

CS 536 Announcements for Monday, February 5, 2024

Programming Assignment 1

- symbol table files due Thursday, Feb. 8 by 11:59 pm

Homework 0

- available in schedule
- practice with DFAs, regular expressions

Homework 1

- available tomorrow
- practice with NFA→DFA translation, JLex

Last Time

- non-deterministic FSMs
- equivalence of NFAs and DFAs
- regular languages
- regular expressions

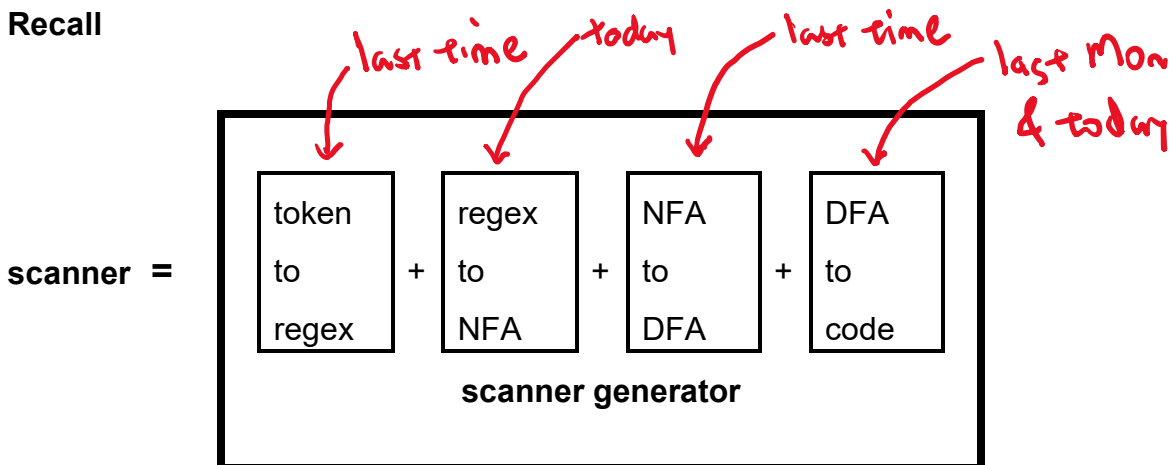
Today

- regular expressions → DFAs
- language recognition → tokenizers
- scanner generators
- JLex

Next Time

- CFGs

Recall



From regular expressions to NFAs

Overview of the process

- Conversion of literals and epsilon \rightarrow simple FAs
- Conversion of operators
 - Convert operands to NFAs
 - join NFAs

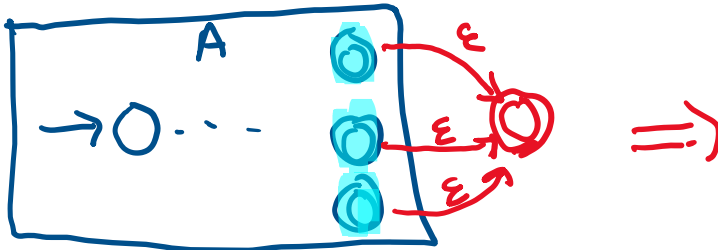
Regex to NFA rules

Rules for operands

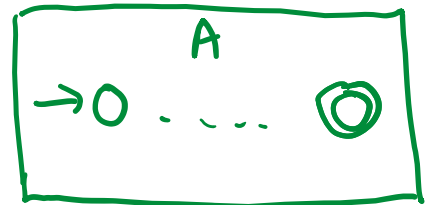
literal 'a' \rightarrow $0 \xrightarrow{a} \odot$

epsilon $\epsilon \rightarrow 0 \xrightarrow{\epsilon} \odot$

Suppose A is a regex with NFA:



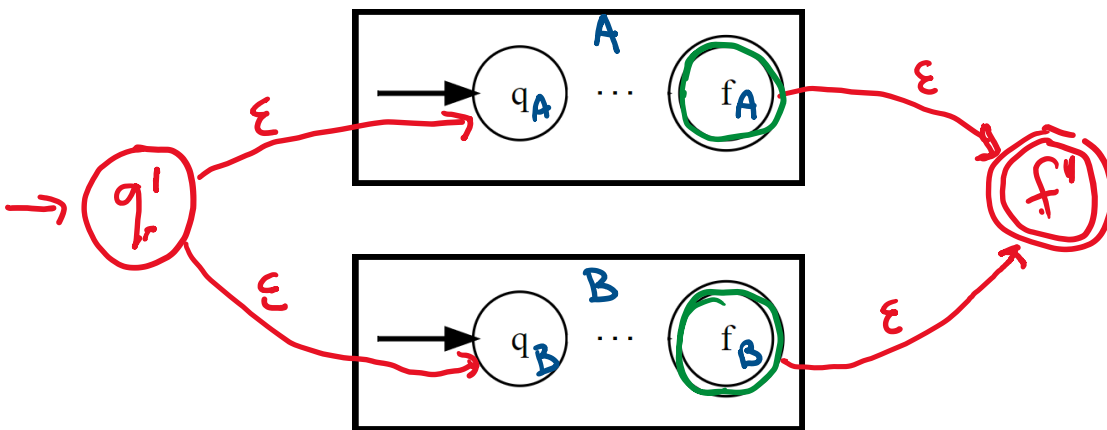
Convert so only 1 final state



\uparrow make these non-final

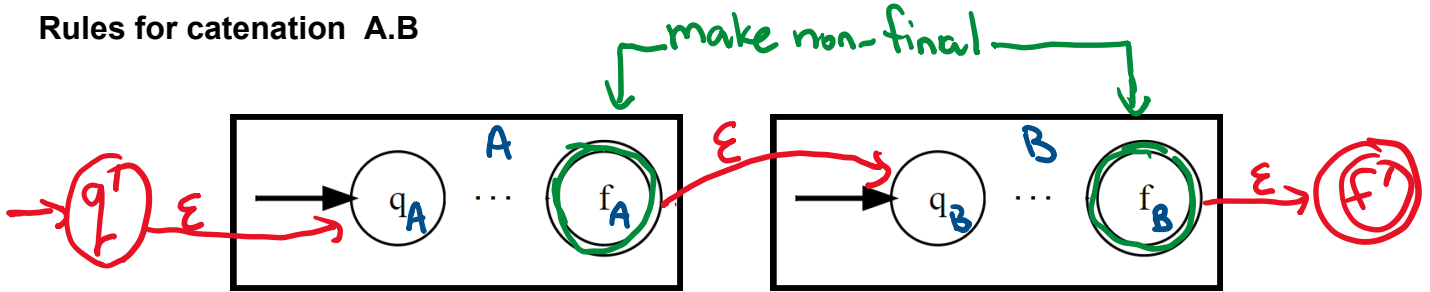
Rules for alternation A|B

\downarrow make f_A, f_B non-final

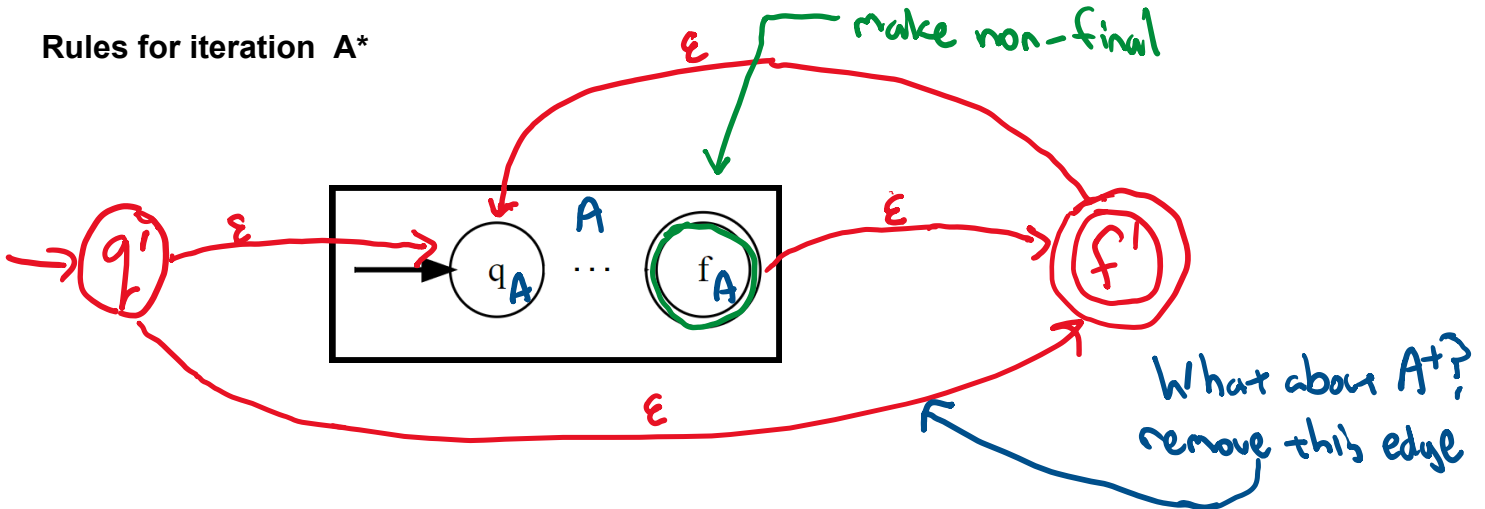


Regex to NFA rules

Rules for catenation A.B

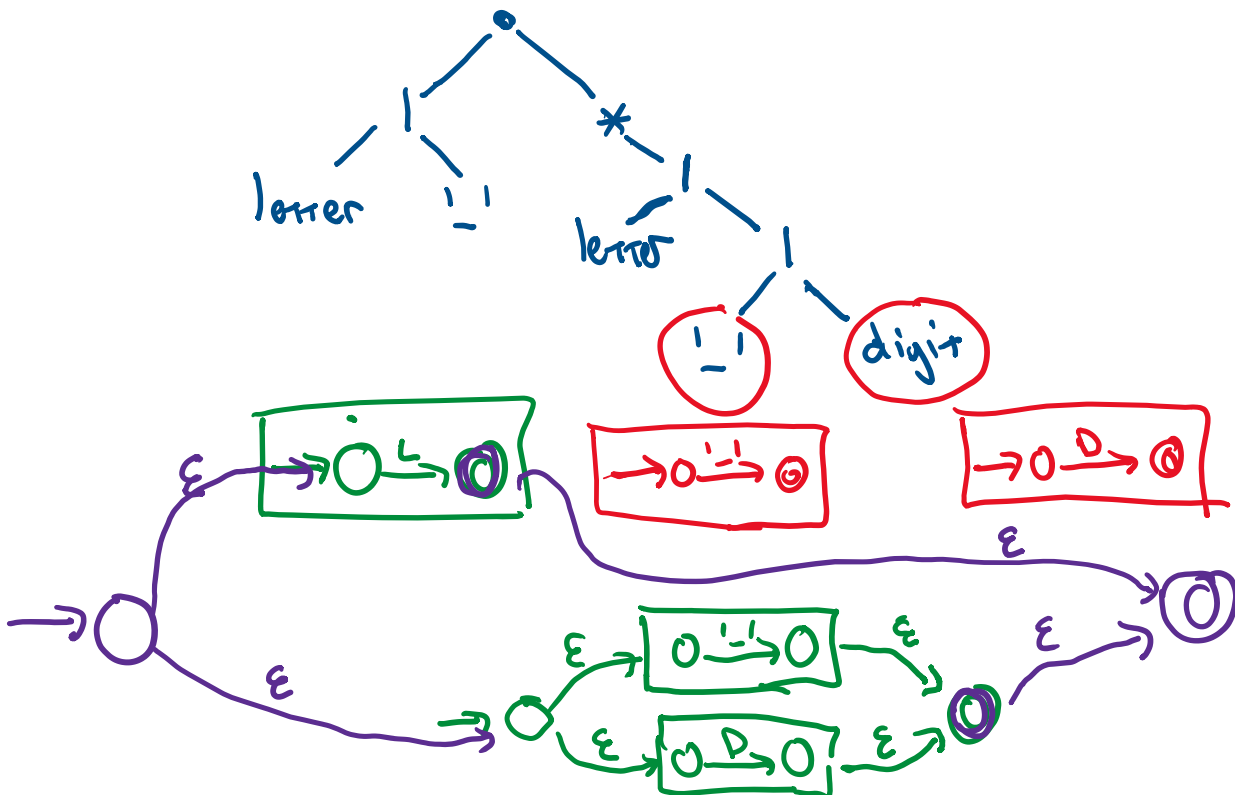


Rules for iteration A*



Tree representation of a regex

Consider regex: (letter | '_') (letter | '_' | digit)*



Regex to DFA

We now can do:



We can add one more step: **optimize DFA**

Theorem: For every DFA M , there exists a unique equivalent smallest DFA M^* that recognizes the same language as M .

\hookrightarrow fewer # of states

To optimize:

- remove **unreachable** states
- remove **dead** states
- merge **equivalent** states

\rightarrow can't get to from start state

\rightarrow can't get to a final state from it

\hookrightarrow same transitions (out) w/ same labels

But what's so great about DFAs?

Recall: state-transition function (δ) can be expressed as a table

\rightarrow very efficient array representation



	a	b	c
S ₁	S ₂	S ₂	
S ₂	S ₁		S ₂

\rightarrow efficient algorithm for running (any) DFA

```
s = start state
while (more input){
    c = read next char
    s = table[s][c]
}
if s is final, accept
else reject
```

What else do we need?

FSMs – only check for **language membership** of a string

scanner needs to

- recognize a **stream** of many different tokens using the **longest match**
- know what was matched

Table-driven DFA → tokenizer

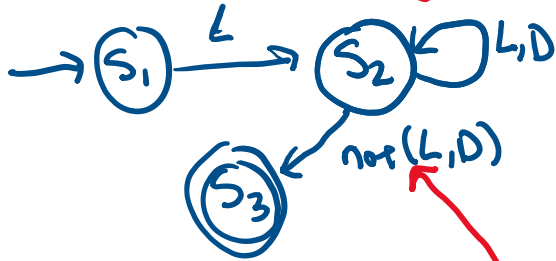
Idea: augment states with actions that will be executed when state is reached

Consider: $(\text{letter})(\text{letter} | \text{digit})^*$



state	action
S ₂	return ID ← token

Problem: **Don't get longest match**



$a \vee a = 7$

state	action
S ₃	return ID

To fix:
put back
1 char,
return ID

$a \vee a = 7$

Problem: **maybe we need this char**

Actions needed:

- return a token
- put back a character
- report an error

Also add EOF token,
EOF symbol to alphabet Σ

Scanner Generator Example

Language description:

consider a language consisting of two statements

- assignment statements: $\text{ID} = \text{expr}$
- increment statements: $\text{ID} += \text{expr}$

where expr is of the form:

- $\text{ID} + \text{ID}$
- $\text{ID} \wedge \text{ID}$
- $\text{ID} < \text{ID}$
- $\text{ID} \leq \text{ID}$

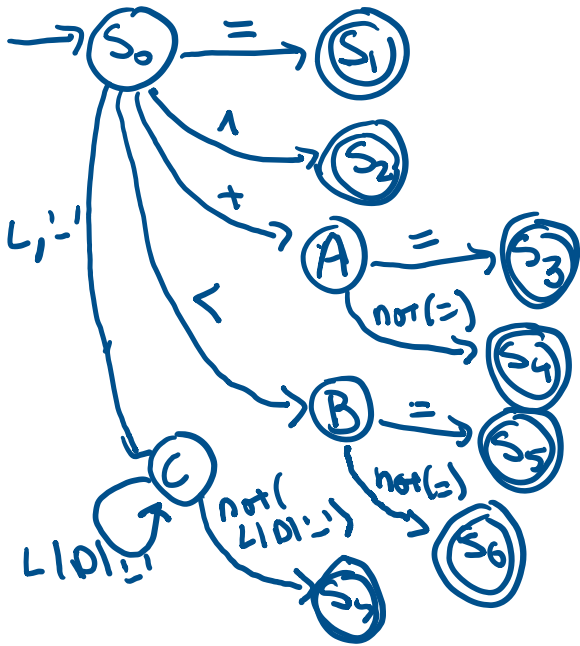
and ID are identifiers following C/C++ rules (can contain only letters, digits, and underscores; can't start with a digit)

Tokens:

Token	Regular expression
ASSIGN	" = "
INCR	" += "
PLUS	" + "
EXP	" ^ "
LESSTHAN	" < "
LEQ	" <= "
ID	

$(\text{letter} | _ | ')(\text{letter} | _ | \text{digit})^*$

Combined DFA



Actions
 S₁: return ASSIGN
 S₂: return EXP
 S₃: return INC
 S₄: put 1 back, return PLUS
 S₅: return LEQ
 S₆: put 1 back, return LESSTHAN
 S₇: put 1 back, return ID

State-transition table

	=	+	^	<	_	letter	digit	EOF	none of these
S₀	ret ASSIGN	A	ret EXP	B	C	C		ret EOF	
A	ret INC	put 1 back, ret PLUS							
B	ret LEQ	put 1 back, ret LESSTHAN							
C	put 1 back, ret ID				C	C	C	put 1 back, ret ID	

```
do {
    read char
    perform action / update state
    if (action was to return a token)
        start again in start state
} while not(EOF or stuck)
```

Lexical analyzer generators (aka scanner generators)

Formally define transformation from regex to scanner

Tools written to synthesize a lexer automatically

- Lex : UNIX scanner generator, builds scanner in C
- Flex : faster version of Lex
- JLex : Java version of Lex

JLex

Declarative specification (non-procedure)

- you don't tell JLex how to scan / how to match tokens
- you tell JLex what you want scanned (tokens) & what to do when a token is matched

Input: set of regular expressions + associated actions,

Output: Java source code for a scanner

Flex specification

• jlex eg xyz.jlex

↳ xyz.jlex.java

↓ compile to get

Yylex.class

- ctor: takes input stream as arg

- next_token: return next token of input

Format of JLex specification

3 sections separated by %%

- user code section
- directives
- regular expression rules

Regular expression rules section

Format: <regex>{code} where <regex> is a regular expression for a single token

- can use macros from Directives section – surround with curly braces { }
- characters represent themselves (except special characters)
- characters inside " " represent themselves (except \ ")
- . matches anything

Regular expression operators: | * + ? ()

Character class operators: - ^ \

JLex example

```
// This file contains a complete JLex specification for a very
// small example.

// User Code section: For right now, we will not use it.

%%

DIGIT=      [0-9]
LETTER=     [a-zA-Z]
WHITESPACE= [\040\t\n]

%state SPECIALINTSTATE

%implements java_cup.runtime.Scanner
%function next_token
%type java_cup.runtime.Symbol

%eofval{
System.out.println("All done");
return null;
%eofval}

%line

%%

({LETTER}|"_" )({DIGIT}|{LETTER}|"_" )* {
    System.out.println(yyline+1 + ": ID "
        + yytext()); }

"="        { System.out.println(yyline+1 + ": ASSIGN"); }
"+"        { System.out.println(yyline+1 + ": PLUS"); }
"^"        { System.out.println(yyline+1 + ": EXP"); }
"<"        { System.out.println(yyline+1 + ": LESSTHAN"); }
"+="       { System.out.println(yyline+1 + ": INCR"); }
"<="       { System.out.println(yyline+1 + ": LEQ"); }
{WHITESPACE}* { }
.          { System.out.println(yyline+1 + ": bad char"); }
```

Using scanner generated by JLex in a program

```
// inFile is a FileReader initialized to read from the
// file to be scanned
Yylex scanner = new Yylex(inFile);
try {
    scanner.next_token();
} catch (IOException ex) {
    System.err.println(
        "unexpected IOException thrown by the scanner");
    System.exit(-1);
}
```