

CS536

Intro to Parsing

Announcements: Grades

- Things are graded
 - Project 1 is on Learn@UW
 - Homework 3 is available at end of class



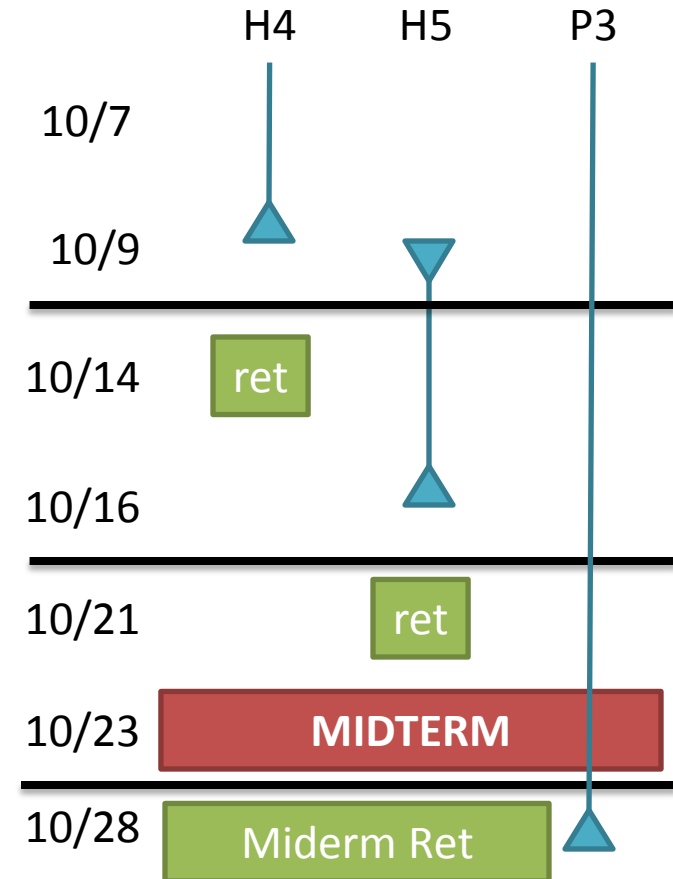
Announcements: Materials

- Screencasts live
 - Java CUP
 - Using Windows
- Upcoming
 - Linux Tips n' Tricks
- Still up for suggestions



Announcements

- Midterm 1 approaches
 - 2 weeks from Thursday
 - Last assignment before the midterm assigned Thursday
 - We'll have at least 1 review session before test



Last Time

- Showed how to blindly use CUP for getting ASTs
- But we never saw HOW the parser works



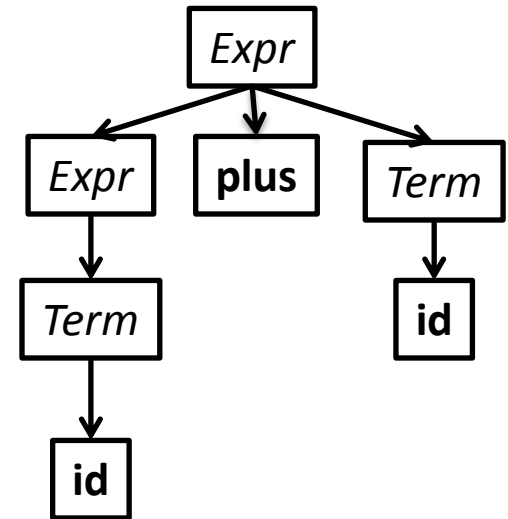
This Time

- Dip our toe into parsing
 - Approaches to Parsing
 - CFG Transformations
 - Useless Nonterminals
 - CNF: A form of grammar that's easier to deal with
 - CYK:
 - powerful, heavyweight approach to parsing



Approaches to Parsing

- Top Down / “Goal driven”
 - Start at root of parse tree, grow downward to match the string
- Bottom Up / “Data Driven”
 - Start at terminal, generate subtrees until you get to the start



CYK: A general approach to Parsing

- Operates in $O(n^3)$
- Works Bottom-Up
- Only takes a grammar in CNF
 - This will not turn out to be a limitation

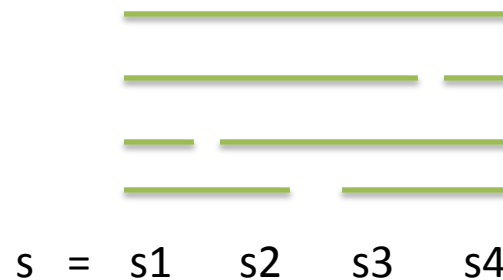
Chomsky Normal Form

- All rules must be one of two forms:
 $X \rightarrow t$
 $X \rightarrow AB$
- The only rule allowed to derive epsilon is the start S , in which case it's forbidden on the RHS of any rule



What CNF buys CYK

Fact that nonterminals come in pairs allows you to think of subtree as a subspan of the input



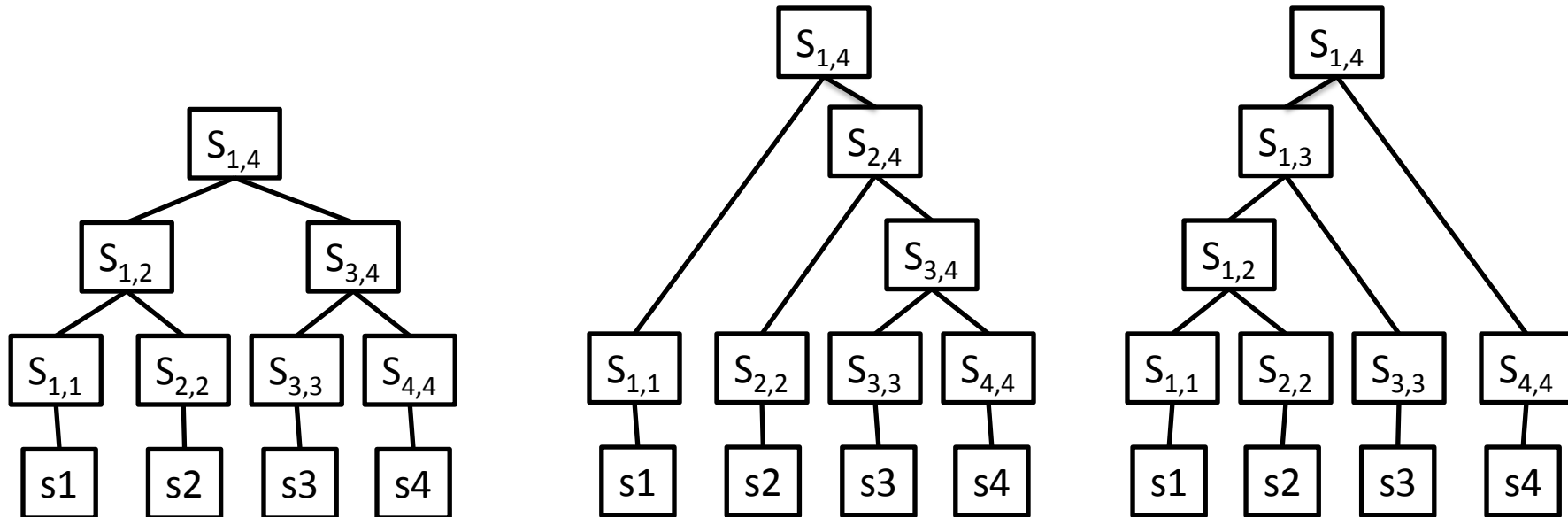
CYK: Dynamic Programming

$X \rightarrow t$

Prods. form the leaves of the parse tree

$X \rightarrow A B$

Form binary nodes

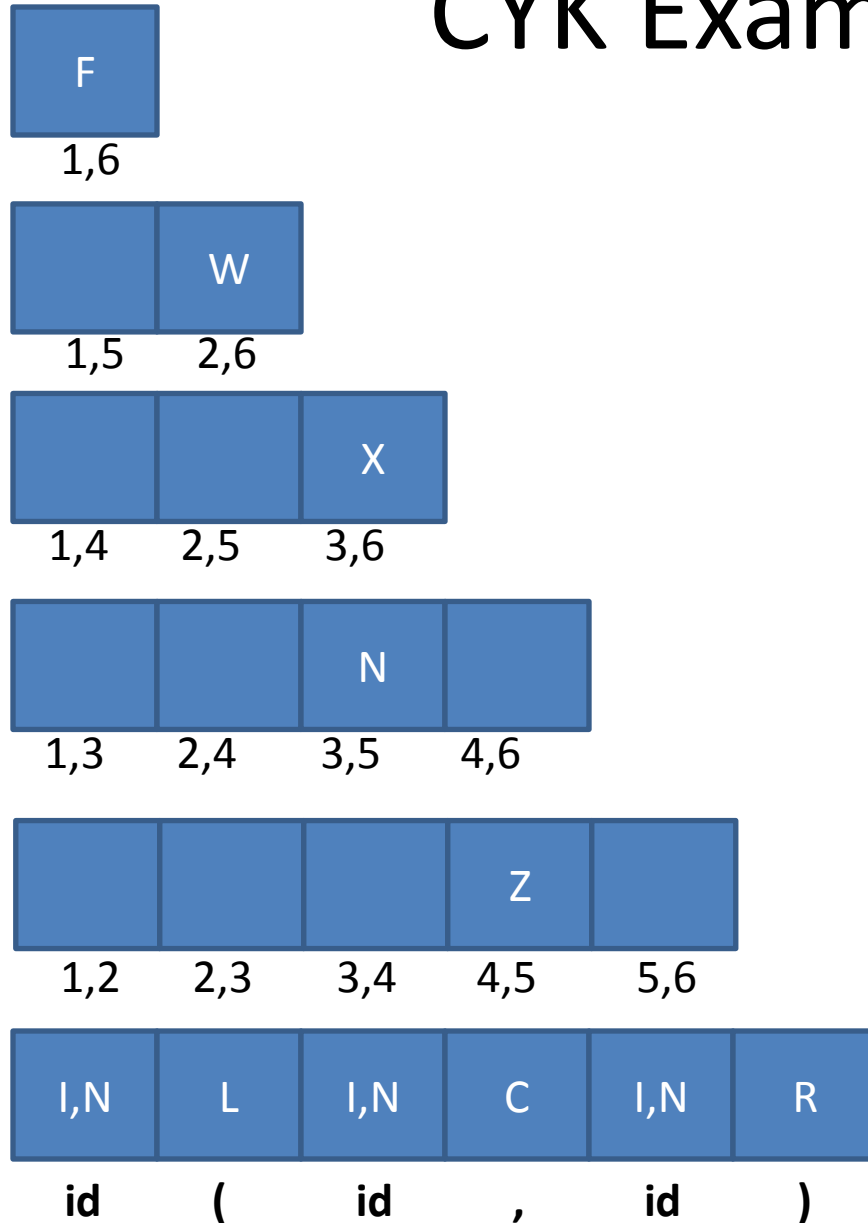


Running CYK...

- Track every viable subtree from leaf to root. Here are all the subspans for a string of 6 terminals

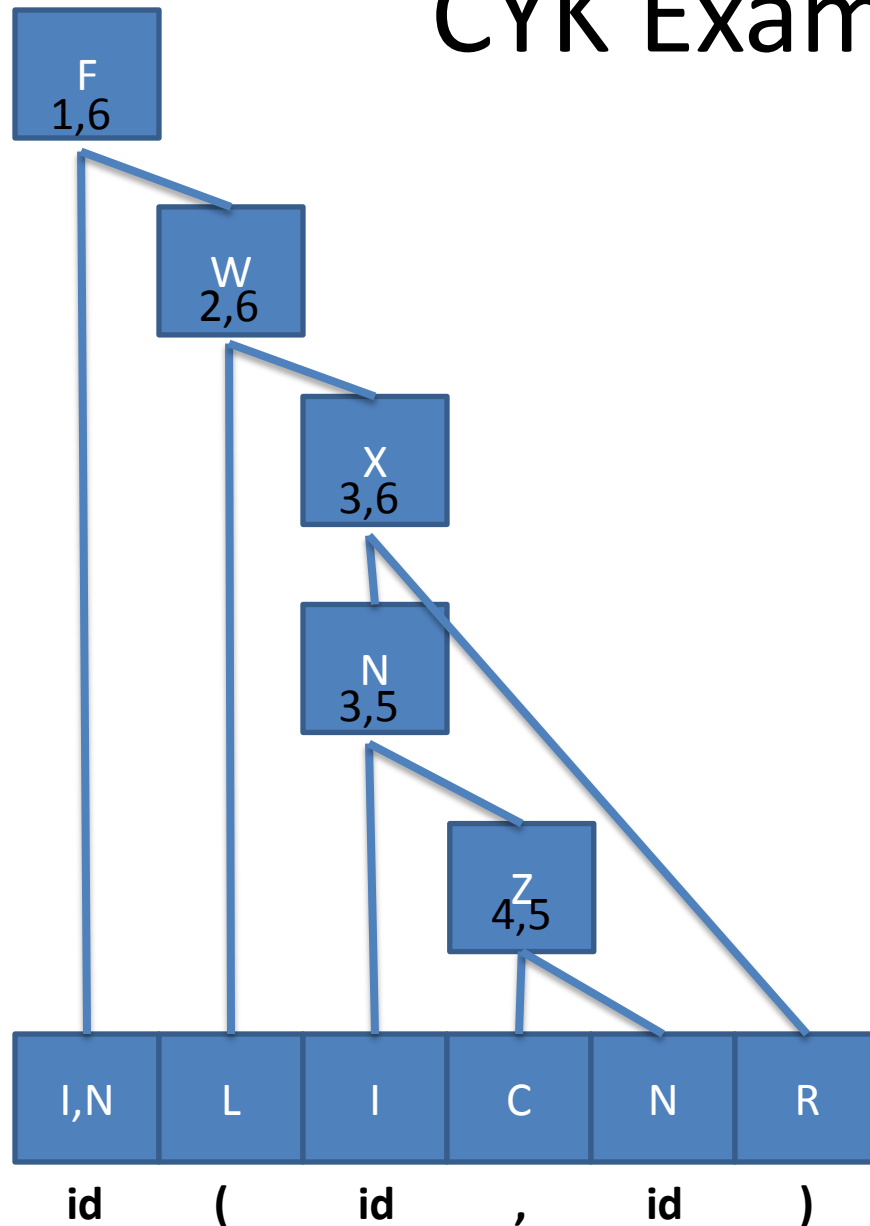
1,6					
1,5	2,6				
1,4	2,5	3,6			
1,3	2,4	3,5	4,6		
1,2	2,3	3,4	4,5	5,6	
1,1	2,2	3,3	4,4	5,5	6,6

CYK Example



F	→	I W
F	→	I Y
W	→	L X
X	→	N R
Y	→	L R
N	→	id
N	→	I Z
Z	→	C N
I	→	id
L	→	(
R	→)
C	→	,

CYK Example



F	→	I W
F	→	I Y
W	→	L X
X	→	N R
Y	→	L R
N	→	id
N	→	I Z
Z	→	C N
I	→	id
L	→	(
R	→)
C	→	,

Cleaning up our grammars

- We want to avoid unnecessary work
 - Remove *useless* rules



Eliminating Useless Nonterminals

1. If a nonterminal cannot derive a terminal symbol then it is useless
2. If a nonterminal cannot be derived from the start symbol, then it is useless

Eliminate Useless Nonterms

- If a nonterminal cannot derived a terminal symbol, then it is useless

Mark all terminal symbols

Repeat

If all symbols on the righthand side of a production are marked

mark the lefthand side

Until no more non-terminals can be marked

Example:

S	→	X Y
X	→	()
Y	→	(Y Y)

Eliminate Useless Nonterms

- If a nonterminal cannot be derived from the start symbol, then it is useless

Mark the start symbol

Repeat

If the left-hand side of a production is marked

mark all right-hand non-terminal

Until no more non-terminals can be marked

Example:

S	→	A B
A	→	+ - ε
B	→	digit B digit
C	→	. B

Chomsky Normal Form

- 4 Steps
 - Eliminate epsilon rules
 - Eliminate unit rules
 - Fix productions with terminals on RHS
 - Fix productions with > 2 nonterminals on RHS

Eliminate (Most) Epsilon Productions

- If a nonterminal A immediately derives epsilon
 - Make copies of all rules with A on the RHS and delete all combinations of A in those copies

Example 1

F	→	id (A)
A	→	ϵ
A	→	N
N	→	id
N	→	id , N



F	→	id (A)
F	→	id ()
A	→	N
N	→	id
N	→	id , N

Example 2

X	\rightarrow	$A x A y A$
A	\rightarrow	ϵ
A	\rightarrow	z



X	\rightarrow	$A x A y A$
	$ $	$A x A y$
	$ $	$A x y A$
	$ $	$A x y$
	$ $	$x A y A$
	$ $	$x A y$
	$ $	$x y A$
	$ $	$x y$
A	\rightarrow	z

Eliminate Unit Productions

- Productions of the form $A \rightarrow B$ are called unit productions
- Place B anywhere A could have appeared and remove the unit production

Example 1

F	→	id (A)
F	→	id ()
A	→	N
N	→	id
N	→	id , N



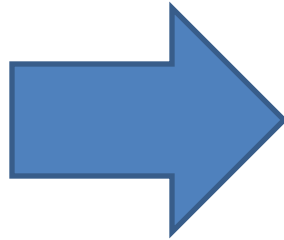
F	→	id (N)
F	→	id ()
N	→	id
N	→	id , N

Fix RHS Terminals

- For productions with Terminals and something else on the RHS
 - For each terminal t add the rule
$$X \rightarrow t$$
 - Replace t with X in the in the original rules

Example

F → id (N)
F → id ()
N → id
N → id , N



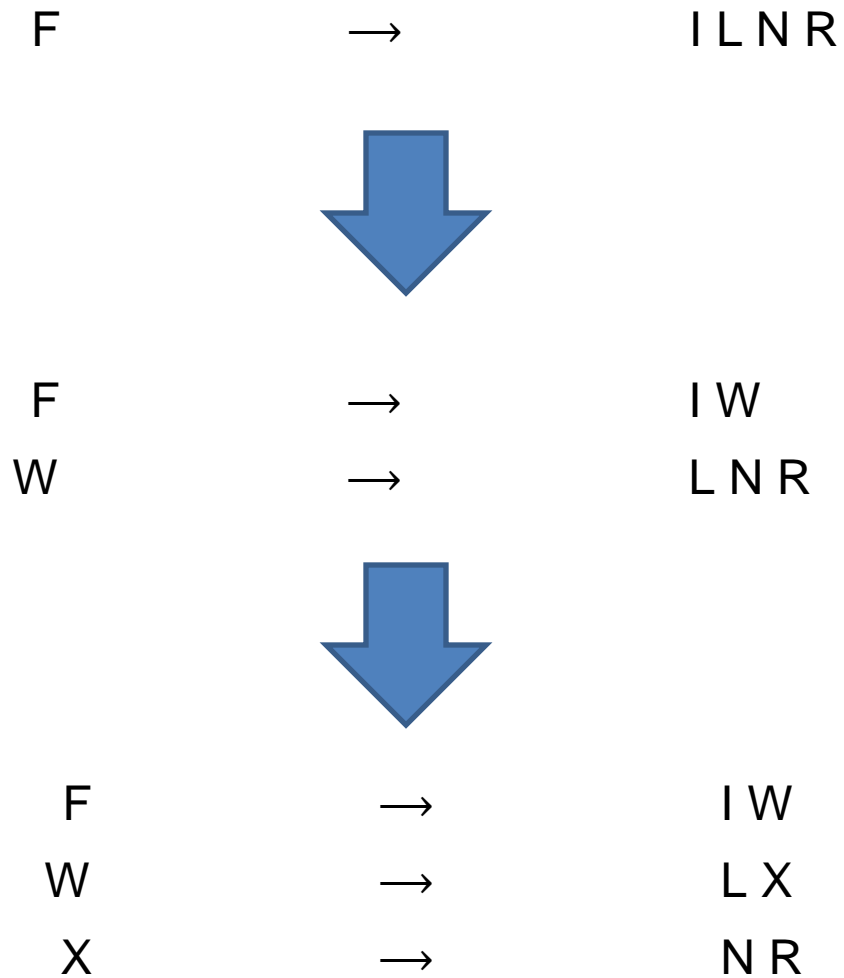
F → I L N R
F → I L R
N → id
N → I C N

I → id
L → (
R →)
C → ,

Fix RHS Nonterminals

- For productions with > 2 Nonterminals on the RHS
 - Replace all but the *first* nonterminal with a new nonterminal
 - Add a rule from the new nonterminal to the replaced nonterminal sequence
 - Repeat

Example



Parsing is Tough

- CYK parses an arbitrary CFG, but
 - $O(n^3)$
 - Too slow!
- For special class of grammars
 - $O(n)$
 - Includes LL(1) and LALR(1)



Classes of Grammars

- LL(1)
 - Scans input from Left-to-right (first L)
 - Builds a Leftmost Derivation (second L)
 - Can peek (1) token ahead of the token being parsed
 - Top-down “predictive parsers”
- LALR(1)
 - Uses special lookahead procedure (LA)
 - Scans input from Left-to-right (second L)
 - Rightmost derivation (R)
 - Can also peek (1) token ahead
- LALR(1) strictly more powerful, much harder to understand