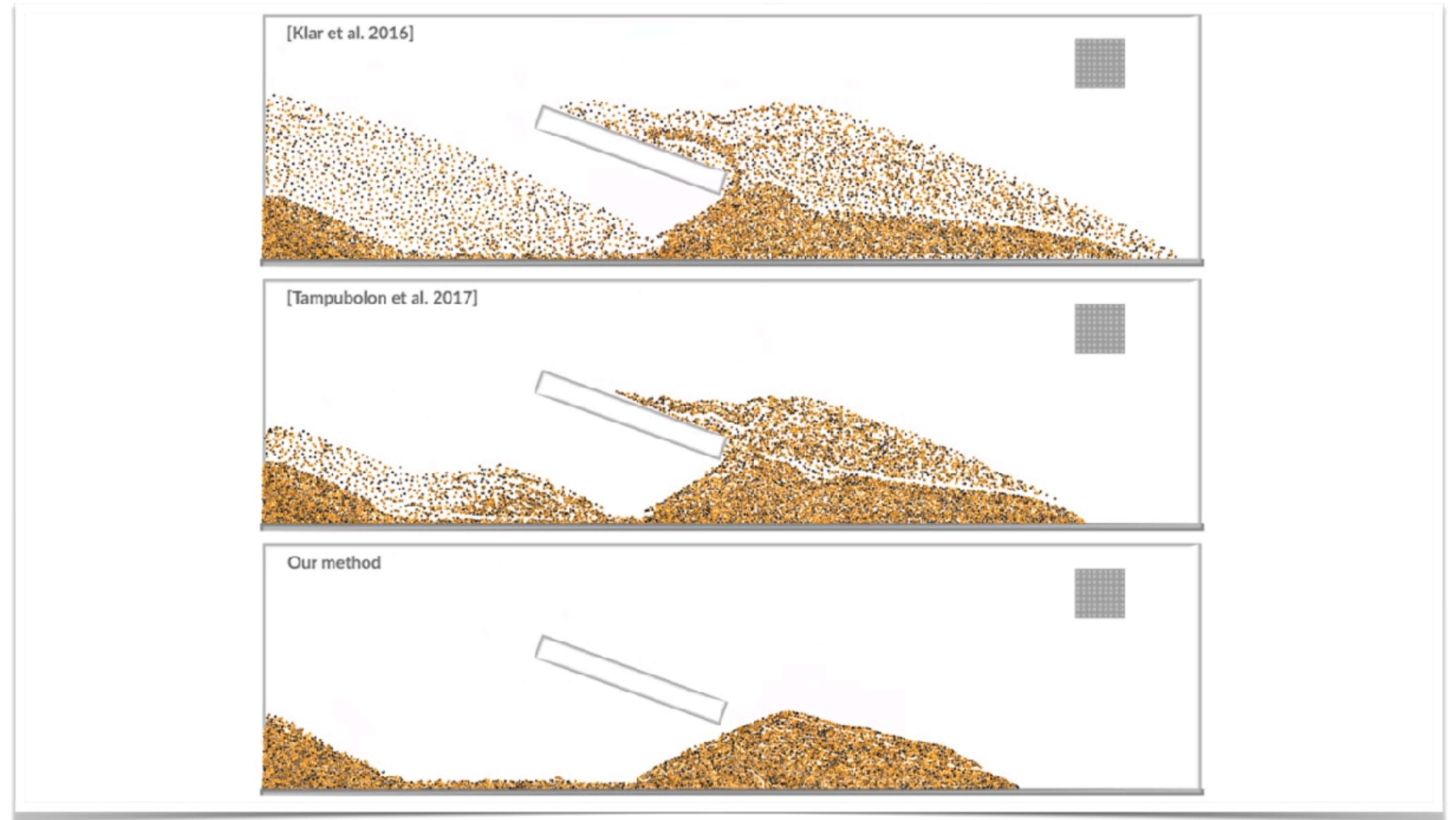
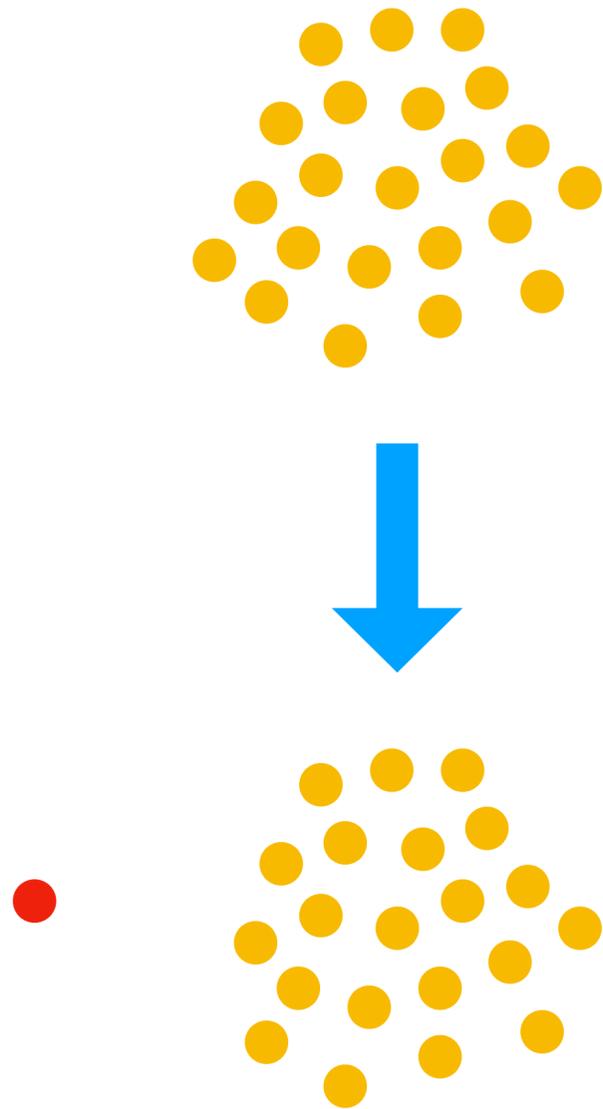


DEM - discrete view



MPM - continuum view

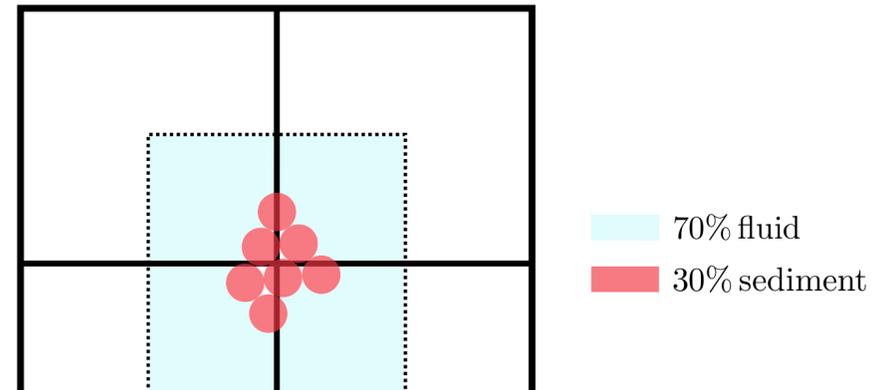
# Challenge of MPM: handle discrete particles



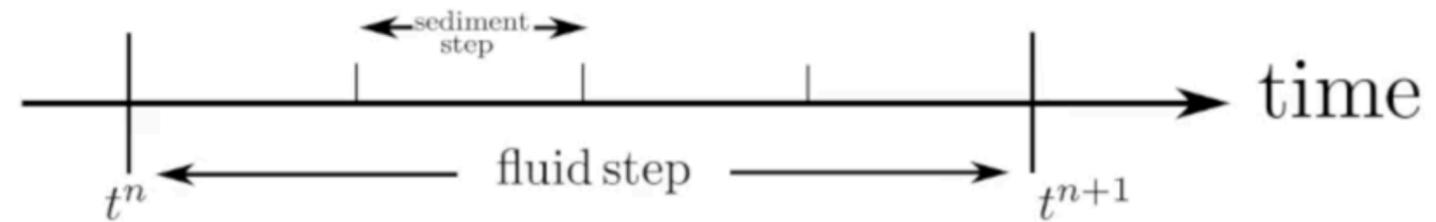
Volume gain problem

# Challenges

- Mixture theory

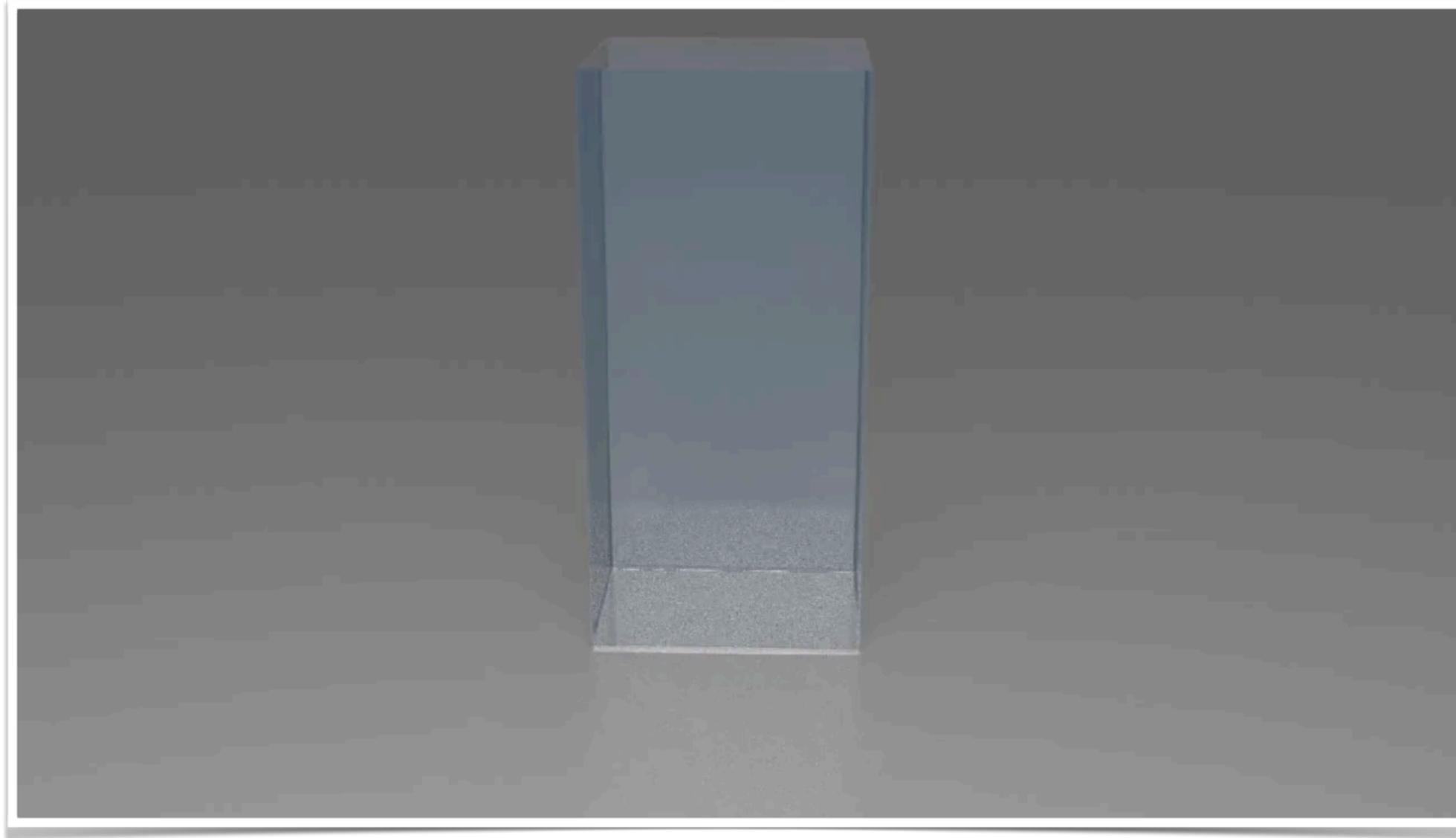


- Sub-stepping

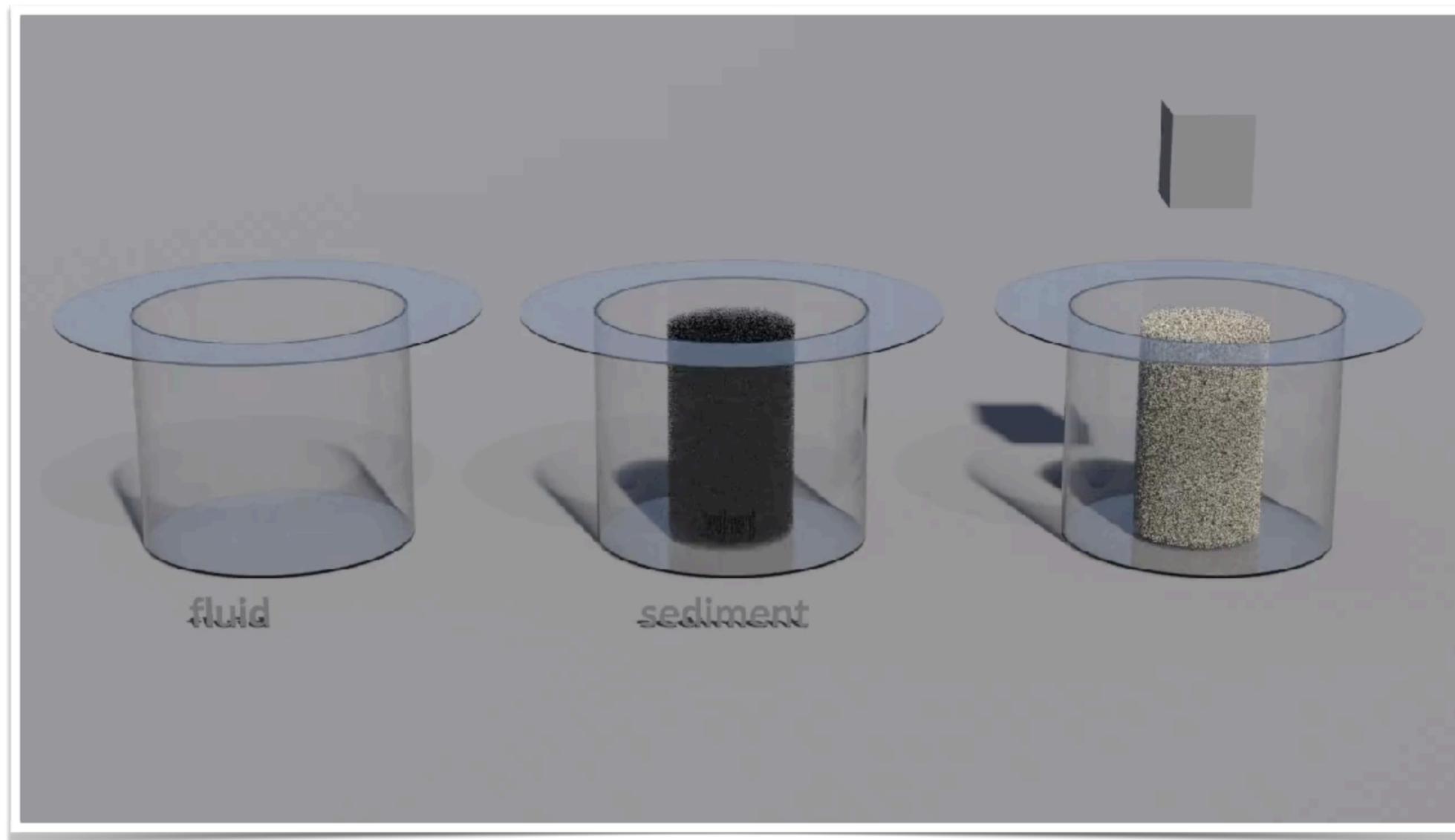


- Momentum conservation

# Results



# Results



# GPU Optimization of Material Point Method

GPU Optimization of Material Point Methods

Paper ID: 250

ANONYMOUS AUTHOR(S)

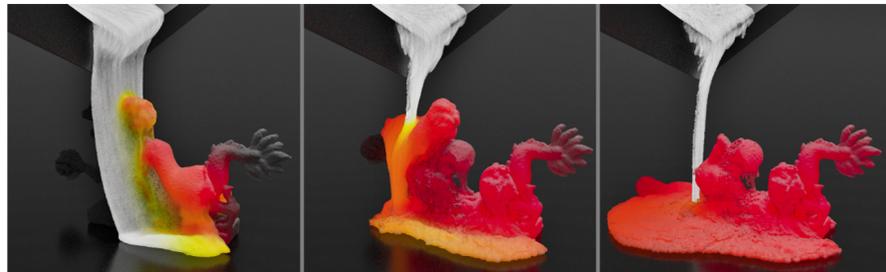


Fig. 1. How to melt your dragon. Melting an elastoplastic dragon with 4.2 million particles on a  $256^3$  grid using our GPU-optimized implicit MPM dynamics and heat solvers on a Nvidia Quadro P6000 GPU at an average 10.5 seconds per 48Hz frame.

The Material Point Method (MPM) has been shown to facilitate effective simulations of physically complex and topologically challenging materials, with a wealth of emerging applications in computational engineering and visual computing. Borne out of the extreme importance of regularity, MPM is given attractive parallelization opportunities on high-performance modern multiprocessors. Unlike the conceptually simple CPU parallelization, a GPU optimization of MPM that fully leverages computing resources presents challenges that require exploring an extensive design-space for favorable data structures and algorithms. In this paper we introduce methods for addressing the computational challenges of MPM and extending the capabilities of general simulation systems based on MPM, particularly concentrating on GPU optimization. In addition to our open-source high-performance framework, we also perform performance analyses and benchmark experiments to compare against alternative design choices which may superficially appear to be reasonable, but can suffer from suboptimal performance in practice. Our explicit and fully implicit GPU MPM solvers are further equipped with a Moving Least Squares MPM heat solver and a novel sand constitutive model to enable fast simulations of a wide range of materials. We demonstrate that more than an order of magnitude performance improvement can be achieved with our GPU solvers. Practical high-resolution examples with up to ten million particles run in less than one minute per frame.

CCS Concepts: • Computing methodologies → Physical simulation;

Additional Key Words and Phrases: Material Point Method (MPM), GPU, SPGrid, GVDB, Hybrid Particle/Grid

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DOI: 10.1145/3197517.3201309

ACM Reference format:  
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DOI: 10.1145/3197517.3201309

## 1 INTRODUCTION

The Material Point Method (MPM) is a hybrid Lagrangian/Eulerian computational scheme that has been shown to simulate a large variety of traditionally-challenging materials with visually rich animations in computer graphics. Recent examples of MPM-based methods developed for such materials include simulations of snow [Stomakhin et al. 2013], granular solids [Klár et al. 2016], multi-phase mixtures [Gao et al. 2018; Stomakhin et al. 2014; Tampubolon et al. 2017], cloth [Jiang et al. 2017a] and many others. MPM has been shown to be particularly effective for simulations involving a large number of particles with complex interactions. However, the size and the complexity of these simulations lead to substantial demands on computational resources, thereby limiting the practical use cases of MPM in computer graphics applications.

Using the parallel computation power of today's GPUs is an attractive direction for addressing computational requirements of simulations with MPM. However, the algorithmic composition of an MPM simulation pipeline can pose challenges in fully leveraging compute resources in a GPU implementation. Indeed, MPM simulations include multiple stages with different computational profiles, and the choice of data structures and algorithms used for handling some stages can have cascading effects on the performance of the remaining computation. Thus, discovering how to achieve a performant GPU implementation of MPM involves a software-level design-space exploration for determining the favorable combinations of data structures and algorithms for handling each stage.

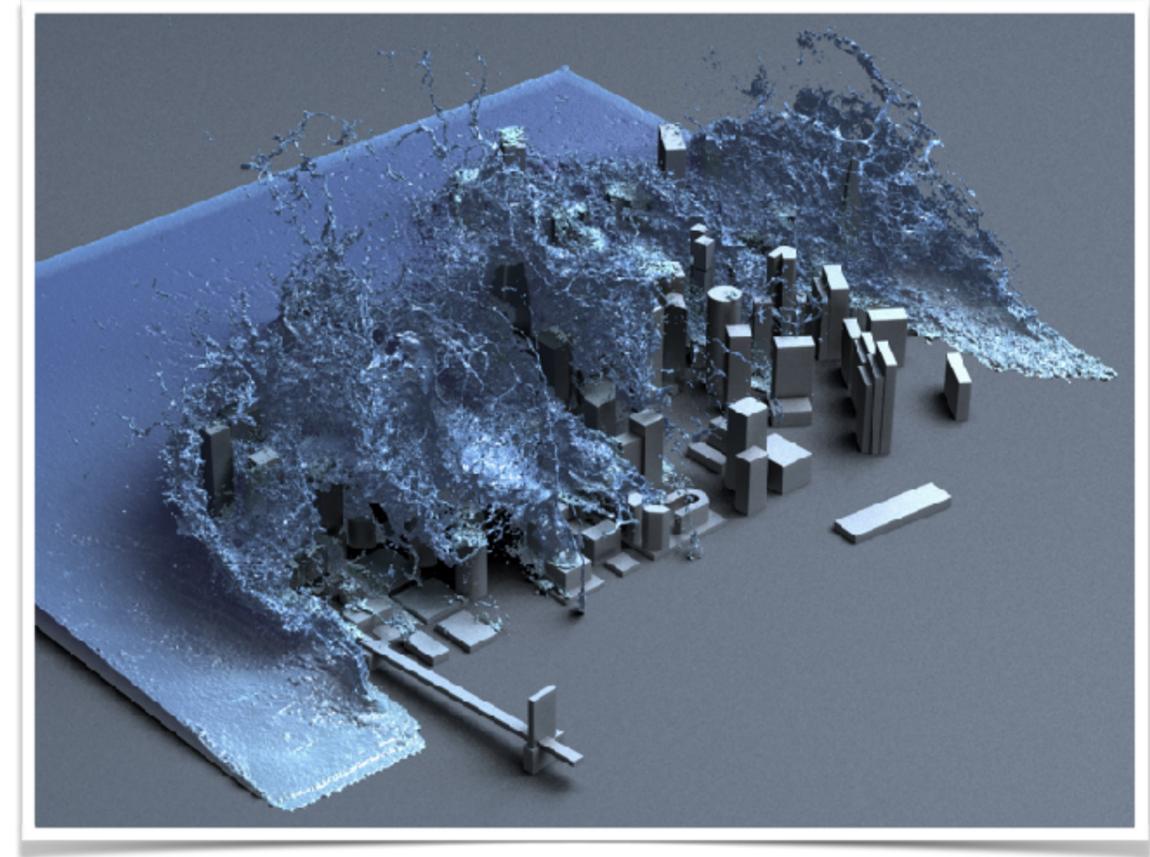
**M. Gao\***, X. Wang\*, K. Wu\* (joint first authors),  
A. Tampubolon, E. Sifakis, C. Yuksel, C. Jiang  
SIGGRAPH Asia 2018 (under review)



# Acceleration for hybrid methods

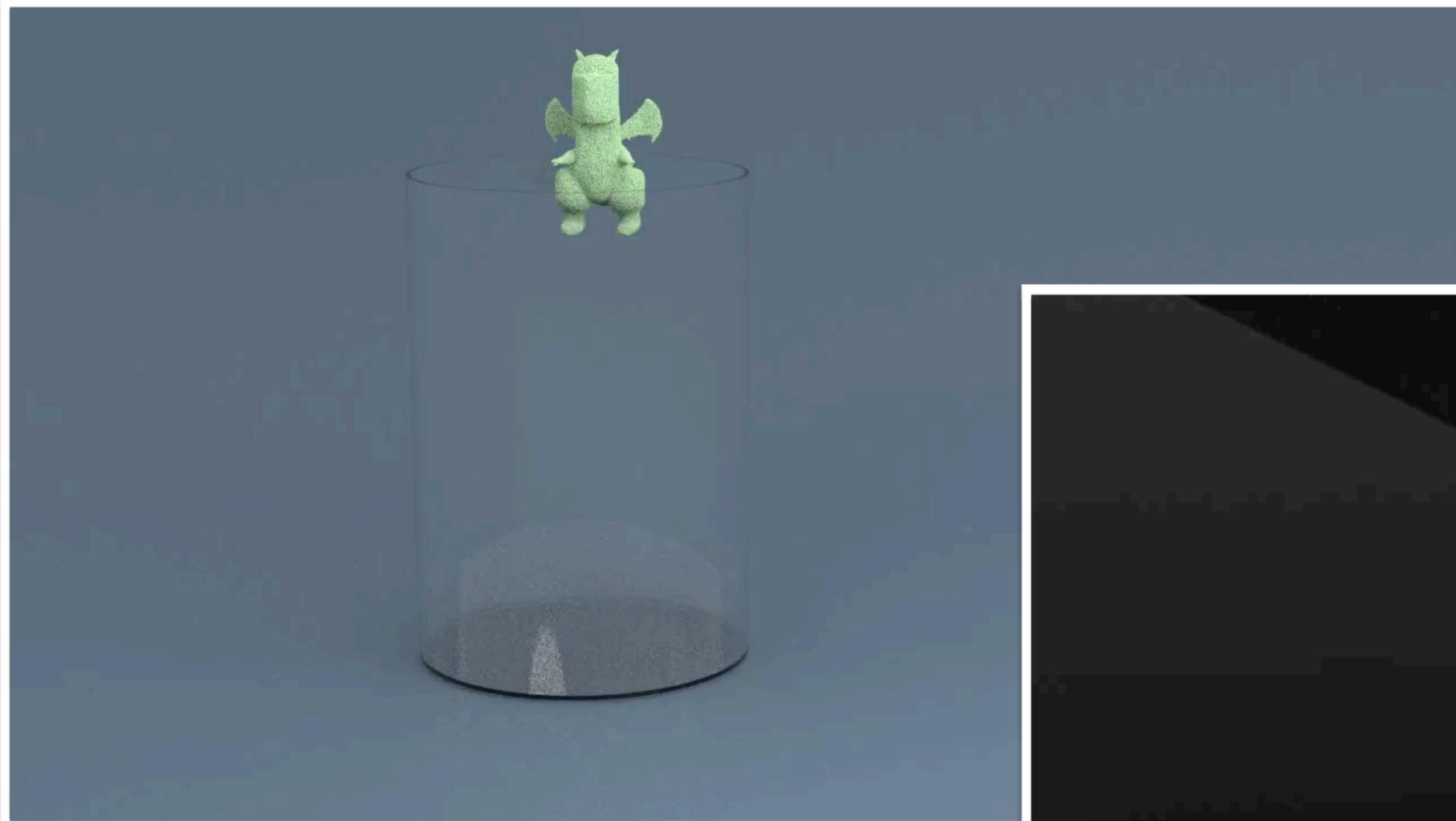


Klar et al. 17



Wu et al. 18

# Target benchmarks

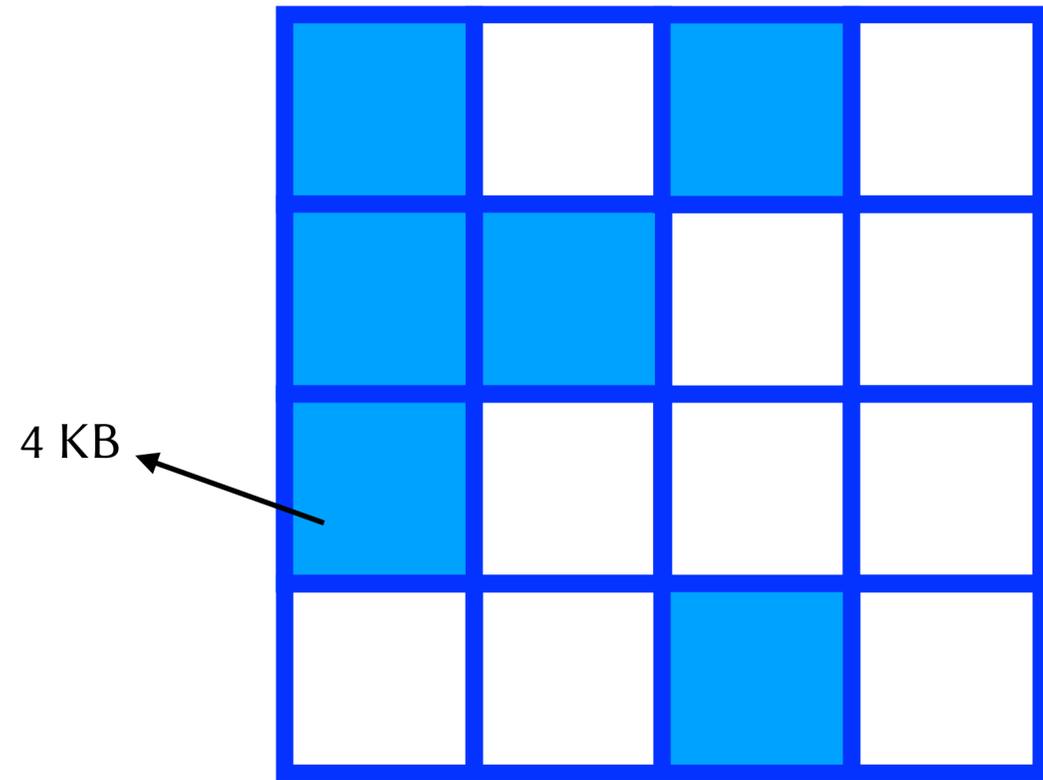


Particles: 4.2 M  
Grid resolution:  $256^3$   
Simulation: 10.48 secs/frame

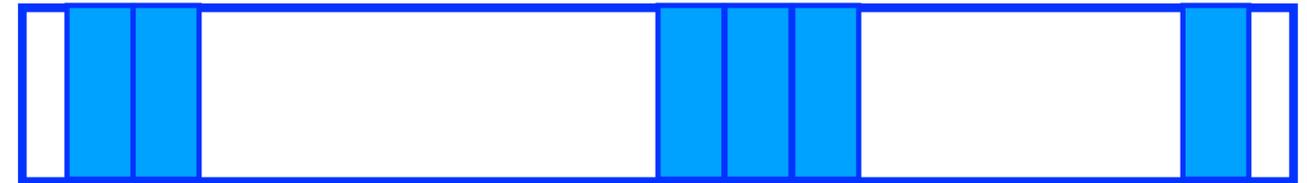


Particles: 9.0 M  
Grid resolution:  $512^3$   
Simulation: 21.88 secs/frame

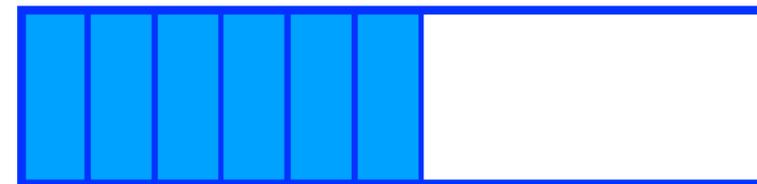
# Sparsity - (G)SPGrid



CPU virtual memory



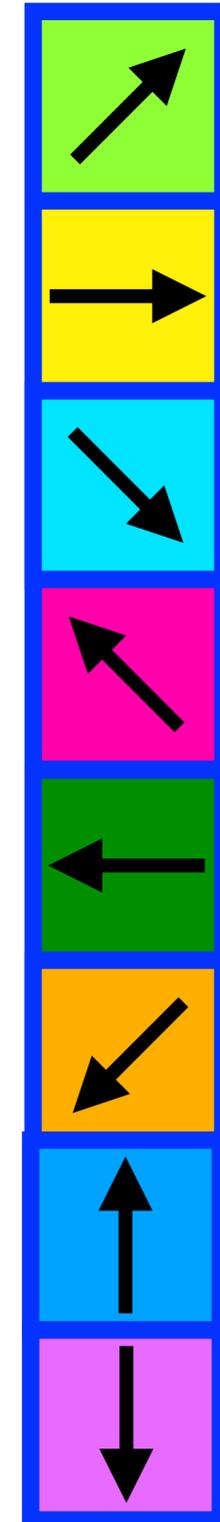
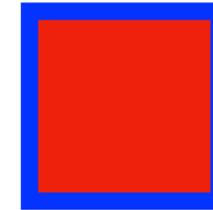
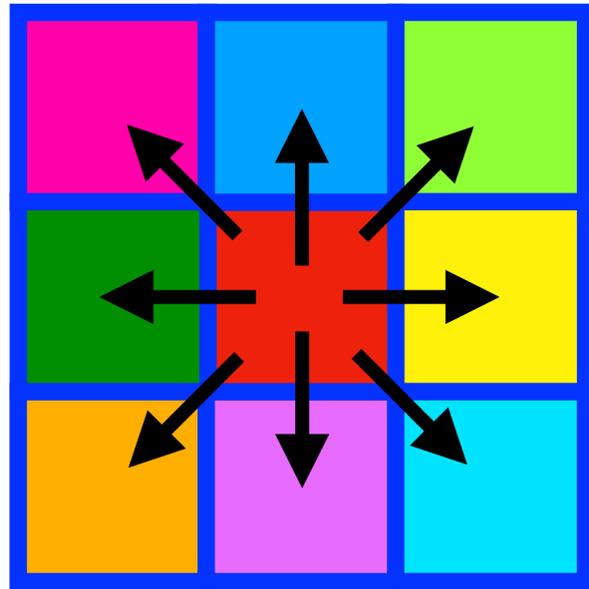
GPU memory



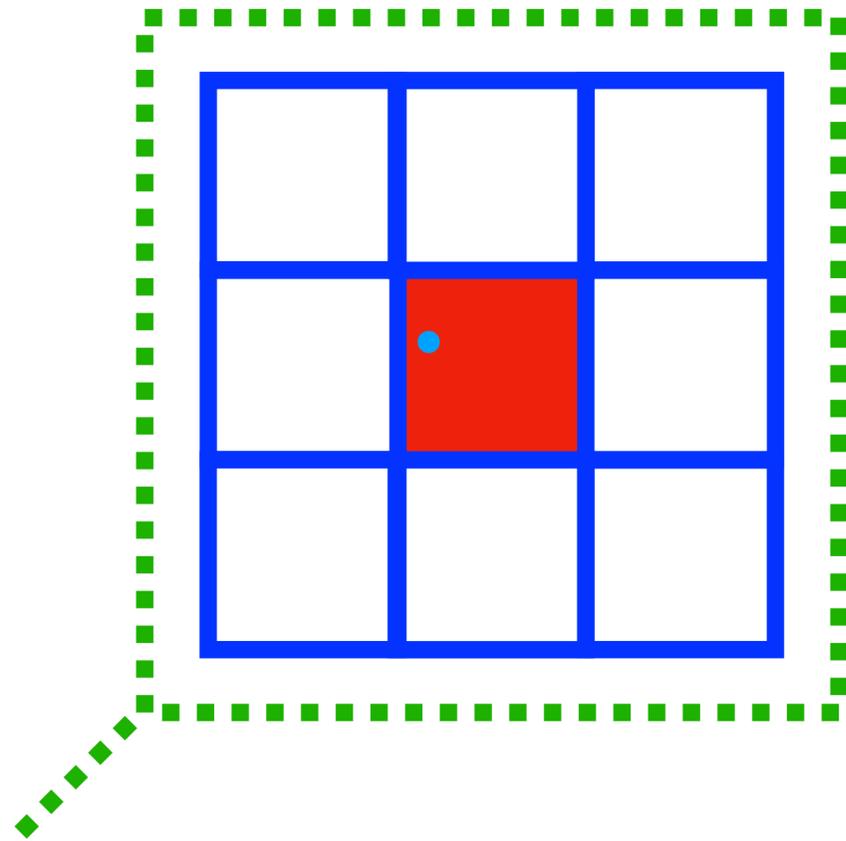
CPU - SPGrid

GPU - GSPGrid

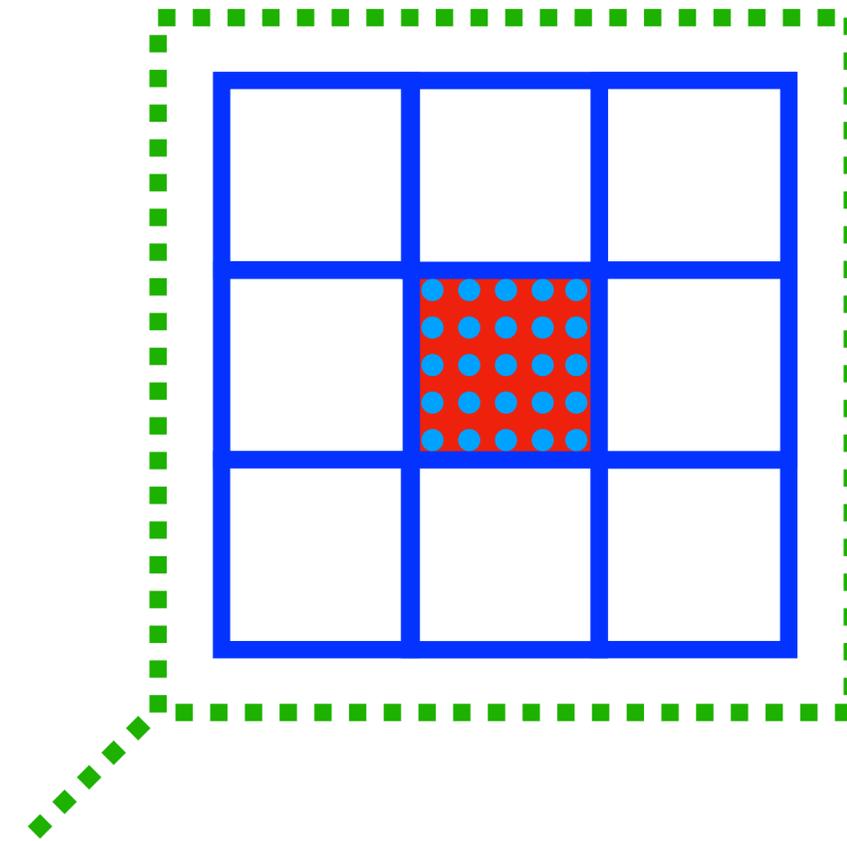
# Sparsity - GSPGrid



# Sparsity - GSPGrid

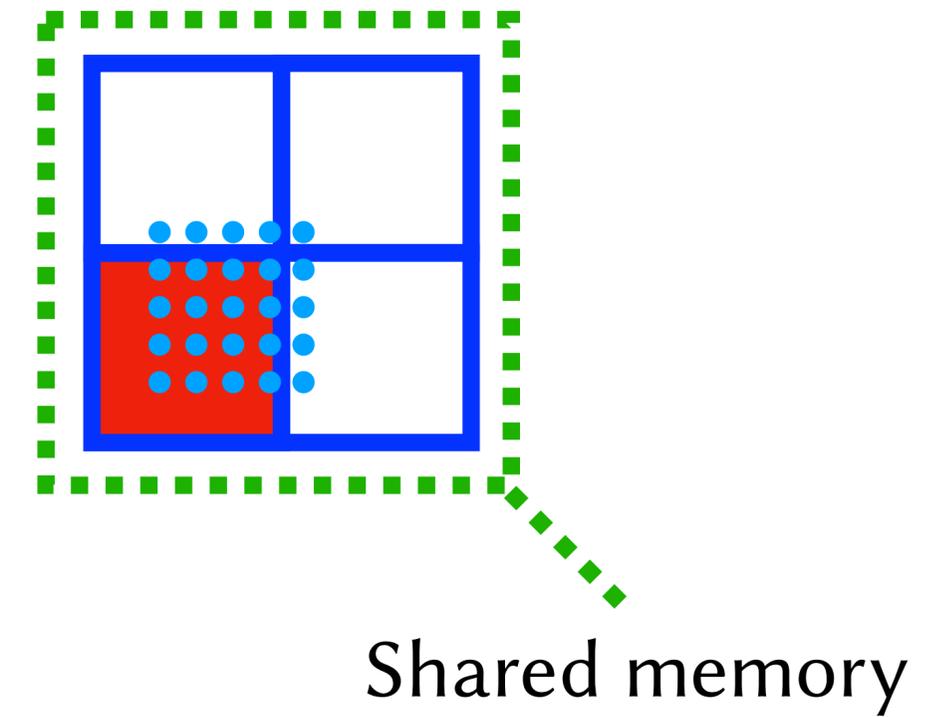
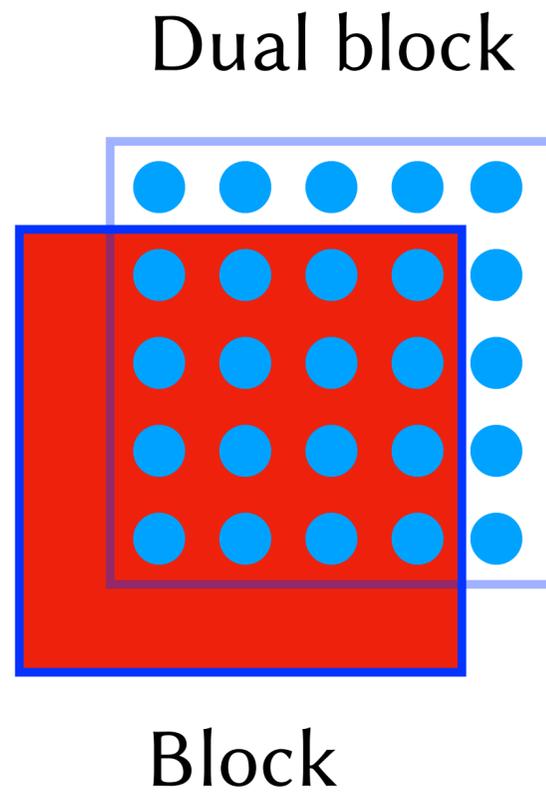
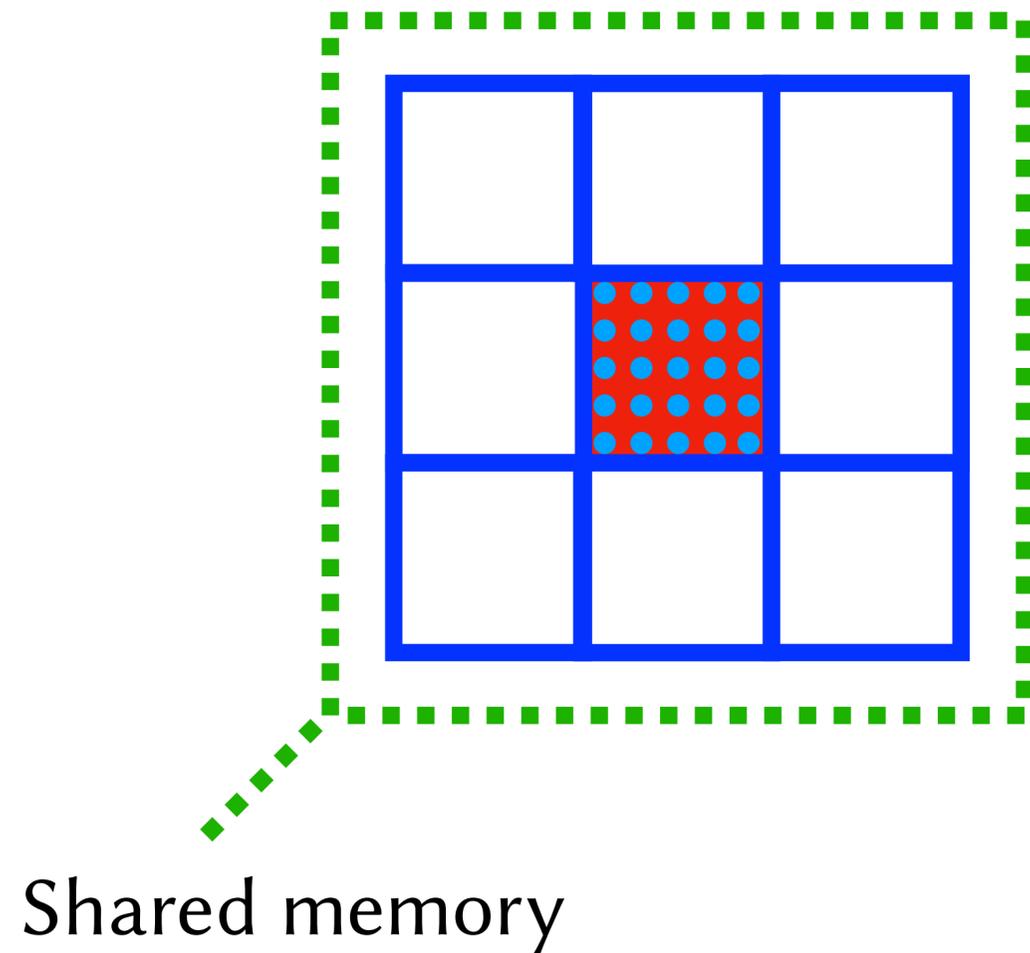


Shared memory

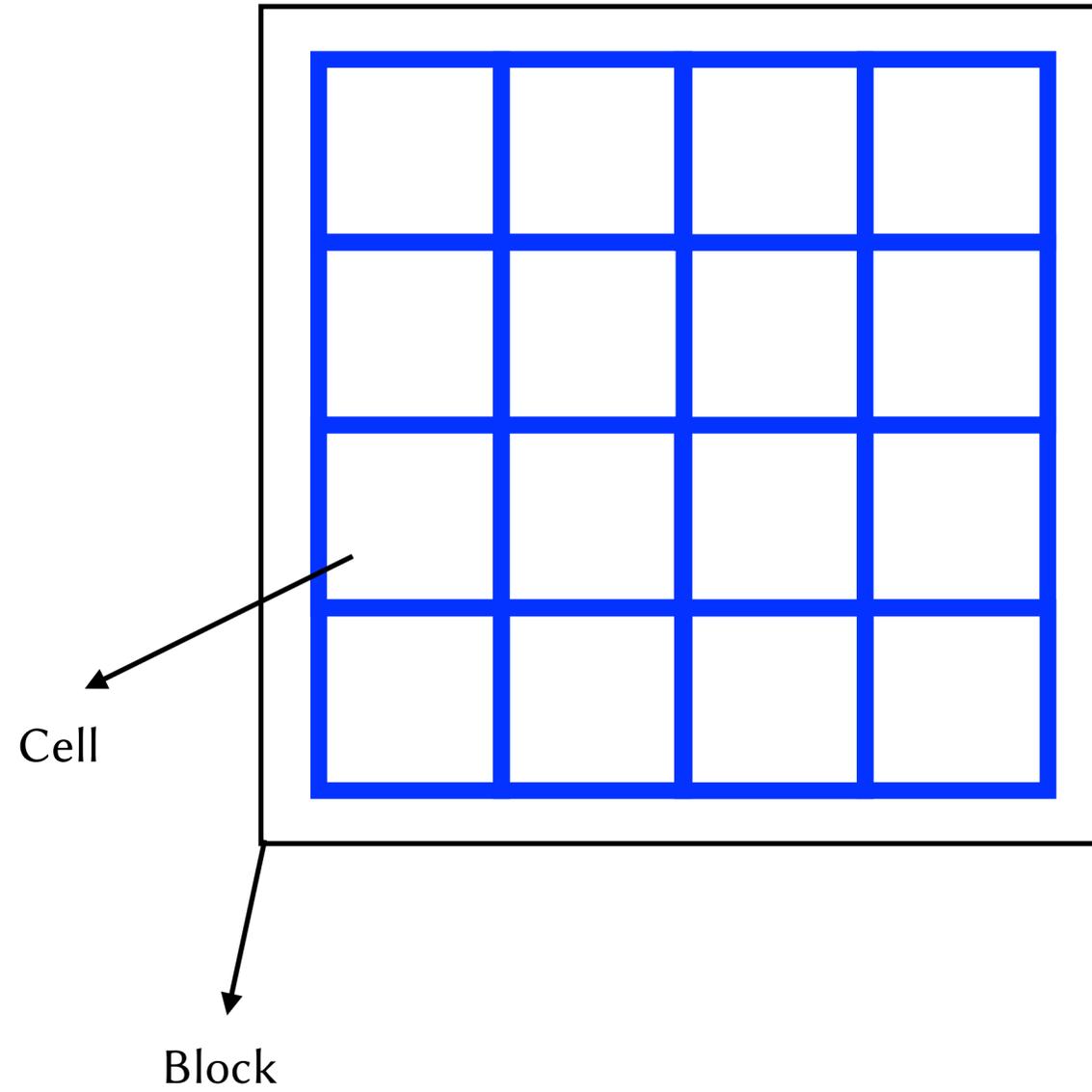


Shared memory

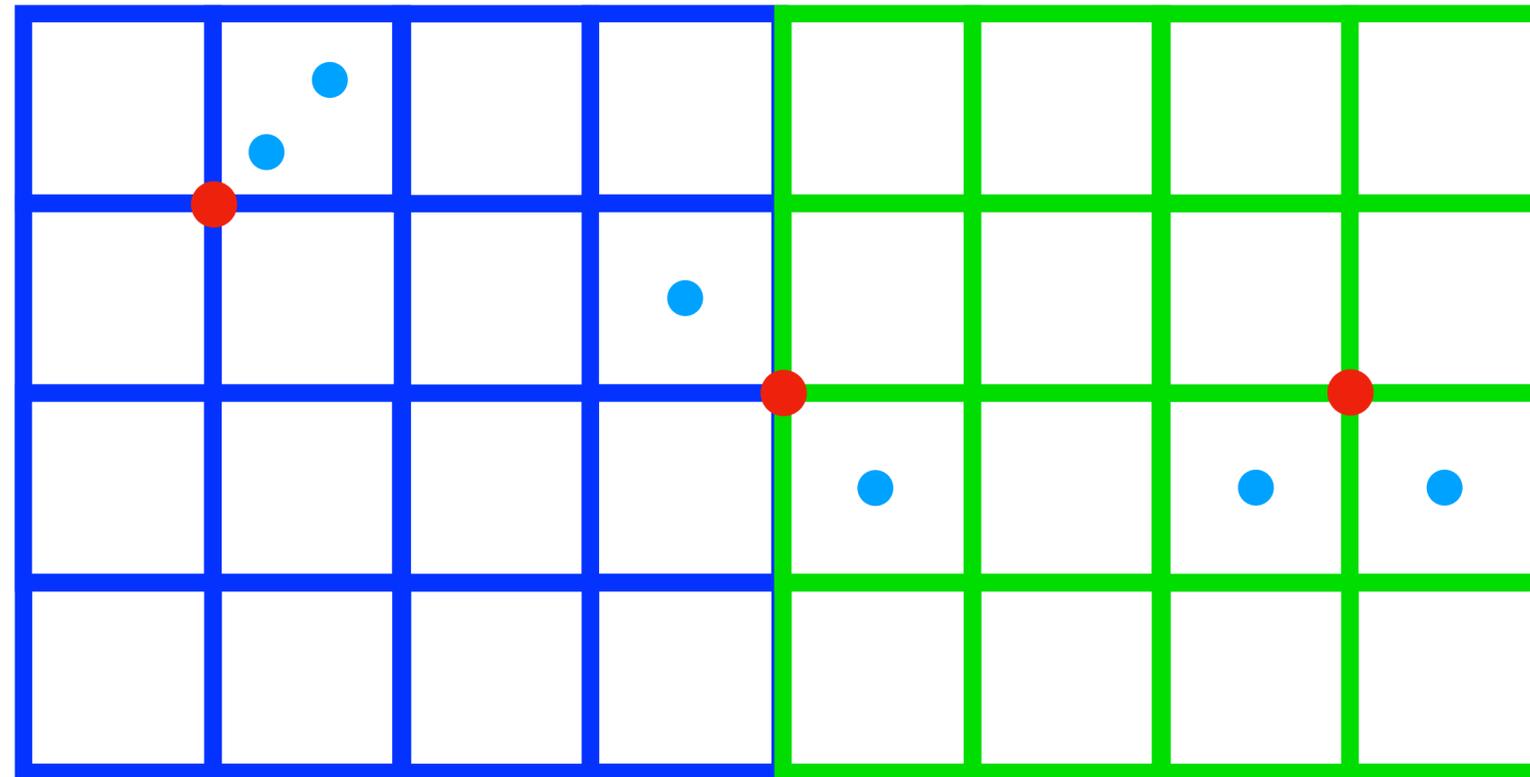
# Sparsity - GSPGrid



# Write hazards



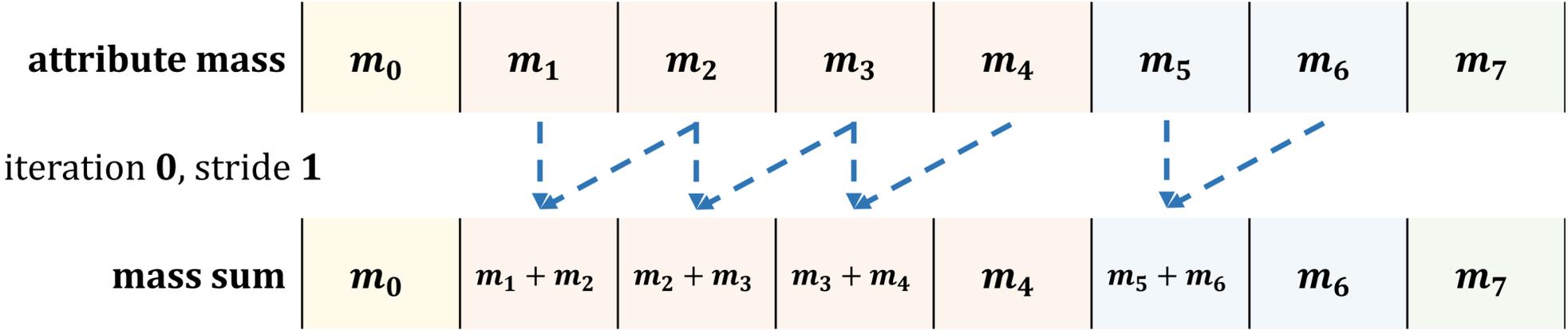
# Write hazards



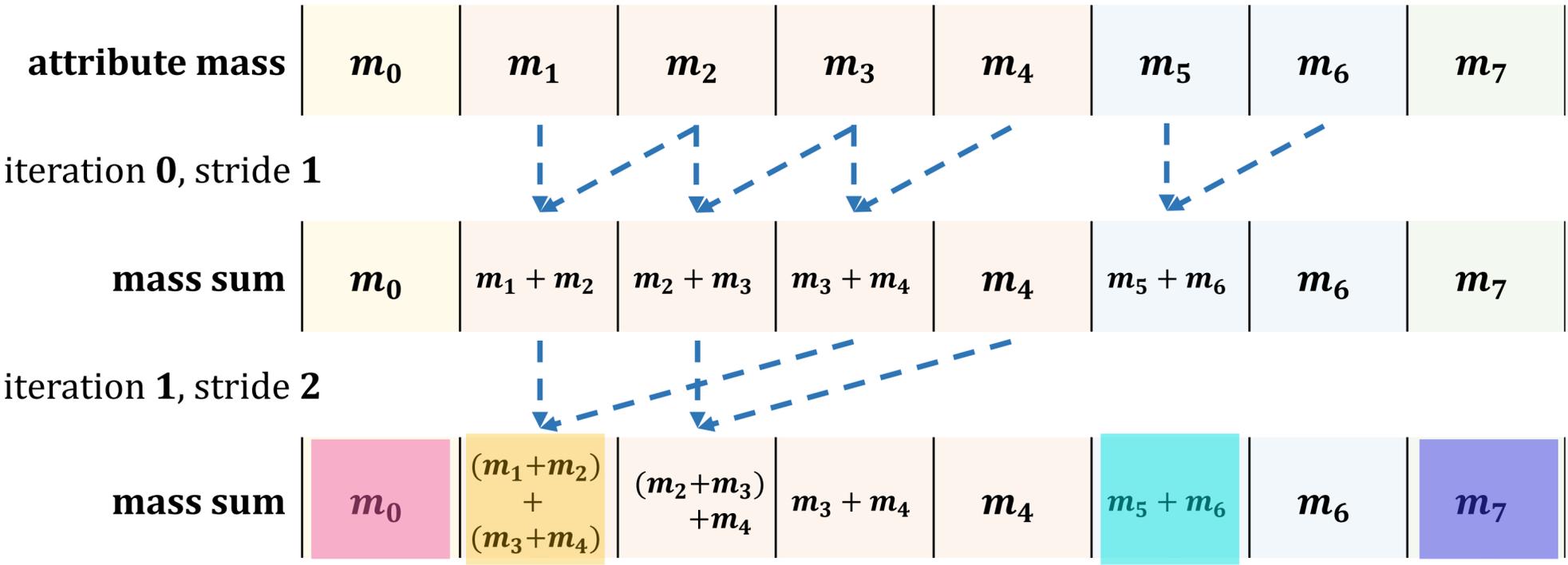
CUDA thread - ●

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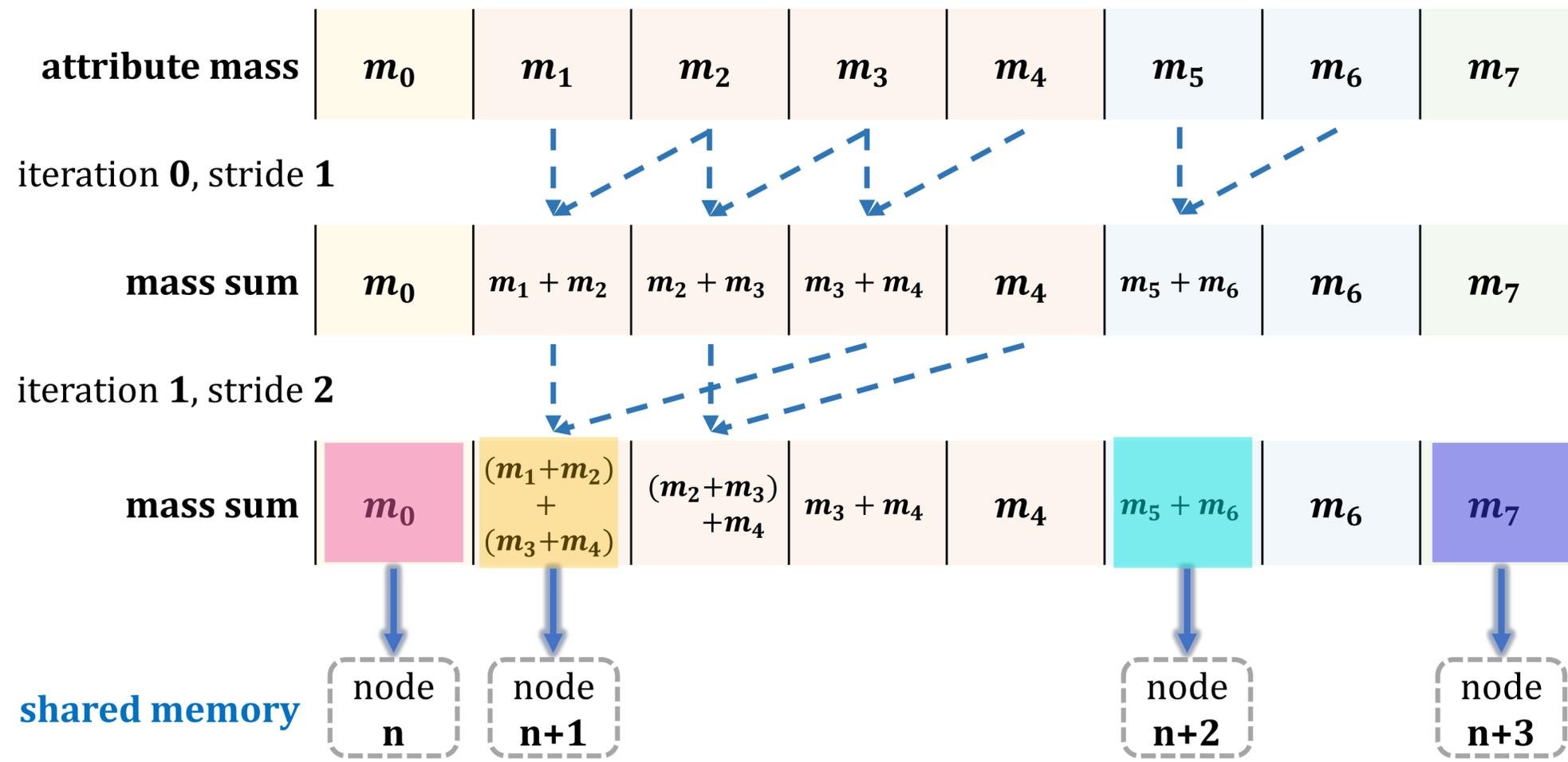
lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



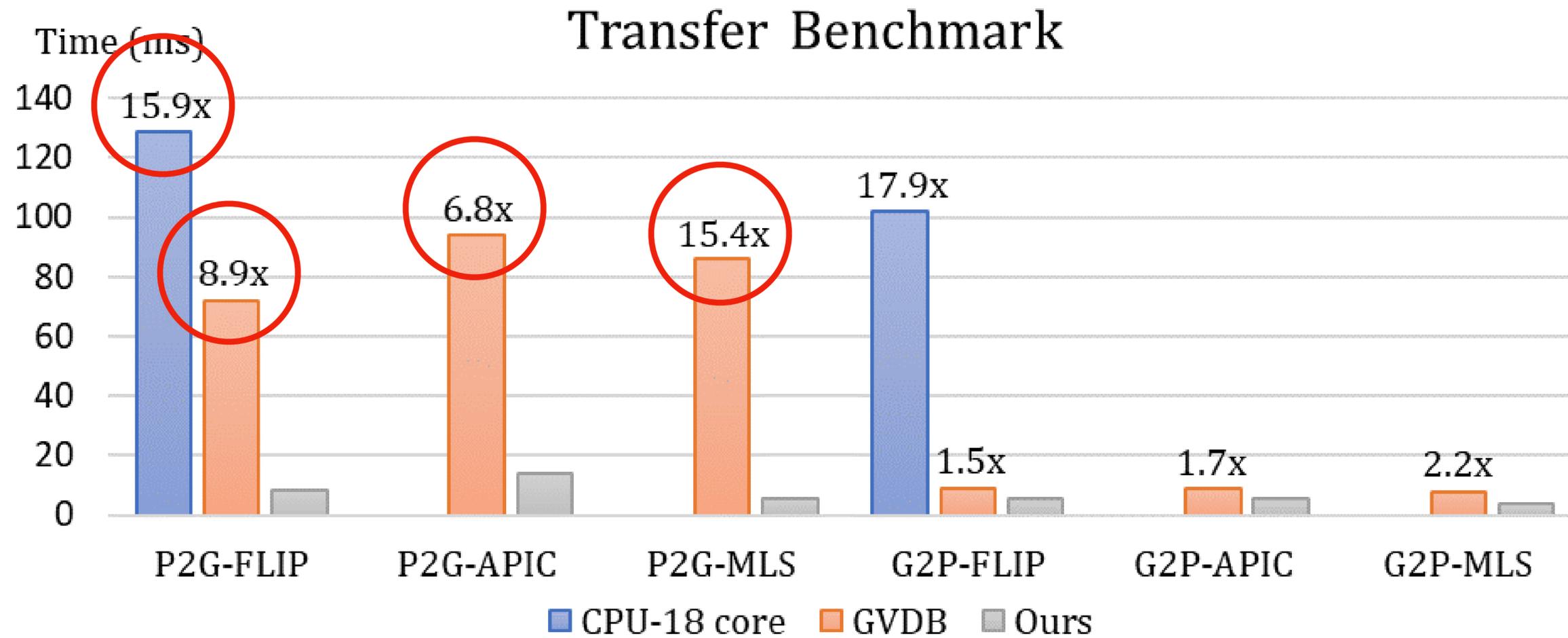
lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



lane id	0	1	2	3	4	5	6	7
node id	n	n+1	n+1	n+1	n+1	n+2	n+2	n+3



# Benchmark



# Additional contributions

- Accelerated particle sorting
- Avoiding explicit particle reordering
- A new sand model for semi-implicit integration
- A MPM-based heat solver

# Conclusion

SPGrid  
GSPGrid



# Conclusion

Breadth of simulation



Parallel efficiency

Price paid:

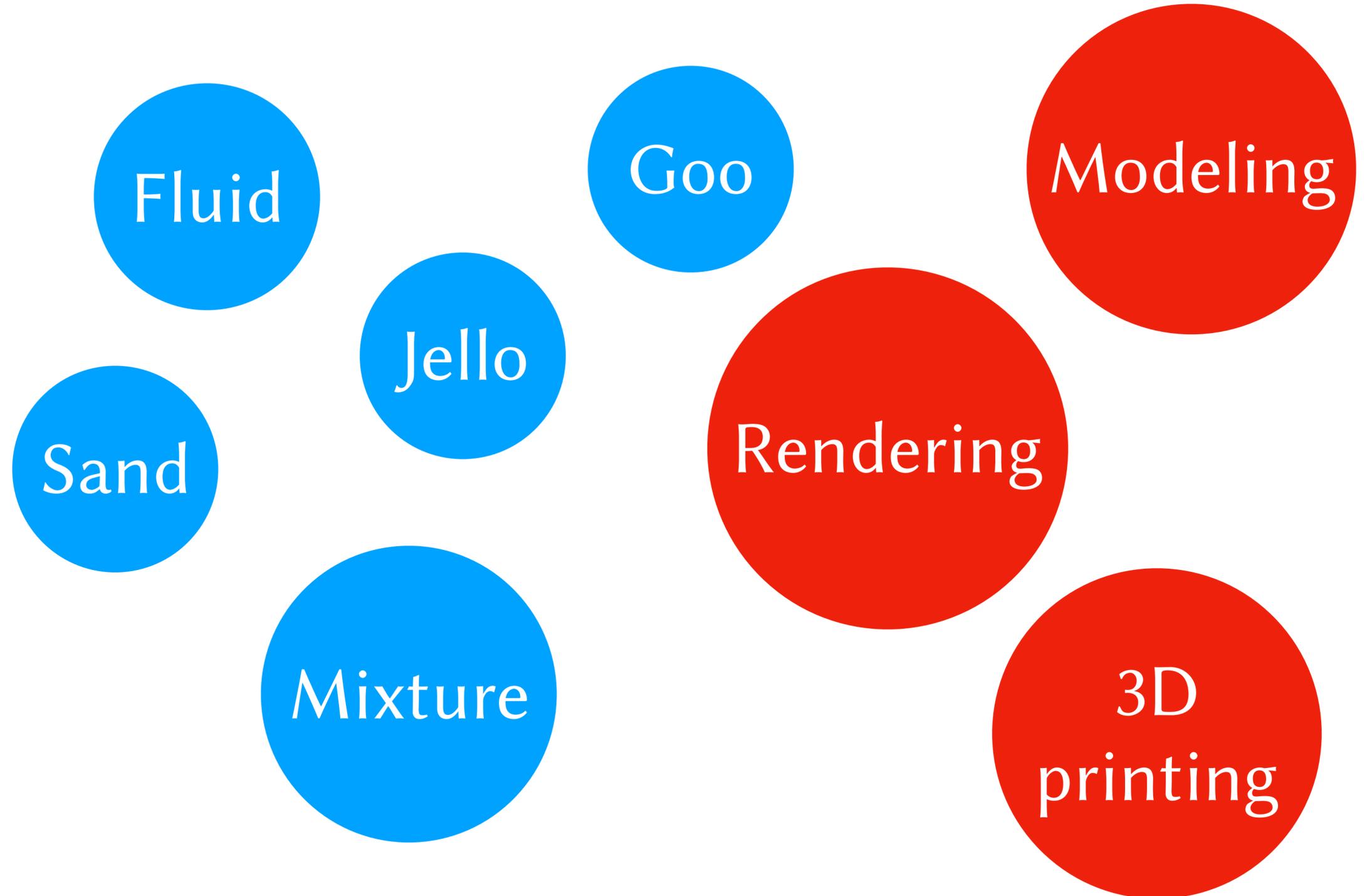
Platform-specific solutions

Optimizations far from automatic

Focus on **visual** appeal

# Future work

SPGrid  
GSPGrid



# Acknowledgement

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