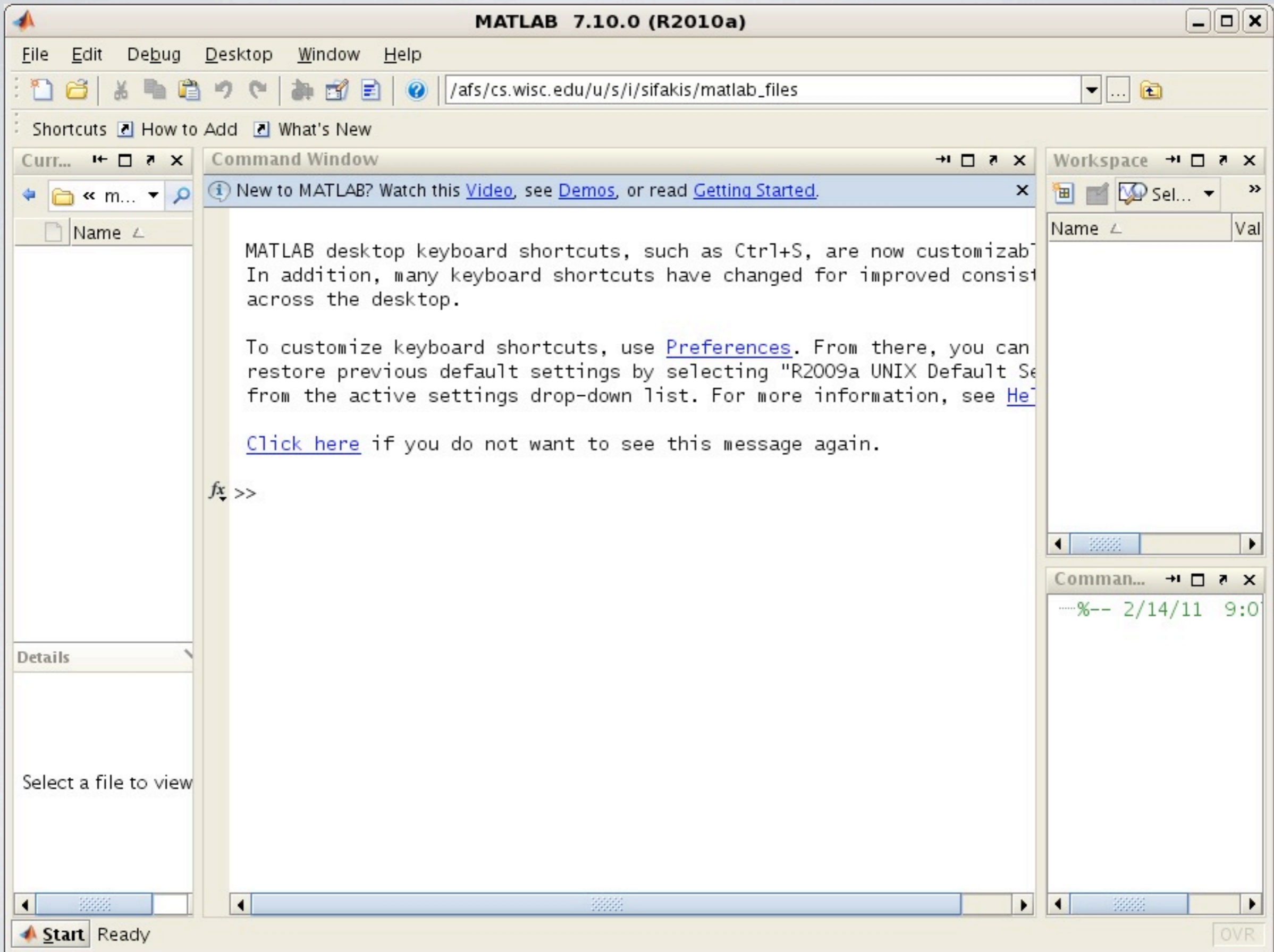


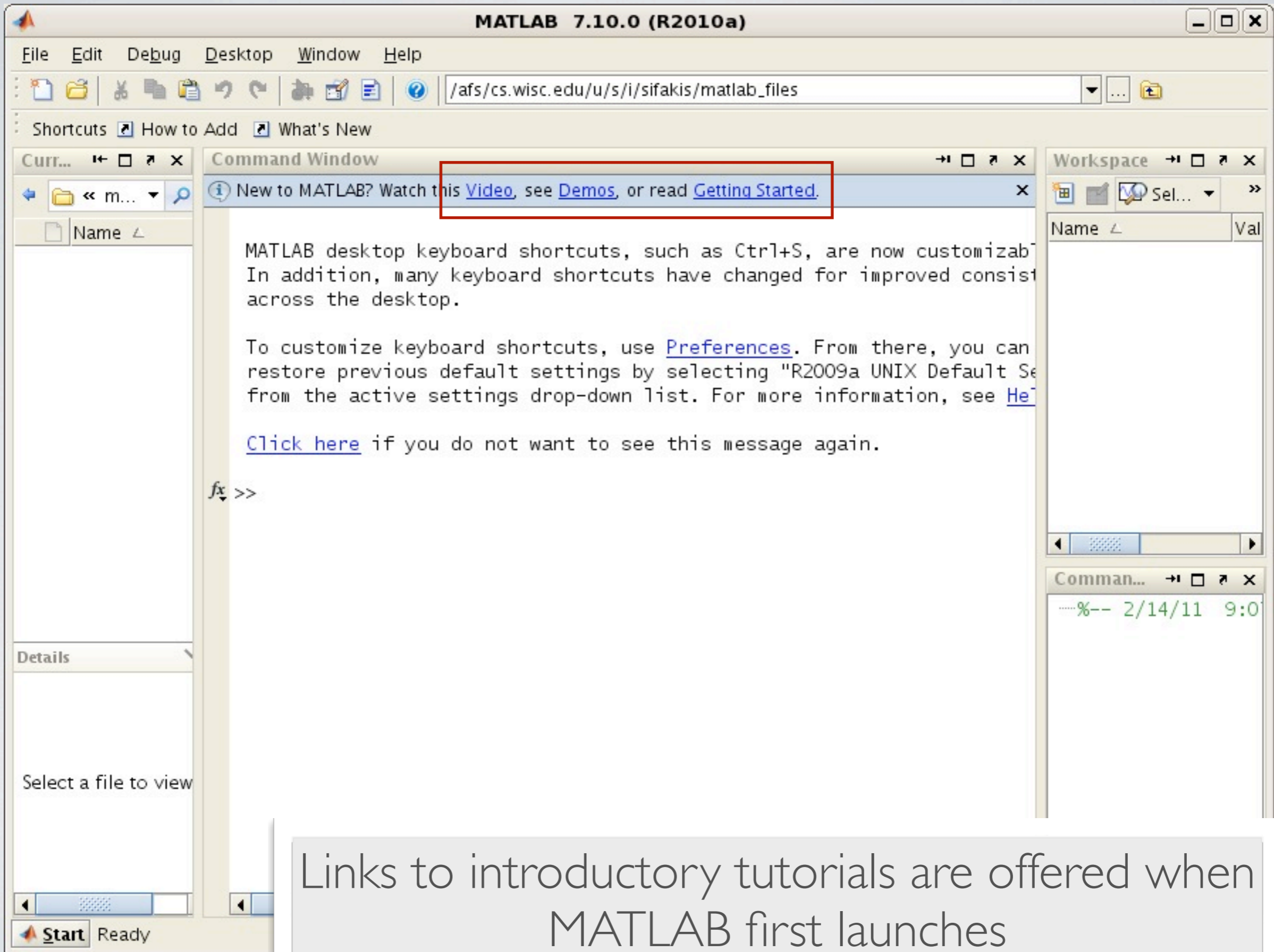
MATLAB BASICS

CS412 Spring 2011

Instructor : Eftychios Sifakis

To launch MATLAB from an instructional lab machine:
Enter *matlab* at the shell prompt





Links to introductory tutorials are offered when MATLAB first launches

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
>> help
HELP topics:

matlab/general          - General purpose commands.
matlab/ops              - Operators and special characters.
matlab/lang            - Programming language constructs.
matlab/elmat           - Elementary matrices and matrix manip
matlab/randfun         - Random matrices and random streams.
matlab/elfun           - Elementary math functions.
matlab/specfun         - Specialized math functions.
matlab/matfun          - Matrix functions - numerical linear
matlab/datafun         - Data analysis and Fourier transforms
matlab/polyfun         - Interpolation and polynomials.
matlab/funfun          - Function functions and ODE solvers.
matlab/sparfun         - Sparse matrices.
matlab/scribe          - Annotation and Plot Editing.
matlab/graph2d         - Two dimensional graphs.
matlab/graph3d         - Three dimensional graphs.
matlab/specgraph       - Specialized graphs.
matlab/graphics        - Handle Graphics.
matlab/uitools         - Graphical User Interface Tools.
matlab/strfun          - Character strings.
matlab/imagesci        - Image and scientific data input/outp
matlab/iofun           - File input and output.
matlab/audiovideo      - Audio and Video support.
matlab/timefun         - Time and dates.
matlab/datatypes       - Data types and structures.
matlab/verctrl         - Version control.
```

Workspace

Name	Val

Command Window

```
%-- 2/14/11 9:0
help
```

Start

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window displays the output of the `help` command, which lists various MATLAB topics and their descriptions. The `>> help` command is highlighted with a red box. The Workspace window is empty, and the Command Window shows the command history with the `help` command entered.

Command Window Output:

```
>> help
HELP topics:

matlab/general          - General purpose commands.
matlab/ops              - Operators and special characters.
matlab/lang             - Programming language constructs.
matlab/elmat           - Elementary matrices and matrix manip
matlab/randfun         - Random matrices and random streams.
matlab/elfun           - Elementary math functions.
matlab/specfun         - Specialized math functions.
matlab/matfun          - Matrix functions - numerical linear
matlab/datafun         - Data analysis and Fourier transforms
matlab/polyfun         - Interpolation and polynomials.
matlab/funfun          - Function functions and ODE solvers.
matlab/sparfun         - Sparse matrices.
matlab/scribe          - Annotation and Plot Editing.
matlab/graph2d         - Two dimensional graphs.
matlab/graph3d         - Three dimensional graphs.
matlab/specgraph       - Specialized graphs.
matlab/graphics        - Handle Graphics.
matlab/uitools         - Graphical User Interface Tools.
matlab/strfun          - Character strings.
matlab/imagesci        - Image and scientific data input/outp
matlab/iofun           - File input and output.
matlab/audiovideo     - Audio and Video support.
```

Command Window History:

```
%-- 2/14/11 9:0
help
```

The *help* command provides documentation for practically all MATLAB features

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
>> help
HELP topics:

matlab/general          - General purpose commands.
matlab/ops              - Operators and special characters.
matlab/lang             - Programming language constructs.
matlab/elmat           - Elementary matrices and matrix manip
matlab/randfun         - Random matrices and random streams.
matlab/elfun           - Elementary math functions.
matlab/specfun         - Specialized math functions.
matlab/matfun          - Matrix functions - numerical linear
matlab/datafun         - Data analysis and Fourier transforms
matlab/polyfun         - Interpolation and polynomials.
matlab/funfun          - Function functions and ODE solvers.
matlab/sparfun         - Sparse matrices.
matlab/scribe          - Annotation and Plot Editing.
matlab/graph2d         - Two dimensional graphs.
matlab/graph3d         - Three dimensional graphs.
matlab/specgraph      - Specialized graphs.
matlab/graphics        - Handle Graphics.
matlab/uitools         - Graphical User Interface Tools.
matlab/strfun          - Character strings.
matlab/imagesci       - Image and scientific data input/outp
matlab/iofun           - File input and output.
matlab/audiovideo     - Audio and Video support.
matlab/timefun        - Time and dates.
```

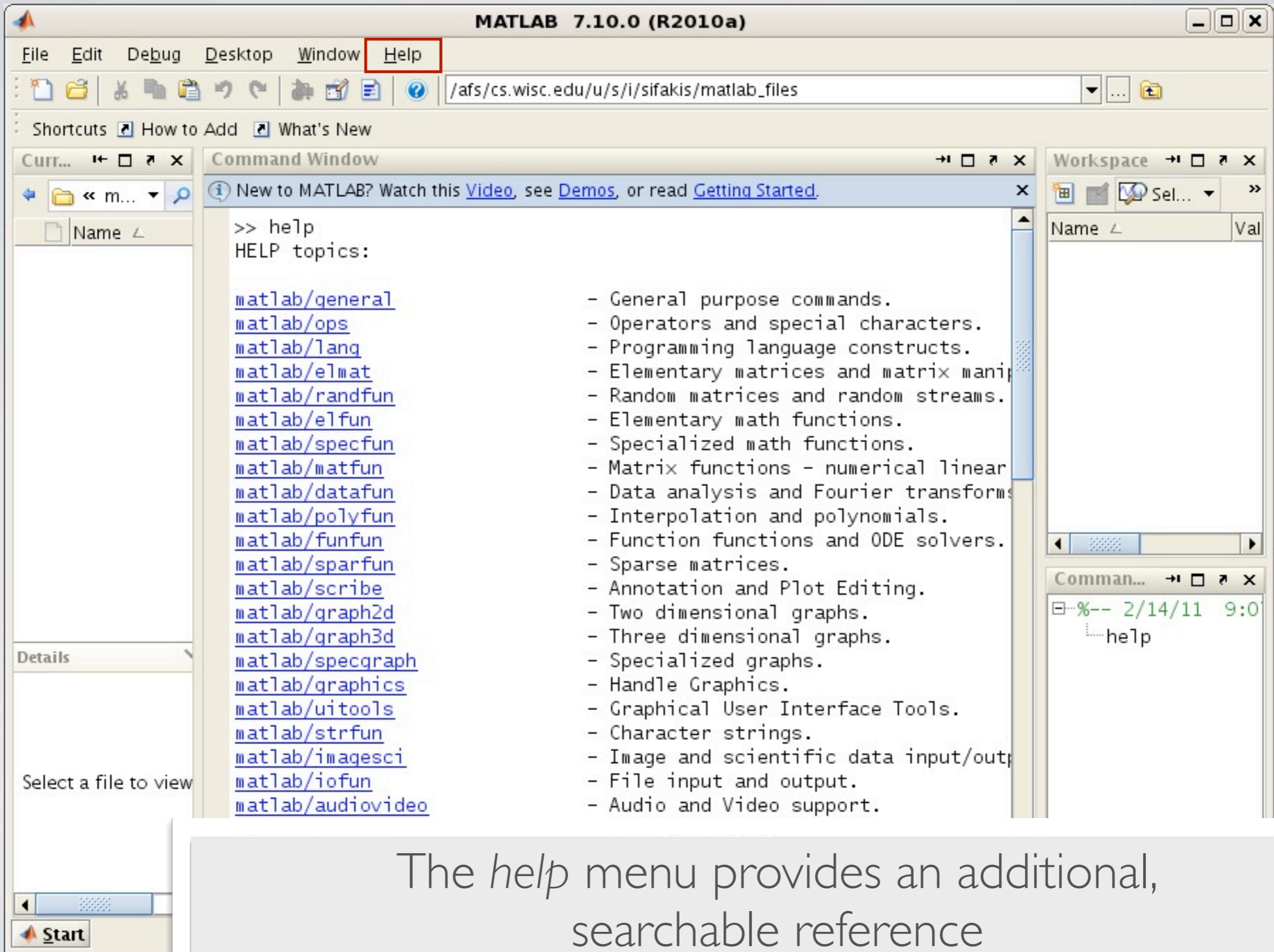
Workspace

Name	Val
------	-----

Command Window

```
%-- 2/14/11 9:0
help
```

Additional help is available by clicking on the subtopics



The *help* menu provides an additional, searchable reference

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
>> x=3  
  
x =  
  
    3  
  
fx >>
```

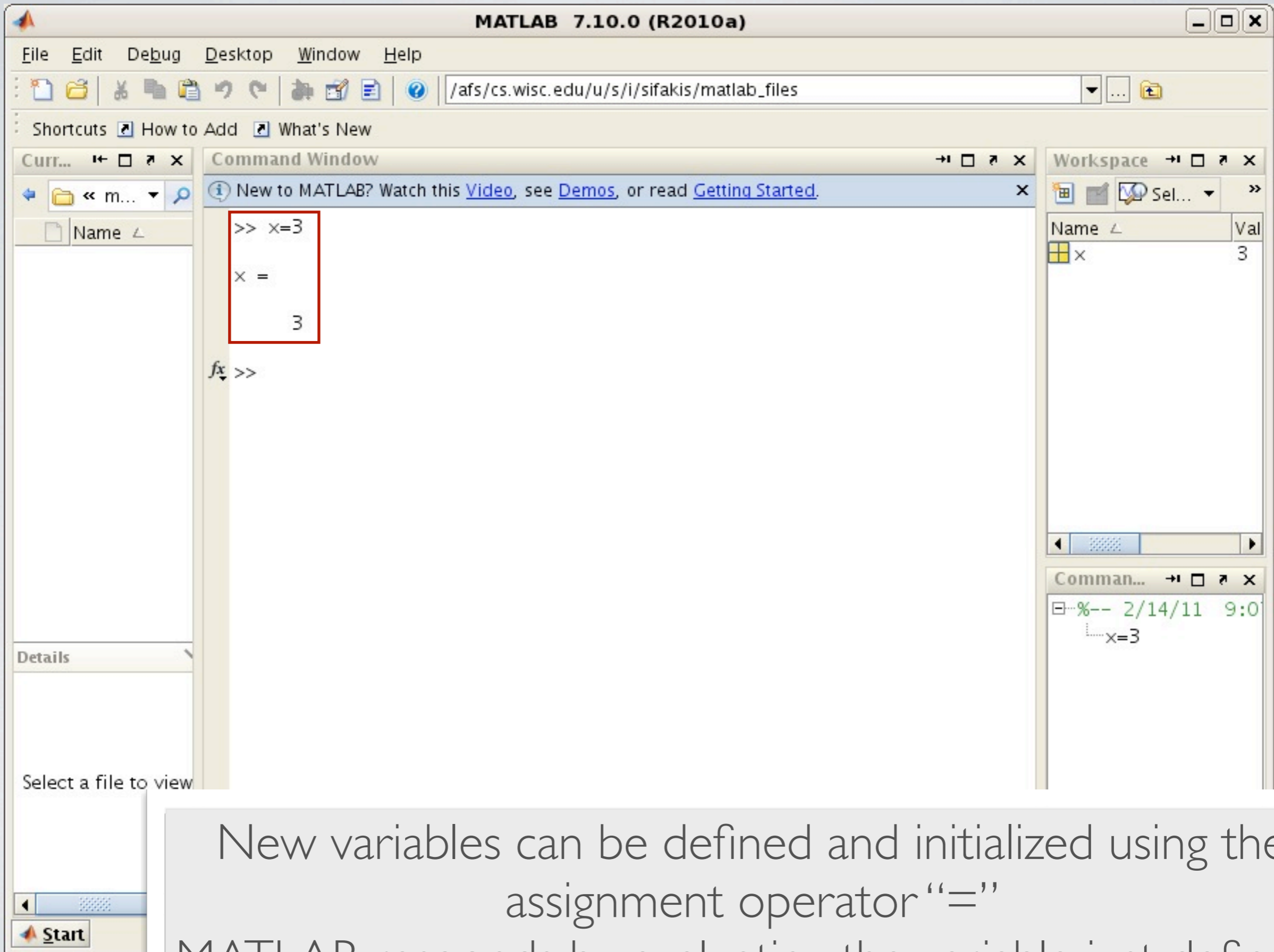
Workspace

Name	Val
x	3

Command Window

```
%-- 2/14/11 9:0  
└─ x=3
```

Start OVR



New variables can be defined and initialized using the assignment operator “=”
MATLAB responds by evaluating the variable just defined.

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window displays the following code and output:

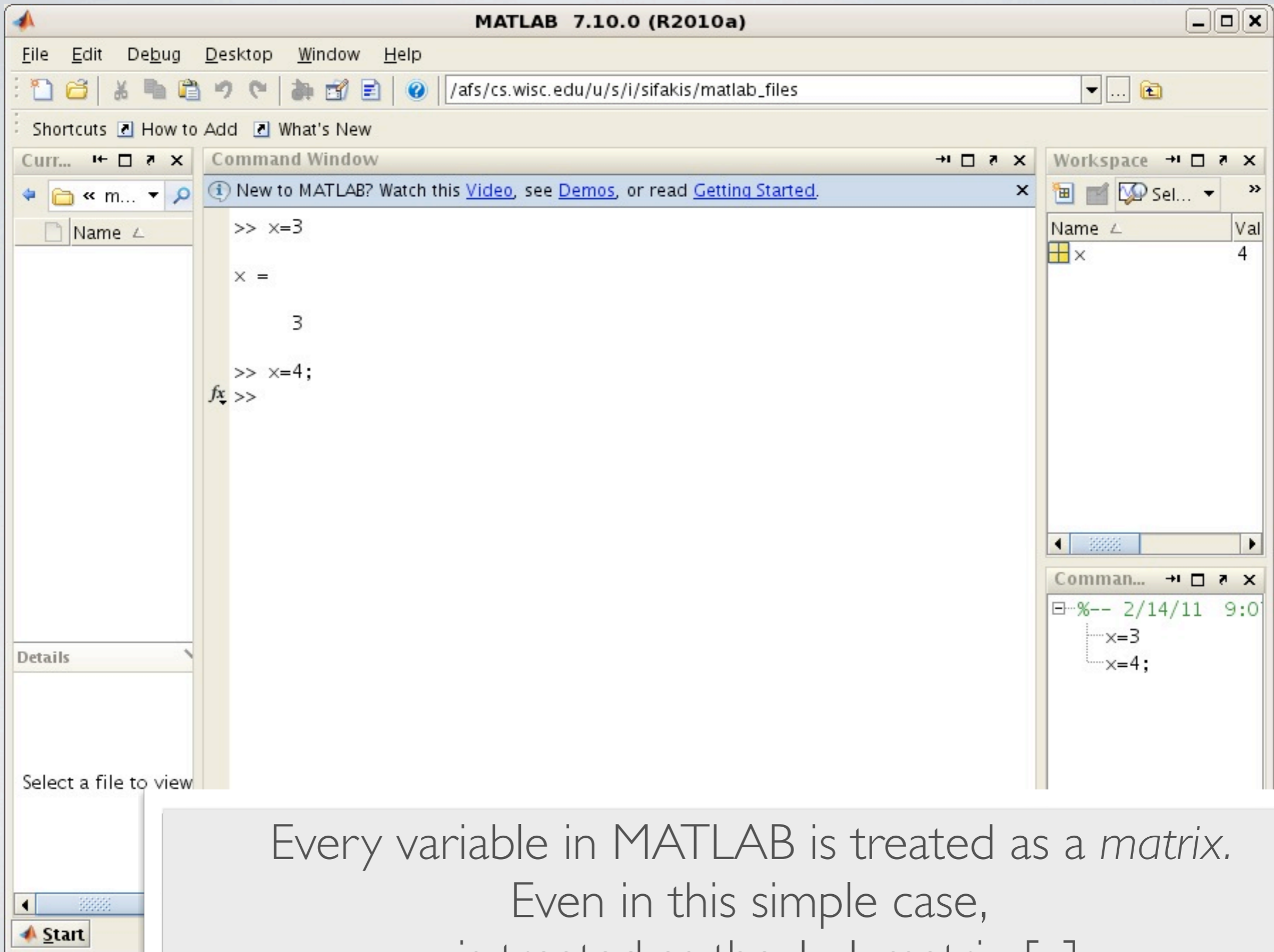
```
>> x=3  
  
x =  
  
    3  
  
>> x=4;  
fx >>
```

The Workspace window shows a table with the following data:

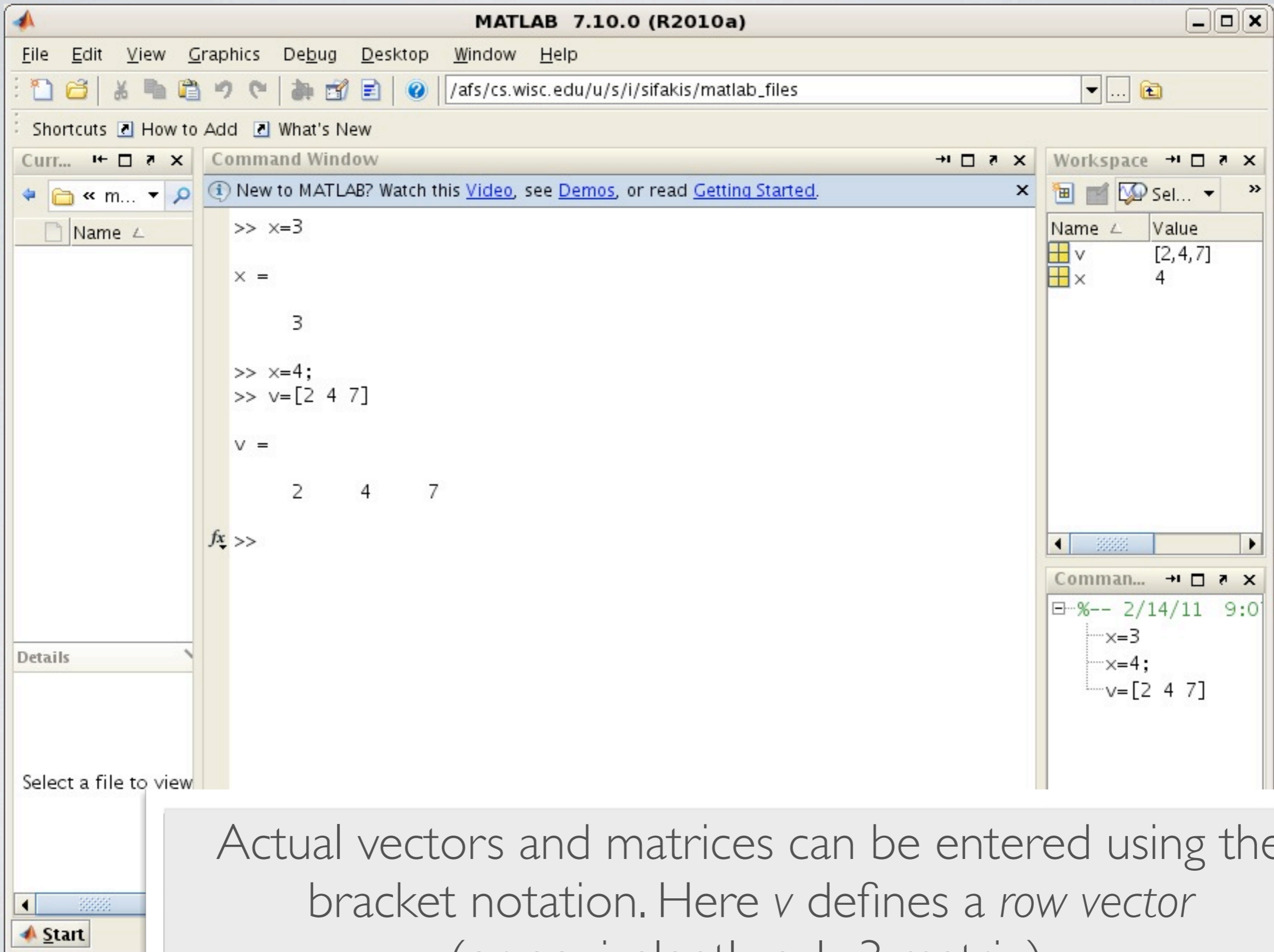
Name	Val
x	4

The Command Window also shows a timestamp: %-- 2/14/11 9:00. The workspace window shows the command history: x=3, x=4;.

Ending a statement with a semicolon (;) suppresses MATLAB's output -- this is useful in programs.



Every variable in MATLAB is treated as a *matrix*.
Even in this simple case,
 x is treated as the 1×1 matrix $[x]$



Actual vectors and matrices can be entered using the bracket notation. Here v defines a *row vector* (or, equivalently a 1×3 matrix).

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts

Curr... ←

← << n

File Nam

Details

Select a file to view

Start

OVR

Elements of row vectors can also be entered with commas (,) between them. A matrix is entered by using commas between elements of the same row, and separates each row from the next using semicolons (;)

```
v =  
    2    4    7  
  
>> u=[3,5,8]  
u =  
    3    5    8  
  
>> A=[1,2,3;4,5,6;7,8,9]  
A =  
    1    2    3  
    4    5    6  
    7    8    9  
  
fx >>
```

Comman... → □ ↗ ×

%-- 2/14/11 9:0

```
x=3  
x=4;  
v=[2 4 7]  
u=[3,5,8]  
A=[1,2,3;4,5,6
```

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Column vectors can be entered either by separating elements with semicolons, or by defining a row vector and using the apostrophe (') to denote its *transpose*.

```
A =  
    1    2    3  
    4    5    6  
    7    8    9
```

```
>> v=[2;4;7]  
  
v =  
  
    2  
    4  
    7
```

```
>> u=[3,5,8]'  
  
u =  
  
    3  
    5  
    8
```

```
Command Window  
%-- 2/14/11 9:0  
x=3  
x=4;  
v=[2 4 7]  
u=[3,5,8]  
A=[1,2,3;4,5,6]  
v=[2;4;7]  
u=[3,5,8]'
```

Start OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
u =  
    3    5    8  
  
>> A=[1,2,3;4,5,6;7,8,9]  
  
A =  
    1    2    3  
    4    5    6  
    7    8    9  
  
>> v=[2;4;7]
```

Workspace

Name	Value
A	[1,2,3;4,5,6;7,8,9]
u	[3;5;8]
v	[2;4;7]
x	4

Command History

```
%-- 2/14/11 9:0  
x=3  
x=4;  
v=[2 4 7]  
u=[3,5,8]  
A=[1,2,3;4,5,6;7,8,9]  
v=[2;4;7]  
u=[3,5,8]'
```

Note the command history window, which lists the last executed commands

Start

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
u =  
    3    5    8  
  
>> v=[2;4;7]  
  
v =  
    2  
    4  
    7  
  
>> u=[3,5,8]'  
  
u =  
    3  
    5  
    8  
  
fx >>
```

The variable display window lists the defined variables and its contents

Workspace

Name	Value
A	[1,2,3;4,5,6;]
u	[3;5;8]
v	[2;4;7]
x	4

Command Window

```
%-- 2/14/11 9:0  
x=3  
x=4;  
v=[2 4 7]  
u=[3,5,8]  
A=[1,2,3;4,5,6;  
v=[2;4;7]  
u=[3,5,8]'
```

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
>> v=[2;4;7]

v =

     2
     4
     7

>> u=[3,5,8]'

u =

     3
     5
     8

>> v(3)

ans =

     7

>> u(3,1)

ans =

     8
```

Workspace

v(1,1)
v(1,2)
A=[1,2,3;4,5
v=[2;4;7]
u=[3,5,8]'
v(3)
u(3,1)

Select a file to view

Start

OVR

We can access components of matrices and vectors using the parenthesis operator (). In the case of a column vector, an element can be accessed either with a single index, or in matrix notation (with a column index of 1)

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> A=[1,2,3;4,5,6;7,8,9]

A =

     1     2     3
     4     5     6
     7     8     9

>> A(2,3)

ans =

     6

>> A(3,4)
??? Index exceeds matrix dimensions.

>> A(3,4)=10

A =

     1     2     3     0
     4     5     6     0
     7     8     9    10

fx >>
```

Workspace

Name	Value
A	<3x4 double
ans	6
u	[3;5;8]
...	...

Details

Select a file to view

Start

OVR

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

v(1,1)
v(1,2)
A=[1,2,3;4,5
v=[2;4;7]
u=[3,5,8]'
v(3)
u(3,1)
A=[1,2,3;4,5
A(2,3)
A(3,4)
A(3,4)=10

We can use the same notation to access the element of a matrix

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> A=[1,2,3;4,5,6;7,8,9]

A =

     1     2     3
     4     5     6
     7     8     9

>> A(2,3)

ans =

     6

>> A(3,4)
??? Index exceeds matrix dimensions.

>> A(3,4)=10

A =

     1     2     3     0
     4     5     6     0
     7     8     9    10

fx >>
```

Workspace

Name	Value
A	<3x4 double
ans	6
u	[3;5;8]
..	...

Details

Select a file to view

Start

OVR

If we try to read a element that is out of bounds, MATLAB reports an error

```
v(1,1)
v(1,2)
A=[1,2,3;4,5
v=[2;4;7]
u=[3,5,8]'
v(3)
u(3,1)
A=[1,2,3;4,5
A(2,3)
A(3,4)
A(3,4)=10
```

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
>> A=[1,2,3;4,5,6;7,8,9]

A =

     1     2     3
     4     5     6
     7     8     9

>> A(2,3)

ans =

     6

>> A(3,4)
??? Index exceeds matrix dimensions.
```

>> A(3,4)=10

```
A =

     1     2     3     0
     4     5     6     0
     7     8     9    10

fx >>
```

Workspace

Name	Value
A	<3x4 double

Details

Select a file to view

Start

OVR

However, if we try to write to an element out of bounds, MATLAB resizes the matrix to fit the new entry.

```
A=[1,2,3;4,5,6;7,8,9]
v=[2;4;7]
u=[3,5,8]'
v(3)
u(3,1)
A=[1,2,3;4,5,6;7,8,9]
A(2,3)
A(3,4)
A(3,4)=10
```

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#)

```
A =  
    1    2    3  
    4    5    6  
    7    8    9
```

```
>> A(:,2)  
ans =  
     2  
     5  
     8
```

```
>> A(3,:)  
ans =  
     7     8     9
```

```
>> A(:, :)  
ans =  
     1     2     3  
     4     5     6  
     7     8     9
```

fx >>

Workspace

Details

Select a file to view

Start

OVR

The colon (:) is a special index, denoting *all* possible rows and/or columns. For example $A(:,2)$ means *elements on the second column for all rows (i.e. the second row of A)*

A(3,4)=10
A=[1,2,3;4,5
A(:,2)
A(3,:)
A(:, :)

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
A =  
    1    2    3  
    4    5    6  
    7    8    9  
  
>> A(:,2)  
  
ans =  
     2  
     5  
     8  
  
>> A(3,:) ans =  
     7     8     9  
  
>> A(:, :)  
  
ans =  
     1     2     3  
     4     5     6  
     7     8     9  
  
fx >>
```

Workspace

Name	Value
A	[1,2,3;4,5,6;7,8,9]
ans	[1,2,3;4,5,6;7,8,9]
u	[3;5;8]

Details

Select a file to view

Start

OVR

$A(3,:)$ are the elements on the 3rd row, for all columns (i.e. the 3rd row of A)

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

New to MATLAB? Watch this [Video](#), see [Demos](#), or read [Getting Started](#).

```
A =  
    1    2    3  
    4    5    6  
    7    8    9  
  
>> A(:,2)  
  
ans =  
     2  
     5  
     8  
  
>> A(3,:)   
  
ans =  
     7     8     9  
  
>> A(:, :)   
  
ans =  
     1     2     3  
     4     5     6  
     7     8     9
```

Workspace

Name	Value
A	[1,2,3;4,5,6;7,8,9]
ans	[1,2,3;4,5,6;7,8,9]
u	[3;5;8]
v	[2;4;7]
x	4

Details

Select a file to view

Start

OVR

$A(:, :)$ means all rows and columns of A (i.e. the entire matrix)

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window displays the following code and output:

```
>> v=1:5
v =
     1     2     3     4     5
>> u=1:2:11
u =
     1     3     5     7     9    11
fx >>
```

A red box highlights the first command and its output. A text box on the right explains the colon operator. A smaller Command Window window is visible in the bottom right corner, showing a timestamp and the same code.

The colon operator can also define a *range*, i.e. a vector whose elements form an arithmetic progression

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> v=1:5  
v =  
    1    2    3    4    5  
  
>> u=1:2:11  
u =  
    1    3    5    7    9   11  
  
fx >>
```

Using two colons we can define a custom step; in this case we use a step of 2

Comman... 2/14/11 9:00
v=1:5
u=1:2:11

Start OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> v=1:5  
v =  
    1    2    3    4    5  
  
>> u=1:2:11  
u =  
    1    3    5    7    9   11  
  
>> if(u(2)==3)  
u(2)^2  
end  
ans =  
     9  
  
>> if(u(2)==4)  
u(2)^2  
end  
fx >>
```

Workspace

Name	Value
ans	9
u	[1,3,5,7,9,11]
v	[1,2,3,4,5]

if statements evaluate an expression (or execute a command) conditionally, based on the truth value of the expression in the parenthesis.

Select a file to view

Start

OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> for i=1:5
i^2
end

ans =

    1

ans =

    4

ans =

    9

ans =

   16

ans =

   25

fx >>
```

Workspace

Name	Value
ans	25
i	5

for statements evaluate an expression (or execute a command) for all values of a given range

Start

OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> for i=1:3:20
if (i>10)
i*2
end
end

ans =

    26

ans =

    32

ans =

    38

fx >>
```

Workspace

Name	Value
ans	38
i	19

if/for statements can be combined and nested.

Select a file to view

Start

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
26
ans =
32
ans =
38
>> sqrt(2)
ans =
1.4142
>> cos(pi/4)
ans =
0.7071
>> exp(1)
ans =
2.7183
```

Workspace

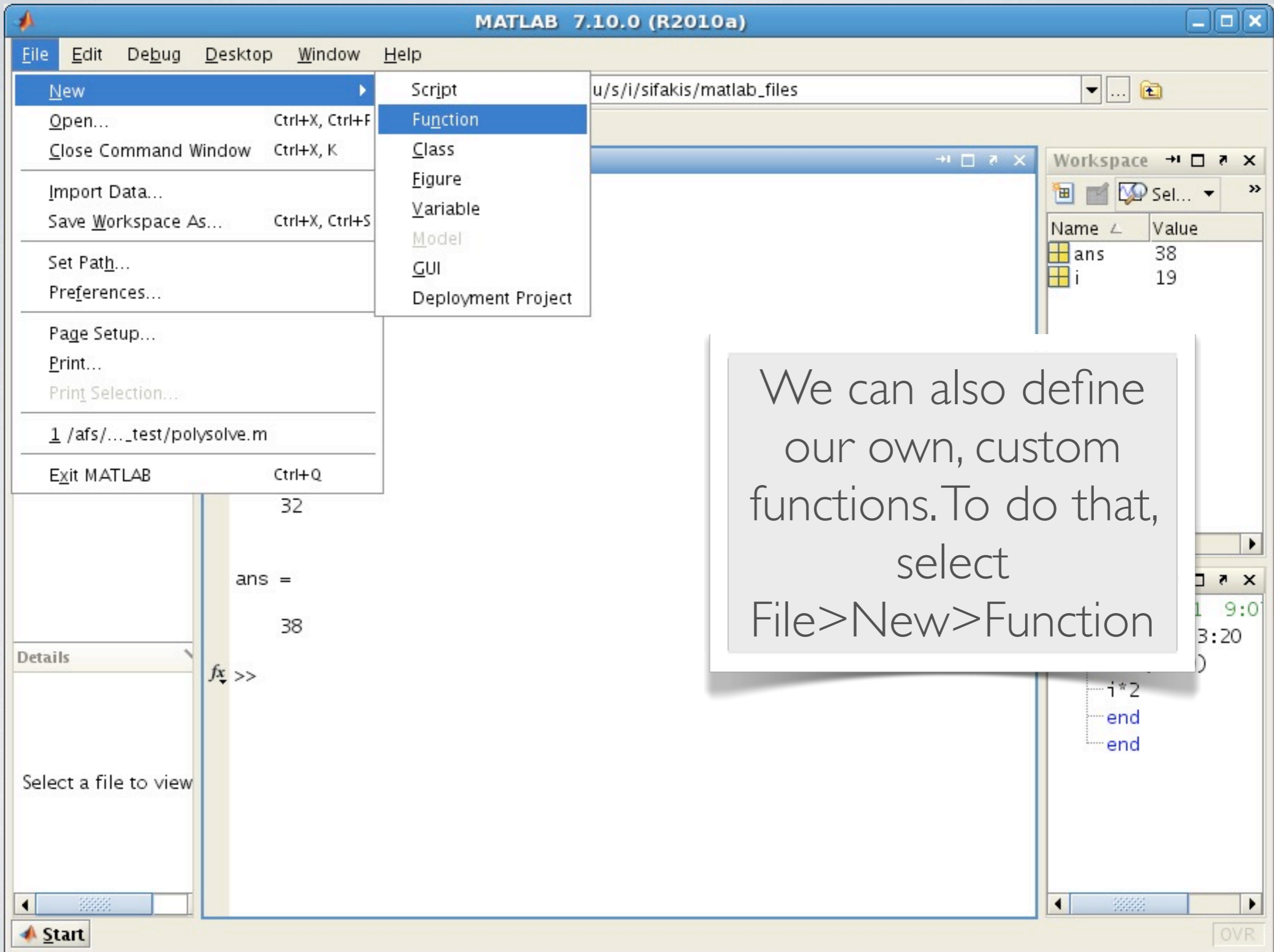
Name	Value
sqrt(2)	1.4142
cos(pi/4)	0.7071
exp(1)	2.7183

Select a file to view

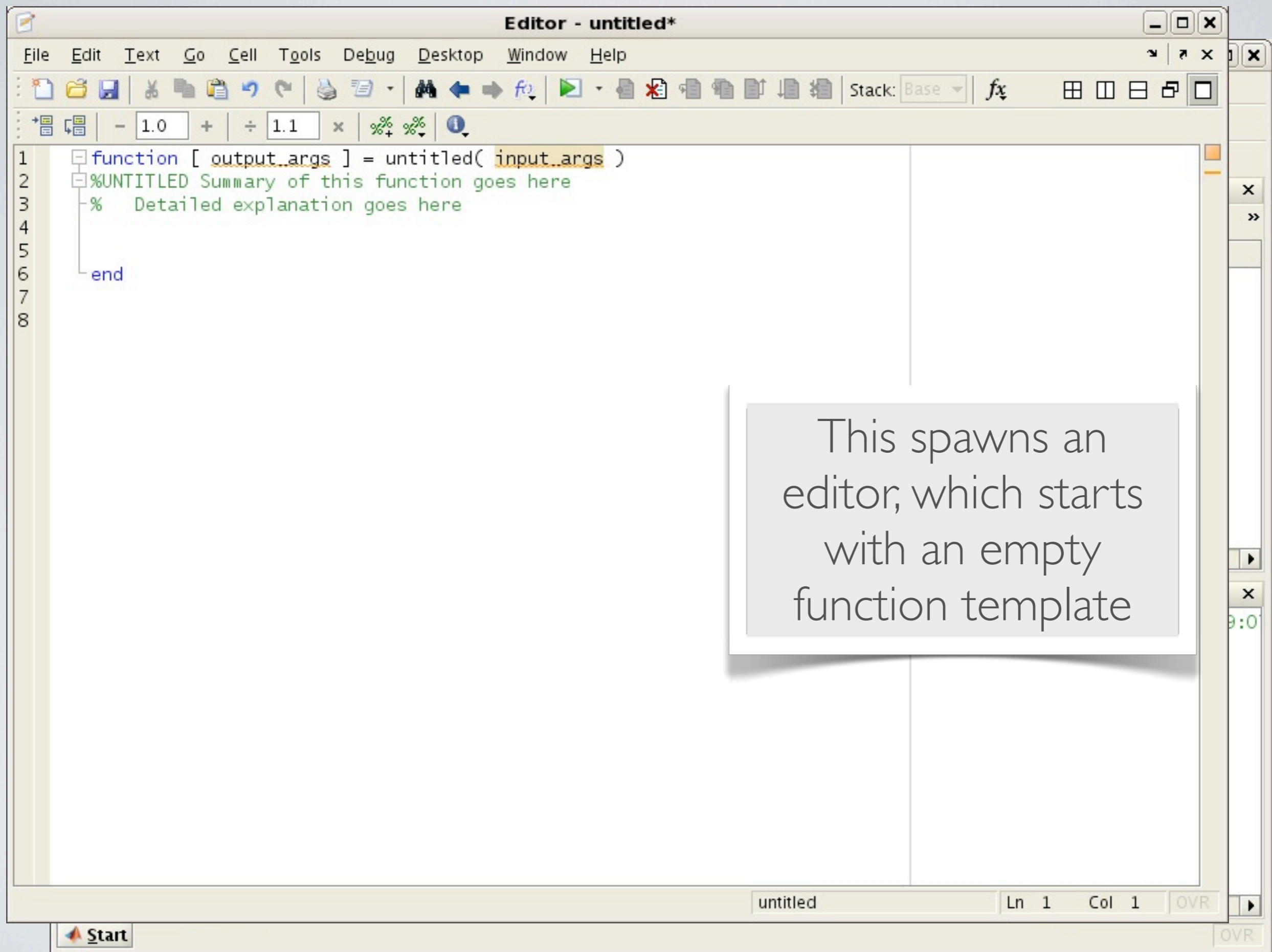
Start

OVR

MATLAB includes a number of built-in functions, such as square root, trigonometric functions, and exponentials/logarithms



We can also define our own, custom functions. To do that, select File>New>Function



This spawns an editor, which starts with an empty function template

Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/myfunc.m

File Edit Text Go Cell Tools Debug Desktop Window Help

Stack: Base fx

```
1 function [ y ] = myfunc( x )
2 % returns y=x^2+sqrt(x)
3
4 x_squared=x^2;
5 x_root=sqrt(x);
6
7 y=x_squared+x_root;
8
9 end
10
11
```

myfunc Ln 9 Col 1 OVR

Start OVR

This is an example of a function, corresponding to the expression $f(x) = x^2 + \sqrt{x}$

Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/myfunc.m

File Edit Text Go Cell Tools Debug Desktop Window Help

Stack: Base fx

```
1 function [ y ] = myfunc( x )
2 % returns y=x^2+sqrt(x)
3
4 x_squared=x^2;
5 x_root=sqrt(x);
6
7 y=x_squared+x_root;
8
9 end
10
11
```

The value(s) inside the bracket after the *function* keyword is the return variable of the function. When the return value has been computed, simply assign it to the respective variable.

myfunc Ln 9 Col 1 OVR

Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/myfunc.m

File Edit Text Go Cell Tools Debug Desktop Window Help

Stack: Base fx

```
1 function [ y ] = myfunc( x )
2 % returns y=x^2+sqrt(x)
3
4 x_squared=x^2;
5 x_root=sqrt(x);
6
7 y=x_squared+x_root;
8
9 end
10
11
```

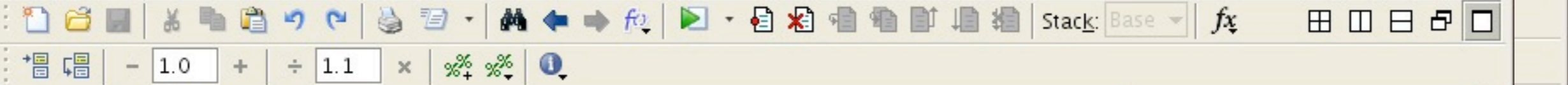
Note that a function can return a vector or a matrix, too (we will see this later).

myfunc Ln 9 Col 1 OVR

Start OVR

```
1 function [ y ] = myfunc( x )
2 % returns y=x^2+sqrt(x)
3
4 x_squared=x^2;
5 x_root=sqrt(x);
6
7 y=x_squared+x_root;
8
9 end
10
11
```

After the “=” sign we list the function name and the argument list (which can again be either numbers or matrices).



```
1 function [ y ] = myfunc( x )
2   % returns y=x^2+sqrt(x)
3
4   x_squared=x^2;
5   x_root=sqrt(x);
6
7   y=x_squared+x_root;
8
9   end
10
11
```

Additional local variables can be defined as needed

```
1 function [ y ] = myfunc( x )
2 % returns y=x^2+sqrt(x)
3
4 x_squared=x^2;
5 x_root=sqrt(x);
6
7 y=x_squared+x_root;
8
9 end
10
11
```

When finished, save the function definition file with the same name as the new function, and the extension .m

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> myfunc(4)

ans =

    18

fx >>
```

Workspace

Name	Value
ans	18

Command Window

```
%-- 2/14/11 9:0
└─ myfunc(4)
```

Start OVR

Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/myfunc.m

File Edit Text Go Cell Tools Debug Desktop Window Help

Stack: Base fx

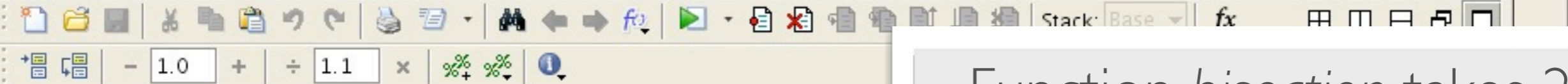
```
1 function [ y ] = myfunc( x )
2   % returns y=x^2-5
3
4   x_squared=x^2;
5   y=x_squared-5;
6
7   end
8
9
```

myfunc.m x bisection.m x

myfunc Ln 4 Col 15 OVR

Start OVR

Here, we will describe 2 new user-defined functions, one of which depends on the other. *myfunc* (x) returns x^2-5 .



```
1
2 function [ y1 y2 ] = bisection( x1 , x2 )
3 % Perform one step of bisection method
4 % Assumption myfunc(x1)*myfunc(x2)<0
5 % Returns a narrower interval containing the solution
6
7 x_midpoint=(x1+x2)/2;
8
9 if(myfunc(x_midpoint)==0)
10     y1=x_midpoint;
11     y2=x_midpoint;
12
13 elseif(myfunc(x1)*myfunc(x_midpoint)<0)
14     y1=x1;
15     y2=x_midpoint;
16
17 else
18     y1=x_midpoint;
19     y2=x2;
20
21 end
22
23 end
24
25
```

Function *bisection* takes 2 arguments (x_1, x_2) and performs one step of the bisection method on the function *myfunc*. The new shorter interval is given in the 2 return values.

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Curr... ← □ ↗ ×

« m... 🔍

Name
bisection.m
bisection.m~
myfunc.m

bisection.m (MATLA

Perform one step o
bisection method

bisection(x1, ...

Command Window ↔ □ ↗ ×

```

>> xmin=2;
>> xmax=3;
>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2

xmax =

    2.5000

>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2

xmax =

    2.2500

fx >>

```

Workspace ↔ □ ↗ ×

Sel... >>

Name	Value
xmax	2.2500
xmin	2

Comman... ↔ □ ↗ ×

```

%-- 2/14/11 9:0
  |  xmin=2;
  |  xmax=3;
  |  [xmin xmax] =

```

Start OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Curr... ← □ ↗ ×

← ⌂ << m... 🔍

Name
bisection.m
bisection.m~
myfunc.m

bisection.m (MATLA

Perform one step o
bisection method

bisection(x1, ...

Command Window ↔ □ ↗ ×

```

>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2.1875

xmax =

    2.2500

>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2.2188

xmax =

    2.2500

```

fx >>

Workspace ↔ □ ↗ ×

🔍 🗑️ 🔗 Sel... ➡

Name	Value
xmax	2.2500
xmin	2.2188

Comman... ↔ □ ↗ ×

```

%-- 2/14/11 9:0
  |-- xmin=2;
  |-- xmax=3;
  |-- [xmin xmax] =
  |-- [xmin xmax] =
  |-- [xmin xmax] =

```

Start OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Curr... ← □ ↗ ×

← m... 🔍

Name
bisection.m
bisection.m~
myfunc.m

bisection.m (MATLA

Perform one step o
bisection method

bisection(x1, ...

Command Window ↔ □ ↗ ×

```
>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2.2344

xmax =

    2.2500

>> [xmin xmax] = bisection(xmin,xmax)

xmin =

    2.2344

xmax =

    2.2422

fx >>
```

Workspace ↔ □ ↗ ×

Sel... >>

Name	Value
xmax	2.2422
xmin	2.2344

Comman... ↔ □ ↗ ×

```
%-- 2/14/11 9:0
...xmin=2;
...xmax=3;
...[xmin xmax] =
...[xmin xmax] =
...[xmin xmax] =
```

Start OVR

```
Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/bisection_poly.m*
File Edit Text Go Cell Tools Debug Desktop Window Help
Stack: Base fx
- 1.0 + ÷ 1.1 x %>% %>%
1
2 function [ y1 y2 ] = bisection_poly( P, x1 , x2 )
3 % Perform one step of bisection method on the polynomial
4 % p(x) = a0 + a1*x + a2*x^2 + ... + aN*x^N
5 % P = [a0 ; a1 ; ... ; aN] (column vector) contains the polynomial coefficients
6 % Returns a narrower interval containing the solution
7
8 x_midpoint=(x1+x2)/2;
9 f1=0;
10 f2=0;
11 f_midpoint=0;
12
13 for i=1:size(P)
14     f1=f1+P(i)*x1^(i-1);
15     f2=f2+P(i)*x2^(i-1);
16     f_midpoint=f_midpoint+P(i)*x_midpoint^(i-1);
17 end
18
19 if(f_midpoint==0)
20     y1=x_midpoint;
21     y2=x_midpoint;
22
23 elseif(f1*f_midpoint<0)
24     y1=x1;
25     y2=x_midpoint;
26
27 else
28     y1=x_midpoint;
29     y2=x2;
30
31 end
32
```

Here we describe another function, which performs one step of bisection search on a general polynomial function $p(x)$

```
Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/bisection_poly.m*
File Edit Text Go Cell Tools Debug Desktop Window Help
Stack: Base fx
- 1.0 + ÷ 1.1 x %>% %>% ⓘ
1
2 function [ y1 y2 ] = bisection_poly( P, x1 , x2 )
3 % Perform one step of bisection method on the polynomial
4 % p(x) = a0 + a1*x + a2*x^2 + ... + aN*x^N
5 % P = [a0 ; a1 ; ... ; aN] (column vector) contains the polynomial coefficients
6 % Returns a narrower interval containing the solution
7
8 x_midpoint=(x1+x2)/2;
9 f1=0;
10 f2=0;
11 f_midpoint=0;
12
13 for i=1:size(P)
14     f1=f1+P(i)*x1^(i-1);
15     f2=f2+P(i)*x2^(i-1);
16     f_midpoint=f_midpoint+P(i)*x_midpoint^(i-1);
17 end
18
19 if(f_midpoint==0)
20     y1=x_midpoint;
21     y2=x_midpoint;
22
23 elseif(f1*f_midpoint<0)
24     y1=x1;
25     y2=x_midpoint;
26
27 else
28     y1=x_midpoint;
29     y2=x2;
30
31 end
32
```

Note the function `size(..)` which returns the length of a column vector. Also note the *if/elseif/else* structure.

Editor - /afs/cs.wisc.edu/u/s/i/sifakis/matlab_files/bisection_poly.m*

File Edit Text Go Cell Tools Debug Desktop Window Help

Stack: Base f_x

```
1 function [ y1 y2 ] = bisection_poly( P, x1 , x2 )
2 % Perform one step of bisection method on the polynomial
3 % p(x) = a0 + a1*x + a2*x^2 + ... + aN*x^N
4 % P = [a0 ; a1 ; ... ; aN] (column vector) contains the polynomial coefficients
5 % Returns a narrower interval containing the solution
6
7
8 x_midpoint=(x1+x2)/2;
9 f1=0;
10 f2=0;
11 f_midpoint=0;
12
13 for i=1:size(P)
14     f1=f1+P(i)*x1^(i-1);
15     f2=f2+P(i)*x2^(i-1);
16     f_midpoint=f_midpoint+P(i)*x_midpoint^(i-1);
17 end
18
19 if(f_midpoint==0)
20     y1=x_midpoint;
21     y2=x_midpoint;
22
23 elseif(f1*f_midpoint<0)
24     y1=x1;
25     y2=x_midpoint;
26
27 else
28     y1=x_midpoint;
29     y2=x2;
30
31 end
32
```

bisection_poly Ln 30 Col 1 OVR

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```
>> xmin=1;
>> xmax=2;
>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )

xmin =
    1.5000

xmax =
     2

>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )

xmin =
    1.5000

xmax =
    1.7500
```

Workspace

Name	Value
xmax	1.7500
xmin	1.5000

Command Window

```
%-- 2/14/11 9:0
    xmin=1;
    xmax=2;
    [xmin xmax] =
```

bisection.m (MATLAB)

Perform one step of bisection method

bisection(x1, ...)

Start

Here we use *bisection_poly* to solve the equation $x^2 - x - 1 = 0$ (near the root $x \sim 1.618..$)

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```

1.5000
xmax =
1.7500
>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )
xmin =
1.5000
xmax =
1.6250
>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )
xmin =
1.5625
xmax =
1.6250
fx >>

```

Workspace

Name	Value
xmax	1.6250
xmin	1.5625

Comman... 2/14/11 9:0

```

xmin=1;
xmax=2;
[xmin xmax] =

```

bisection.m (MATLA

Perform one step o
bisection method

bisection(x1, ...

Start

Here we use *bisection_poly*
to solve the equation
 $x^2 - x - 1 = 0$
(near the root $x \sim 1.618..$)

MATLAB 7.10.0 (R2010a)

File Edit Debug Desktop Window Help

/afs/cs.wisc.edu/u/s/i/sifakis/matlab_files

Shortcuts How to Add What's New

Command Window

```

1.5625
xmax =
1.6250
>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )
xmin =
1.5938
xmax =
1.6250
>> [xmin xmax] = bisection_poly ( [-1;-1;1] , xmin , xmax )
xmin =
1.6094
xmax =
1.6250
fx >>

```

Workspace

Name	Value
xmax	1.6250
xmin	1.6094

Comman... 2/14/11 9:0

```

x=1;
x=2;
[xmin xmax] =

```

bisection.m (MATLA

Perform one step o
bisection method

bisection(x1, ...

Start

Here we use *bisection_poly*
to solve the equation
 $x^2 - x - 1 = 0$
(near the root $x \sim 1.618..$)

The screenshot shows the MATLAB 7.10.0 (R2010a) environment. The Command Window contains the following code and output:

```
>> x=-pi:.5:pi
x =
Columns 1 through 7
-3.1416 -2.6416 -2.1416 -1.6416 -1.1416 -0.6416 -0.1416
Columns 8 through 13
0.3584 0.8584 1.3584 1.8584 2.3584 2.8584
>> y=sin(x)
y =
Columns 1 through 7
-0.0000 -0.4794 -0.8415 -0.9975 -0.9093 -0.5985 -0.1411
Columns 8 through 13
0.3508 0.7568 0.9775 0.9589 0.7055 0.2794
>> plot(x,y)
fx >>
```

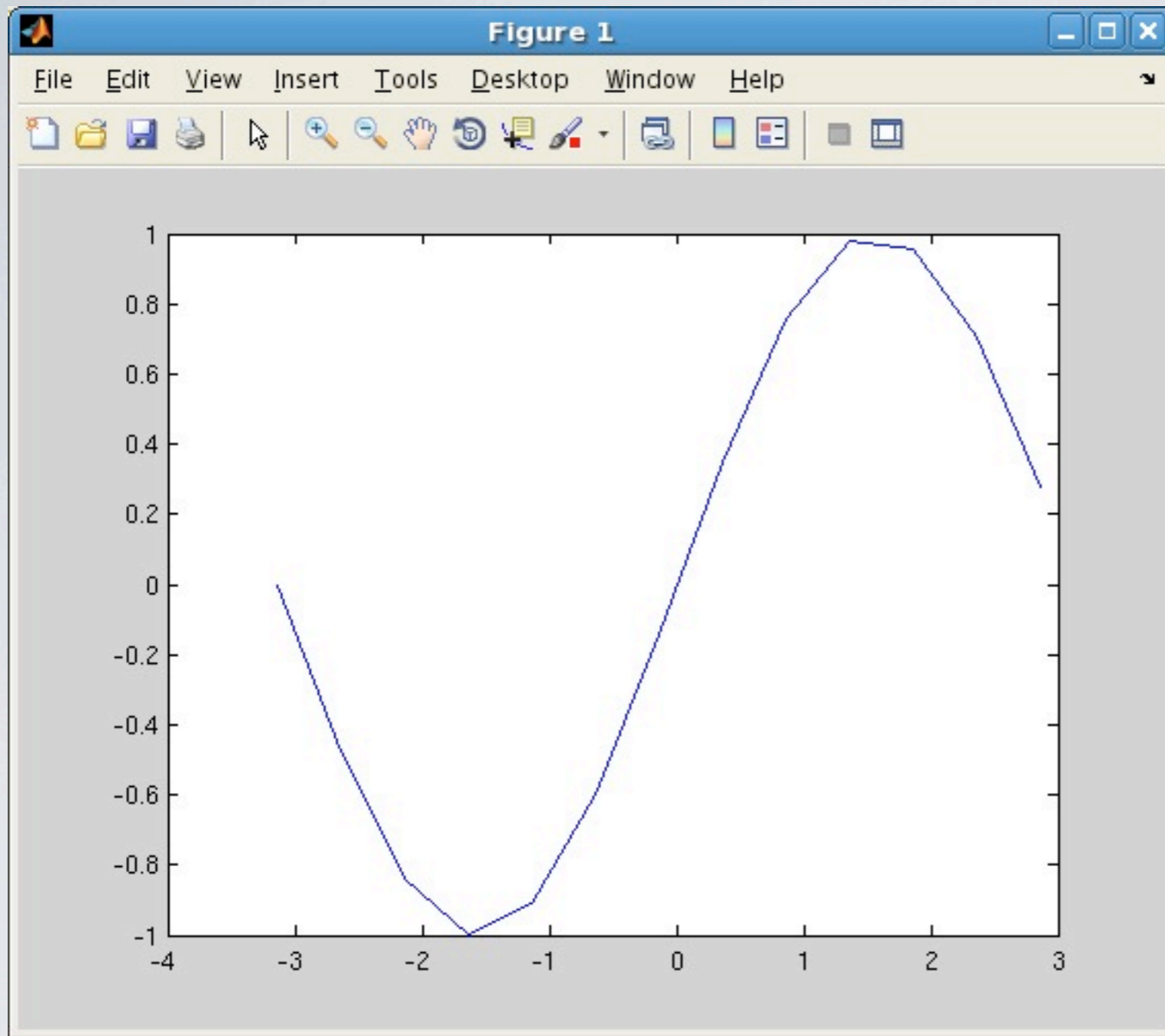
The Workspace window shows the following variables:

Name	Value
x	<1x13 double>
y	<1x13 double>

The Command Window history shows the following commands:

```
%-- 2/15/11 8:0
x=-pi:.5:pi
y=sin(x)
plot(x,y)
```

To generate a plot, we define a vector (say, x) of variable values, and another vector (say, y) of function values. The command $plot(x,y)$ connects them with a line



files

Workspace

Name	Value
x	<1x13 doub
y	<1x13 doub

416 -0.6416 -0.1416

584 2.8584

093 -0.5985 -0.1411

Command Window

```
%-- 2/15/11 8:0
x=-pi:.5:pi
y=sin(x)
plot(x,y)
```

Select a file to view

```
>> plot(x,y)
fx >>
```

0.3508 0.7568 0.9775 0.9589 0.7055 0.2794

Start

To generate a plot, we define a vector (say, x) of variable values, and another vector (say, y) of function values. The command $plot(x,y)$ connects them with a line

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window contains the following code:

```
>> x=-pi:.01:pi;  
>> y=sin(x);  
>> plot(x,y);  
>>
```

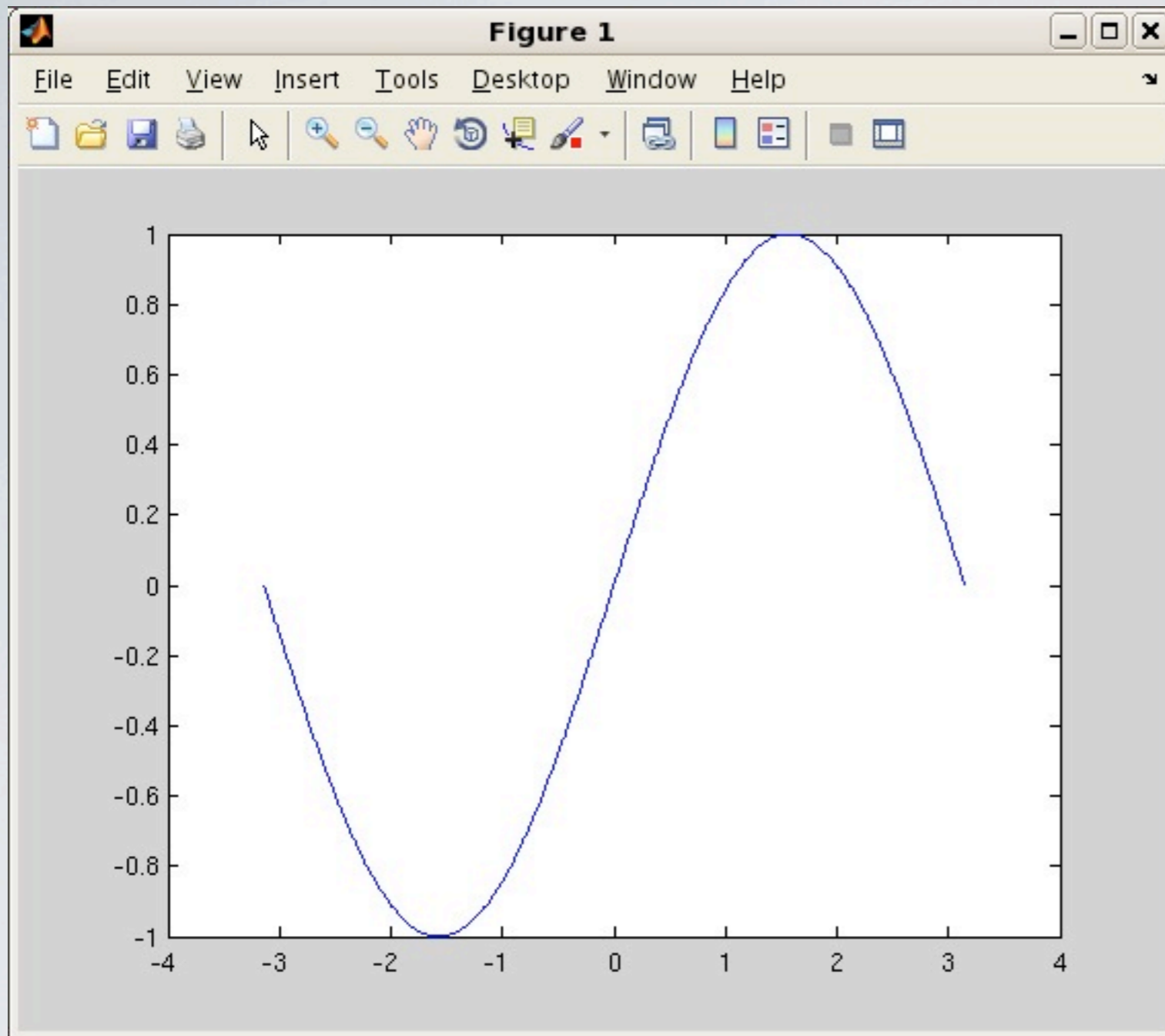
The Workspace window shows the following variables:

Name	Value
x	<1x629 dou
y	<1x629 dou

The Command Window also shows a history of commands:

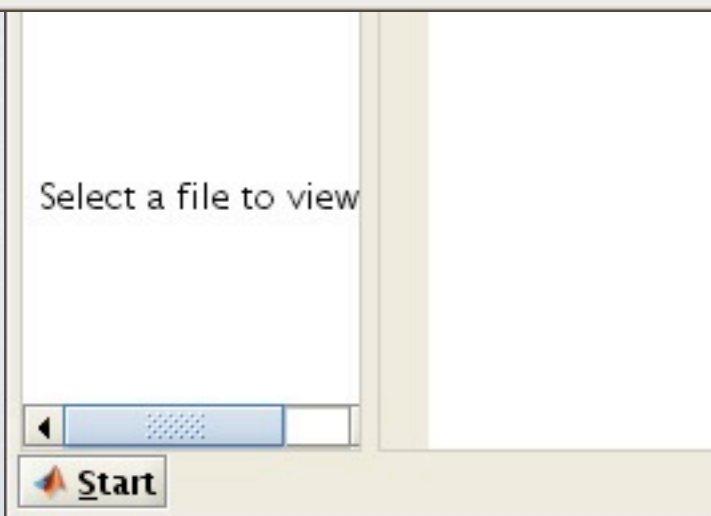
```
%-- 2/15/11 8:0  
x=-pi:.5:pi  
y=sin(x)  
plot(x,y)  
x=-pi:0.01:pi  
x=-pi:.01:pi;
```

If we decrease the step size in defining x and y , the resulting plot will be smoother, instead of a jagged curve of line segments



```
%-- 2/15/11 8:00
x=-pi:.5:pi
y=sin(x)
plot(x,y)
x=-pi:0.01:pi
x=-pi:.01:pi;
```

Name	Value
x	<1x629 dou
y	<1x629 dou



If we decrease the step size in defining x and y , the resulting plot will be smoother, instead of a jagged curve of line segments

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window contains the following code:

```
>> x=-1:0.01:2;  
>> y=x.^3+2*x-1;  
>> z=exp(x);  
>> plot(x,y,x,z);  
>> xlabel('This is the X-axis');  
>> ylabel('This is the Y-axis');  
>> title('This is the plot title');  
>>
```

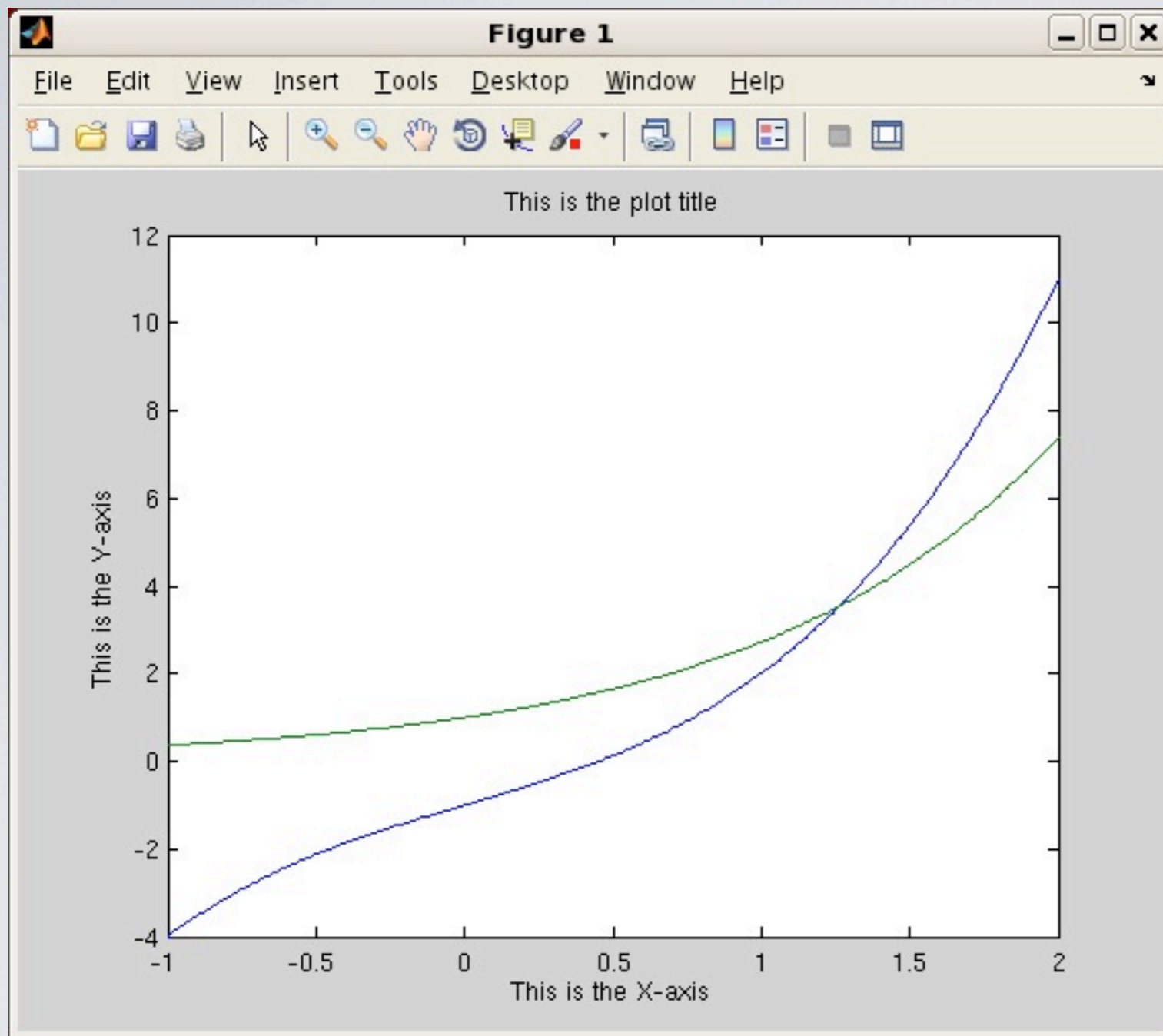
The Workspace window shows the following variables and their values:

Name	Value
x	<1x301 dou
y	<1x301 dou
z	<1x301 dou

The Command Window also shows the execution history:

```
plot(x,y,x,z)  
xlabel('This  
ylabel('This  
title('This  
x=-1:0.01:2;
```

We can also draw several curves on the same plot by calling $plot(x_1, y_1, x_2, y_2 \dots x_N, y_N)$. Note the use of operator $.$ to denote raising to a power on an element-by-element basis



files

Workspace

Name	Value
x	<1x301 dou
y	<1x301 dou
z	<1x301 dou

Command Window

```

plot(x,y,x,z)
xlabel('This
ylabel('This
title('This
x=-1:0.01:2;

```

Select a file to view

Start

We can also draw several curves on the same plot by calling $plot(x_1, y_1, x_2, y_2 \dots x_N, y_N)$. Note the use of operator $.$ to denote raising to a power on an element-by-element basis

The image shows the MATLAB 7.10.0 (R2010a) interface. The Command Window contains the following code:

```
>> x=-1:0.01:2;
>> y=x.^3+2*x-1;
>> z=exp(x);
>> plot(x,y,x,z);
>> xlabel('This is the X-axis');
>> ylabel('This is the Y-axis');
>> title('This is the plot title');
>> print -dps figure.ps
>> print -dpdf figure.pdf
>>
```

The Workspace window shows the following variables and their values:

Name	Value
x	<1x301 dou
y	<1x301 dou
z	<1x301 dou

The Command Window also shows the execution of the plot and print commands:

```
ylabel('This
title('This
x=-1:0.01:2;
y=x.^3+2*x-1
z=exp(x);
plot(x,y,x,z
```

The figure.pdf (pdf File) window shows "No details available".

We can output the current plot to a Postscript or PDF file, using the commands *print -dps <filename>* or *print -dpdf <filename>*