

Recursive XML Schemas, Recursive XML Queries, and Relational Storage: XML-to-SQL Query Translation

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Abstract

We consider the problem of translating XML queries into SQL when XML documents have been stored in an RDBMS using a schema-based relational decomposition. Surprisingly, there is no published XML-to-SQL query translation algorithm for this scenario that handles recursive XML schemas. We present a generic algorithm to translate path expression queries into SQL in the presence of recursion in the schema and queries. This algorithm handles a general class of XML-to-Relational mappings, which includes all techniques proposed in literature. Some of the salient features of this algorithm are: (i) It translates a path expression query into a single SQL query, irrespective of how complex the XML schema is, (ii) It uses the “with” clause in SQL99 to handle recursive queries even over non-recursive schemas, (iii) It reconstructs recursive XML subtrees with a single SQL query and (iv) It shows that the support for linear recursion in SQL99 is sufficient for handling path expression queries over arbitrarily complex recursive XML schema.

1. Introduction

This paper is the first to present a generic algorithm that translates path expression queries to SQL in the presence of recursion in the schema in the context of *schema-based XML Storage* shredding of XML into relations. Here, we refer to path expression queries having the descendant axis (//) as recursive XML queries and to techniques that store XML data into an RDBMS based on an XML schema (or DTD) as *schema-based XML Storage* techniques.

The reader may justifiably be skeptical of this claim. After all, there have been many schema-based techniques proposed for shredding XML data into relations [3, 18, 20, 28]. There has also been a lot of work on schema-oblivious shredding of XML into relations [9, 15, 24], where the target relational schema is fixed oblivious to the XML schema.

Moreover, there has been a great deal of work on translating XML queries into SQL [4, 12, 16, 21, 25, 27] in the context of publishing existing relational data as XML (the “XML Publishing” scenario). It seems plausible that somewhere in all this work must lie the solution to the problem we claim to solve in this paper. Unfortunately, that is not the case — none of this previous work solves the query translation problem for schema-based shredding in the presence of recursion in the XML schema.

Firstly, while [20, 28] propose schema-based XML shredding methods applicable over recursive XML schemas, there has been no published work presenting algorithms for translating XML queries into SQL in this context. Secondly, while the schema-oblivious methods (for example, the Edge approach [15]) can handle recursive schemas and recursive queries with ease, the query translation algorithms for these approaches are not applicable in the context of schema-based shredding. Finally, in the “Publishing” domain the class of XML schemas that have been considered includes only (non-recursive) tree schemas.

At this point the reader may be wondering if this gap in the literature exists because the problem is not well motivated. We think that is not the case. In a recent study of real-world DTDs [6], out of the 60 DTDs analyzed, more than half (35) of them were recursive, which suggests that recursive XML schemas are common in practice. Furthermore, recursion is ubiquitous in XML queries, as it appears in any path expression that uses the descendant axis (//). Finally, there is a growing body of work suggesting that for many query workloads, schema-based shredding approaches yield far better performance than schema-oblivious shredding [29, 30].

We present a generic algorithm that translates path expression queries to SQL in the presence of recursion in the XML schema and queries in the context of schema-based shredding of the XML into relations. This algorithm always outputs an SQL query of size polynomial in size of the input XML-to-Relational mapping and the XML query. An interesting aspect of this is that we need the SQL99 *with*

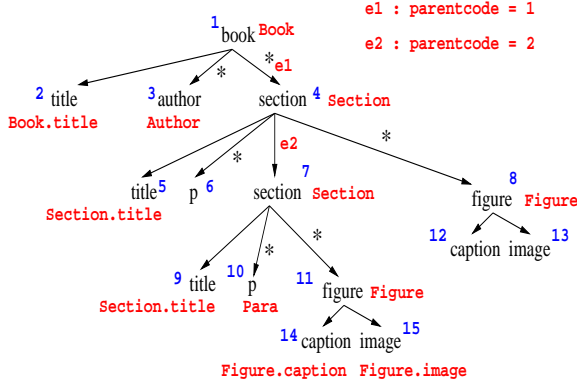


Figure 1. Sample XML-to-Relational mapping schema

construct to get this bound. This is not merely an artifact of our algorithm, as we show that if we restrict ourselves to only SPJU (select, project, join, union) relational queries, then no algorithm can give this polynomial size guarantee even for non-recursive schemas. We also show how the support for linear recursion in SQL99 is sufficient for translating a path expression query into a single SQL query for an arbitrary XML-to-Relational mapping. We also show how we can reconstruct recursive XML subtrees in a single SQL query.

The rest of the paper is organized as follows. We first describe the class of XML-to-Relational mappings considered in this paper in Section 2. We then present the algorithm to translate path expression queries into SQL in Section 3 when both the XML schema and query may be recursive. We then extend the algorithm to handle branching path expression queries and reconstruct XML subtrees in Section 4. We discuss related work in Section 5 and present our conclusions.

2. Formal Model

In order to express our translation techniques, we need a representation for XML to Relational mappings. Any reasonable representation would serve our purpose; for concreteness, in this section we present a formal way to represent XML to Relational mappings that covers all the lossless mapping techniques proposed in existing literature.

2.1. XML Schema Graph

An XML schema can be viewed as a directed graph $SG = (V, E)$, where V is the set of vertices and E is the set of edges. The vertices correspond to elements and attributes and the edges represent containment (parent-child)

relationships. The vertices are labeled with the name of the element or attribute. The edges have an additional multiplicity label that can take a value from $\{?, *, +, \epsilon\}$. A sample non-recursive schema graph is given in Figure 1. With each schema node, we associate an integer to identify the node. If the schema graph is a tree, then we call it a *Tree* schema graph. If it is acyclic, we call it a *DAG* schema graph (directed acyclic graph). Otherwise, it is a *recursive* schema graph.

2.2. XML to Relational Mappings

We represent the mapping between XML elements and relational columns through annotations on the schema graph. For example, one way of mapping the XML schema in Figure 1 into relations results in the following relational schema.

- **Book** (*id*, title, . . .)
- **Author** (*id*, parentid, . . .)
- **Section** (*id*, parentid, parentcode, title, . . .)
- **Para** (*id*, parentid, . . .)
- **Figure** (*id*, parentid, caption, image, . . .)

The annotations on the schema graph in Figure 1 correspond to this decomposition. Each non-leaf (internal) node in the schema is associated with a relation name (shown next to the node). Each leaf node is associated with a column name as well. The relational schema into which we shred the XML data is the set of relations that occur in the node annotations. Each relation has an *id* field, which is the primary key. In addition, *parentid* and *parentcode* fields are included as required to preserve document structure.

A node annotation for a leaf node n , $Annot(n)$, is of the form $R.C$, where R denotes a relation and C denotes a column in R . A node annotation for a non-leaf node n , $Annot(n)$, is of the form R indicating a relation name R . If a node n in the schema has multiple in-coming edges, then each of these edges is annotated with a condition of the form $parentcode = val$, indicating a code for the parent of an element matching n in the document. For a relational column $R.C$, we define $LeafNodes(R.C)$ to be the set of leaf schema nodes annotated with $R.C$.

We now discuss what properties we expect from an XML-to-Relational mapping.

- The decomposition algorithm that actually shreds the XML data into relations must respect the mapping.
- All the XML data must be completely shredded into relations and no part of the XML data must be stored multiple times.
- There must be no data in the relations other than that which is present in the XML document.

- Enough information must be maintained in the relational data to enable reconstruction of the original XML data.

Every lossless decomposition scheme we have encountered in the literature satisfies the above properties. We formalize these as follows.

With every path $p = \langle n_1, \dots, n_k \rangle$, we associate an SQL query, $SQL(p)$ as given in Figure 2. Intuitively, the SQL query retrieves from the relational shredding the information that appeared in portions of the original document that match the path p .

procedure SQL(path p)

begin

add $Annot(n_1)$ to the From clause

for (i from 2 to k) do

Let e be the edge from n_{i-1} to n_i

if ($Annot(n_i)$ is different from $Annot(n_{i-1})$) then

add $Annot(n_i)$ to the From clause

add $Annot(n_{i-1}).id = Annot(n_i).parentid$
to the Where clause

else if ($Annot(e)$ is of the form $parentcode = val$) then

add $Annot(n_i)$ to the From clause

if ($Annot(e)$ is of the form $C = val$) then

/* C may be parentcode */

Let the last relation added to the From clause be R

add $R.C = val$ to the Where clause

Add $Annot(n_k) = R.C$ to the Select clause

/* if there are multiple instances of the relation R ,

use the last instance */

end

Figure 2. Query associated with a path p

With a leaf (schema) node l , we associate a root-to-leaf SQL query, $RtoL(l)$ as follows. Let the root-to-leaf paths to l be p_1, \dots, p_m . Then, $RtoL(l) = \cup_{i=1}^m SQL(p_i)$. The union operation here preserves duplicates. If the mapping schema is recursive, the number of root-to-leaf paths will be infinite for certain leaf nodes and the $RtoL$ query for such nodes is the union of infinitely many queries.

For example, for the schema in Figure 1, $RtoL(9)$ is given below.

```
select S2.title
from   Book B, Section S1, Section S2
where  B.id = S1.parentid and S1.parentcode = 1
       and S1.id = S2.parentid and S2.parentcode = 2
```

Again, intuitively, $RtoL(l)$ retrieves from the relations the information that would be found in the original XML document by starting at the route and traversing all paths that match l . If the XML-to-Relational mapping satisfies the properties mentioned above, then the following properties also hold.

1. For each root-to-leaf path p , $SQL(p)$ returns the values of all elements that satisfy p . This is under multiset semantics.
2. For each leaf node l in the schema, $RtoL(l)$ returns the values of all elements (attributes) associated with l . This is under multiset semantics.
3. For every relational column $R.C$ with $LeafNodes(R.C) \neq \phi$, let Q be the SQL query: “select $R.C$ from R ”. Then,

$$Q = \bigcup_{l \in LeafNodes(R.C)} RtoL(l)$$

4. Consider edge $e = \langle n_i, n_j \rangle$ where $Annot(n_i) = R_i$ and $Annot(n_j) = R_j$ or $R_j.C$. If $R_i \neq R_j$, then e must be annotated with the condition $parentcode = i$.

The final condition ensures that if a relation R_j “points to” more than one relation, then by examining the parent code, we can find out which relation is being pointed to by a given tuple. This information is needed to reconstruct the original XML data. We note here that if R_j points to only one relation in the entire mapping, then this annotation can be omitted.

We refer to the annotated schema graph illustrating the XML-to-Relational mapping as the *mapping schema graph*. Any mapping schema graph that satisfies the above mentioned properties is a *valid* mapping schema.

In general, we allow two additional features in the mapping: selection conditions as edge annotations and presence of dummy nodes. Any edge e from n_1 to n_2 may have an optional annotation of the form $C = val$, where C is a column in the relation $Annot(n_1)$. In XML documents, certain elements may be introduced just to group elements that appear beneath them. We refer to such schema nodes as *dummy* nodes. For example, we could have a dummy **Sections** node in-between nodes 1 and 4 to group together all the sections in a book. An algorithm that shreds this document into relations need not take any action on finding a dummy node. We can detect that a shredding algorithm has considered a node n to be a dummy node by the fact that (1) n is a non-leaf node, (2) n is annotated with the same relation as its parent, (3) each in-coming edge is labeled ϵ and, (4) each in-coming edge has a null annotation. For ease of exposition, we assume that any non-leaf node that is not a dummy node has an **elemid** attribute that uniquely identifies an element within an XML document.

2.2.1. Path Expression Queries

A simple path expression (SPE) can be denoted as “ $s_1 l_1 s_2 l_2 \dots s_k l_k$,” where each of the l_i is a tag name and each of the s_i is either $/$ (denoting a parent-child traversal) or $//$ (denoting an ancestor-descendant traversal). Each $s_i l_i$

pair is a navigation step of the path expression and k is the number of steps in the query.

A generalized simple path expression (GSPE) can be denoted as “ $p_1 p_2 \dots p_k$ ” where each p_i is of the form $p_i^1 | p_i^2 \dots | p_i^{k_i}$ ($k_i \geq 1$). Here, each p_i^j is a simple path expression. Each p_i thus denotes a disjunction of simple path expressions. Also, the special tag name ‘*’ matches any tag name in a GSPE query.

The result of a generalized path expression is the *set* of all nodes that match the path expression query. This is similar to XPath semantics, where the result is an ordered list of matching nodes. We assume an unordered data model in this paper and discuss how our algorithm can be modified to work in an ordered model in Section 4.3. There are two possible ways to return the set of matching nodes:

- **Select** mode: For leaf nodes, this corresponds to returning the values of the elements. For non-leaf nodes, we return the value of the corresponding `elemid` attributes.
- **Reconstruct** mode: For leaf nodes, this corresponds to returning the values of the elements. For non-leaf nodes, we reconstruct the subtree rooted at the element.

3. Query Translation Over Recursive XML schemas

In this section, we present an XML-to-SQL query translation algorithm over recursive mapping schemas for the class of generalized simple path expression (GSPE) queries defined in Section 2.2.1. We will assume the **Select** mode in this section and present our solution for the **Reconstruct** mode in Section 4.2.

Evaluating a path expression query over an XML-to-Relational mapping can be viewed as a two stage process: (i) use the XML query to identify the paths in the XML schema graph that satisfy the query, and (ii) use the annotations from the XML-to-Relational mapping to construct an equivalent relational query. We refer to these stages as the *PathId* and *SQLGen* stages respectively. We explain the two stages in the next two subsections.

3.1. PathId stage

In the *PathId* stage, we execute the GSPE query $Q = p_1 \dots p_k$ on a schema graph and identify the satisfying paths in the schema graph. Since the mapping schema may be recursive, the number of paths may be infinite, so we cannot enumerate all the possible matching paths. Even when the mapping schema is non-recursive, for DAG schema graphs, it is possible for the number of matching paths to be exponential in the size of the mapping schema and the query.

So, we should not attempt to enumerate all complete paths. Instead, just like the DAG schema graph represents shared information across multiple paths in a compact fashion, we represent the matching paths as a graph. This will allow us to handle recursive and non-recursive mapping schemas in a unified fashion. As an added benefit, we shall see later how preserving the relationship across multiple paths that existed in the original mapping schema will help us in the *SQLGen* stage.

Consider the evaluation of a query Q over a mapping schema S . We treat the mapping schema as an automaton A_S and the query as an automaton A_Q . We construct the cross-product automaton A_{SQ} from A_S and A_Q . We eliminate all the dead-states in A_{SQ} and the resulting automaton has all the matching paths in it. This approach is similar to the one proposed in [14] for evaluating regular path queries over graph schemas. We illustrate the main idea with an example and explain the parts where our algorithm differs from the one in [14]. The reader is referred to [14] for more details.

Consider the schema S given in Figure 3, which is a part of the schema in Figure 1. The corresponding automaton A_S is shown next to it. Similarly, the query $Q = /book/section/title$ is translated into the automaton A_Q , where state 3 corresponding to the `title` element in Q is the accepting state. We construct the cross-product automaton A_{SQ} and remove the dead states. The resulting automaton A_{SQ} is shown in the figure. A state with number (i, j) in A_{SQ} represents a combination of state i in A_S with state j in A_Q . Since state 3 in A_Q is an accepting state, all states with state number $(i, 3)$ are accepting states in A_{SQ} (in this case just $(5, 3)$). Notice how A_{SQ} has simulated the query over the mapping schema and identified the single matching path. The state numbers in A_{SQ} illustrate exactly how each path matched the query. In general, A_S and A_Q are non-deterministic, and as a result A_{SQ} is also a non-deterministic automaton. This cross-product automaton can then be viewed as a mapping schema S_{SQ} . The node (edge) annotations for S_{SQ} are the same as the underlying annotations in S .

The *PathId* stage for the query $Q_1 = /book/section//title$ is also shown in the figure. Notice how the `//` operation in the query translates into a self-loop on node 2 in A_{Q_1} . Also, there are two matching paths in the schema for this query. So, there are two root-to-leaf paths in the cross-product automaton A_{SQ_1} .

For purposes of exposition, we assume that all accepting states in S_{SQ} correspond to a leaf node in the original schema. If an accepting state $s \in S_{SQ}$ corresponds to a non-leaf node $n \in S$, we add the state corresponding to the `elemid` child of n as a final state in S_{SQ} (instead of s). Informally, this corresponds to returning the `elemid`’s of non-leaf nodes as the result of the query. This corresponds to the

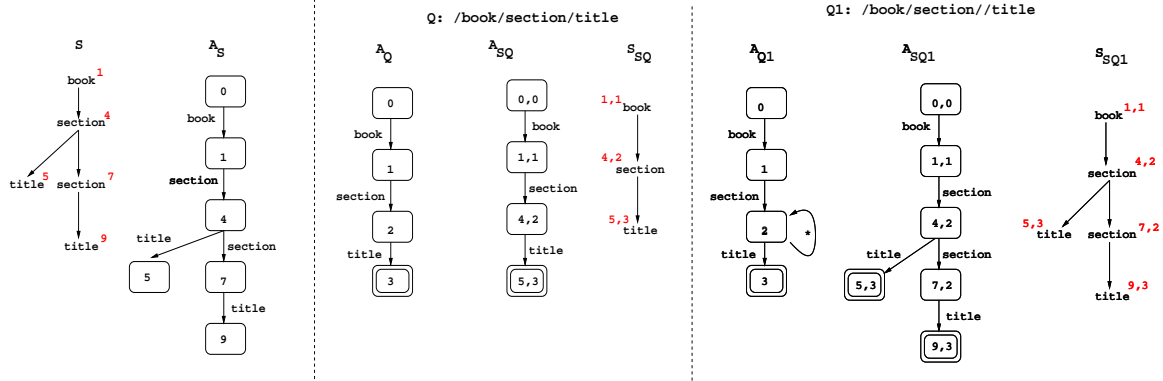


Figure 3. Example to illustrate *PathId*

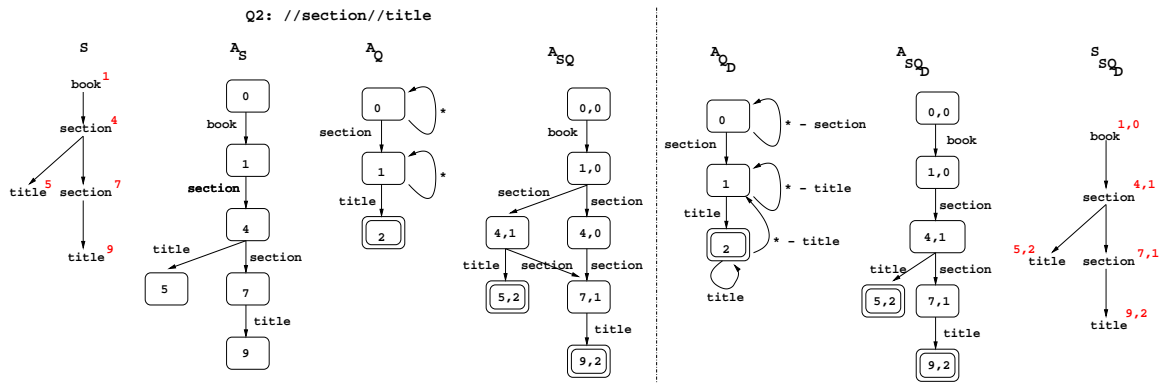


Figure 4. Example to illustrate duplicate counting in *PathId*

Select mode described in Section 2.2.1. We will present our solution for the **Reconstruct** mode in Section 4.2.

3.1.1. Handling XPath semantics

According to XPath semantics, the result of a path expression query is a duplicate-eliminated sequence of nodes. So, even if an element has multiple derivations with respect to the query, it should appear in the query result only once. For example, consider the evaluation of query $Q_2 = //section//title$. The cross-product automaton A_{SQ} for this query is given in Figure 4. Notice how there are two matching paths in A_{SQ} for the **title** node under the second-level section (node 9). This is due to the fact that either of the **section** nodes in S (4 or 7), can match the $//section$ part of Q_1 . For both the cases, the $//title$ part of the query is matched by the **title** node (node 9) in S . As a result, the $/section/section/title$ path in the schema is replicated twice in A_{SQ} . So, if we construct a SQL query based on this cross-product automaton, we may get duplicate results. But, according to XPath semantics, we should return each satisfying element exactly once. In this section, we explain our approach to handling this issue.

We first examine what the primary reason for the presence of duplicate paths in A_{SQ} is and how we can avoid it. Going back to the above example, we see that the two paths for $book/section/section/title$ have the following property: the first component of the nodes occurring in the two paths are identical, while the second component differs in (at least) one place. In other words, a single path in the schema gets duplicated, once with each of the two different derivations for the query. So, if the query automaton is a DFA, then the cross-product automaton will not have any schema path duplicated.

For an SPE query with k steps, we have an algorithm to construct an equivalent DFA with $k + 1$ states. We explain this algorithm using the query Q_2 . The resulting deterministic automaton A_{QD} is shown in Figure 4. We partition the query into blocks such that each block has a leading $//$ and there is no occurrence of $//$ in that block. In this case, there are two blocks, one each for $//section$ and $//title$. Then, we process these blocks from left to right. For the first block $//section$, we create a start state (state 0) and add a transition to state 1 on the label **section**. For any other label, since there is a leading $//$, we add a transition into state 0

procedure *PathId*(Q, S)

begin

1. Let A_S be the automaton corresponding to S
2. If (Q is an SPE query) then
3. Let A_{Q_D} be the DFA corresponding to Q
4. return the cross-product automaton A_{SQ_D}
5. Else // Q is a GSPE query
6. Let A_Q be the NFA corresponding to Q
7. Let A_Q^2 be the automaton that accepts all strings with two or more accepting paths in A_Q
8. Compute the cross-product automaton A_{SQ^2}
9. If (A_{SQ^2} is empty) then
10. return the cross-product automaton A_{SQ}
11. Else
12. Convert A_Q into a DFA A_{Q_D}
13. If (A_{Q_D} does not have an exponential increase in size)
14. return the cross-product automaton A_{SQ_D}
15. Else
16. return the cross-product automaton A_{SQ}
17. // a *distinct* clause needs to be added in this case
18. // to the final SQL query

end

Figure 5. *PathId* stage

itself (the start state of the current block). In general, when there are multiple steps in a block, there may be a partial match with the current string and we may have to transition not to the start state but to some intermediate state. This can be found by identifying the longest suffix that matches the current set of labels and is similar to the Knuth-Morris-Pratt string matching algorithm [7]. State 1 is the final state for this block and will act as the start state for the next block. We repeat the process for //title and add state 2 and a transition from 1 to 2 on title. We also add transitions on other labels for state 1. Since this is the last block, we also compute the transitions from state 2 and set state 2 as the final state for A_{Q_D} . The general algorithm is omitted for want of space.

LEMMA 1 *For an SPE query Q having k steps, the equivalent DFA having $k + 1$ states can be computed in $O(k^2)$ time.*

On the other hand, for GSPE queries, there are scenarios when the smallest equivalent DFA is exponential in the size of the query. In this case, we use the following approach. Let A_Q denote the NFA corresponding to the query Q . We first compute an NFA A_Q^2 that accepts all input strings that have two or more accepting paths in A_Q . Then, we compute the cross-product automaton A_{SQ^2} between A_S and A_Q^2 . If this automaton is empty, then it means that the cross-product automaton A_{SQ} obtained from the original query and schema automata (A_Q and A_S respectively) will not have any duplicate schema paths and we use A_{SQ} as the output of the *PathId* stage. On the other hand, if A_{SQ^2}

is not empty, then we have two options: (1) convert A_Q into a DFA A_{Q_D} and compute cross-product between A_S and A_{Q_D} or (2) apply a *distinct* clause for the query obtained from A_{SQ} . We choose one of these options based on whether there is a size explosion when we convert A_Q into a DFA¹.

The *PathId* algorithm along with the above modifications to handle the semantics of XPath is given in Figure 5.

3.1.2. Analysis of *PathId* stage

In this section, we present an analysis of the number of states in the resulting cross-product automaton and the running time of the above algorithm. We omit the proofs due to lack of space.

Let s and e be the number of nodes in the schema and k be the number of steps in the query. Then the number of states in A_S is $n_s = s + 1$ and the number of states in A_Q is $n_q = k + 1$. For an SPE query, the number of states in $A_{Q_D} = k + 1$.

LEMMA 2 *The number of states in the cross-product automaton A_{SQ} is no greater than $n_s * n_q$.*

LEMMA 3 *If S is a Tree schema and Q is an SPE query, then the number of states in A_{SQ_D} is no greater than n_s .*

For an SPE query Q , for every label x , let $\text{ChildOccur}(x, Q)$ denote the number of occurrences of the pattern $/x$ in Q . For example, for the query $Q = /section//section//title$, $\text{ChildOccur}(\text{section}, Q) = 1$ and $\text{ChildOccur}(\text{title}, Q) = 0$. Let $\text{MaxChildOccur}(Q)$ denote the maximum across all values for $\text{ChildOccur}(x, Q)$ over all labels. In this case, $\text{MaxChildOccur}(Q) = 1$.

Let $\text{DescendantSteps}(Q)$ denote the number of // steps in Q . For the above example, $\text{DescendantSteps}(Q) = 2$. Notice how $\text{DescendantSteps}(Q) + \text{MaxChildOccur}(Q) \leq n_q$

LEMMA 4 *For an SPE query Q , the number of states in the cross-product automaton A_{SQ_D} is no greater than $n_s * (\text{DescendantSteps}(Q) + \text{MaxChildOccur}(Q))$.*

Let us now consider the running time of the various steps in the *PathId* stage.

From Lemma 1, we see that the DFA corresponding to a query Q can be computed in time $O(n_q^2)$.

LEMMA 5 *The cross-product automaton of two state machines with n_1 and n_2 states respectively can be computed in $O(n_1^2 * n_2^2)$.*

LEMMA 6 *For a query Q , the automaton A_Q^2 can be computed in $O(n_q^4)$.*

¹This can be achieved by placing a bound on the number of states explored in the NFA-to-DFA conversion

procedure $SQLGen(S_{SQ})$

begin

1. Identify strongly connected components (SCCs) in S_{SQ}
2. Let C be the set of SCCs
3. Merge adjacent components in C that are acyclic
if one of them dominates the other
4. foreach ($c \in C$ in top-down topological order) do
5. if (c is not recursive) then
6. generate the query for c using $SQLForDAG(c)$
7. else
8. generate the query for c using $SQLForRecursive(c)$
// a relational query $T(n)$ is associated with
// each leaf node n now
- endFor
9. Let finalQ be \cup_n is a leaf node "select * from $T(n)$ "
10. If (duplicate elimination is required) then
11. Output the query "select distinct(*) from finalQ"
12. else output the query "select * from finalQ"

end

Figure 6. $SQLGen$ Algorithm for recursive mapping schemas

THEOREM 1 *The running time of the PathId stage for an SPE query is $O(n_s^2 * n_q^2)$, while for a GSPE query, the running time is $O(n_s^2 * n_q^4)$.*

3.2. $SQLGen$ stage

Once we have identified all matching paths in the schema S corresponding to query Q , we have a cross-product schema S_{SQ} with all the matching paths encoded in it. Informally, the union of all root-to-leaf paths in S_{SQ} corresponds to the query result. A simple algorithm to generate an SQL query corresponding to Q is to return $RQ = \bigcup RtoL(l)$ over all leaf nodes in S_{SQ} . While this is a good algorithm when S_{SQ} is a tree, it does not suffice when S_{SQ} is a DAG or is recursive. If S_{SQ} is a DAG, then the number of matching paths may be exponential. Moreover, by unfolding a DAG we may also be missing shared computation in the form of common subexpressions in the final SQL query. So, we need to somehow reflect the DAG structure of S_{SQ} in the SQL query. Similarly, if S_{SQ} is recursive, then RQ is the union of infinite queries. In this section, we show how using the support for linear recursion in SQL99 (with operator) along with the *outer union* approach, we can construct the equivalent (finite!) SQL query for a recursive cross-product schema.

In order to illustrate our algorithm for handling complex cross-product schema, we use the schema graph S in Figure 7. Notice how this schema has a DAG part and a recursive part. The edge annotations are omitted for clarity. We use the shorthand i to denote the schema node corresponding to element Ei and refer to the `elemid` node as node 11.

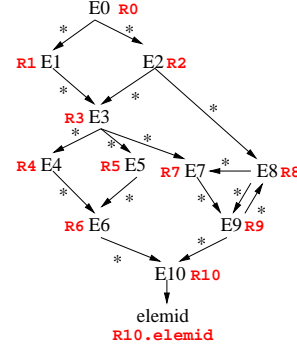


Figure 7. Sample recursive schema

We explain the algorithm by running through the evaluation of the query $Q = /E0//E10$ on the schema graph S in Figure 7. The *PathId* stage will result in a cross-product schema S_{SQ} identical to S . Notice how since $E10$ is a leaf node, we add the `elemid` attribute node to S_{SQ} and make that the accepting state.

The outline of the algorithm is given in Figure 6. We first identify the components in S_{SQ} that are recursive. The rest of the nodes are grouped into a set of non-recursive components. We perform this computation by first identifying the strongly connected components in S_{SQ} (step 1) and then merging adjacent non-recursive components wherever possible (step 3). Recall that a component c_1 dominates component c_2 if every path from the root to a node in c_2 passes through some node in c_1 . After the first 3 steps in Figure 6, there are three components in C . They are $c_1 = \{0, 1, 2, 3, 4, 5, 6\}$, $c_2 = \{7, 8, 9\}$ and $c_3 = \{10, 11\}$ (Here node 11 refers to the `elemid` node). We then process these components in top-down topological order, namely c_1 followed by c_2 followed by c_3 . For each component, we generate the appropriate relational queries. In the process, we associate a temporary relation $T(n)$ with every schema node n that is either a leaf node or has a child node in a different component. Once we have processed all components, we generate the final relational query in steps 10-12 using the temporary relations defined earlier.

The algorithm for generating SQL queries corresponding to a non-recursive and a recursive component are given in Figures 8 and 9 respectively. We discuss these in the next two subsections.

3.2.1. Handling a non-recursive component

For non-recursive components, a straightforward approach is to translate each path in the DAG component into a SQL query and take the union of all these queries. However, the number of paths can be exponential in the size of the component. The question arises whether there is any way in

procedure SQLFromDAG(c)**begin**

1. Let N be the set of nodes in c with either a parent or a child in a different component
2. Add any node in c to N if it corresponds to a leaf node in S .
3. Add all nodes in c with $>$ one in-coming edge to N
4. Add all nodes in c with $>$ one out-going edge to N
5. With each node $n \in N$, associate a unique temporary relation $T(n)$
6. foreach ($n \in N$ in top-down topological order) do
7. //generate SQL fragment to populate $T(n)$
8. foreach (in-coming edge e into n) do
9. Backtrack along e till either a node $m \in N$ or a node $m \notin c$ is obtained.
10. Let the unique m to n path be p
11. Generate $SQL(p)$ using $T(m)$ as the relation corresponding to m
12. //Other node and edge annotations in S_{SQ} are //same as underlying ones in the mapping S
13. Call this query $SQL(e)$
14. $T(n)$ is defined as the union of all the $SQL(e)$
15. endFor

end**Figure 8.** *SQLGen* Algorithm for DAG component

which we can at least guarantee a query that is polynomial in the size of the DAG component. We show that this is impossible if we only consider relational queries involving the select, project, join and union operations (SPJU queries). We formalize this claim as follows. Let C_1 denote the class of relational queries whose relational algebra expression has the select, project, join and union operators. Let the size of a query $SQ \in C_1$, $RelInst(SQ)$, be the number of relation instances in the relational algebra expression. Then we have the following result.

THEOREM 2 *There is a family of mapping schemas SG such that, for each schema $S_i \in SG$, there is a simple path expression query p_i that has the following property. No relational query $SQ \in C_1$, whose size is polynomial in the size of S_i and p_i , is a correct translation for p_i .*

The proof for the above theorem is based on the fact that there are instances of acyclic Deterministic Finite Automata (DFA) whose minimum equivalent regular expression is of length $O(n^{lg n})$ [11].

It turns out that we can use the *with* clause to solve this problem. Even though the *with* clause was primarily introduced for supporting recursive queries, it also provides us with a mechanism for creating temporary relations in a SQL query. So, whenever there is some computation that can be shared by multiple paths, we create a temporary relation corresponding to this shared computation, which can

be used repeatedly in the rest of the query. Notice how creating temporary relations in the query allows us to reduce the size of the generated SQL query from (potentially) exponential in the size of the component to a guaranteed polynomial bound.

Component c_1 is non-recursive and an example of a DAG component. We use the algorithm for generating the relational query corresponding to a DAG component given in Figure 8. We associate temporary relations with any node that is either a leaf node (part of the final query result), has a parent or child in a different component, or represents shared computation (multiple incoming/outgoing edges). For component c_1 , the set N is $N = \{2, 3, 6\}$. So, we generate SQL *with* clauses for three temporary relations corresponding to $T(2)$, $T(3)$ and $T(6)$ in that order. The query corresponding to $T(3)$ is given below.

```
with T3 as (
  select R3.*
  from R0, R1, R3
  where R0.id = R1.parentid and
        R1.id=R3.parentid and R3.parentcode=1
  union all
  select R3.*
  from T2, R3
  where T2.id=R3.parentid and R3.parentcode=2
)
```

Notice how the query is the union of two subqueries, one corresponding to each in-coming edge into node 3. Also note how we use $T2$ in the definition of $T3$, as node $2 \in N$ and has a temporary relation associated with it. In a similar fashion, the query for $T6$ will have $T3$ in it. This illustrates how shared computation can be efficiently reflected in the relational query. We would like to point out that the use of the *with* clause has two benefits. Firstly, it avoids the potential size blowup for complex DAG schema. Secondly, it represents the shared computation across different root-to-leaf paths explicitly. The relational optimizer can choose from the two options of either sharing computation across different fragments in the final execution plan or unfolding the *with* clause into the union of several conjunctive queries. In fact, we know of one commercial RDBMS whose optimizer does this exploration. On the other hand, if we did not use the *with* clause in the SQL query, then the relational optimizer has the additional task of finding common subexpressions, which is known to be a difficult task.

3.2.2. Handling a recursive component

Let us now look at how to generate the relational query for a recursive component. This algorithm is given in Figure 9. For each recursive component c , we associate a temporary relation T_R whose schema is the outer-union of the schemas of relations annotating some node in T_R and generate a recursive query for T_R as follows. A recursive query has two

procedure SQLFromRecursive(*c*)**begin**

1. Let T_R be a temporary relation whose schema is the outer union of all relations in c
//Construct the initialization query for T_R
2. foreach (in-coming edge e into c from node $n \notin c$) do
3. Let $n' \in c$ be the target of e
4. Let Q_e be the query:
select $R2.*, id(n)$
from $T(n) R1, Annot(n') R2$
where $Annot(e)$ and $R2.parentid = R1.id$ "
5. Null pad Q_e appropriately to reflect outer-union schema
6. Let Q_{init} be $\cup Q_e$ over all in-coming edges e
//Construct the recursive part for T_R
7. foreach (edge e with both end-points in c) do
8. Let e be from n_1 to n_2
9. if (e corresponds to a join edge) then
10. Let Q_e be the query:
select $R2.*, id(n_2)$
from $T_R R1, Annot(n_2) R2$
where $R1.schemanode = id(n_1)$ and
 $R2.parentid = R1.id$ and $Annot(e)$
11. else
// e corresponds to a selection or n_2 is a dummy node
12. Let Q_e be the query:
select $R1.*, id(n_2)$
from $T_R R1$
where $R1.schemanode = id(n_1)$ and $Annot(e)$
13. Null pad Q_e appropriately
14. Let Q_{rec} be $\cup Q_e$ where the union is taken over edges e with both end-points in c
15. T_R is a recursive query defined with Q_{init} as the initialization condition and Q_{rec} as the recursive component
16. With each node $n \in c$ we associate the query $T(n)$:
select * from T_R where $schemanode = id(n)$

end**Figure 9. SQLGen Algorithm for recursive component**

parts, an initialization part and a recursive part. The initialization part for the query defining T_R (steps 2-6) captures all incoming edges into c from a different component. For the component c_2 , there are two such edges (2, 8) and (3, 7) and the initialization part will be the union of two conjunctive queries, one for each incoming edge. The recursion in the component c is captured by the recursive part of the definition of T_R . Each edge in c is translated into a query as shown in steps 8-13 and the recursive part of the query defining T_R is the union across all edges within the component. For the component c_2 , there are four edges and so the recursive query Q_{rec} is the union of four recursive queries. In this case, all four edges are join edges. For example, the edge (8, 7) will translate to the following query:

```
select R7.*, id(7)
from TR, R7
where R7.parentid=TR.id and TR.schemanode=id(8)
and R7.parentcode=8
```

Notice how the condition $TR.schemanode$ ensures that the parent tuple corresponds to schema node 8 and the other conditions capture the annotations on the edge. By projecting the id of the child node, we ensure that the queries for outgoing edges from node 7 can be correctly constructed.

Returning to the example query, finally, component c_3 is non-recursive and we generate the equivalent relational query using the algorithm in Figure 8.

If S_{SQ} has two root-to-leaf paths matching the same path in S , then duplicate elimination is required and we add the distinct clause (recall discussion in previous section, step 16 in Figure 5). In such a scenario, for each leaf node $n \in S_{SQ}$, the id of n and the key column of R , where $Annot(n) = R.C$ also have to be projected along with $Annot(n)$ while creating the temporary relations $T(n)$.

For a recursive component C , let N_C denote the number of columns in the outer union schema for C . This is the sum of the number of columns over all relations annotating some node in C . For a mapping schema S , let $N_C^{max}(S)$ denote the maximum across all values for N_C over all recursive components in S .

THEOREM 3 For a mapping schema S and query Q , let the output of the PathId stage, A_{SQ} have V nodes and E edges. The equivalent SQL query can be obtained using the SQL-Gen algorithm in $O((V + E) * N_C^{max}(A_{SQ}))$ time.

The proof is omitted due to lack of space.

3.3. Preliminary Evaluation of Running Time

We implemented the above algorithm for evaluating SPE queries over a generic XML-to-Relational mapping. Using the XMark benchmark schema [31] and SPE query fragments that appear in the associated query test suite, we evaluated the equivalent SQL queries using the above query translation algorithm. The XML-SQL query translation process took less than 6ms for each SPE query. The XML-to-Relational mapping schema has 101 nodes. We also observed that in all cases, the size of the cross-product schema was less than 100 nodes (the size of the schema).

In order to test the running time of the algorithm under extreme scenarios, when the cross-product schema may have $n_s * n_q$ states, we used a more complex XML schema. This mapping schema was a *complete* graph of n nodes and all transitions were on a single label x . We then measured the running time of the query translation for the query $//x//x//x//x//x$, which has 5 steps. The cross-product automaton has approximately $4n$ states and $4n^2$ transitions.

Table 1. Execution time of translation algorithm

Clique size (n)	Time Taken (ms)
5	6
10	19
20	80

The running time for different values of n are given in Table 1.

Notice how while the running time shows a quadratic growth due to the quadratic increase in the number of transitions in the schema, it is still small for reasonable clique sizes. The size of every recursive component that we have seen in real-world DTDs has been less than 10. So we believe that the running time of our translation algorithm will be small in practice.

4. Extensions to more complex path expressions

In this section, we briefly describe our approach to handle branching path expression queries and reconstruct XML subtrees.

4.1. Branching path expression queries

Let us first consider the class of branching path expression (BPE) queries that have a single predicate at the end of the path expression. These queries are of the form $p_1[p_2]$ or $p_1[p_2 \text{ op value}]$, where p_1 and p_2 are GSPE queries.

The *PathId* stage works as follows. First, we compute the set of all satisfying paths for the GSPE query p_1 . Let A_{SQ} be the resulting cross-product automaton and let F be the set of final states. For each $f \in F$, we compute an auxiliary automaton, $A_{\text{pred}}(f)$, that corresponds to evaluating the path expression query p_2 with f as the start state.

In the *SQLGen* stage, we first compute the SQL query corresponding to A_{SQ} without the predicates. Now, for each final state $f \in F$, we add the SQL fragment corresponding to the predicate as follows. Let $T(f)$ be the temporary relation corresponding to the state f . Then we add a *with* clause of the form

```
with T_Pred as (
  select *
  from T
  where exists (PQ)
)
```

where PQ is the query corresponding to the predicate automaton $A_{\text{pred}}(f)$. The final query is the union of all the T_Pred relations.

Let us now consider a more general BPE query with one or more predicates occurring in any step of the path expression. This query is of the form $p_1\{Pred_1\}..p_k\{Pred_k\}$, where each p_i is a GSPE query and each $Pred_i$ is of the form p_j or $p_j \text{ op value}$. An example query is $Q = //section[//caption = 'v1']/title$. Our algorithm proceeds as follows:

In the *PathId* stage, we first apply the above procedure to evaluate $p_1\{Pred_1\}$. Let F be the set of final states in the resulting automaton. Then with F as the set of start states, we compute $p_2\{Pred_2\}$. We continue this process k times to obtain the automaton for the entire query. The *SQLGen* stage is also extended in a similar manner to process the resulting automaton.

Let $\text{PrimaryPath}(Q)$ be the query $\text{PP}(Q) = p_1p_2..p_k$. If the cross-product automaton obtained from A_S and $A_{\text{PP}(Q)}$ is not empty, then the above algorithm may generate duplicate results and we add a *distinct* clause to the final SQL query. We illustrate why this is needed with an example. Consider the evaluation of Q over the mapping schema in Figure 1. The section nodes 4 and 7 match the path expression *//section*. In other words, any instance element e in an XML document corresponding to either of these schema nodes will match this path expression. On the other hand, whether e will match *//section[caption = 'v1']* is going to depend on whether e satisfies the predicate. Notice how while (incoming) structural conditions can be verified during query translation time (without looking at the data), predicate conditions depend on the data. So, given a pair of parent-child section elements, e_1 and e_2 , matching nodes 4 and 7, while we can be sure that both match *//section*, we cannot be sure of whether one or both of them will match the predicate at query translation time. So, the SQL query has to handle all possible cases and as a result, it may produce duplicate results (when both of them satisfy the predicate, then the child of e_2 will appear twice in the result).

4.2. Reconstructing XML subtrees

In [12, 26], algorithms were presented for reconstructing XML subtrees when the mapping schema is a tree. In this section, we describe how to handle the reconstruction of a recursive component and a DAG component.

Notice that the *SQLGen* algorithm for handling a recursive component in Figure 9 actually reconstructs the XML data corresponding to the entire recursive component. But, what is missing in order to reconstruct the XML subtree is structural information about the different elements. Recall that in [12, 26], this could be determined statically as for a tree XML schema, the number of distinct root-to-leaf paths is fixed. On the other hand, for recursive components, we need to construct the root-to-leaf path dynamically. Notice that the *schemanode* column in relation T_R keeps track of

the schema node corresponding to the tuple. We maintain an additional `rtol` column that keeps track of the path from the root of the subtree being constructed. This is similar to the approach proposed in [29] for constructing dewey numbers dynamically.

In order to handle a DAG component, we have two options. We could either unroll the DAG into a tree and apply prior techniques. If this may lead to a size explosion, we could reconstruct a DAG directly by keeping track of the root-to-leaf path as mentioned above.

4.3. Handling order in XPath semantics

According to XPath semantics, the results of a path expression query have to be returned in document order. In order to support this, the schema-based shredding of XML into relations will need to maintain the relative position among sibling XML elements in some form. This was the primary focus of [29], where solutions were proposed to handle order in XML for an arbitrary query translation algorithm. Hence, in particular, their techniques can be integrated with our algorithm in a straightforward fashion.

5. Related Work

The prior literature on XML-to-SQL query translation can be broadly classified into three areas: (1) schema-based XML storage, (2) schema-oblivious XML storage and (3) XML Publishing.

A number of approaches have been proposed for using an RDBMS to store and query XML data in a schema-based fashion [3, 18, 20, 28, 29]. The main focus of [3, 18, 20, 28] was defining a “good” relational schema for the given XML schema. In [28] the general approach to translating XML queries into SQL is illustrated with examples without any algorithmic details. In [29], the focus is on supporting order-based queries. The authors give an algorithm for the schema-oblivious scenario and briefly mention how the ideas for adding support to order-based queries can be applied with any existing schema-based approach. We are not aware of any published XML-to-SQL query translation algorithm in this scenario.

Several techniques have been proposed for the schema-oblivious XML storage scenario [9, 15, 24, 32] approaches. Each of these approaches (except [9]) proposed a fixed relational schema for storing the XML data and algorithms were presented for translating path expression queries into SQL. In [9], the relational schema is decided based on the XML data. Since the techniques are schema-oblivious, they are applicable irrespective of whether the XML schema is recursive or not. The techniques also consider the presence of the `//` axis in path expression queries. In [8], an algorithm for translating more general XQuery queries into SQL is

presented. Our work is complementary to these techniques because we consider the query translation problem in the schema-based XML storage scenario. In [29, 30], it was shown that for many query workloads over non-recursive XML schema, schema-based shredding approaches yield far better performance than schema-oblivious shredding. So, it is conceivable that the same result holds in a number of scenarios even when the XML schema and/or query is recursive.

In the XML Publishing scenario, there has been a lot of work on translating complex XML queries into SQL [4, 10, 12, 13, 16, 19, 21, 25, 26]. While the class of XML queries considered are fairly complex in these approaches (a significant subset of XQuery/XSLT), the focus is on (non-recursive) tree XML schemas. In contrast, our focus is on XML-to-SQL query translation over recursive XML schema. While some of the above techniques handle `//` in the XML query by enumerating all satisfying paths, we present a different solution that represents all satisfying paths in a more compact manner.

In [2], an algorithm for reconstructing a recursive XML view was presented. Their solution does not use the support for recursion in SQL and simulates the recursion in middleware instead. In contrast, we show how we can use the support for linear recursion in SQL99 and by combining it with the “outer union” approach construct a single SQL query to reconstruct a recursive XML subtree.

A more detailed description of the existing published work on XML-to-SQL query translation in the above three scenarios is given in [17].

There has been some work on optimizing queries in a semi-structured framework [5, 14, 22] using graph schemas. These techniques are similar to the *PathId* stage of query translation, and we adapted the cross-product automaton technique proposed in [14], for the *PathId* algorithm in Section 3.1.

In [1, 23], algorithms for minimizing tree pattern queries, both in the presence and absence of XML schema information, are presented. These algorithms remove redundant parts of the XML query that are implied by either other parts of the query or by the XML schema or a combination of both. These algorithms are complementary to our algorithm and can be used as the first stage to minimize the input XML queries.

6. Conclusions

We presented a generic algorithm to translate path expression queries to SQL in the presence of recursion in the XML schema and queries. This algorithm is applicable over a wide class of techniques for schema-based shredding of XML into relations. We also showed how the *with* clause in SQL99 is useful in XML-to-SQL query translation over

DAG XML schema and how the support for linear recursion in SQL99 is sufficient for translating path expression queries into a single SQL query over an arbitrary (recursive) XML-to-Relational mapping.

The algorithm presented in this paper for translating path expression queries into SQL can be adapted to the “Publishing” domain as well. The details of the algorithm will change based on the view definition language, but the main ideas about how to handle recursive schemas, DAG schemas and recursive queries remain the same.

There are a number of avenues for future research. Extending the work in this paper to perform XML-to-SQL query translation for more complex FLWOR XQuery queries, when the XML schema is recursive, is open. Comparing the schema-based and schema-oblivious solutions for XML storage in the presence of recursive XML schema is another important area for future research. Similarly, combining the interval-based techniques used in XML-to-SQL query translation in the schema-oblivious scenario along with the techniques proposed in this paper is another interesting avenue for future work.

Acknowledgement: This work was supported in part by NSF grants ITR-0086002 and CCR-0208013, and a Microsoft fellowship.

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