## CS/ECE 252: INTRODUCTION TO COMPUTER ENGINEERING

# UNIVERSITY OF WISCONSIN—MADISON 

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## Examination 1

In Class ( 50 minutes)
Monday, September 28, 2016
Weight: 17.5\%

NO: BOOK(S), NOTE(S), CALCULATORS OR ELECTRONIC DEVICES OF ANY SORT. The exam has nine pages. You must turn in the pages 1-8. Circle your final answers. Plan your time carefully since some problems are longer than others. Use the blank sides of the exam for scratch work.

LAST NAME: $\qquad$
FIRST NAME: $\qquad$
Section: $\qquad$
ID\#: $\qquad$

| Problem | Maximum Points | Points Earned |
| :---: | :---: | :---: |
| 1 | 1 |  |
| 2 | 3 |  |
| 3 | 2 |  |
| 4 | 2 |  |
| 5 | 4 |  |
| 6 | 4 |  |
| 7 | 6 |  |
| 8 | 4 |  |
| 9 | 4 |  |
| 10 | 3 |  |
| Total | 33 |  |

Which of the following statements are true?
i) There can be many different microarchitectures implementing a single ISA.
ii) In logic circuits, there is only one way to implement any particular function (e.g. addition).
iii) The translation from the unique assembly language of a computer to its ISA is done by an assembler.

Select one answer below:
a) i \& ii

## b) i \& iii

c) ii \& iii
d) i, ii \& iii

## Problem 2

Match the following computer abstraction layers with their definitions specified in the table.
a) ISA
b) Program
c) Algorithm
d) Microarchitecture
e) Devices

| D | A detailed organization of the implementation of an ISA. |
| :--- | :--- |
| E | Specific hardware technology used to implement logical components of the computer <br> system. (Ex. CMOS/NMOS transistors) |
| B | A 'mechanical language' that is used to specify a sequence of instructions to a computer. |
| A | The complete specification of the interface between programs that have been written and the <br> underlying computer hardware that must carry out the work of those programs. |
| C | A step by step procedure that is guaranteed to terminate, such that each step is precisely <br> stated and can be carried out by the computer |

(a) What is the difference between high level and low level languages?

High level languages are easier to comprehend and are machine independent.
(b) Why are natural languages unsuitable for programming on a computer?

## They are ambiguous and thus a computer cannot interpret them.

## Problem 4

(2 points)
A class has 269 students enrolled in it. Each student is to be assigned a unique ID number (in unsigned binary notation).
(a) What is the minimum number of bits needed to assign each student a unique binary ID number?

9
(b) If we were to increase the number of bits by 1 , how many more students can be accommodated in the class and still be assigned a unique binary ID number?

## Problem 5

(a) Using 8 bits for each number, write the 1's complement, 2's complement, and signed magnitude binary number of the decimal numbers in the table below:

| Decimal | 1's Complement | 2's Complement | Signed Magnitude |
| :--- | :--- | :--- | :--- |
| 21 | $\mathbf{0 0 0 1 0 1 0 1}$ | $\mathbf{0 0 0 1 0 1 0 1}$ | $\mathbf{0 0 0 1 0 1 0 1}$ |
| -12 | $\mathbf{1 1 1 1 0 0 1 1}$ | $\mathbf{1 1 1 1 0 1 0 0}$ | $\mathbf{1 0 0 0 1 1 0 0}$ |

(b) Why do computers more often use 2's complement representation over 1's complement representation?

There are two representations of 0 in 1's complement. Also 2's complement is easier for computers to perform arithmetic in.

## Problem 6

Convert the following 32-bit single-precision IEEE floating point number into decimal value. Show your work for full credit:

11000000110110000000000000000000
The bits for the IEEE single-precision floating point number ( N ) are allocated as follows:

| Sign (1 bit) | Exponent (8 bits) | Fraction (23 bits) |
| :--- | :--- | :--- |

Where the value $\mathbf{N}=(\mathbf{- 1})^{\text {Sign }} \mathbf{x}$ 1.Fraction $\times 2{ }^{\text {Exponent-127 }}$
-6.75

## Problem 7

Perform binary arithmetic for the following numbers as directed. All the numbers are represented in 2's complement form.
(a) Add the following 2's complement numbers. Write the final result as a 6-bit number.

010110
$\begin{array}{r}+\quad 1000 \\ \hline\end{array}$
001110

Did an overflow error occur in the previous addition? State how you know.

Overflow cannot occur when adding a positive number with a negative number.
(b) Subtract the following 2's complement numbers. Write the final result as a 6-bit number. 110011

- 110010 000001

Did an overflow error occur in the previous operation? State how you know.
Overflow cannot occur when subtracting a negative number from a negative number.
(c) Convert the answers for (a) and (b) into decimal numbers. Show your work for full credit.
$001110=14$
$000001=1$
(a) Convert the following 3 hexadecimal numbers to unsigned binary. A 0x before a set of symbols (from 0 to F ) indicates a hexadecimal number.

0x28
00101000

0xBA
10111010

0xE7
11100111
(b) Perform the specified logical operations on the following hexadecimal numbers. Write your result in unsigned binary. (Hint: first convert the hexadecimal to binary, which you did in part (a), and then perform the operations)

NOT(0x28 OR (0xBA AND 0xE7))

## 01010101

(c) Convert the result of part (b) into hexadecimal.

The ASCII table on the last page will be useful in solving this problem. You can detach it to make it easier to consult without flipping pages.

Consider two strings of two ASCII characters each: "54" and "\$@". The ASCII characters in the string are the two characters between the quotation marks, and there is no null character terminating the string.
(a) First, convert each of these two strings into their corresponding 16-bit binary values.

54: 0011010100110100
\$@: 0010010001000000
(b) Now, suppose that the two 16 -bit binary values were added as if they were signed integers in 2's complement, and the resulting 16 bits treated as if they were a string of ASCII characters. What would the resulting ASCII string be? Show your work for full credit.

## Sum: 0101100101110100

ASCII: Y+

## Problem 10

Give an example of an integer that can be represented in floating point format (32-bit IEEE format), but cannot be represented as a 32-bit 2's complement integer. Show its 32-bit IEEE format representation.

The biggest 2's complement integer that can be represented with 32 bits is $\mathbf{2 \wedge} \mathbf{3 1} \mathbf{- 1}$, so any integer number greater than $\mathbf{2}^{\wedge} 31-1$, but less than $2^{\wedge} 128$, is the answer to this question. so $\mathbf{2}^{\wedge} 31,2^{\wedge} 31+1,2^{\wedge} 31+2$ and $2^{\wedge} 32$ are some examples.

## Then convert it to IEEE.

ASCII Table

| Character | Hex | Character | Hex | Character | Hex | Character | Hex |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| nul | 00 | sp | 20 | @ | 40 | - | 60 |
| soh | 01 | ! | 21 | A | 41 | a | 61 |
| stx | 02 | * | 22 | B | 42 | b | 62 |
| etx | 03 | \# | 23 | C | 43 | c | 63 |
| eot | 04 | \$ | 24 | D | 44 | d | 64 |
| enq | 05 | \% | 25 | E | 45 | e | 65 |
| ack | 06 | \& | 26 | F | 46 | f | 66 |
| bel | 07 | - (Apostr.) | 27 | G | 47 | g | 67 |
| bs | 08 | ( | 28 | H | 48 | h | 68 |
| ht | 09 | ) | 29 | I | 49 | i | 69 |
| If | 0A | * | 2A | J | 4A | j | 6A |
| vt | 0B | + | 2B | K | 4B | k | 6B |
| ff | 0 C | , (Comma) | 2C | L | 4C | 1 | 6C |
| cr | 0 D | - | 2D | M | 4D | m | 6 D |
| so | OE | . (Period) | 2E | N | 4 E | n | 6 E |
| si | 0F | , | 2F | 0 | 4F | - | 6 F |
| dle | 10 | 0 | 30 | P | 50 | p | 70 |
| dc1 | 11 | 1 | 31 | Q | 51 | q | 71 |
| dc2 | 12 | 2 | 32 | R | 52 |  | 72 |
| dc3 | 13 | 3 | 33 | S | 53 | s | 73 |
| dc4 | 14 | 4 | 34 | T | 54 | t | 74 |
| nak | 15 | 5 | 35 | U | 55 | u | 75 |
| syn | 16 | 6 | 36 | V | 56 | v | 76 |
| etb | 17 | 7 | 37 | W | 57 | w | 77 |
| can | 18 | 8 | 38 | X | 58 | x | 78 |
| em | 19 | 9 | 39 | Y | 59 | y | 79 |
| sub | 1A | : | 3A | Z | 5A | z | 7 A |
| esc | 1B | ; | 3B | [ | 5B | \{ | 7 B |
| fs | 1 C | $<$ | 3 C | \} | 5 C | \| | 7 C |
| gs | 1D | $=$ | 3D | ] | 5D | \} | 7D |
| rs | 1 E | $>$ | 3 E | $\wedge$ | 5 E | $\sim$ | 7 E |
| us | 1 F | ? | 3F | _ (Undrscre) | 5F | del | 7F |

