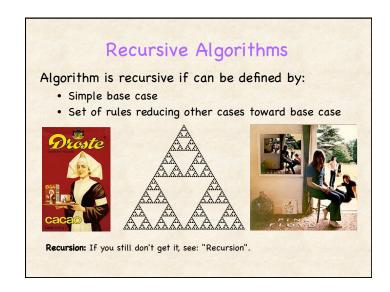


Previous Lecture Two intuitive, but slow sorting algorithms Selection sort: • Repeat for each key in list - Find minimum key in unsorted portion - Move to next position of sorted portion Insertion sort: • Repeat for each key in unsorted list - Insert into its correct position in sorted portion Both algorithms O(N²) where N is length of list



Recursive Definition of Factorial

Example: Fact(5) = 5! = 5 * 4 * 3 * 2 * 1Recursive definition:

- Fact(1) = 1 [base case]
- For all integers n > 1: Fact(n) = n * Fact (n-1)

Fact(5) = ??

- = 5 * Fact (4)
- = 5 * 4 * Fact(3)
- = 5 * 4 * 3 * Fact(2)
- = 5 * 4 * 3 * 2 * Fact (1)
- = 5 * 4 * 3 * 2 * 1 Recursion ends!

Merge Sort Algorithm: Uses Recursion

Base case:

• If list of length 0 or 1, done (sorted)

Otherwise:

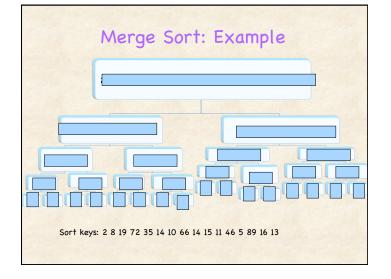
- Divide unsorted list of size M into two sublists of size M/2
- · Sort each sublist recursively using mergesort
- · Merge two sublists back into one sorted list

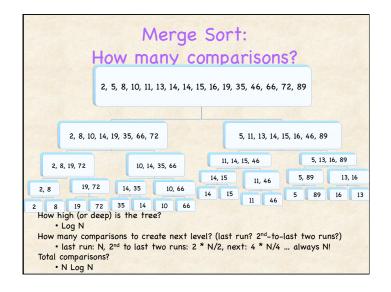
How to merge two lists into one?

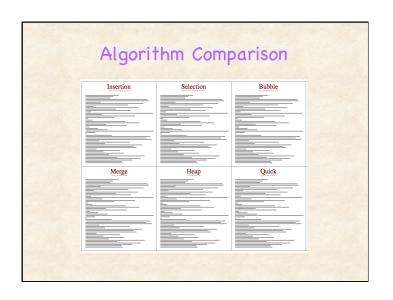
Merging Two Sorted Runs 2 4 5 8 6 9 10 13 End End Algorithm: Compare 1st element of each list, remove the smaller as next element of sorted run

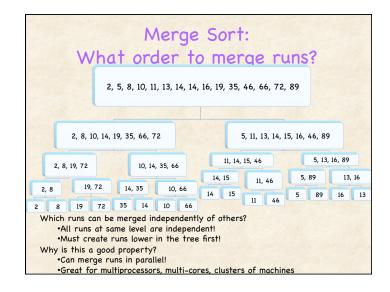
Very efficient! Very few comparisons needed for merge How many comparisons needed to create list of size N?

O(N) comparisons









Quicksort (Qsort) Algorithm:
Recursive

Base case: list of size one is sorted by definition

Otherwise:
Pick an element (pivot) from list

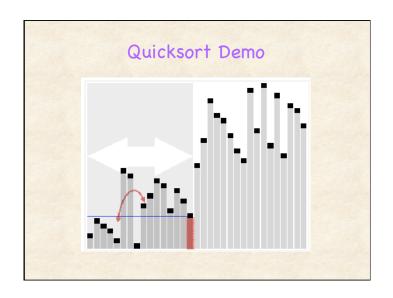
Reorder:

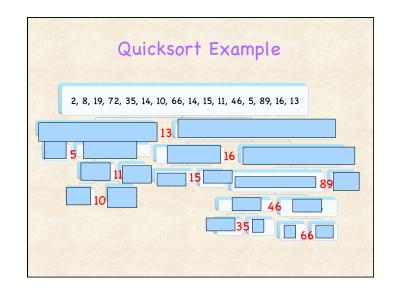
• All keys < pivot → move key before pivot
• All keys > pivot → move key after pivot

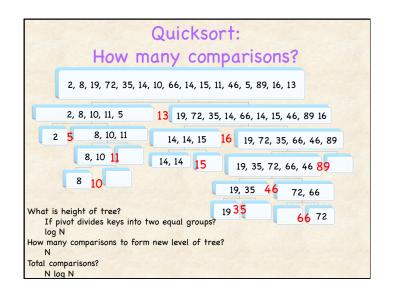
- Equal values can go either way

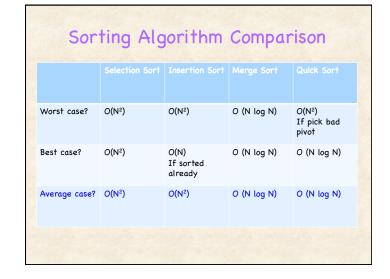
• Pivot is now in its final sorted position

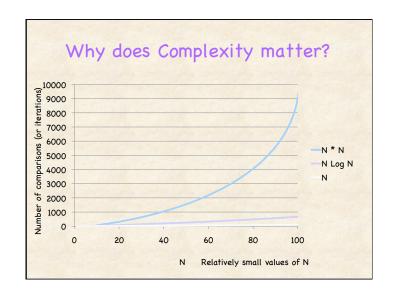
Recursively sort (w/ quick sort!) two sub-lists

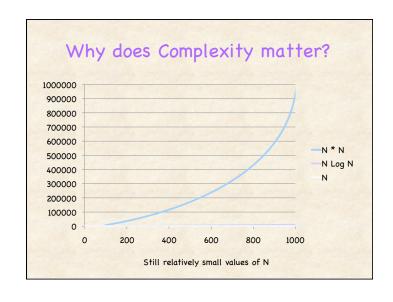


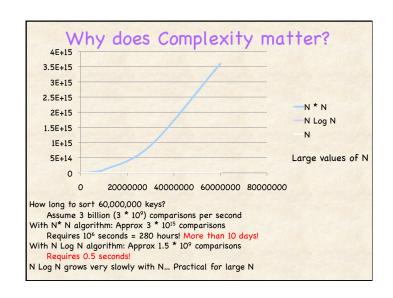














Today's Summary

Sorting algorithms

- O(N2) sorting algorithms
 - Selection sort: Find minimum and make next
 - Insertion sort: Take next and insert in correct place
- O(N log N) sorting algorithms (expected, not worst-case)
 - Merge sort: Recursively combine sub-lists into larger lists
 - Quicksort: Recursively partition list into sub-lists around pivot

Reading: 3.3.4 for Order of Magnitude

Announcements

- Exam 2 Solutions posted
- Homework 8 and 9 available (due Friday 12/3 and Wed 12/8)
- Homework 10: Project 2 Website Comments and Demo attendance
 Upload by Thursday 12/9; Comment by Fri 12/10
- Project 2: Due with In-class demos Monday 12/13