

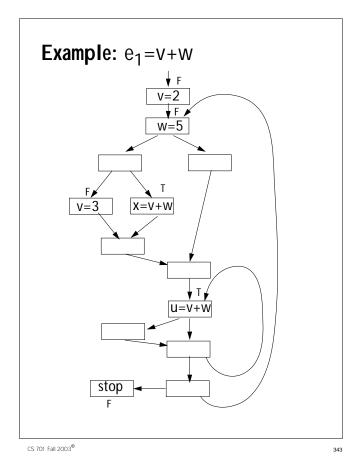
T (Expression is Very Busy)

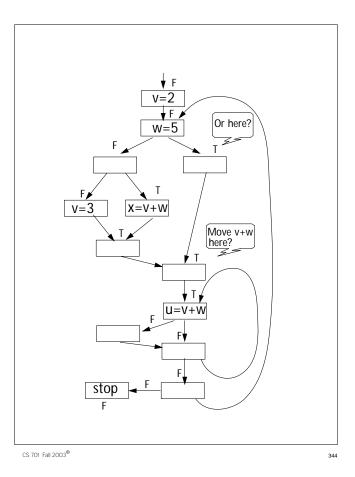
F (Expression is Not Very Busy)

As initial values, at the end of all exit nodes, nothing is very busy. Hence, for a given expression,

VeryBusyOut(b<sub>last</sub>) = F

The transfer function for  $e_1$  in block b is defined as: If  $e_1$  is computed in b before any of its operands Then VeryBusyIn(b) = T Elsif any of  $e_1$ 's operands are changed before  $e_1$  is computed Then VeryBusyIn(b) = F Else VeryBusyIn(b) = VeryBusyOut(b) The meet operation (to combine solutions) is: VeryBusyOut(b) = AND VeryBusyIn(s)  $s \in Succ(b)$ 





Identifying Identical Expressions

We can hash expressions, based on hash values assigned to operands and operators. This makes recognizing potentially redundant expressions straightforward.

For example, if H(a) = 10, H(b) = 21and H(+) = 5, then (using a simple product hash),  $H(a+b) = 10 \times 21 \times 5$  Mod TableSize

## Effects of Aliasing and Calls

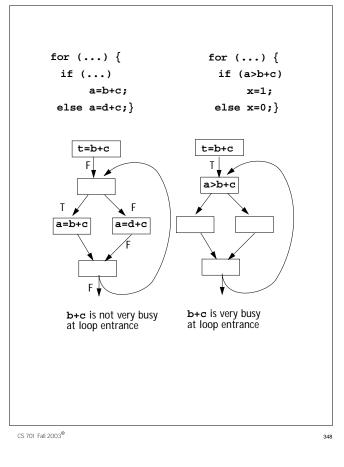
When looking for assignments to operands, we must consider the effects of pointers, formal parameters and calls.

An assignment through a pointer (e.g,  $*_{\mathbf{p}} = \mathbf{val}$ ) kills all expressions dependent on variables  $_{\mathbf{p}}$  might point too. Similarly, an assignment to a formal parameter kills all expressions dependent on variables the formal might be bound to.

A call kills all expressions dependent on a variable changeable during the call.

Lacking careful alias analysis, pointers, formal parameters and calls can kill all (or most) expressions.

# <section-header><text><text><text><text>



### **Reaching Definitions**

We have seen reaching definition analysis formulated as a set-valued problem. It can also be formulated on a per-definition basis.

That is, we ask "What blocks does a particular definition to v reach?"

This is a boolean-valued, forward flow data flow problem.

Initially,  $Defln(b_0) = false$ . For basic block b: DefOut(b) = If the definition being analyzed is the last definition to v in b Then True Elsif any other definition to v occurs in b Then False Else Defln(b) The meet operation (to combine solutions) is: DefIn(b) =OR DefOut(p)  $p \in Pred(b)$ To get all reaching definition, we do a series of single definition analyses.

### Live Variable Analysis

This is a boolean-valued, backward flow data flow problem. Initially, LiveOut( $b_{last}$ ) = false. For basic block b: Liveln(b) =If the variable is used before it is defined in b Then True Elsif it is defined before it is used in b Then False Else LiveOut(b) The meet operation (to combine solutions) is: LiveOut(b) = OR LiveIn(s)  $s \in Succ(b)$ 

CS 701 Fall 2003

# Bit Vectoring Data Flow Problems

The four data flow problems we have just reviewed all fit within a *single* framework.

Their solution values are Booleans (bits).

The meet operation is And or OR.

The transfer function is of the general form

 $Out(b) = (In(b) - KiII_b) U Gen_b$ 

or

 $ln(b) = (Out(b) - Kill_b) U Gen_b$ 

where  $Kill_b$  is true if a value is "killed" within b and  $Gen_b$  is true if a value is "generated" within b.

CS 701 Fall 2003<sup>©</sup>

351

In Boolean terms: Out(b) = (In(b) AND Not Kill<sub>b</sub>) OR Gen<sub>b</sub>

or

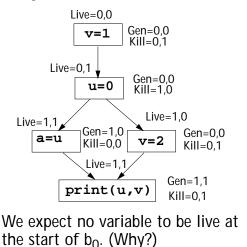
 $In(b) = (Out(b) AND Not Kill_b) OR Gen_b$ 

An advantage of a bit vectoring data flow problem is that we can do a series of data flow problems "in parallel" using a bit vector.

Hence using ordinary word-level ANDs, ORs, and NOTs, we can solve 32 (or 64) problems simultaneously.

## Example

Do live variable analysis for u and v, using a 2 bit vector:



### **Depth-First Spanning Trees**

Sometimes we want to "cover" the nodes of a control flow graph with an acyclic structure.

This allows us to visit nodes once, without worrying about cycles or infinite loops.

Also, a careful visitation order can approximate forward control flow (very useful in solving forward data flow problems).

A Depth-First Spanning Tree (DFST) is a tree structure that covers the nodes of a control flow graph, with the start node serving as root of the DFST.

### **Building a DFST**

We will visit CFG nodes in depth-first order, keeping arcs if the visited node hasn't be reached before.

To create a DFST, T, from a CFG, G:

- 1. T  $\leftarrow$  empty tree
- 2. Mark all nodes in G as "unvisited."
- 3. Call DF(start node)

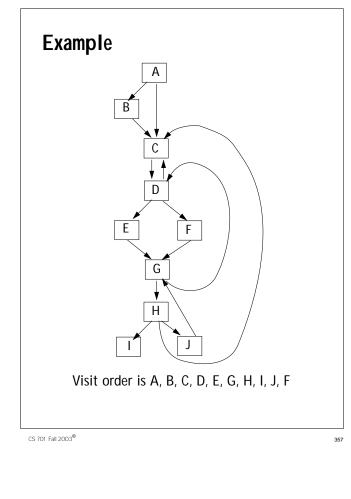
### DF (node) {

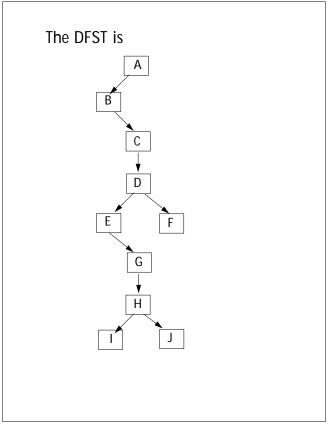
CS 701 Fall 2003

- 1. Mark node as visited.
- 2. For each successor, s, of node in G:
  - If s is unvisited
    - (a) Add node  $\rightarrow$  s to T
    - (b) Call DF(s)

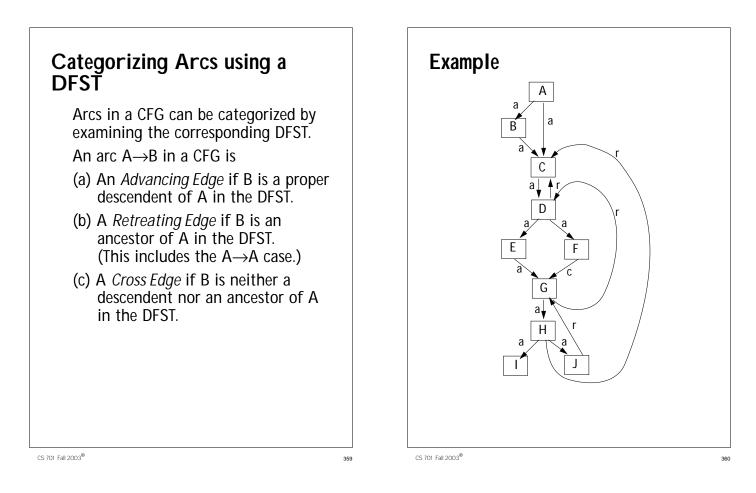
CS 701 Fall 2003®

355





CS 701 Fall 2003®



### Depth-First Order

Once we have a DFST, we can label nodes with a *Depth-First Ordering* (DFO).

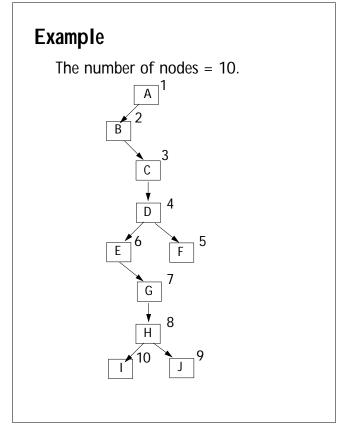
Let i = the number of nodes in a CFG (= the number of nodes in its DFST). DFO(node) {

```
For (each successor s of node) do
DFO(s);
```

```
Mark node with i;
```

```
i--;
```

}



CS 701 Fall 2003®

# Application of Depth-First Ordering

- Retreating edges (a necessary component of loops) are easy to identify:

   a→b is a retreating edge if and only if dfo(b) ≤ dfo(a)
- A depth-first ordering in an excellent *visit order* for solving forward data flow problems. We want to visit nodes in essentially topological order, so that all predecessors of a node are visited (and evaluated) before the node itself is.

CS 701 Fall 2003®