

## CS367 Lecture 20

Monday 21 July 2014

### Announcements/Reminders:

- HW5 due tonight
- Midterms graded, statistics'd, returned today
- HW3, HW4, P2 graded, feedback available
- Readings

### Last class:

- Binary Search Trees
  - Operations: `print`, `lookup`, `min/max`, `succ/pred`, `insert`, `delete`

### Today:

- (Last) Week in Review
- Associative Arrays/Maps
- Binary Search Trees
  - `delete` method (finish)
  - Complexities
- Balanced Search Trees (intro)

## (Last) Week in Review

- Trees (general)
  - Terminology
  - Implementing trees
  - Traversals
- Binary Trees
  - Types and heights
- Priority Queues
- Heaps
  - Concept
  - Insert/Delete
  - Complexities
- Binary Search Trees (BSTs)
  - Concept, Examples
  - Implementation
  - Operations: print, lookup, min/max, succ/pred, insert, delete

## **Associative Arrays/Key-Value Maps/Dictionaryes**

Concept:

Examples:

Operations:

Possible implementations:

## Lowest Common Ancestor (LCA) of two nodes

In a BST:

In a (regular) binary tree:

Using only constant additional storage:

## Deleting from a BST

High-level algorithm:

Example

## BST operations complexities

Assume the number of nodes is  $n$ , arranged in a tree of height  $h$ .

`print()`:

`lookup(E)`:

`min/max`:

`succ(E)/pred(E)`:

`insert(E)`:

`delete(E)`:

Height of an “average” BST (with  $n$  nodes):

## Final BST example

Starting with an empty BST, insert 7, 14, 18, 23, 1, 11, 20, 29, 25, 27 .

Now delete 18 and 23:

# Balanced Search Trees

Goal

How?

Rotations

Types