HOMEWORK 2: Written Exercise Part

1 Information Theory [25/4 pts]

Suppose X, Y are two random variables taking values in a discrete finite set V. Let H(Y) denote the entropy of Y, and let H(Y|X) denote the conditional entropy of Y conditioned on X. Prove that if X, Y are independent, then H(Y) = H(Y|X). Solution goes here.

2 Standardizing Numeric Features [25/4 pts]

Standardize the data set with four points in 2 dimension: (7,7), (3,7), (3,3), (7,3). Solution goes here.

3 *k*-Nearest Neighbors [25/4 pts]

Consider the training data set $x_1 = (7, 7), y_1 = 0; x_2 = (3, 7), y_2 = 1; x_3 = (3, 3), y_3 = 1; x_4 = (7, 3), y_4 = 2$. Suppose the Manhattan distance is used. What is the label for x = (0, 0) in the following settings? Show the calculation steps.

- 1. 1-nearest neighbors.
- 2. 3-nearest neighbors.
- 3. 3-nearest neighbors, distance weighted. The weight for the *i*-th neighbor z is $1/d(x, z)^2$.

Solution goes here.

4 Performance Measurements [25/4 pts]

Consider the following confusion matrix for 2 classes.

| | actual positive | actual negative |
|------------------|-----------------|-----------------|
| predict positive | 76 | 18 |
| predict negative | 24 | 82 |

Compute the accuracy, error, true positive rate, false positive rate, precision, and recall. Solution goes here.