

CS 744: BIG DATA SYSTEMS

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ADMINISTRIVIA

- Midterm grades up today
- Pick up papers office hours today or Tuesday class
- Course Projects: round 2 meetings

GRAPH MINING

WHATS DIFFERENT ?

Graph Analytics

Examples

PageRank

Shortest path

Connected components

...

Graph Mining

Examples

Counting motifs

Frequent sub-graph mining

Finding cliques

...

GRAPH MINING: DEFINITIONS

Graph $G = (V, E)$ Vertices and edges have unique ids.

Embedding sub-graph of G , i.e., subset of vertices and edges

- Vertex-induced – start from vertices, include all edges for vertices
- Edge-induced – start from edges, include all endpoint vertices

Pattern any arbitrary graph

Pattern is a **template**, embedding is an **instance**

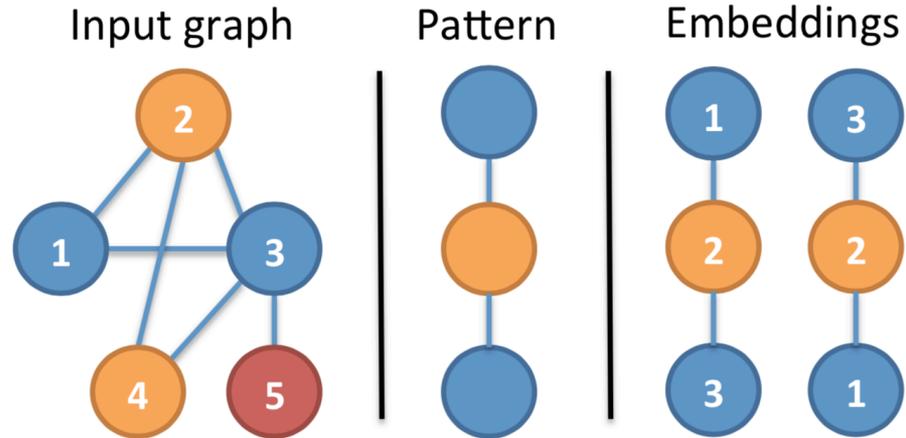
AUTOMORPHISM, ISOMORPHISM

Embedding is isomorphic to pattern iff

one-to-one mapping between
vertices, edges

vertex mapped has same label
edges connect matching vertices

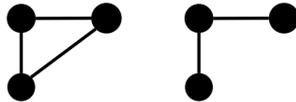
Embedding e is automorphic to e' iff
contain same edges and vertices



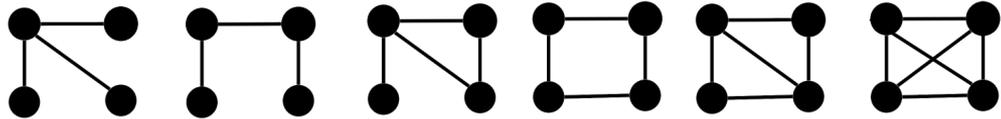
EXAMPLE: MOTIF COUNTING

Motifs: Connected patterns that are **non-isomorphic**

$k=3$ – two patterns



$k=4$ – six patterns



Goal:

Find counts of each pattern in graph

FILTER PROCESS MODEL

Two UDFs: Filter embedding Φ and Process embedding π

Algorithm

Initial embedding set I

For each embedding in set

$C \leftarrow \text{generate embeddings}(\text{add one vertex})$

For each embedding e in C

If $\Phi(e)$:

$F \leftarrow F \cup \pi(e)$

Terminate if F is empty

else loop with $I \leftarrow F$

BSP Execution by
parallelizing this loop



AGGREGATION FUNCTIONS

Aggregation functions:

Filter function α , Aggregate function β

Similar to `groupByWindowAndApply` ?

Consistency properties

If embeddings are automorphic, all UDFs return same value

Anti-monotonicity – filter return same values for extensions

OTHER APPROACHES

Think like Vertex

- Vertex has local embedding
- “Push” message to border vertex

Cons

- Highly connected vertex → hotspot
- Duplicate messages, one per border

Think like Pattern

- Don't materialize embeddings
- Store patterns, recompute embeddings on the fly

Cons

- Partition by pattern (fewer ?)
- Popular pattern, load imbalance

ARABESQUE API: EXAMPLE

```
boolean filter(Embedding e){
    return (numVertices(e) <= MAX_SIZE);
}

void process(Embedding e){
    mapOutput (pattern(e),1);
}

Pair<Pattern,Integer> reduceOutput (
    Pattern p, List<Integer> counts){
    return Pair (p, sum(counts));
}
```

Counting
Motifs

DISTRIBUTED EXECUTION

Apache Giraph based distributed implementation

Synchronous super-steps (BSP)

- Workers receive messages sent previously [Embeddings]
- Process messages [Filter Process]
- Send new messages to be delivered [Aggregate output?]

Can be implemented in any BSP system ? (e.g., Spark)

EXPLORATION STRATEGY

Goals

- Prune embeddings that are “identical” (i.e. automorphic)
- Need to do this without coordination (why ?)

Approach

- Determine a “canonical” embedding (unique and extensible)
- Canonical property
 - Start with smallest id
 - Add the neighbor with smallest id not visited yet
- Incremental check while adding vertex to embedding

EFFICIENT STORAGE: ODAG

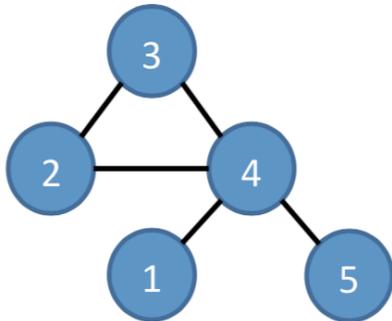
Storage model: Ordered lists of vertex / edge ids (integers)

ODAG format

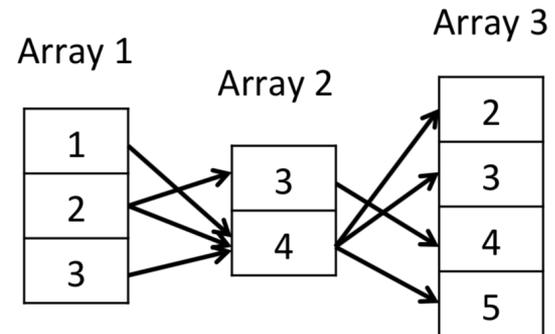
Store all first elements of embeddings in one array (and so on)

Links between array indices if embedding has a such link

Could lead to spurious embeddings



Canonical embeddings		
1	4	2
1	4	3
1	4	5
2	3	4
2	4	5
3	4	5



EFFICIENT STORAGE: ODAG

ODAG benefits

N vertices can have up to N^k embeddings of size k

ODAG upper bound $O(k \cdot N^2)$ ($k \ll N$)

Using ODAGs

Avoid spurious embeddings using `filter`, `aggregateFilter`

Merging ODAGs

Every worker creates ODAG outputs

Use map-reduce to do the merge!

Map each entry based on position to worker

OTHER OPTIMIZATIONS

Partitioning Embeddings

Performed at start of every iteration

Round-robin scheme with **block size b**

Estimate embeddings that start from a vertex

Two-level aggregation

Need to aggregate by pattern. Equality requires **isomorphism** check

Quick pattern calculated locally and aggregated

Use canonical pattern to do second level aggregation

SUMMARY

Graph Mining: new workload that is compute and data intensive

First system to do distributed graph mining

Challenges: Lots of intermediate state (trillions of embeddings)

Key ideas:

- Filter / prune embeddings using canonical definition

- Efficient storage using ODAGs