

# CS/ECE 252: INTRODUCTION TO COMPUTER ENGINEERING

## UNIVERSITY OF WISCONSIN—MADISON

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*Midterm Examination 2*

*In Class (50 minutes)*

*Friday, October 24, 2014*

*Weight: 17.5%*

**NO: BOOK(S), NOTE(S), OR CALCULATORS OF ANY SORT.**

The exam has **nine** pages. **Circle your final answers.** Plan your time carefully since some problems are longer than others. You **must turn in the pages 1-9**. Use the blank sides of the exam for scratch work.

LAST NAME: \_\_\_\_\_

FIRST NAME: \_\_\_\_\_

ID#: \_\_\_\_\_

<b>Problem</b>	<b>Maximum Points</b>	<b>Points Earned</b>
<b>1</b>	4	
<b>2</b>	6	
<b>3</b>	3	
<b>4</b>	5	
<b>5</b>	3	
<b>6</b>	9	
<b>Total</b>	30	

**Problem 1**

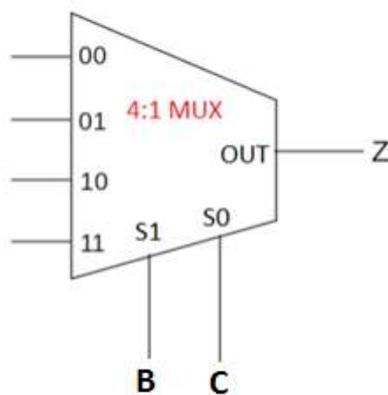
**(4 Points)**

Consider the logic equation  $Z = B \text{ OR } (A \text{ AND } C)$ .

a. (1 point) Draw a **gate-level** circuit for Z using NOT gates and 2-input AND/OR gates.

b. (1 points) Draw a **gate-level** circuit for Z using only 2-input NAND gates.

c. (2 points) Implement a logic circuit for Z using a 4x1 multiplexer where B and C are connected to the select lines. Draw your answer using the 4x1 multiplexer below. **Do not use any additional logic gates.**



**Problem 2**

**(6 Points)**

The finite state machine (FSM) below (in Figure 1(a)) recognizes a certain bit sequence. The machine takes one input every clock cycle, which can be 1 or 0. The machine outputs a '1' when this certain bit sequence is recognized; otherwise it outputs a '0'. Each state is represented as  $S_1S_0$ . For example, the state marked as "01" has  $S_1 = 0$ , and  $S_0 = 1$ .  $X$  is the output in each state.  $S_1'S_0'$  represents the next state. Assume that the initial state is 00.

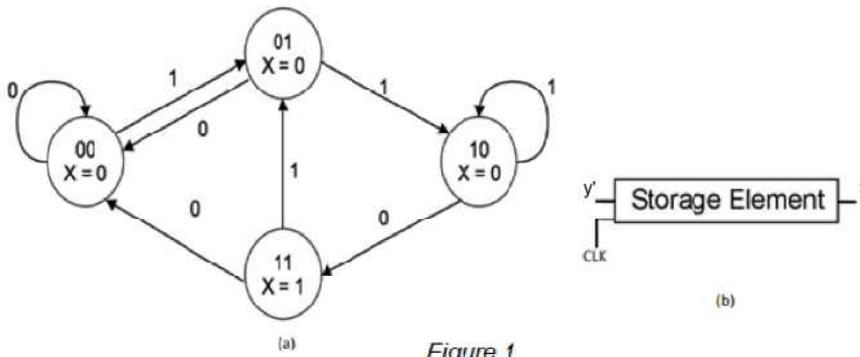


Figure 1

a. (2 points) Complete the Next State truth table for the FSM.

$S_1$	$S_0$	IN	$S_1'$	$S_0'$

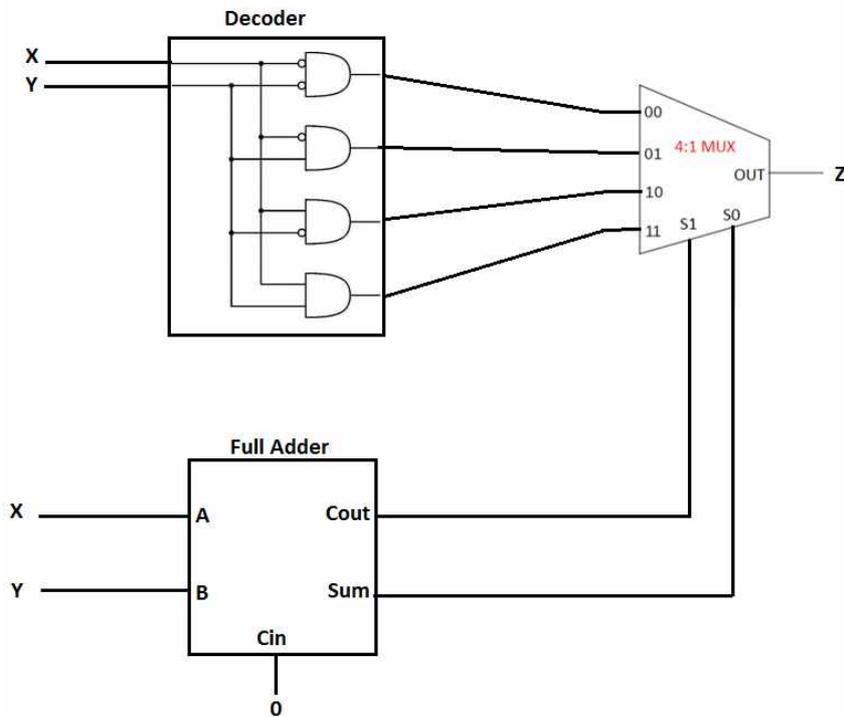
b. (3 Points) Draw the logic circuit which implements the above FSM using combinational logic and flip flops. Use representation shown in figure 1(b) for any 1-bit flip flop required in the circuit (where CLK is the clock). You can use any kind of logic gates for implementing the combinational logic. Note: You should implement both the states ( $S_1, S_0$ ) as well as the output ( $X$ ).

c. (1 point) Which bit sequence does the above FSM recognize? Your answer should be a string of bits (e.g, "1001" or "11001").

**Problem 3**

**(3 Points)**

Consider the following circuit containing a multiplexer, a single-bit full adder and a decoder. X and Y are inputs to this circuit, and the circuit produces an output Z. Fill in the truth table below for this combinational circuit.



X	Y	Z

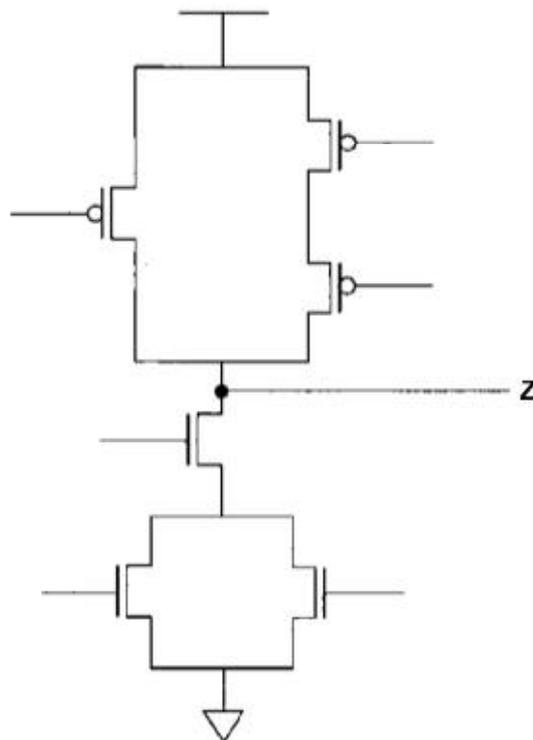
**Problem 4****(5 Points)**

Consider the logic equation  $Z = \text{NOT}(A \text{ AND } \text{NOT}(\text{NOT}(C) \text{ AND } \text{NOT}(B)))$ . (Hint: You may want to use DeMorgan's law to simplify the equation.)

a. **(2 points)** Fill out the following truth table for Z.

A	B	C	Z
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

b. **(3 points)** Label the inputs on the transistor-level circuit below so that the circuit implements the logic function Z.





**Problem 6**

**(9 Points)**

a. **(1 point)** What is the addressability (number of bytes per memory location) of a 1024 byte memory which uses 9 bits for each memory address? Show your work.

b. **(2 points)** How many different n-input Boolean functions are possible? Show your work.

c. **(1 point)** How many select lines does an n-input mux have?

d. **(1 point)** How many outputs does an n-input decoder have?

e. **(1 point)** Mention two important things that happen during the FETCH phase of the instruction cycle.

f. **(2 points)** How many n-type transistors are present in a 16-bit wide register? Show your work.

g. **(1 Point)** Which of the following stages of instruction processing are required for the processing of an ADD instruction which reads value of 2 registers and stores the final value into another register. Circle all that apply:

- Fetch
- Decode
- Evaluate address
- Fetch operands from the memory
- Execute Operation
- Store result