

# Cryptography Intro

## CS642: Computer Security



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## Security Company Tries To Hide Flaws By Threatening Infringement Suit

**Soulskill** posted 2 days ago | from the because-that-always-ends-well dept.

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An anonymous reader writes:

An RFID-based access control system called IClass is used across the globe to provide physical access controls. This system relies on cryptography to secure communications between a tag and a reader. Since 2010, several academic papers have been released which expose the cryptographic insecurity of the IClass system. Based on these papers, Martin Holst Swende implemented the IClass ciphers in a software library, which he [released under the GNU General Public License](#).

# Cryptography



Basic goals and setting

TLS (HTTPS)

Provable security

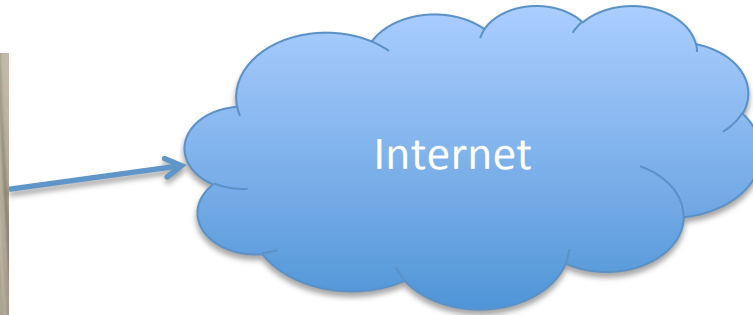
One time pad

Block ciphers

# Cryptography: “Hidden writing”

- Study and practice of building security protocols that resist adversarial behavior
- Blend of mathematics, engineering, computer science

# Cryptography Example

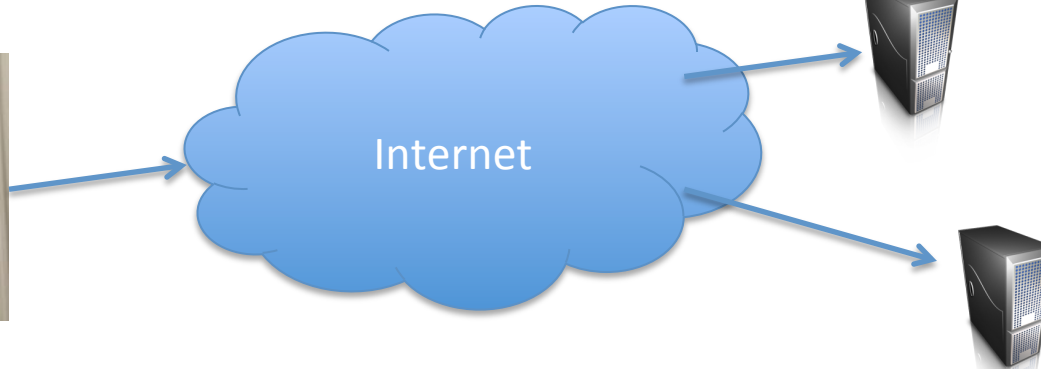


US  
diplomatic  
cables

Don't want to reveal data early

Want to store it in way that it  
can quickly be revealed later

# Cryptography Example



01101010  
10101010  
10101010  
11111101

01101010  
10101010  
10101010  
11111101

Don't want to reveal data early

Want to store it in way that it  
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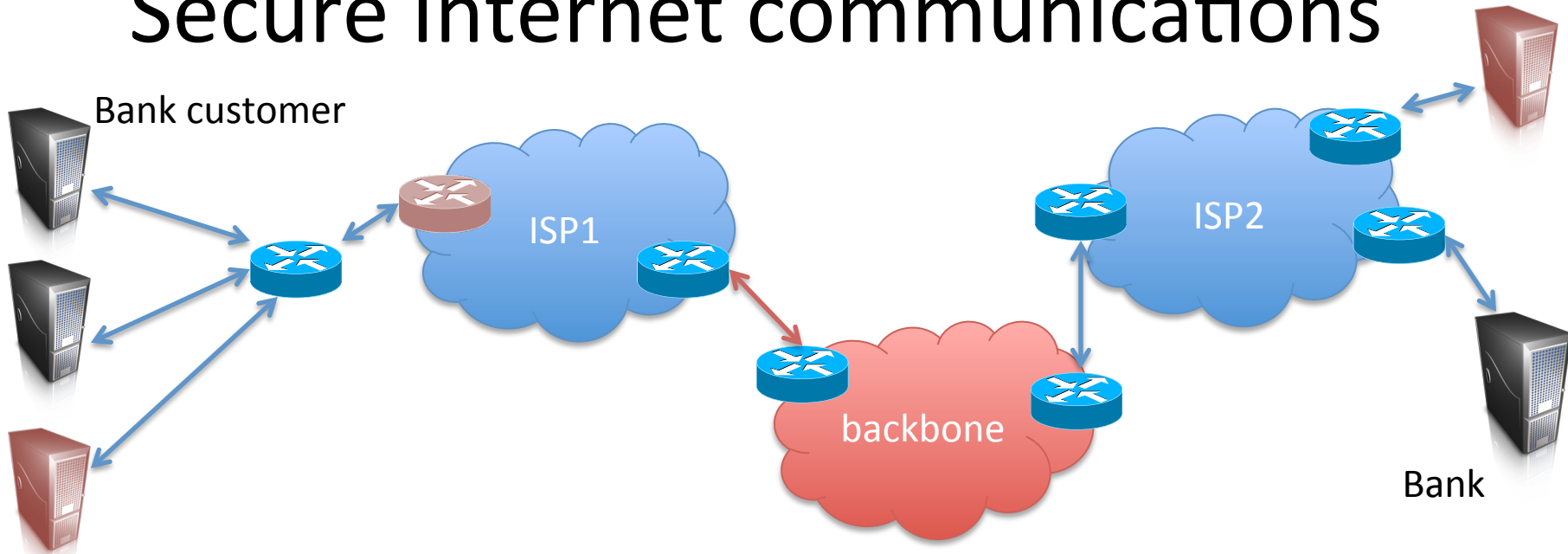
01101010  
10101010  
10101010  
11111101

Modern cryptography enables this:

- Encrypt file
- Store key in secure place ←



# Crypto Example 2: Secure Internet communications

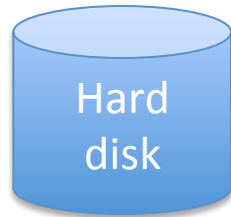


Customer and bank want to communicate securely:

- **Confidentiality** (messages are private)
- **Integrity** (accepted messages are as sent)
- **Authenticity** (is it the bank? is this the customer?)
- Sometimes: anonymity (hide identities)
- Sometimes: steganography (hide that communication took place)

TLS, SSH, IPsec, PGP

# Crypto Example 3: Encrypted hard disks



Company's intellectual property  
Customer records  
Your personal diary

Encrypt hard drives (or volumes):

- Confidentiality of data
- Attacker has physical access to device

Bitlocker, Truecrypt, Seagate



# Crypto

- Powerful tool for confidentiality, authenticity, and more
- But:
  - must design securely
  - must implement designs securely
  - must use properly (e.g., key management)

# Auguste Kerckhoffs' (Second) Principle

“The system must not require secrecy and can be stolen by the enemy without causing trouble”

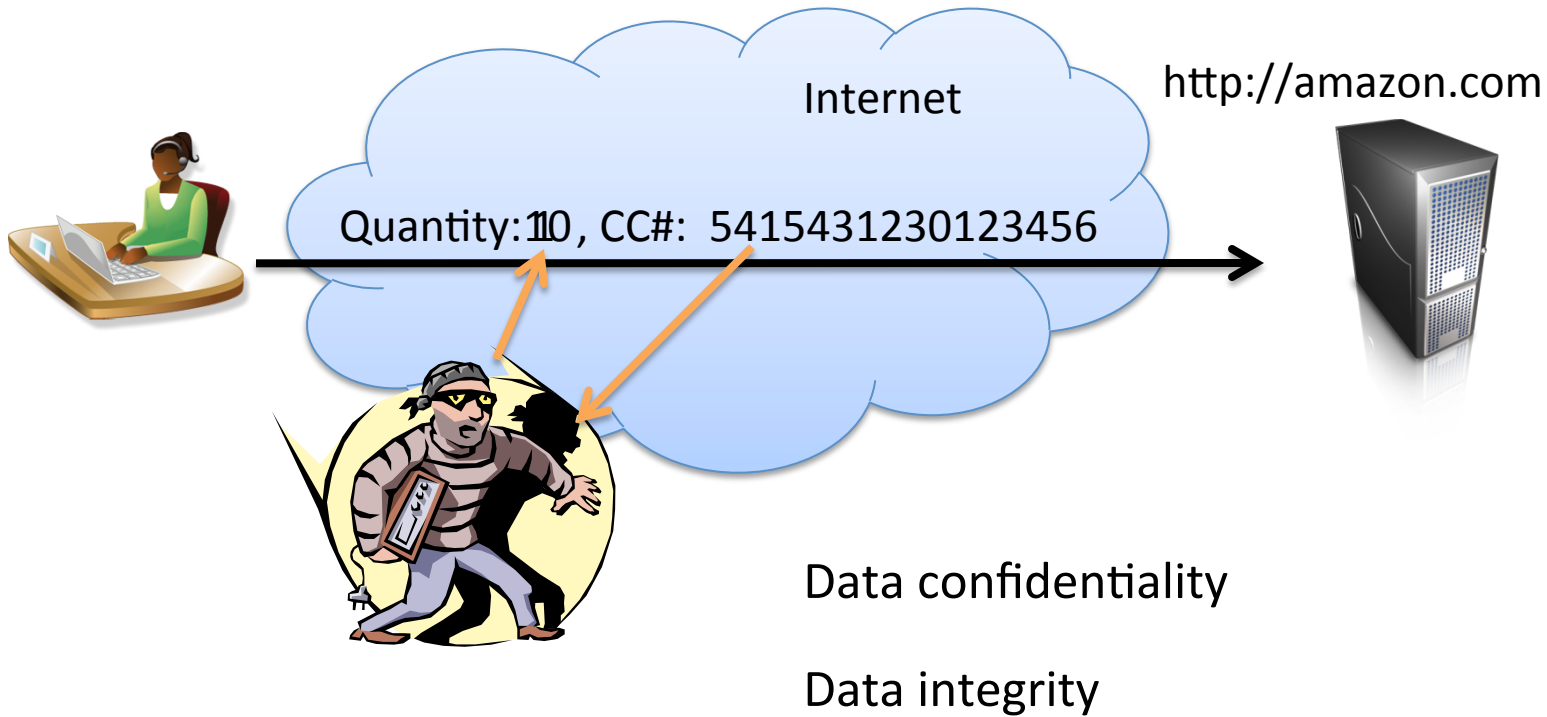
A cryptosystem should be secure even if its algorithms, implementations, configuration, etc. is made public --- the only secret should be a key

Why?

# Some basic primitives

- Symmetric cryptography (shared key  $K$ )
  - encryption & decryption using  $K$
  - message authentication using  $K$
  - pseudorandom functions (PRF)
- Public-key cryptography (public key  $pk$ , secret key  $sk$ )
  - encrypt with  $pk$  and decrypt with  $sk$
  - digitally sign using  $sk$  and verify with  $pk$
- Hash functions (no keys)
  - used to “compress” messages in a secure way

# An example: On-line shopping



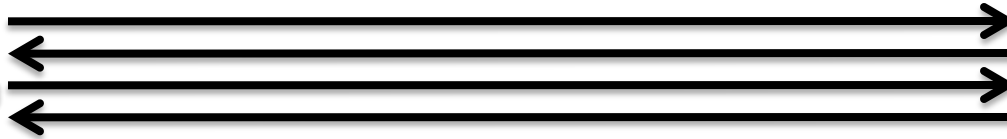
We need secure channels for transmitting data

# An example: On-line shopping **with TLS**

https://amazon.com



**K**



**Enc(K, "Quantity: 1 , CC#: 5415431230123456")**



**K**

Step 1:  
Key exchange  
protocol to  
share secret **K**

Step 2:  
Send data via  
secure  
channel

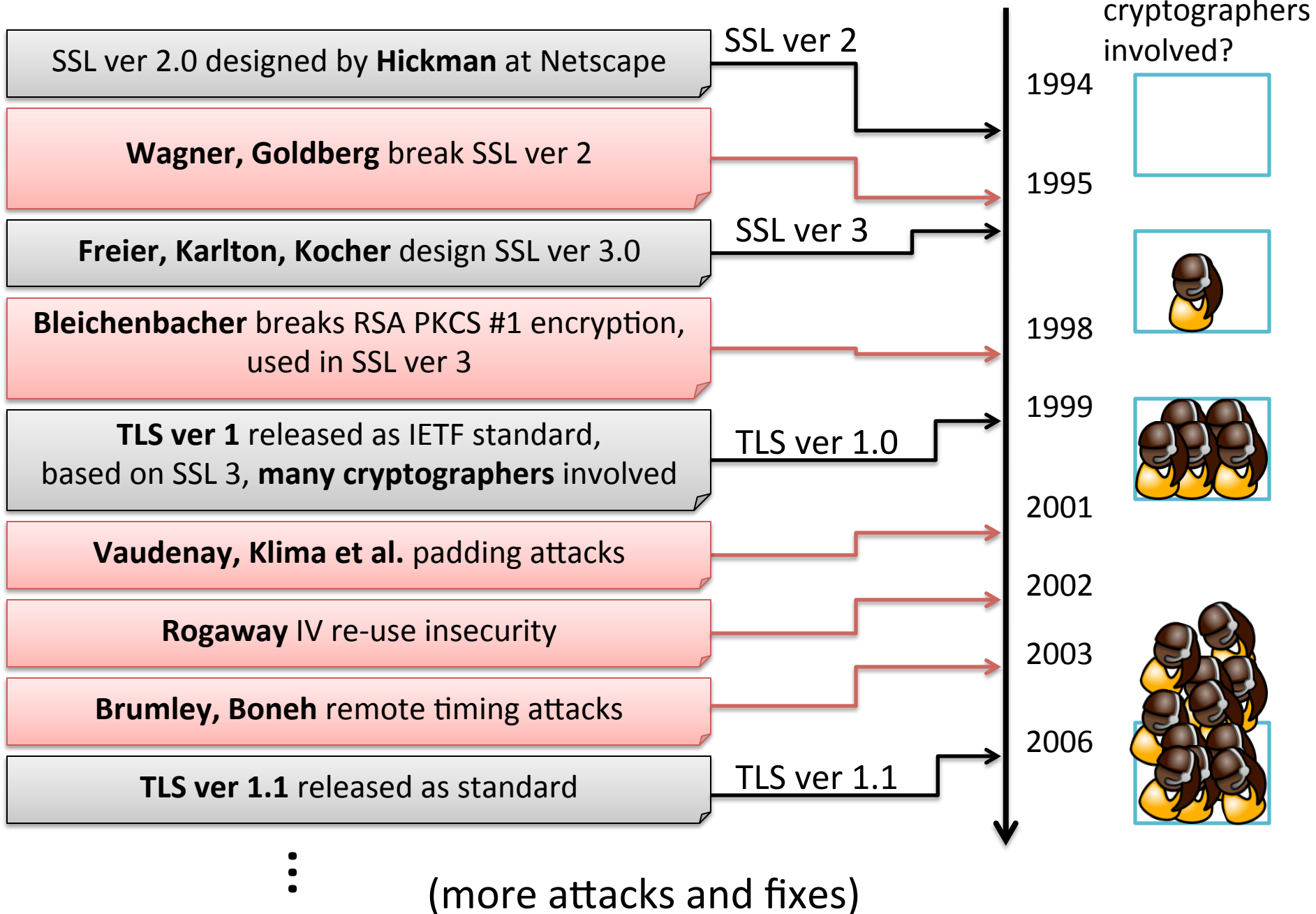
TLS uses many **cryptographic primitives**:

**key exchange:** hash functions, digital signatures, public key encryption

**secure channel:** symmetric encryption, message authentication

Mechanisms to resist **replay attacks**, **man-in-the-middle attacks**,  
**truncation attacks**, etc...

# A short history of TLS up to 2009





# TLS handshake for RSA transport

Bank customer

Bank

Pick random  $N_c$

ClientHello, MaxVer,  $N_c$ , Ciphers/CompMethods

Pick random  $N_s$

ServerHello, Ver,  $N_s$ , SessionID, Cipher/CompMethod

Check CERT  
using CA public  
verification key

CERT = (pk of bank, signature over it)

Pick random PMS  
 $C \leftarrow E(pk, PMS)$

C

$PMS \leftarrow D(sk, C)$

ChangeCipherSpec,  
{ Finished, PRF( $MS$ , "Client finished" ||  $H(\text{transcript})$ ) }

ChangeCipherSpec,  
{ Finished, PRF( $MS$ , "Server finished" ||  $H(\text{transcript}')$ ) }

Bracket notation  
means contents  
encrypted

$MS \leftarrow \text{PRF}(PMS, \text{"master secret"} || N_c || N_s)$



Bank customer

# TLS Record layer



Bank

$$MS \leftarrow \text{PRF}(PS, \text{"master secret"} \parallel N_c \parallel N_s)$$
$$K_1, K_2 \leftarrow \text{PRF}(MS, \text{"key expansion"} \parallel N_s \parallel N_c)$$
$$C_1 \leftarrow E(K_1, \text{Message})$$

C1


$$\text{Message} \leftarrow D(K_1, C_1)$$

C2


$$C_2 \leftarrow E(K_2, \text{Message}')$$
$$\text{Message}' \leftarrow D(K_2, C_2)$$



# Primitives used by TLS

← CERT = (pk of bank, signature over it)




Digital signatures

C →




Public-key encryption  
(RSA)

ChangeCipherSpec,  
{ Finished, PRF(MS, "Client finished" || H(transcript)) }



PRF  
Hash function

C1 →



← C2



Symmetric encryption

TLS was built via “design-**break**-redesign-**break**...”

We're now at TLS ver 1.2

~~No (publicly) known attacks~~

Did the TLS designers get it right?

In last few years host of attacks that affect TLS 1.2 as well have been discovered

[Paterson, Ristenpart, Shrimpton 2011]

Lucky 13 attack [AlFardan, Paterson 2013]

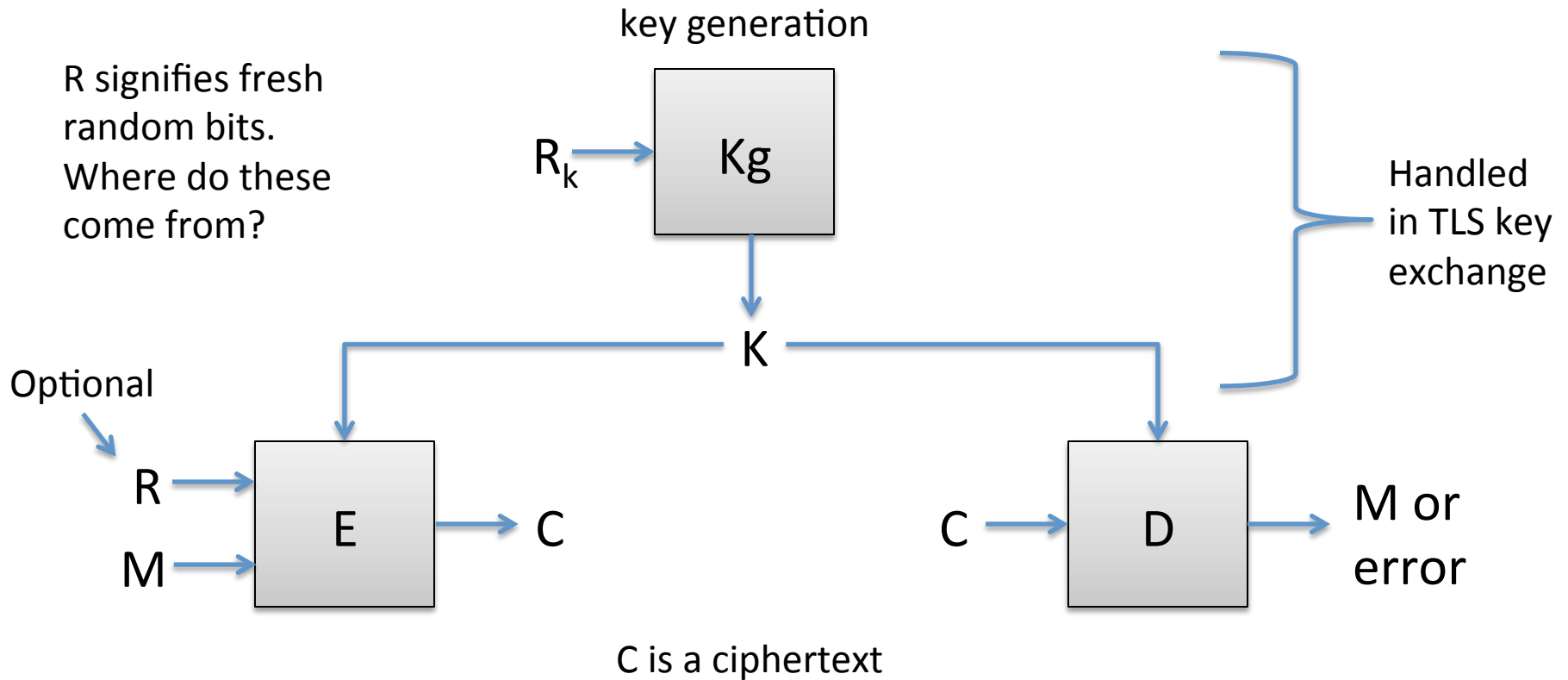
...

Even for “simple” applications (secure channels), secure cryptography is **really hard to design**. The problems are rarely in primitives.

Many other tools have similar story:

SSH, IPsec, Kerberos, WEP/WPA (WiFi security), GSM (cell phone networks), ...

# Symmetric encryption



Correctness:  $D(K, E(K, M, R)) = M$  with probability 1 over randomness used

Kerckhoffs' principle: what parts are public and which are secret?

# Some attack settings

- Unknown plaintext
  - attacker only sees ciphertexts
- Known plaintext
  - attacker knows some plaintext-ciphertext pairs
- Chosen plaintext
  - attacker can choose some plaintexts and receive encryptions of them





THE  
STRONG  
WIRING  
ENIGMA  
MACHINE

# Provable security cryptography

Supplement “design-**break**-redesign-**break**...” with a more **mathematical approach**

1. Design a cryptographic scheme
2. Provide **proof** that no one is able to break it



Shannon 1949

Formal definitions

Scheme semantics

Security

Security proofs

Show it is mathematically impossible to break security

# One-time pads

Fix some message length  $L$

$K_g$ : output random bit string  $K$  of length  $L$

$$E(K, M) = M \oplus K$$

$$D(K, C) = C \oplus K$$



# Shannon's security notion

Def. A symmetric encryption scheme is **perfectly secure** if for all messages  $M, M'$  and ciphertexts  $C$

$$\Pr[ E(K, M) = C ] = \Pr[ E(K, M') = C ]$$

where probabilities are over choice of  $K$

In words:

each message is equally likely to map to a given ciphertext

In other words:

seeing a ciphertext leaks nothing about what message was encrypted

Does a substitution cipher meet this definition?    No!

# Shannon's security notion

Def. A symmetric encryption scheme is **perfectly secure** if for all messages  $M, M'$  and ciphertexts  $C$

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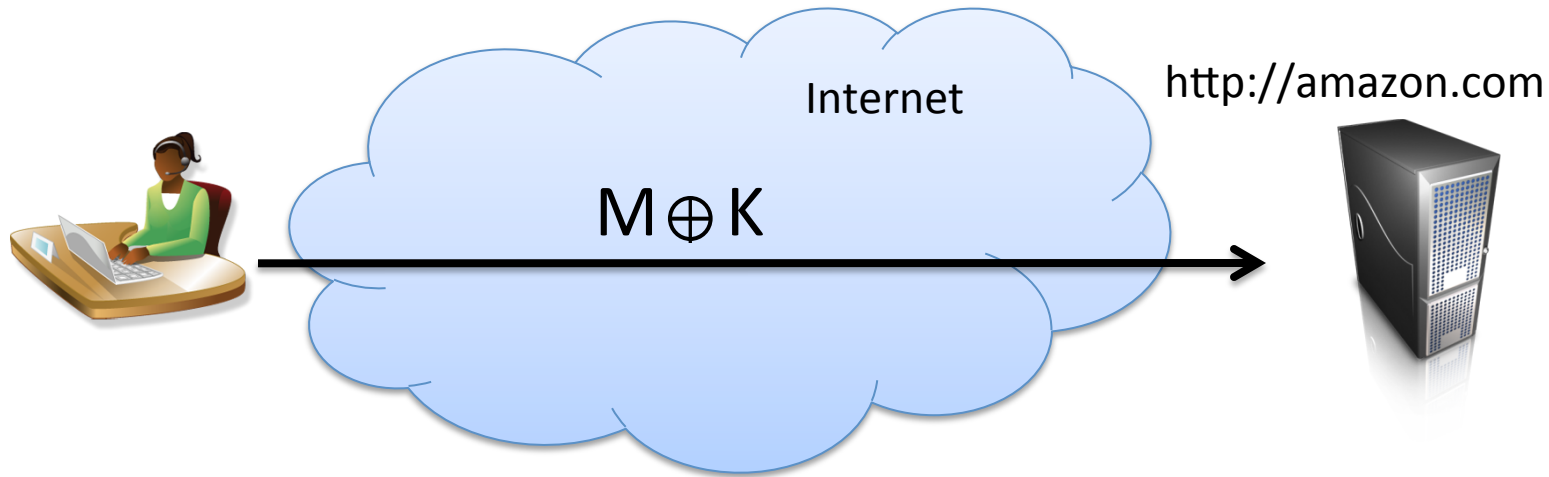
Thm. OTP is **perfectly secure**

For any  $C$  and  $M$  of length  $L$  bits

$$\Pr[ K \oplus M = C ] = 1 / 2^L$$

$$\Pr[ K \oplus M = C ] = \Pr[ K \oplus M' = C ]$$

## Back to our application



Does OTP provide a secure channel?

Integrity easily violated

Reuse of  $K$  for messages  $M, M'$  leaks  $M \oplus M'$

Encrypting same message twice under  $K$  leaks the message equality

$K$  must be as large as message

Message length revealed

# Cryptography as **computational science**

Use computational intractability as basis for confidence in systems

1. Design a cryptographic scheme
2. Provide **proof** that no attacker with limited computational resources can break it



Goldwasser, Micali and Blum circa 1980's

Formal definitions  
Scheme semantics  
Security

Security proofs (reductions)

Breaking scheme



Breaking assumptions

Example:

**Attacker can **not** recover credit card**



Can **not** factor large composite numbers

As long as assumptions hold we believe in security of scheme!

Provable security yields

- 1) **well-defined assumptions and security goals**
- 2) **attackers (cryptanalysts) can focus on assumptions**

But no one knows how to do this. It's been studied for a very long time!

# Typical assumptions

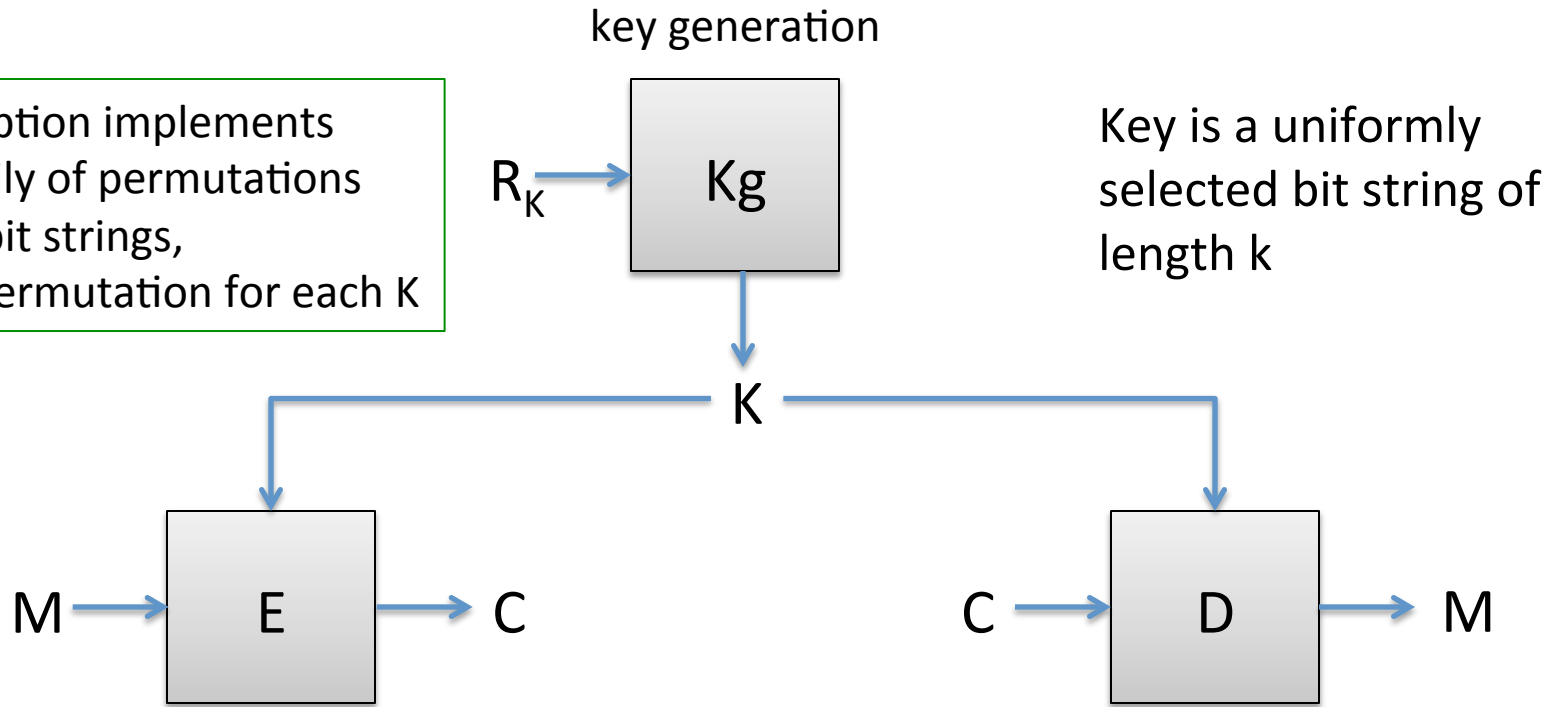
- Basic atomic primitives are hard to break:
  - Factoring of large composites intractable
  - RSA permutation hard-to-invert
  - Block ciphers (AES, DES) are good pseudorandom permutations (PRPs)
  - Hash functions are collision resistant

Confidence in atomic primitives is gained by cryptanalysis, public design competitions

SHA-3 competition, AES competition

# Block ciphers

Encryption implements a family of permutations on  $n$  bit strings, one permutation for each  $K$



$$E: \{0,1\}^k \times \{0,1\}^n \rightarrow \{0,1\}^n$$

# Data encryption standard (DES)

Originally called Lucifer

- team at IBM
- input from NSA
- standardized by NIST in 1976

$n = 64$

$k = 56$

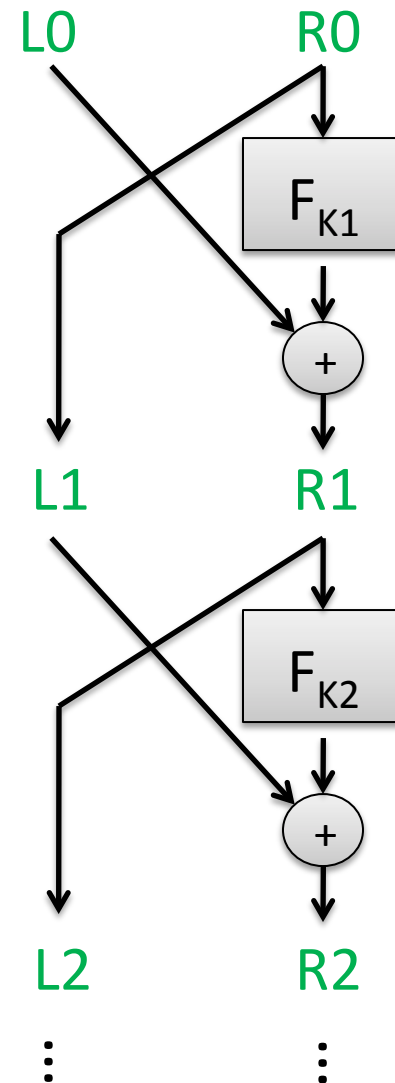
Number of keys:

72,057,594,037,927,936

Split 64-bit input into  $L_0, R_0$  of 32 bits each

Repeat Feistel round 16 times

Each round applies function  $F$  using separate round key



# Best attacks against DES

Attack	Attack type	Complexity	Year
Biham, Shamir	Chosen plaintexts, recovers key	$2^{47}$ plaintext, ciphertext pairs	1992
DESCHALL	Unknown plaintext, recovers key	$2^{56/4}$ DES computations 41 days	1997
EFF Deepcrack	Unknown plaintext, recovers key	~4.5 days	1998
Deepcrack + DESCHALL	Unknown plaintext, recovers key	22 hours	1999

- DES is still used in some places
- 3DES (use DES 3 times in a row with more keys) expands keyspace and still used widely in practice



# Advanced Encryption Standard (AES)

Response to 1999 attacks:

- NIST has design competition for new block cipher standard
- 5 year design competition
- 15 designs, Rijndael design chosen

# Advanced Encryption Standard (AES)

Rijndael (Rijmen and Daemen)

$n = 128$

$k = 128, 192, 256$

Number of keys for  $k=128$ :

340,282,366,920,938,463,374,607,431,768,211,456

Substitution-permutation design.

For  $k=128$  uses 10 rounds of:

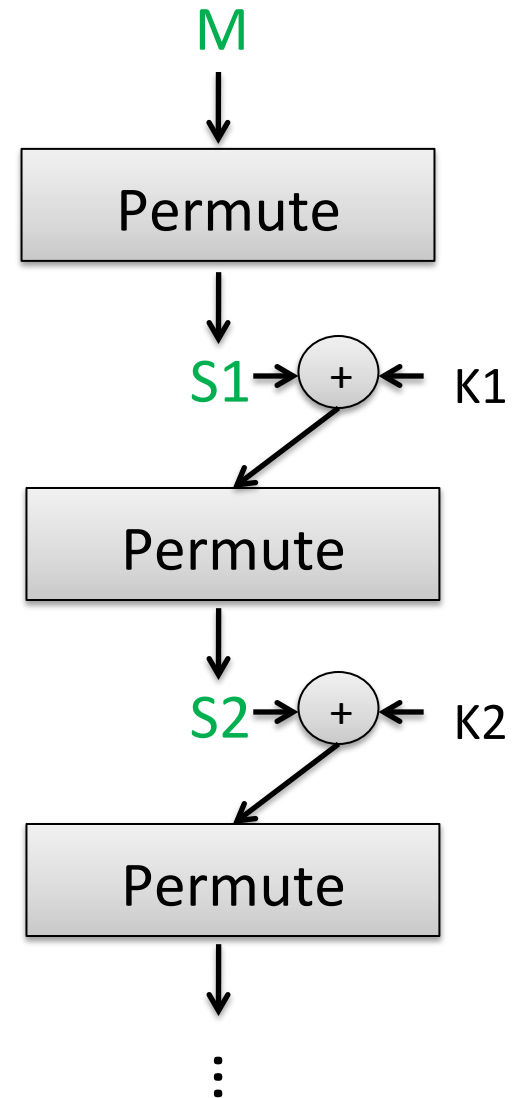
1) Permute:

SubBytes (non-linear S-boxes)

ShiftRows + MixCols (invertible linear transform)

2) XOR in a round key derived from  $K$

(Actually last round skips MixCols)



# Best attacks against AES

Attack	Attack type	Complexity	Year
Bogdanov, Khovratovich, Rechberger	chosen ciphertext, recovers key	$2^{126.1}$ time + some data overheads	2011

- Brute force requires time  $2^{128}$
- Approximately factor 4 speedup

# Summary and next time

- Crypto as computational science
- Overview of TLS
- Symmetric encryption and block ciphers introduced
- Next time:
  - Symmetric encryption from block ciphers
  - Need for active attack security