

ECE/CS 707

Mobile and Wireless Networking

Introduction to MIMO

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Today's agenda

- Overview of MIMO communications
- Single-user MIMO
- Multi-user MIMO
- Network MIMO

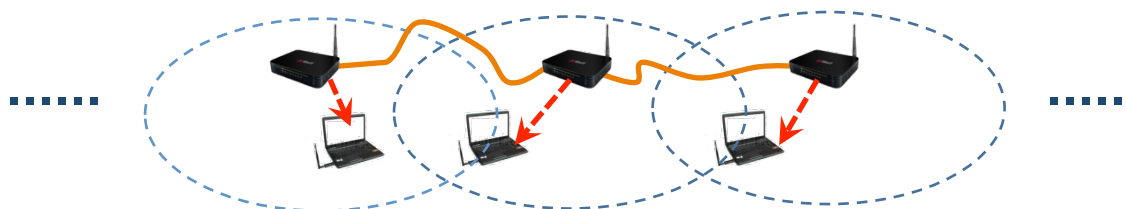
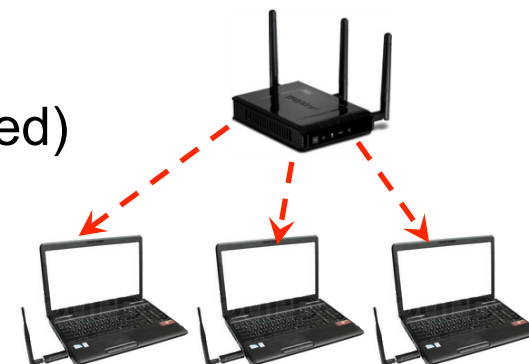
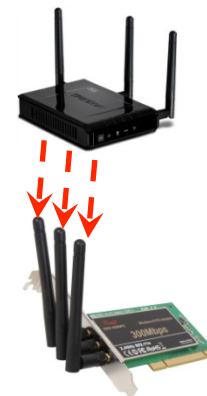
MIMO: an Overview

- MIMO (Multiple-Input Multiple-Output)
 - Transmitter/receiver can have multiple antennas
 - A modern wireless communication technology
 - * Theory: late 1980's
 - * Standards and products: after 2000's
 - * Now: core feature in WLAN (802.11 WiFi) and cellular (3G LTE, WiMax)
 - Two benefits, simply put
 - * Improve link SINR
 - * Improve link concurrency



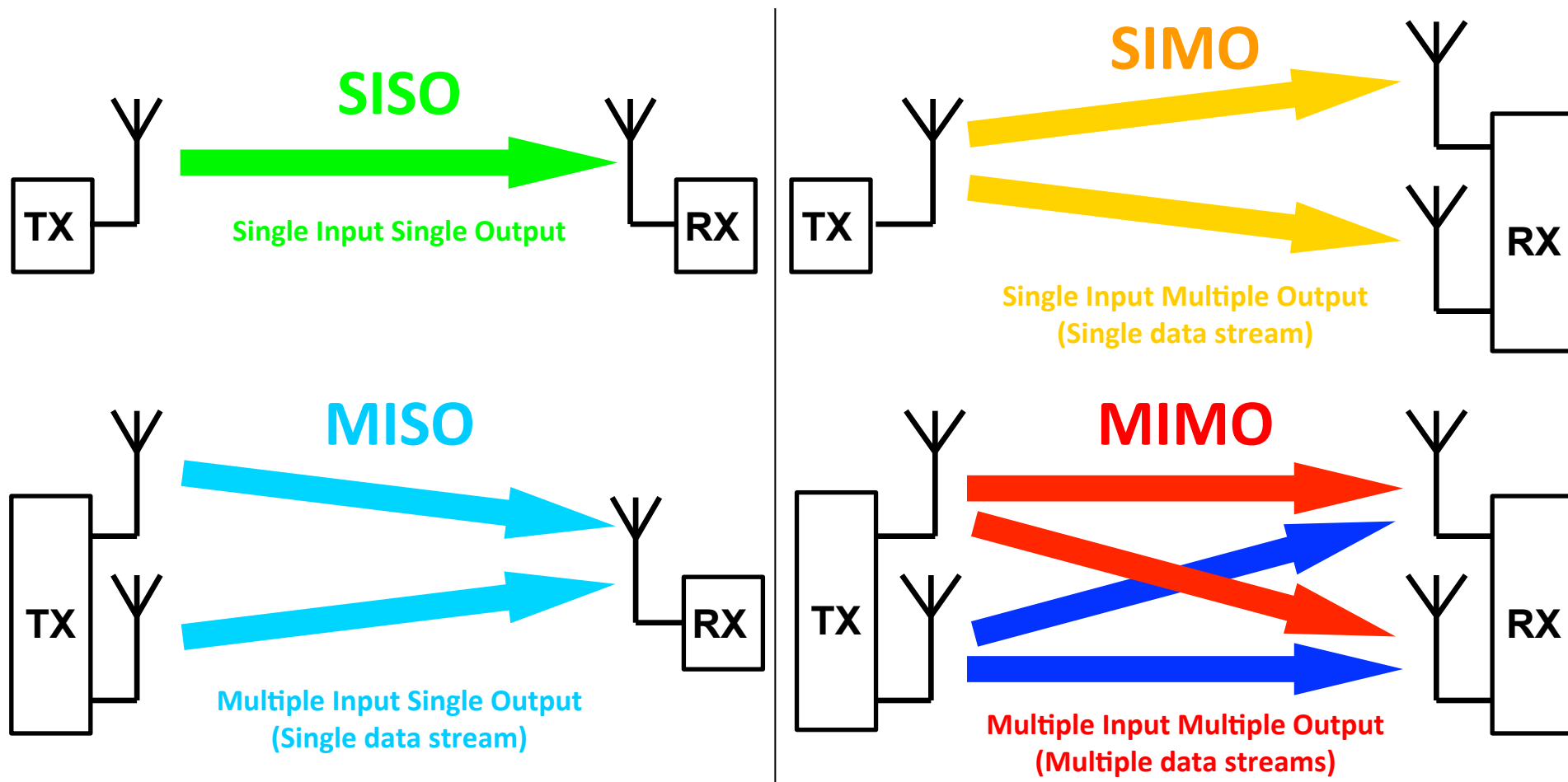
MIMO: an Overview

- MIMO network architectures
 - Single-user MIMO (in 802.11n-2009, LTE)
 - * One TX, one RX. Either TX or RX or both can have multiple antennas
 - Multi-user MIMO (in 802.11ac-2014, LTE-Advanced)
 - * One TX, multiple RX. Parallel transmissions.
 - Network MIMO (expected in near-future)
 - * Multiple TX, multiple RX. Parallel transmissions.



Single-user MIMO

- Basic communication modes



MIMO benefits: an audio metaphor



SISO



SIMO



MISO



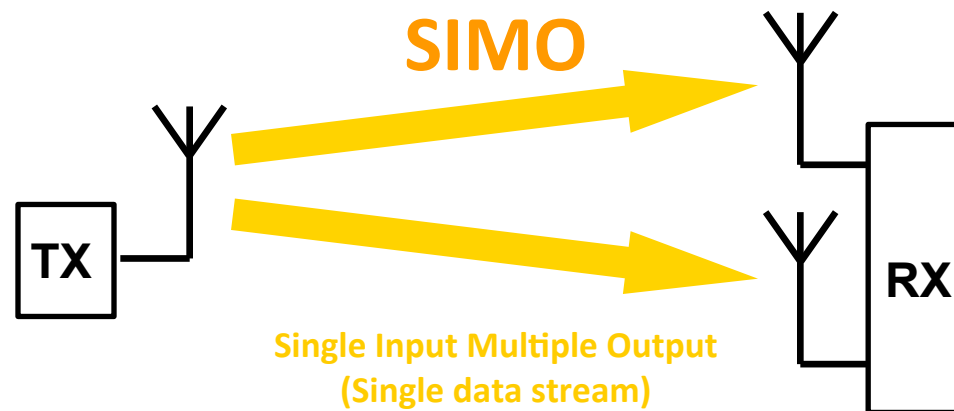
MIMO

Single-user MIMO benefits: capacity gains

- Diversity gain
 - Receiver diversity
 - Transmit diversity
- Multiplexing gain
 - Spatial multiplexing

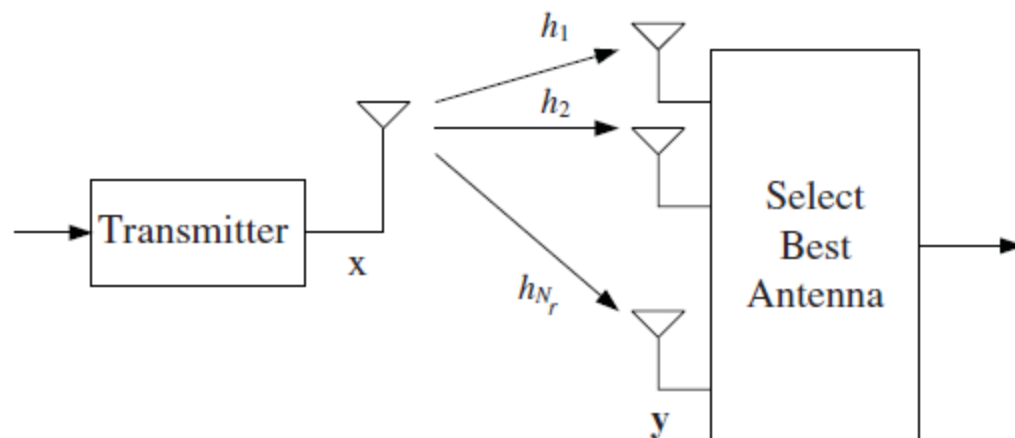
Receiver diversity

- Receiver coherently combines signals received by multiple antennas



- Asymptotic gain: Increasing SNR proportionally to N_r (#of receive antennas)
 - * Intuition: received signal power adds up
- What's the capacity gain?
 - * Logarithmically, according to Shannon's equation: $C = B \log(1 + \text{SNR})$
 - * When SNR is low, $\log(1 + \text{SNR}) \approx \text{SNR}$, so gain is almost linear w.r.t. N_r

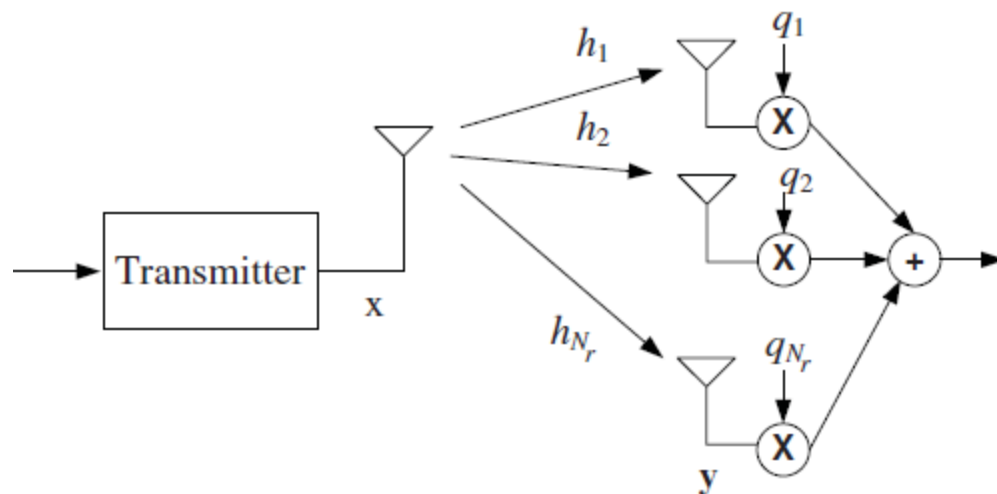
Implementing receiver diversity



- * Selection combining

Improves SNR to

$$avgSNR \cdot \left(1 + \frac{1}{2} + \dots + \frac{1}{N_r}\right)$$

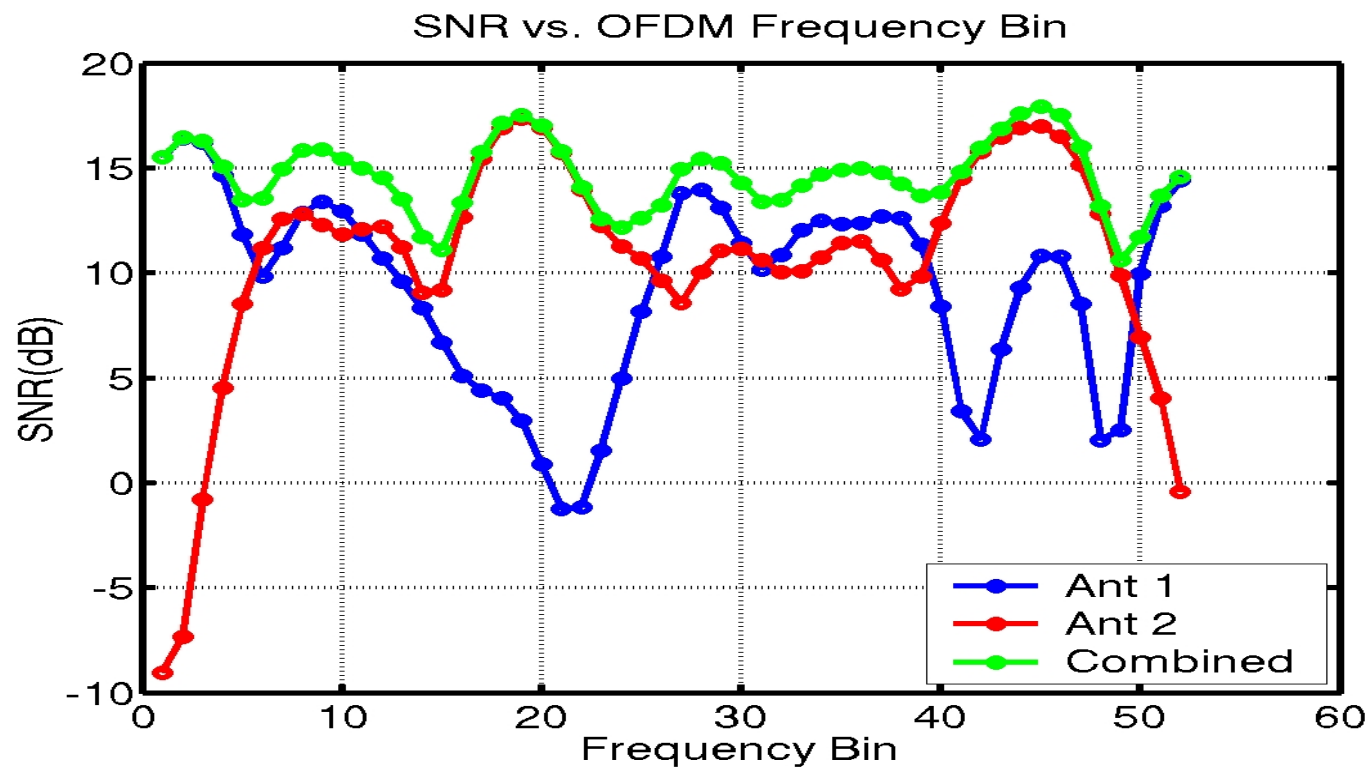


- * Maximum Ratio combining

Improves SNR to

$$\sum_{i=1}^{N_r} SNR_i$$

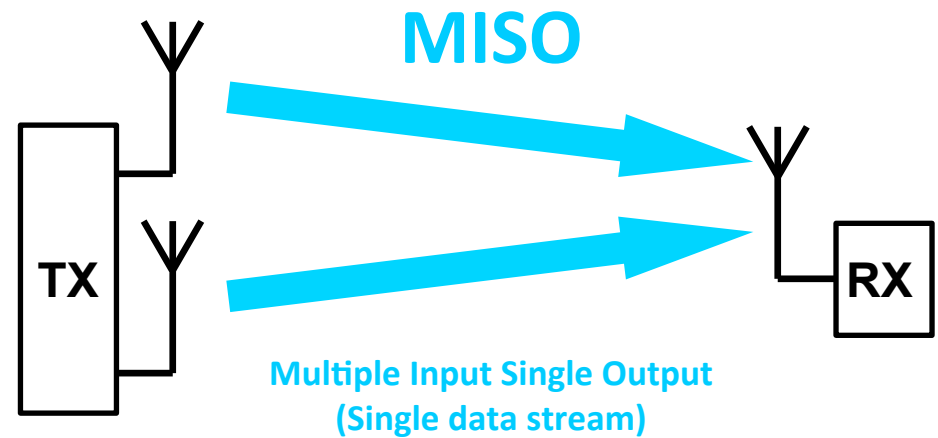
Mitigating fading with receiver diversity



- Multiple receive antennas allow compensation of by non-notches in the other

Transmitter diversity

- Transmitter sends multiple versions of the same signal, through multiple antennas



- Two modes of transmit diversity
 - * Open-loop transmit diversity
 - * Closed-loop transmit diversity

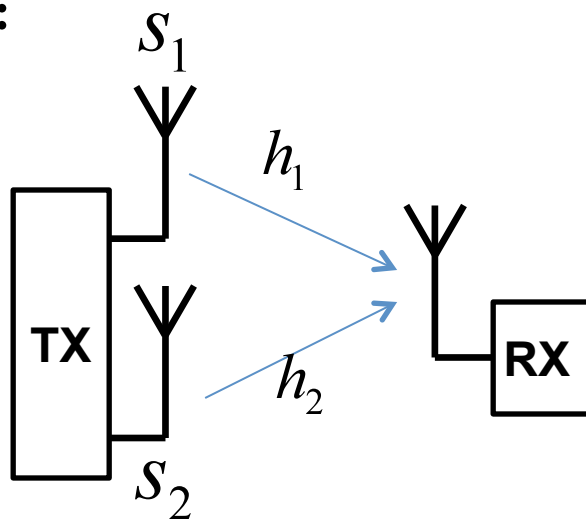
Open-loop transmit diversity

- Principle
 - Send redundant versions of the same signal (symbol), over multiple time slots, and through multiple antennas
 - Encode the symbols differently for different time slots and TX antennas
 - * Space-Time Block Code (STBC)

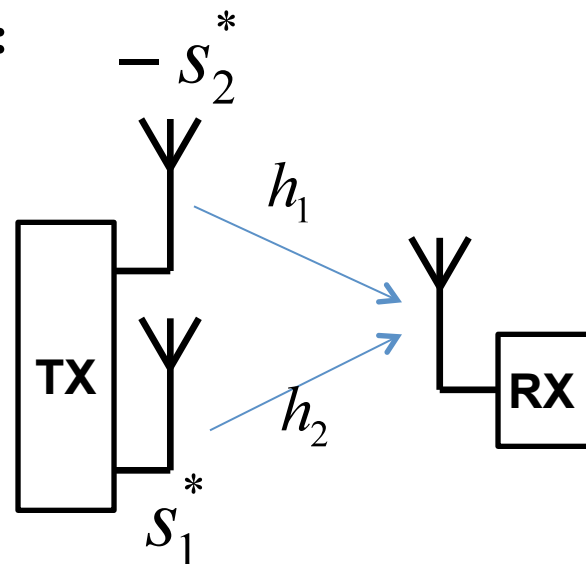
Open-loop transmit diversity

- Example: 2 TX antenna STBC
 - Send two data symbols, s_1 and s_2

Time slot 1:



Time slot 2:



- Received signals:

$$r(t_1) = h_1 s_1 + h_2 s_2$$

$$r(t_2) = -h_1 s_2^* + h_2 s_1^*$$

Open-loop transmit diversity

- Example: 2 TX antenna STBC

- Diversity combining

$$y_1 = h_1^* r(t_1) + h_2 r(t_2) = (|h_1|^2 + |h_2|^2) s_1$$

- i.e., signal power is boosted from $|h_1|^2$ to $|h_1|^2 + |h_2|^2$

- Open-loop transmit diversity gain:

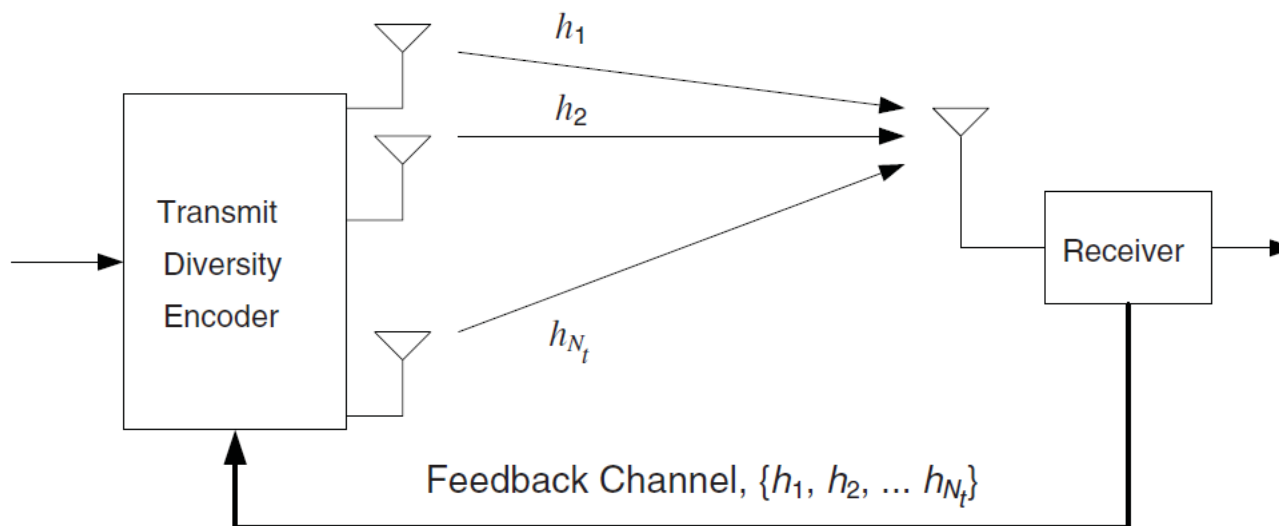
In general, open-loop transmit diversity increases SNR **linearly** with the number of transmit antennas

- What's the capacity gain?

Closed-loop transmit diversity

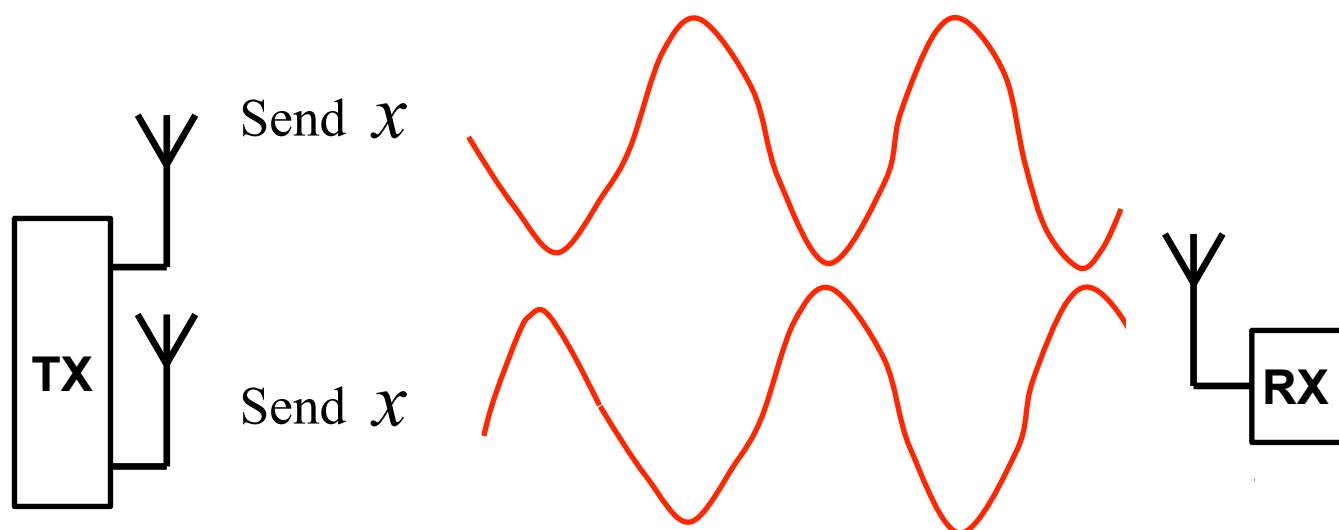
- Principle

- Send redundant versions of the same signal (symbol), over the same time slot
- Encode the symbols differently for different TX antennas
 - * i.e., weight the symbols on different antennas, following a precoding algorithm
 - * Precoding design requires feedback of channel state information (CSI)



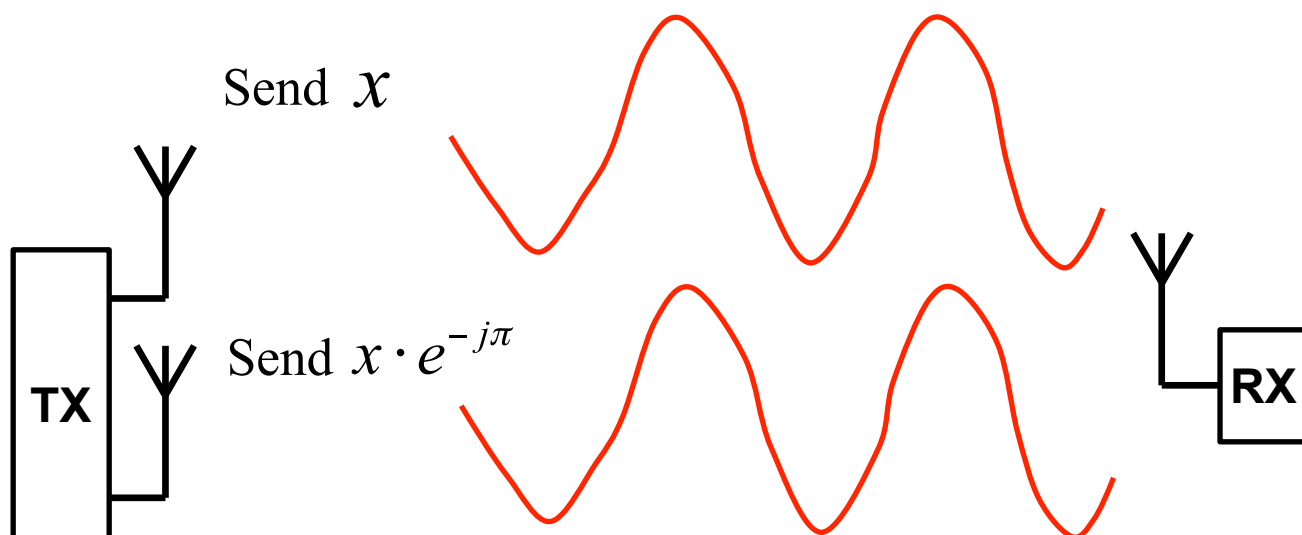
Closed-loop transmit diversity

- Why precoding?
 - Signals from different antennas need to sync (align) their phases
 - But the different channels (between TXantennas and RXantenna) distort signals differently, causing phase offset
- * e.g., both TX antennas sends $x = e^{j2\pi f t}$; RX may receive $e^{j2\pi f t}$ from one TX antenna, but $e^{j(2\pi f t + \pi)}$ from the other, which weaken each other!



Closed-loop transmit diversity

- How does precoding help?
 - Precoding: TX compensates the phase offset, and aligns the phases of signals going through different channels



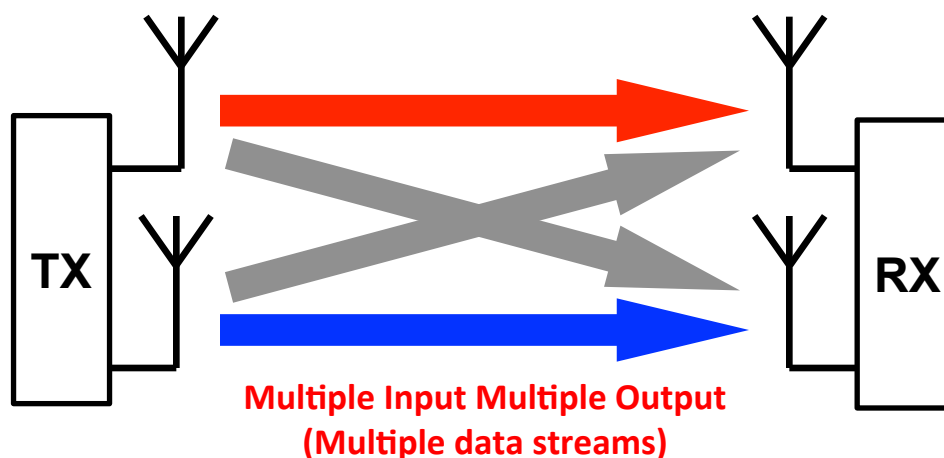
- Why CSI feedback is needed for precoding?
 - * TX must know the phase offset, in order to perform compensation

Closed-loop transmit diversity

- Asymptotic gain from closed-loop transmit diversity
 - Signal level combining, also called transmit beamforming
 - * Suppose we have 2 transmit antennas, then instead of x , we receive: $x+x=2x$, received power becomes $4 |x|^2$, SNR increases to 4 times!
 - * More generally, with N_t TX antennas, SNR increases to N_t^2
 - * What's the capacity gain?

Spatial multiplexing

- Spatial multiplexing concept
 - Form multiple independent links (on the same spectrum band) between TX and RX, and send data in parallel through them
 - Unfortunately, there is cross-talk between antennas
 - Cross-talk must be removed by digital signal processing algorithms



Spatial multiplexing: signal processing

- Example 2x2 MIMO spatial multiplexing

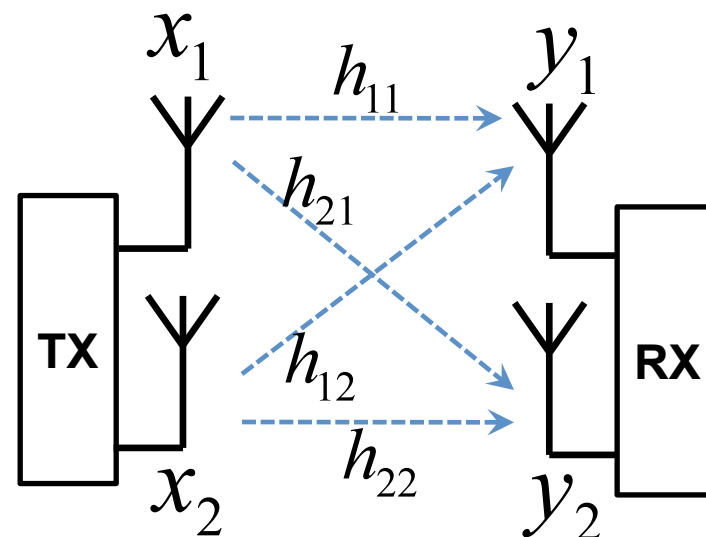
- Data to be sent over two TX antennas:

$$x_1, x_2$$

- Data received on two RX antennas:

$$y_1 = h_{11}x_1 + h_{12}x_2$$

$$y_2 = h_{21}x_1 + h_{22}x_2$$



- * Channel distortions: h_{**} can be estimated by the receiver
- * Only two unknowns: x_1, x_2 , easily obtained by solving the equations!

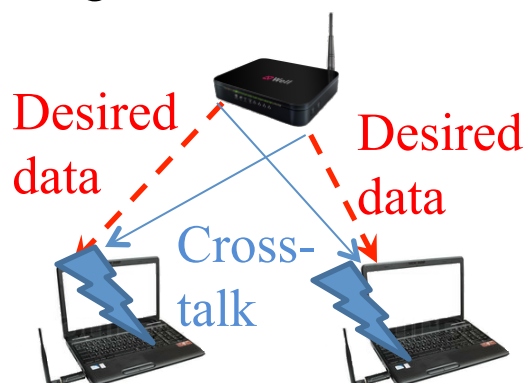
Spatial multiplexing gain

- Asymptotic gain
 - In general, capacity gain from spatial multiplexing scales linearly with
 $\min(N_t, N_r)$
- In practice
 - Spatial multiplexing gain also depends on channel “condition”
 - * If the channels between different antennas are *correlated*, e.g., h_{**} are all the same, then you can’t solve the equations. Spatial multiplexing becomes infeasible!
 - * Channel condition can be profiled using “condition number” (see reference)
 - Practical wireless devices’ multiple antennas are separated sufficiently far (further than half-wavelength), so the channel is usually uncorrelated

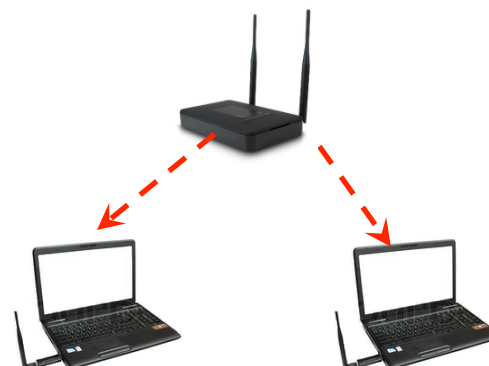
Multi-user MIMO

- Concept of Multi-User MIMO (MU-MIMO)

- * Single-antenna network



- * Multi-user MIMO



- * MU-MIMO enables multiple streams of data to be sent to different users in parallel, without cross-talk interference

Multi-user MIMO: how does it work?

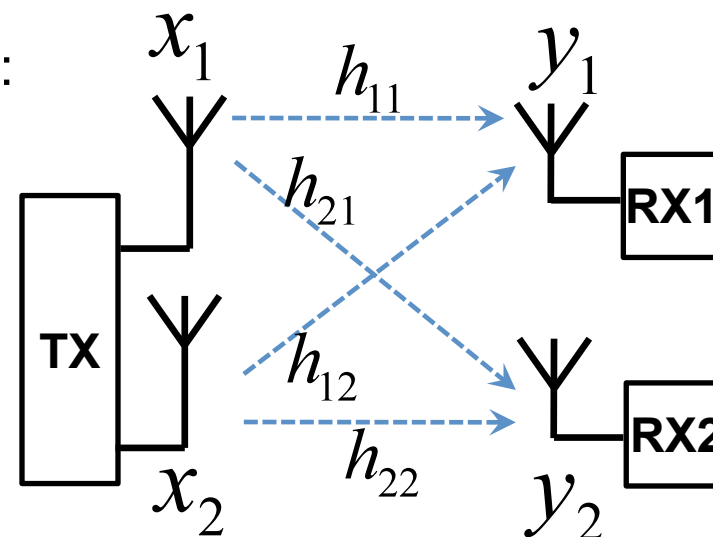
- MU-MIMO differs from traditional MIMO

- Data to be sent over two TX antennas:
 x_1, x_2

- Data received on two RX nodes:

$$y_1 = h_{11}x_1 + h_{12}x_2$$

$$y_2 = h_{21}x_1 + h_{22}x_2$$



- Each RX only has one equation, but two variables; no way to solve it directly
 - * x_2 causes cross-talk interference to x_1 , and vice versa

Multi-user MIMO: how does it work?

- How to remove cross-talk?

- Send a weighted mix of x_1 and x_2

TX antenna1 sends: $w_{11}x_1 + w_{12}x_2$

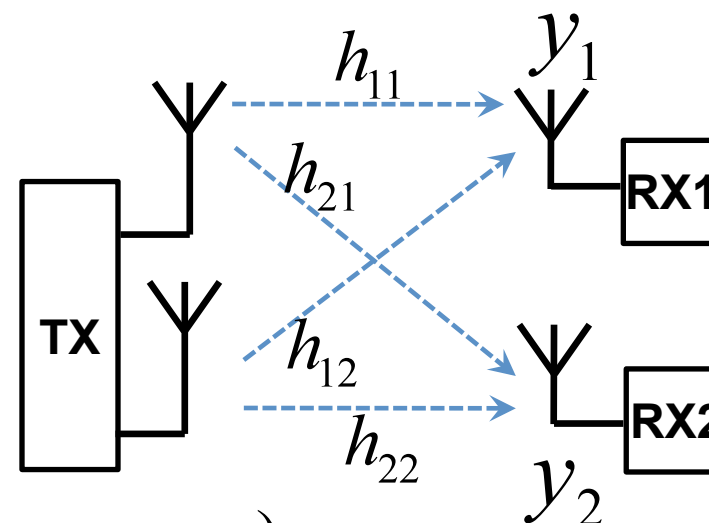
TX antenna2 sends: $w_{21}x_1 + w_{22}x_2$

- Data received on RX1:

$$y_1 = h_{11}(w_{11}x_1 + w_{12}x_2) + h_{21}(w_{21}x_1 + w_{22}x_2)$$

$$= (h_{11}w_{11} + h_{21}w_{21})x_1 + (h_{11}w_{12} + h_{21}w_{22})x_2$$

- RX1 only wants x_1 , so ideally, we should have $(h_{11}w_{12} + h_{21}w_{22}) = 0$



Multi-user MIMO: how does it work?

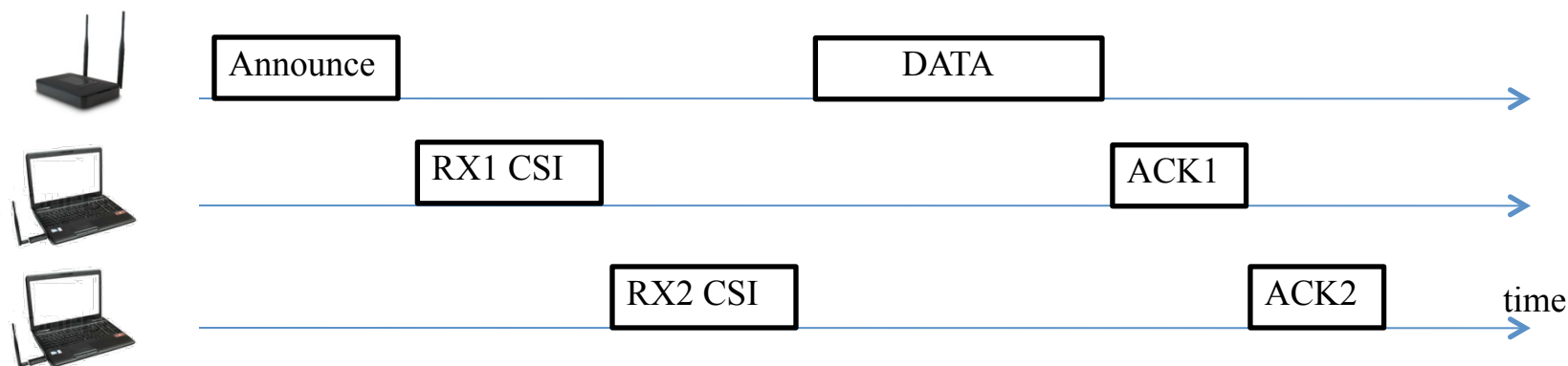
- MU-MIMO precoding

- TX can obtain h_{11}, h_{12} from RXs' feedback, so it can tune w_{12}, w_{22} to satisfy $(h_{11}w_{12} + h_{12}w_{22}) = 0$

- * This cancels the cross-talk interference from x2 to x1
- * Similarly, we can cancel that from x1 to x2
- * This is called Zero-Forcing Beamforming (ZFBF)

- How does TX obtain channel state information h_{**}

- * Simplest approach in 802.11ac: CSI feedback scheduling



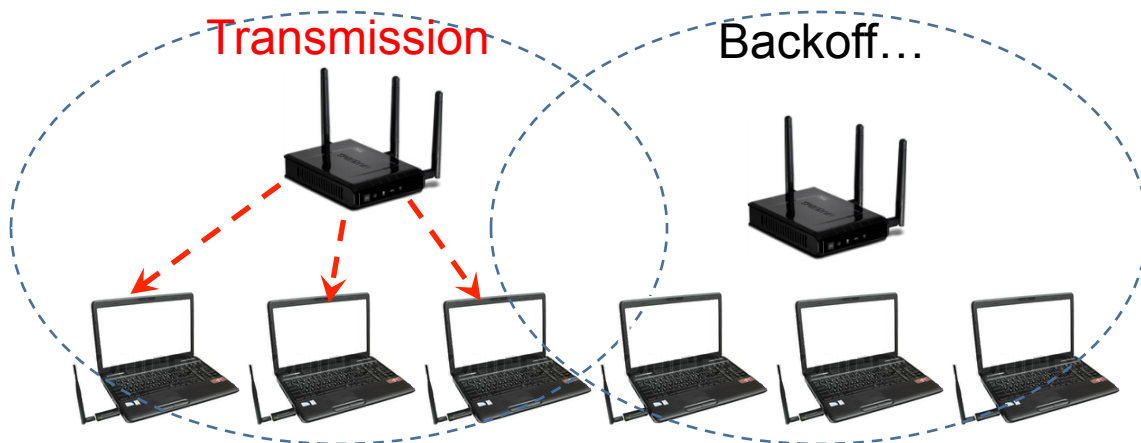
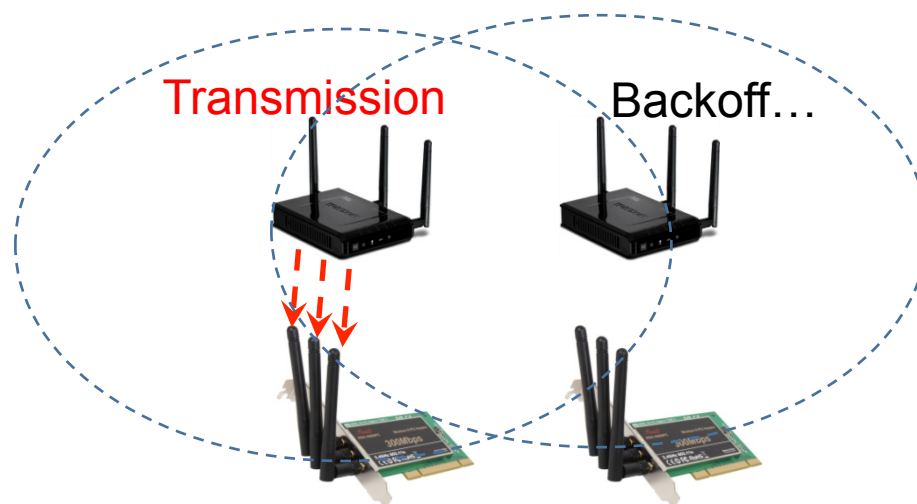
MU-MIMO capacity gain

- Asymptotic capacity gain
 - If the transmitter has N_t antennas, then it can send N_t streams of data simultaneously to N_t users, increasing capacity to N_t times compared with single-antenna transmitter
- Limitation
 - MU-MIMO is essentially a form of spatial multiplexing
 - So the channel must be well-conditioned

MIMO limitation in large networks

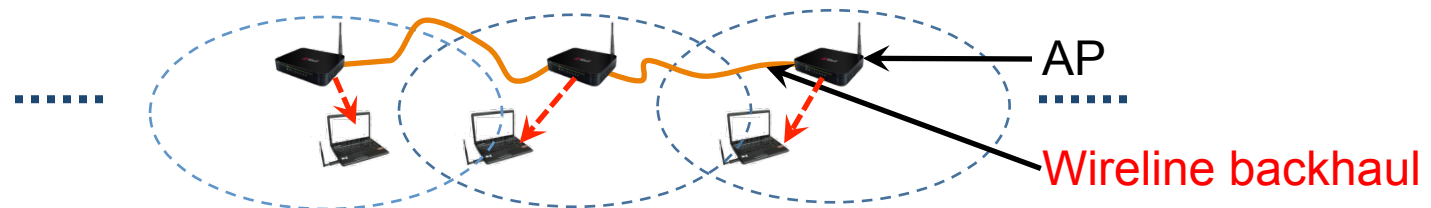
- Limitations of existing MIMO architectures

- Only one transmitter at a time
- Simultaneous transmission from different transmitters causes collision!
- So network capacity doesn't scale with transmitter density



Network MIMO

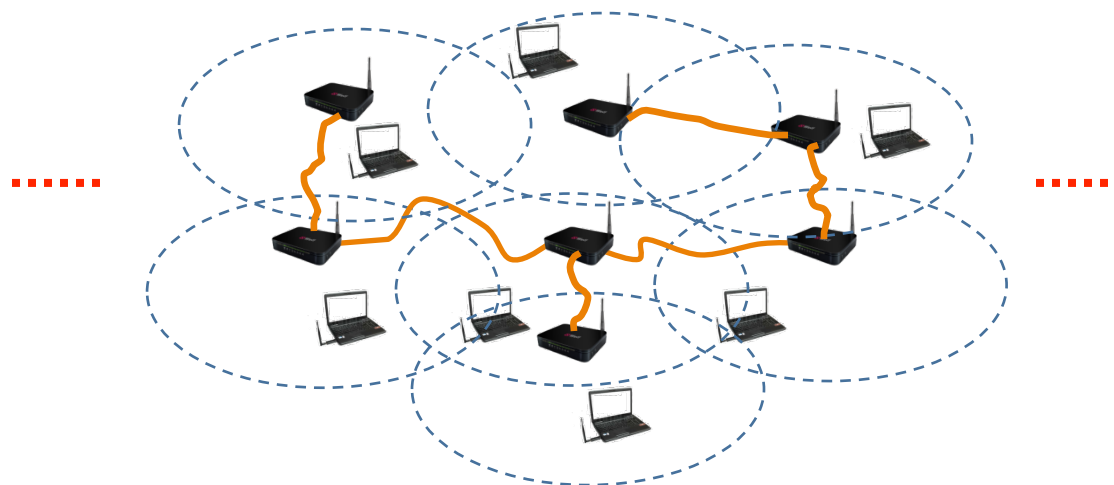
- A **giant-MIMO** comprised of many APs



- APs are tightly synchronized and share data
- Mutual interference can be cancelled
- Asymptotic gain: Network capacity scales **linearly** with the number of APs, theoretically

Network MIMO in large networks

- Is network MIMO practical?



- A super-giant-MIMO solution?

APs need:

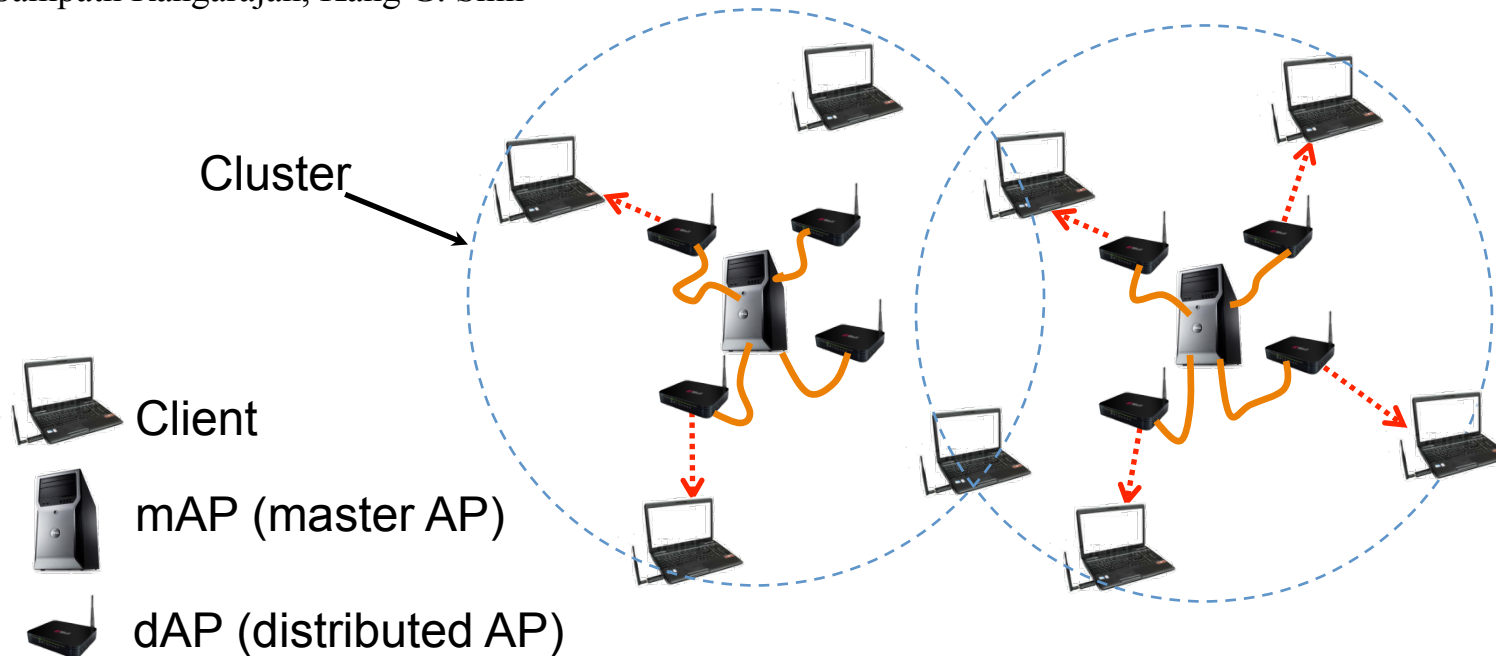
- * Full synchronization: carrier phase, frequency, sampling-clock
- * Full data sharing: large volumes of data and CSI exchange

Infeasible!

NEMOx: making network MIMO scalable

“[NEMOx: Scalable Network MIMO for Wireless Networks](#)”,

ACM MobiCom'13, by Xinyu Zhang, Karthikeyan Sundaresan, Mohammad A. (Amir) Khojastepour, Sampath Rangarajan, Kang G. Shin



- A **hierarchical architecture** to realize scalable network MIMO
 - * **Intra-cluster:** dAPs within each cluster can TX concurrently
 - * **Inter-cluster:** neighboring clusters contend for channel access
 - * **Capacity can scale with #of dAPs within each cluster, and with #of clusters** (capacity ≈ 6 in this case)

Summary

- Take-home message:
 - (1) What are the various modes of operations in MIMO?
 - (2) How does each MIMO mode scale link/network capacity?
- References:
 - * Book1: Fundamentals of LTE
 - * Book2: Fundamentals of Wireless Communications