

CS 536 Announcements for Monday, February 12, 2024

Programming Assignment 2 – due Tuesday, February 20

Last Time

- why regular expressions aren't enough
- CFGs
 - formal definition
 - examples
 - language defined by a CFG

Today

- Makefiles
- parse trees
- resolving ambiguity
- expression grammars
- list grammars

Next Time

- syntax-directed translation

Makefiles

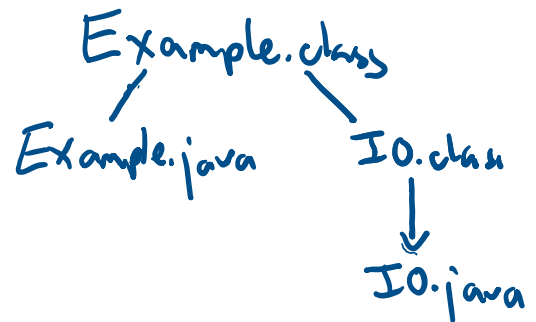
Basic structure

```
<target>: <dependency list>  
    <command to satisfy target>
```

↳ tab

Example

```
Example.class: Example.java IO.class  
    javac Example.java  
  
IO.class: IO.java  
    javac IO.java
```



Make creates an internal **dependency graph**

- a file is rebuilt if one of its dependencies changes

Variables – for common configuration values to use throughout your makefile

Example

```
JC = /s/std/bin/javac  
JFLAGS = -g ← build for use with debugger  
  
Example.class: Example.java IO.class  
    $(JC) $(JFLAGS) Example.java  
  
IO.class: IO.java  
    $(JC) $(JFLAGS) IO.java
```

Phony targets

- target with no dependencies = "phony"
- use make to run commands:

Example

```
clean:
    rm -f *.class
```

```
test:
    java Example inFile.txt outFile.txt
    java Example inErrFile.txt outErrFile.txt
```

Programming Assignment 2

Modify:

- base.jlex
- P2.java
- Makefile

Makefile

```
###
# testing - add more here to run your tester and compare
# its results to expected results
###
test:
    java -cp $(CP) P2
    diff allTokens.in allTokens.out

###
# clean up
###

clean:
    rm -f *~ *.class base.jlex.java

cleantest:
    rm -f allTokens.out
```

Run make to compile P2
(by default make
does 1st target in
Makefile)

Running the tester

```
royal-12 (53) % make test
java -cp ./deps:. P2
3:1 ****ERROR**** ignoring illegal character: a
diff allTokens.in allTokens.out
3d2
< a
make: *** [Makefile:40: test] Error 1
```

Commands
from
Makefile

output of diff command

error msg produced
by base scanner
when P2 is run

from running make

CFG review

formal definition: CFG $G = (N, \Sigma, P, S)$

\leftarrow terminals \equiv tokens

CFG generates a string by applying productions until no non-terminals remain

\Rightarrow^+ means "derives in 1 or more steps"

$q \Rightarrow^+ (q) \Rightarrow^+ (\epsilon)$ ie $()$

language defined by a CFG G

$L(G) = \{ w \mid s \Rightarrow^+ w \}$ where

s = start is the start non-terminal of G , and

w = sequence consisting of (only) terminal symbols or ϵ

$L(G) = \{ \epsilon, (), (()), ((())), \dots \}$

Example: nested parens

$N = \{ q \}$

$\Sigma = \{ (,) \}$

$P = q \rightarrow (q)$
 $\quad \quad \quad \epsilon$

$q \Rightarrow \epsilon$

$q \Rightarrow (q) \Rightarrow ((q)) \Rightarrow (((\epsilon)))$

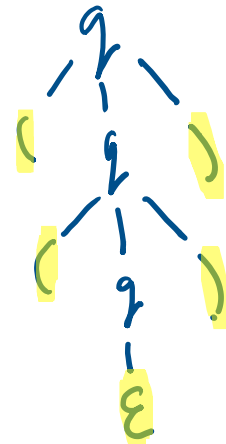
$q \stackrel{\pm}{\Rightarrow} (())$

Parse trees

= way to visualize a derivation

To derive a string (of terminal symbols):

- set **root** of parse tree to **start** symbol
- repeat
 - find a **leaf** non-terminal x
 - find production of the form $x \rightarrow \alpha$
 - "apply" production: **symbols in α** become the **children of x**
- until there are no more leaf non-terminals



Derived sequence determined from leaves, from left to right

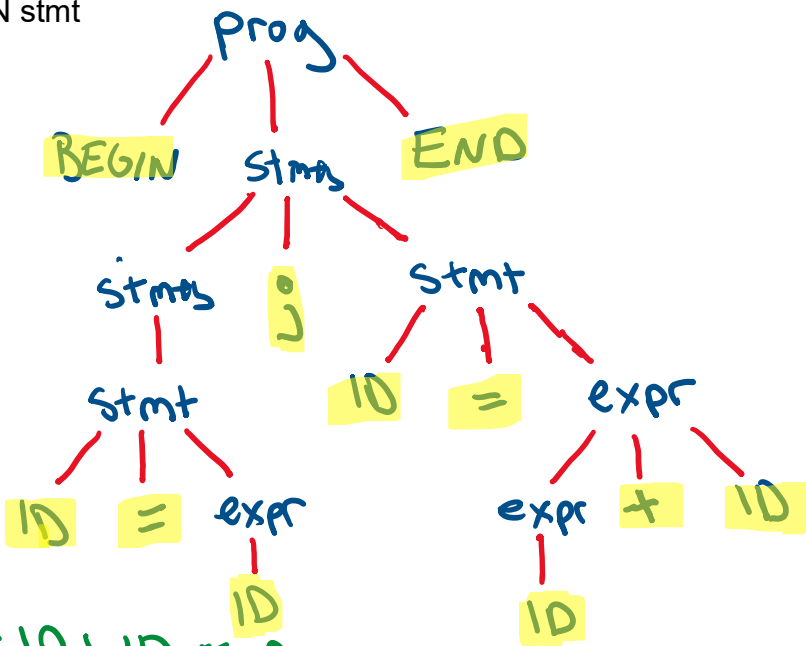
Sequence is: $()$

Parse tree example

Productions

- 1) prog → BEGIN stmts END
- 2) stmts → stmts SEMICOLON stmt
- 3) | stmt
- 4) stmt → ID ASSIGN expr
- 5) expr → ID
- 6) | expr PLUS ID

this notation is
BNF (or extended BNF)
↓
Backus-Naur Form

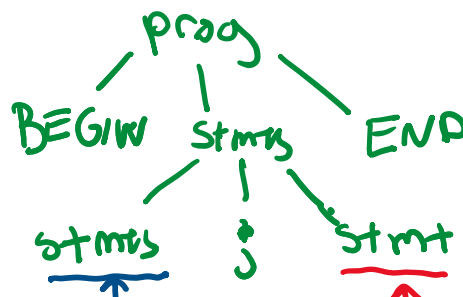


BEGIN ID=ID; ID=ID+ID END

Derivation order

Productions

- 1) prog → BEGIN stmts END
- 2) stmts → stmts SEMICOLON stmt
- 3) | stmt
- 4) stmt → ID ASSIGN expr
- 5) expr → ID
- 6) | expr PLUS ID



Leftmost derivation : leftmost non-terminal
is always expanded

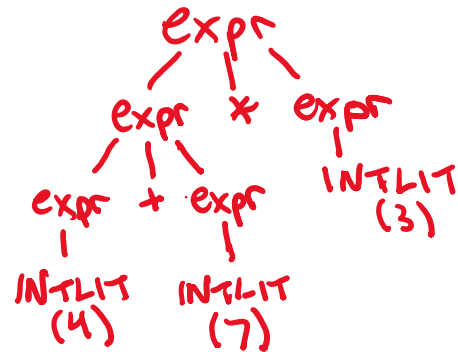
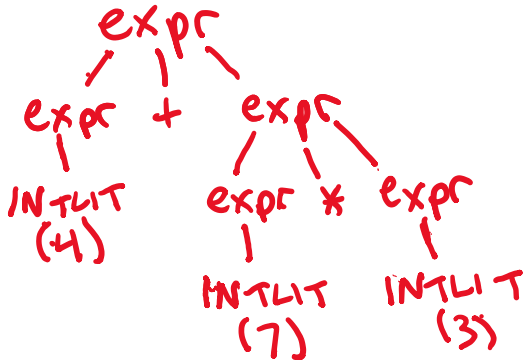
Rightmost derivation : rightmost non-terminal
is always expanded

Expression Grammar Example

- 1) $\text{expr} \rightarrow \text{INTLIT}$
- 2) $\text{expr} \rightarrow \text{expr PLUS expr}$
- 3) $\text{expr} \rightarrow \text{expr TIMES expr}$
- 4) $\text{expr} \rightarrow \text{LPAREN expr RPAREN}$

Goal: create a CFG for arithmetic expressions involving only +, *, parens, & integer literals

Derive: $4 + 7 * 3$



ambiguous grammar!

For grammar G and string w , G is **ambiguous** if there is

> 1 leftmost derivation of w

OR

> 1 rightmost derivation of w

OR

> 1 parse tree for w

these
are all
equivalent

Grammars for expressions

Goal: write a grammar that correctly reflects precedences and associativities

$$a + b * c \leftrightarrow a + (b * c) \quad \hookrightarrow a + b + c \leftrightarrow (a + b) + c$$

$$a = b = c \leftrightarrow a = (b = c)$$

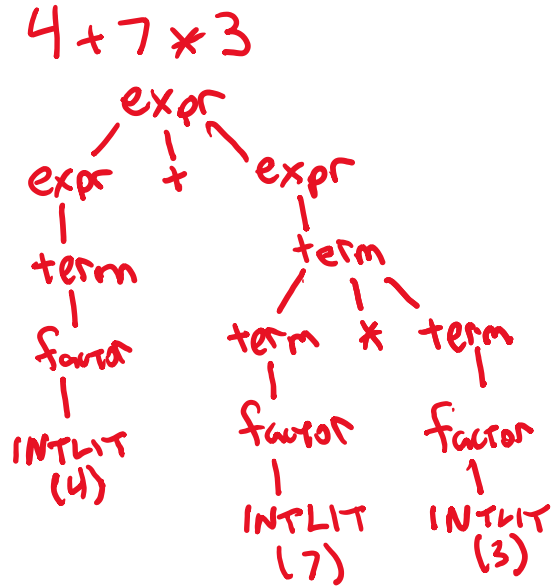
Precedence

- use different non-terminal for each precedence level
- start by re-writing production for lowest precedence operator first

Example

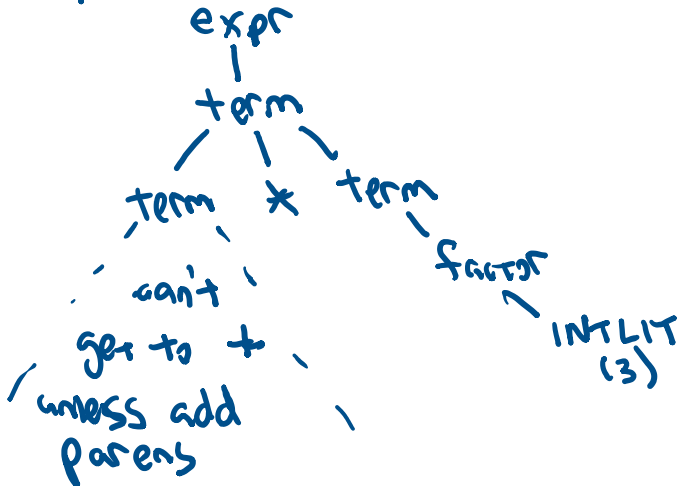
- 1) $\text{expr} \rightarrow \text{INTLIT}$
- 2) $\text{expr} \rightarrow \text{expr PLUS expr}$
- 3) $\text{expr} \rightarrow \text{expr TIMES expr}$
- 4) $\text{expr} \rightarrow \text{LPAREN expr RPAREN}$

$+$ has lowest precedence



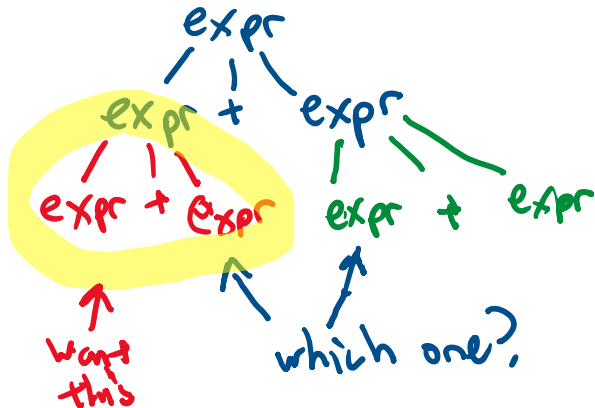
$\text{expr} \rightarrow \text{expr} + \text{expr}$
 $\quad \quad \quad |$
 $\quad \quad \quad \text{term}$
 $\text{term} \rightarrow \text{term} * \text{term}$
 $\quad \quad \quad |$
 $\quad \quad \quad \text{factor}$
 $\text{factor} \rightarrow \text{INTLIT}$
 $\quad \quad \quad |$
 $\quad \quad \quad (\text{expr})$

Try to make $*$ eval'd last



Grammars for expressions (cont.)

What about associativity? Consider $1 + 2 + 3$ equiv to $(1+2) + 3$



Definition: recursion in grammars

A grammar is **recursive** in non-terminal x if $x \Rightarrow + \alpha x \gamma$ for non-empty strings of symbols α and γ

A grammar is **left-recursive** in non-terminal x if $x \Rightarrow + x \gamma$ for non-empty string of symbols γ

A grammar is **right-recursive** in non-terminal x if $x \Rightarrow + \alpha x$ for non-empty string of symbols α

left associative

$+ - * /$

right associative

$= \wedge$

$$2^1 3^1 4 \equiv 2^3^4$$

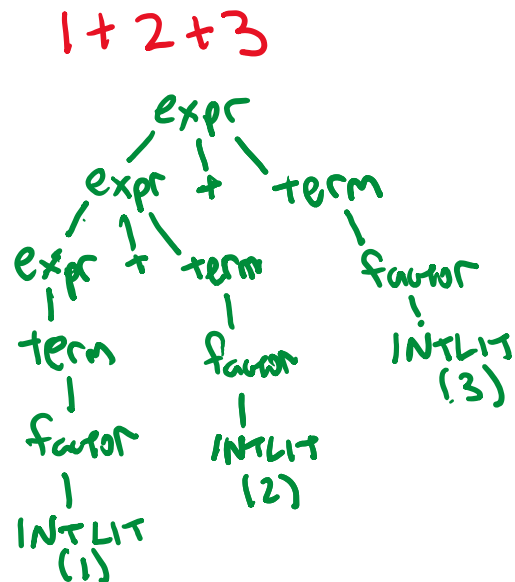
In expression grammars

for left associativity, use left recursion

for right associativity, use right recursion

Example

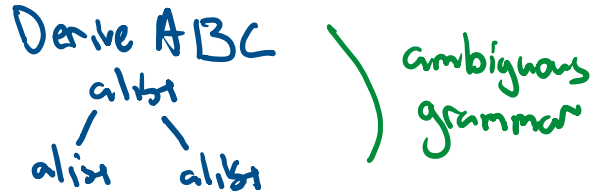
$\text{expr} \rightarrow \text{expr} + \text{~~expr~~ term}$
 $\text{term} \rightarrow \text{term} * \text{~~term~~ factor}$
 $\text{factor} \rightarrow \text{INTLIT} \mid (\text{expr})$



List grammars

Example a list with no separators, e.g., A B C D E F G

$alist \rightarrow ITEM$
 $| alist alist$

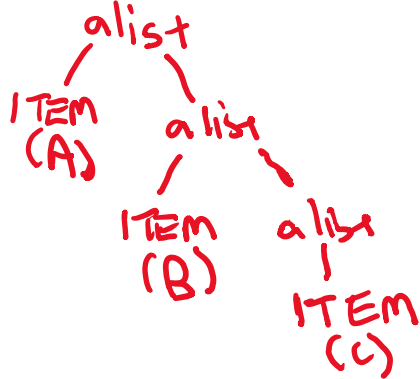


$alist \rightarrow ITEM$
 $| ITEM alist$

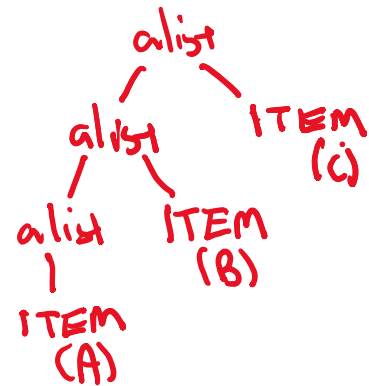
OR

$alist \rightarrow ITEM$
 $| alist ITEM$

Derive ABC



Associativity doesn't matter with lists so either grammar is fine



Another ambiguous example

$stmt \rightarrow$ IF cond THEN stmt
 $|$ IF cond THEN stmt ELSE stmt
 $|$...

Given this sequence in this grammar: if a then if b then s1 else s2
 How would you derive it?

