### CS 367 - Introduction to Data Structures Thursday, March 31, 2016

Homework 7 due 10 pm tomorrow, April 1st

Program 4 due 10 pm Sunday, April 17th

#### Last Time

Binary Search Tree (BST)

- BSTnodes
- BST class
- implementing print
- implementing lookup, insert, delete
- complexities of BST methods

CS Options/Courses

#### Today

Classifying Binary Trees Balanced Search Trees Red-Black Trees

- tree properties
- print, lookup
- insert

#### **Next Time**

**Read:** start *Graphs* Finish Red-Black Trees ADTs/Data Structures Revisited Graphs

• terminology

# **Classifying Binary Trees**

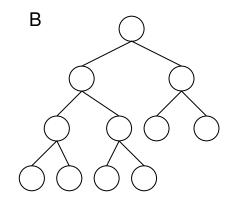
Full

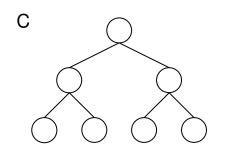
Complete

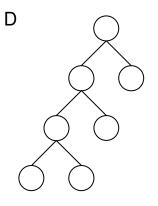
Height-balanced

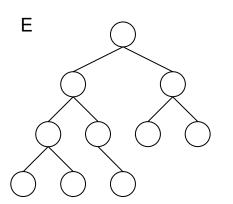
Balanced

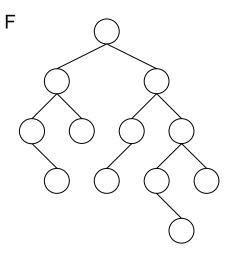
A Q











 $\rightarrow$  Identify which trees below are full, complete and/or height balanced.

## **Balanced Search Trees**

Goal:

Idea:

AVL

**BTrees** 

# **Red-Black Trees (RBT)**

**RBT**:

Example:

## **Red-Black Tree Properties**

root property

red property

black property

#### **Red-Black Tree Operations**

print lookup

insert

delete

## Inserting into a Red-Black Tree

Goal: insert key value K into red-black tree T and \_\_\_\_\_.

#### If T is Empty

#### If T is Non-Empty

- step down tree as done for BST
- add a leaf node containing K as done for BST, and \_\_\_\_\_\_
- •

#### → Which of the properties might be violated as a result of inserting a red leaf node?

root property

black property

red property

**Non-Empty Case 1:** K's parent P is black

# Non-Empty Case 2

Non-Empty Case 2: K's parent P is red

Fixing an RBT

Tri-Node Restructuring is done if P's sibling S is null

Recoloring is done if P's sibling S is red

## Practice

 $\rightarrow$  1. Starting with an empty RBT, show the RBT that results from inserting 7 and 14.

 $\rightarrow$  2. Redraw the tree from above and then show the result from inserting 18.

 $\rightarrow$  3. Redraw the tree from above and then show the result from inserting 23.

 $\rightarrow$  4. Redraw the tree from above and then show the result from inserting 1 and 11.

 $\rightarrow$  5. Redraw the tree from above and then show the result from inserting 20.

## **More Practice!**

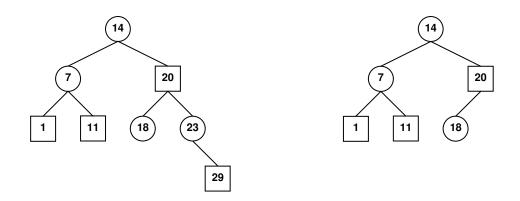
 $\rightarrow$  6. Redraw the tree from the previous page and then show the result from inserting 29.

→ 7. Insert the same list of values into an empty BST: 7, 14, 18, 23, 1, 11, 20, 29

 $\rightarrow$  What does this demonstrate about the differences between a BST and RBT?

## **More Practice?**

 $\rightarrow$  8. Show the result from inserting 25 in the RBT below.



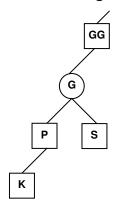
 $\rightarrow$  9. Redraw the tree from above and then show the result from inserting 27.



# **Cascading Fixes**

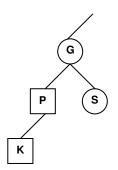
#### Fixing an RBT UPDATED!

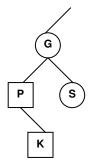
Recoloring is done if P's sibling S is red



 change P & S to black
if G is the root – done otherwise change G to red

Tri-Node Restructuring is done if P's sibling S null





# **RBT Complexity**

print

lookup

insert