Midterm Examination 1

In Class (50 minutes)

Friday, February 15, 2013

Weight: 17.5%

NO: BOOK(S), NOTE(S), OR CALCULATORS OF ANY SORT.

The exam has 108 pages. Circle your final answers. Plan your time carefully since some problems are longer than others. You must turn in the pages 1-8.

LAST NAME: __________________________________________________________

FIRST NAME: __________________________________________________________

ID#: _________________________________________________________________
<table>
<thead>
<tr>
<th>Problem</th>
<th>Maximum Points</th>
<th>Points Earned</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>30</strong></td>
<td></td>
</tr>
</tbody>
</table>
Problem 1
(9 Points)
For the following problems, circle the best answer. Choose only one answer per question.

i. There are n bits to represent all the students in a class, and the students are numbered 0-67. What is the value of n?
   a. 5
   b. 4
   c. 6
   d. 7

ii. Which of the following two’s complement binary numbers is a multiple of 2 (even).
   a. 1010101
   b. 1101011
   c. 0111010
   d. 1110111

iii. Which of the following are properties of an algorithm?
   a. Each step has to be precisely stated.
   b. The program implementing it has to use a minimum amount of memory.
   c. The procedure should terminate.
   d. a and c.
   e. b and c.

iv. Which of the following have two representations for 0?
   a. Two’s complement
   b. Signed magnitude
   c. All of the above
   d. None of the above

v. Two computers A and B are identical except that A has a multiply instruction and B does not. Both have add instructions. Assume the multiply and add instructions take the same amount of time to operate on two numbers. Which of the following is true about computers A and B?
   a. B can compute all the same problems as A, in the same amount of time.
   b. B can compute all the same problems as A, in the same amount of time, given enough memory.
   c. B can compute all the same problems as A, but might take longer.
   d. A can compute more types of problems than B.
vi Which of the following is the fixed point binary representation of $4^{3/8}$?
   a  0100.011
   b  010.011
   c  0110.101
   d  0100.101

vii What is the largest positive value that can be represented by an 9-bit two’s complement integer?
   a  512
   b  511
   c  255
   d  256

viii What is the most negative value that can be represented by a 4-bit two’s complement integer?
   a  -7
   b  -8
   c  -16
   d  -15

ix When using two’s complement notation, which of the following bit patterns represent the negation of 01011010?
   a  10100101
   b  10010110
   c  10010100
   d  10100110
Problem 2  
(4 Points)

a  Convert the ASCII string “Q@t5” to its hexadecimal representation. Only represent the characters within the quotation marks and assume that the string is null terminated. **Hint:** See attached ASCII to hexadecimal table.  
0x51 40 74 35 00

b  Convert the following binary code into an ASCII string.  
0101 1001 0011 0000 0110 1100 0010 110 0000 0000

Y01*

Problem 3  
(3 Points)

Consider the 8-bit binary pattern 1001 0011. What decimal (base 10) value does it represent if we interpret it as:

a  An unsigned integer?  
147

b  A signed magnitude integer?  
-19

c  A two’s complement integer?  
-109
Problem 4
(2 Points)
Perform binary arithmetic for the following pairs of 2’s complement numbers and specify whether or not there is an overflow. Illustrate your answer by converting the operands and result to decimal. Assume the result has the same number of bits as the operands.

a
\[\begin{array}{c}
110 -2 \\
+ 110 -2 \\
\hline
100 -4 \text{ No overflow}
\end{array}\]

b
\[\begin{array}{c}
0101 5 \\
- 1011 -(-5) \\
\hline
1010 -6 \text{ Overflow}
\end{array}\]

Problem 5
(3 Points)
Suppose we have two operands X and Y, where X = 0x34 and Y = 0xAF.

a Convert X and Y into binary.

X=0011 0100
Y=1010 1111

b What is the result of X AND Y? Give your answer in hexadecimal.

0010 0100 = 0x24

c What is the result of X OR Y? Give your answer in hexadecimal.

1011 1111 = 0xBF
Problem 6  
(2 Points)  
Show the result of performing the following bitwise logic operations:

a  \[(\text{NOT}(0011)) \text{ AND } (0110 \text{ OR } 1011)\]

\[1100\]

b  \[\text{NOT}(01001 \text{ OR } (01100 \text{ AND } 10100))\]

\[10010\]

Problem 7  
(1 Point)  
What is the difference between an instruction set architecture (ISA) and a microarchitecture?  
Give your answer in one sentence.

A microarchitecture is the particular way an ISA is implemented on a processor.

Problem 8  
(2 Points)  
Suppose we have two 4-bit 2's complement integers 0101 and 1010. Express their sum as an 8-bit 2's complement number.

\[1111\ 1111\]
Problem 9

Below is a single-precision floating point representation of some value. Note that the exponent bits have been left out.

\[ 0 \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ 11000100000000000000000000000000 \]

Recall that the bits for the IEEE floating point number are as follows:

<table>
<thead>
<tr>
<th>Sign (1 bit)</th>
<th>Exponent (8 bits)</th>
<th>Fraction (23 bits)</th>
</tr>
</thead>
</table>

where \( N = (-1)^{\text{sign}} \times 2^{\text{exponent} - 127} \times 1.\text{fraction} \)

a) Find the smallest value for the exponent field such that the represented number is greater than the decimal value 4.0. Give your answer in binary. (3 Points)

\[
(-1)^0 \times 2^{\text{exponent} - 127} \times 1.110001_2 > 4 \\
\frac{113}{64} > 2^2 \times 2^{127-\text{exponent}} \\
\text{exponent} > 129 - \log(113/64) \\
\text{min val or exponent} = 129 => 1000001 
\]

b) What is the decimal value of the number represented in part a? (1 Point)

\[
(-1)^0 \times 2^2 \times 1.110001_2 = 111.0001_2 = 7\frac{1}{16} 
\]