CS 839: Foundation Models
ML Mini-Review

Fred Sala

University of Wisconsin-Madison

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Announcements

- **Resources**
  - https://mlstory.org/ : fun new book by Hardt and Recht
- Class roadmap:

Thursday Sept. 16	ML Mini-Review
Tuesday Sept. 21	Transformers & Attention
Thursday Sept. 23	Language Models I
Tuesday Sept. 28	Language Models II
Thursday Sept. 30	Prompting I

Mostly Language Models

Outline

- **General Supervised Learning Review**
  - Features, labels, hypothesis classes, training, generalization
- **Neural Networks**
  - Perceptrons, MLPs, training and backprop, CNNs, brief review of RNNs and LSTMs, data augmentation
- **Self-Supervised Learning**
  - Getting representations, pretext tasks, using representations

Supervised Learning: Formal Setup

Problem setting

- Set of possible instances $\mathcal{X}$
- Unknown *target function* $f : \mathcal{X} \rightarrow \mathcal{Y}$
- Set of *models* (a.k.a. *hypotheses*): $\mathcal{H} = \{h | h : \mathcal{X} \rightarrow \mathcal{Y}\}$

Get

- Training set of instances for unknown target function,

$$(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), \ldots, (x^{(n)}, y^{(n)})$$

safe

poisonous

safe

Supervised Learning: Objects

Three types of sets

- Input space, output space, hypothesis class

$$\mathcal{X}, \mathcal{Y}, \mathcal{H}$$

- **Examples**:
  - Input space: feature vectors $\mathcal{X} \subseteq \mathbb{R}^d$

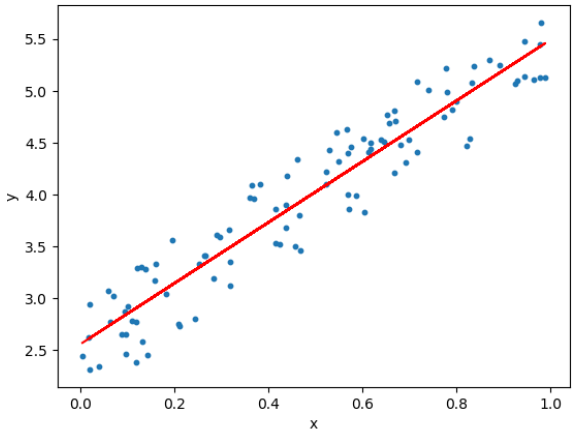
  - Output space:
    - **Binary** $\mathcal{Y} = \{-1, +1\}$ safe poisonous
    - **Continuous** $\mathcal{Y} \subseteq \mathbb{R}$ $13.23°$

Output Space: Classification vs. Regression

Choices of $\mathcal{Y}$ have special names:

- Discrete: "**classification**". The elements of $\mathcal{Y}$ are **classes**
  - Note: doesn't have to be binary

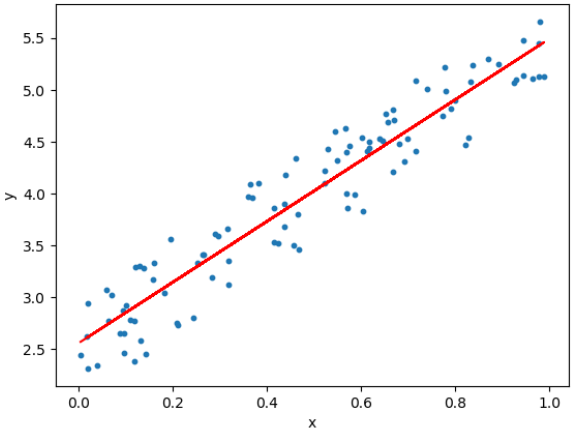
- Continuous: "**regression**"
  - Example: linear regression



- There are other types…

Hypothesis Class

We talked about $\mathcal{X}, \mathcal{Y}$ what about $\mathcal{H}$?



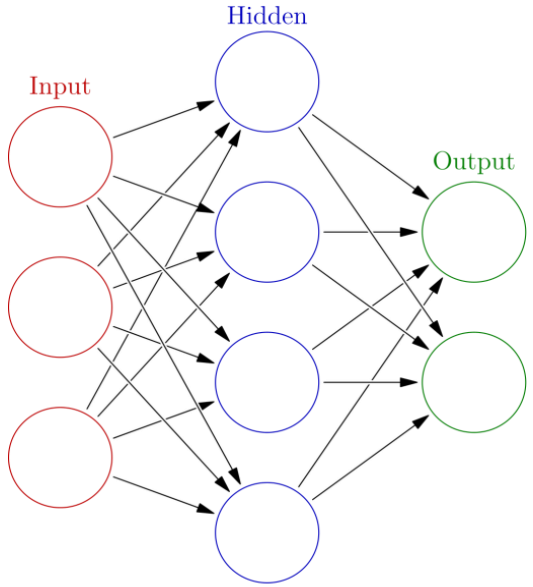
- Pick specific class of models. Ex: **linear models**:

$$h_\theta(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \ldots + \theta_d x_d$$

- Ex: **feedforward neural networks**

$$f^{(k)}(x) = \sigma(W_k^T f^{(k-1)}(x)))$$

- **Parameters:** θ, w.



Wikipedia

SL: Training & Generalization

Goal: model *h* that best approximates *f*

- One way: empirical risk minimization (ERM)

$$\hat{f} = \arg\min_{h \in \mathcal{H}} \frac{1}{n} \sum_{i=1}^{n} \ell(h(x^{(i)}), y^{(i)}))$$

Hypothesis Class

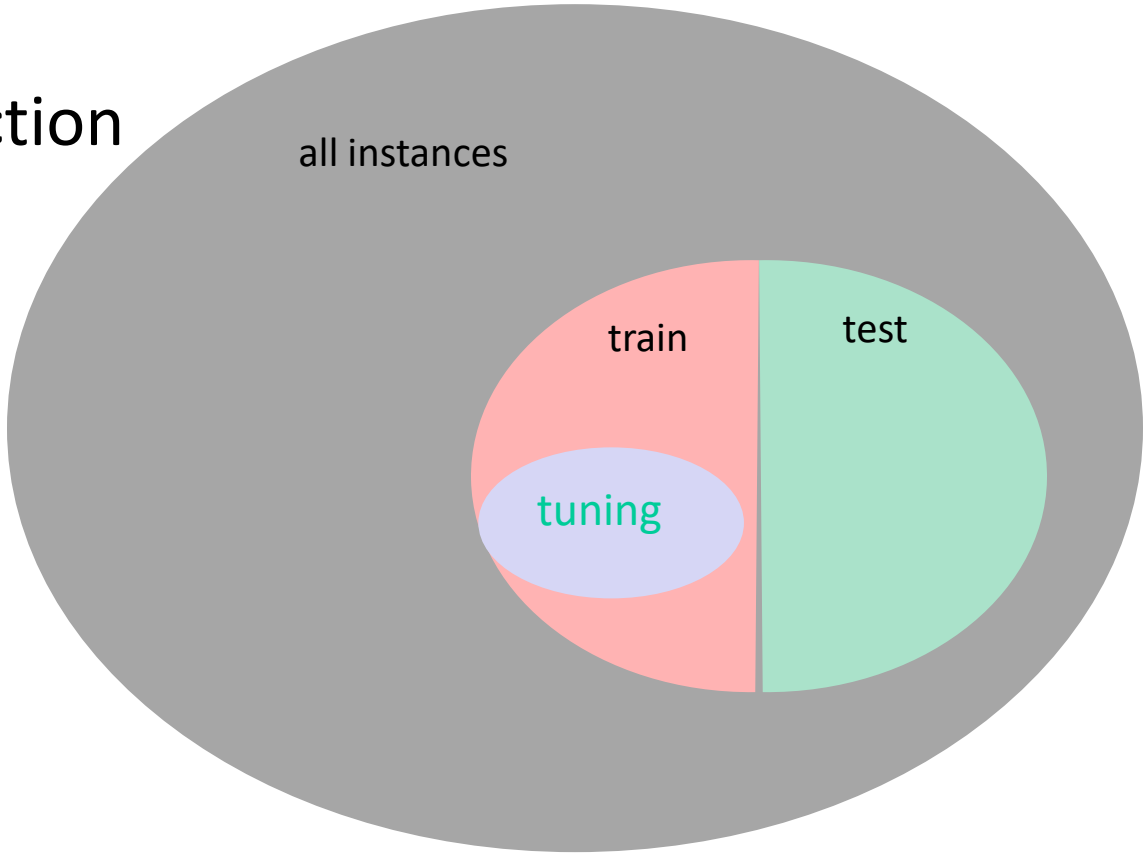
Loss function (how far are we)?

Model prediction

- Generalization?

Evaluation: Validation and Test Sets

- A *validation set* (a.k.a. *tuning set*) is
  - Not used for primary training process, used to select among models
- A *test set*
  - Not used for training or selection
  - Compute metrics



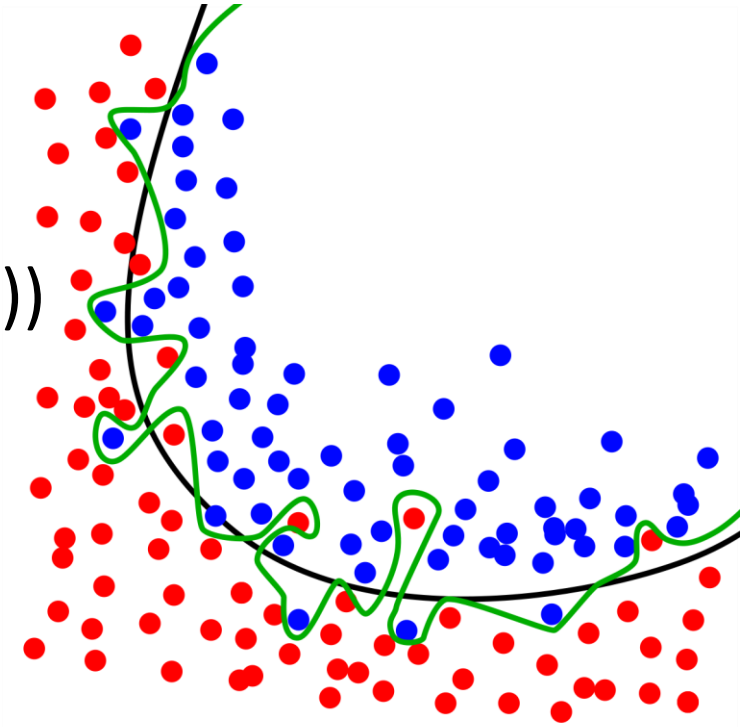
Overfitting

Notation: error of model *h* over

- training data: $\text{error}_D(h)$
- entire distribution of data: $\text{error}_{\mathcal{D}}(h)$

Model *h* **overfits** training data if it has

- a low error on the training data (low $\text{error}_D(h)$)
- high error on the entire distribution (high $\text{error}_{\mathcal{D}}(h)$)

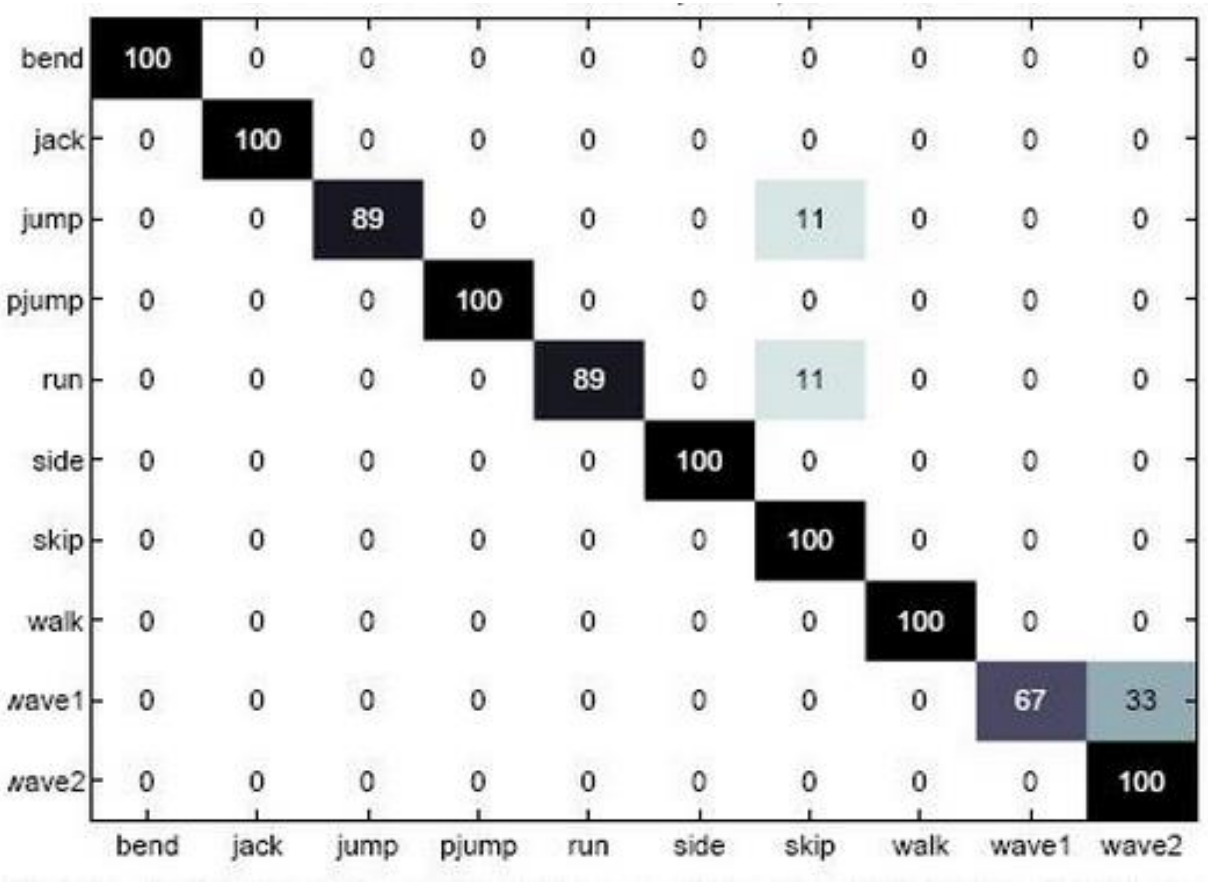


Wikipedia

Beyond Accuracy: Confusion Matrices

- How can we understand what types of mistakes a learned model makes?

task: activity recognition from video

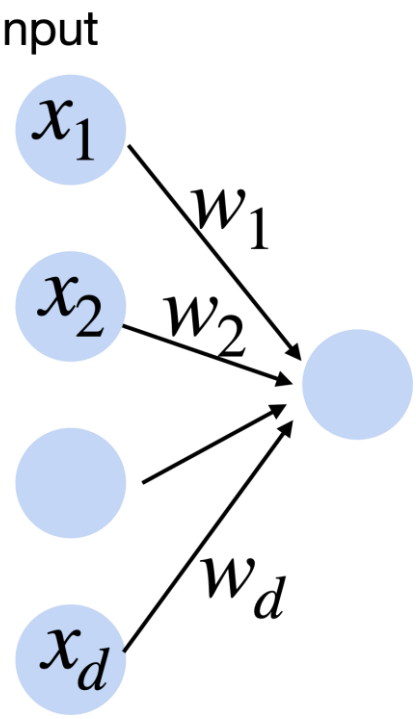


actual class

predicted class

Break & Questions

Perceptron: Simple Network

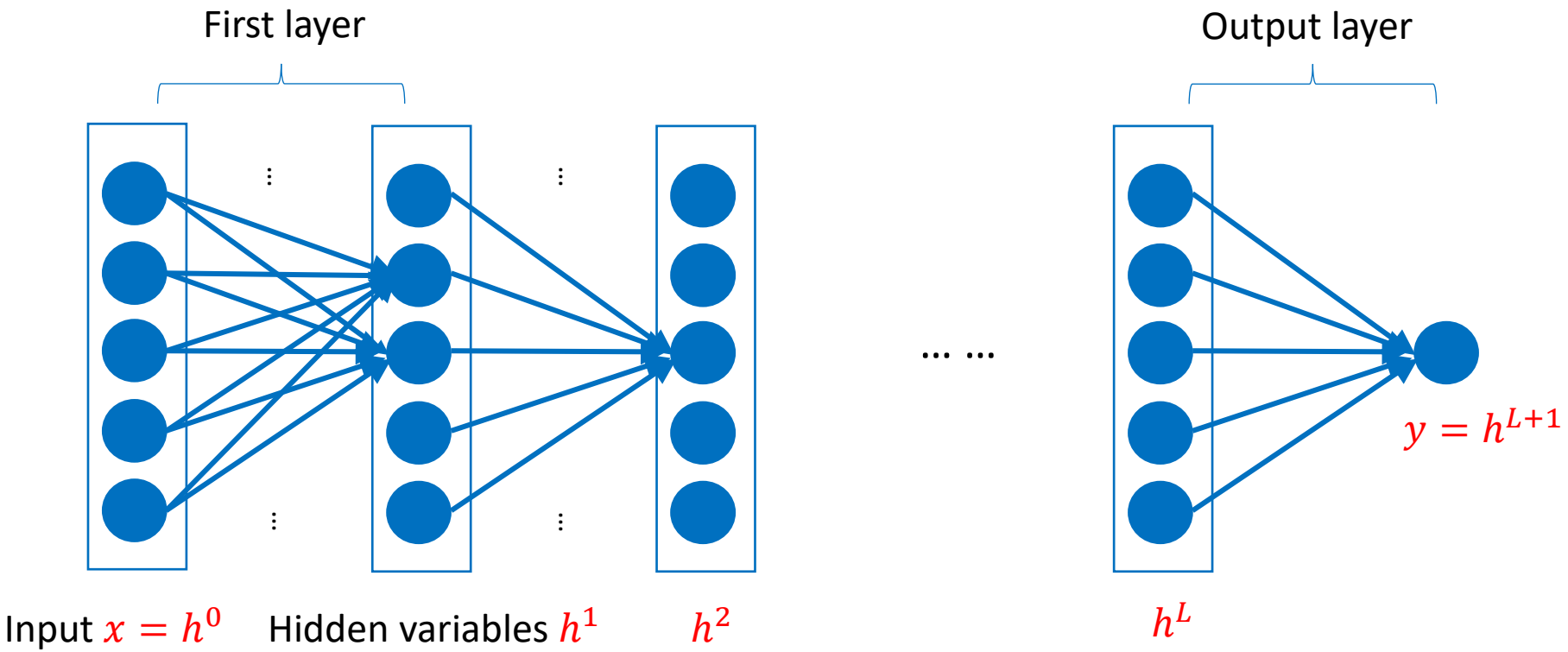


$$\hat{y}(x) = \begin{cases} 1 & w^T x \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

[McCulloch & Pitts, **1943**; Rosenblatt, **1959**; Widrow & Hoff, **1960**]

Neural Networks: Multilayer Perceptrons

An $(L+1)$-layer network

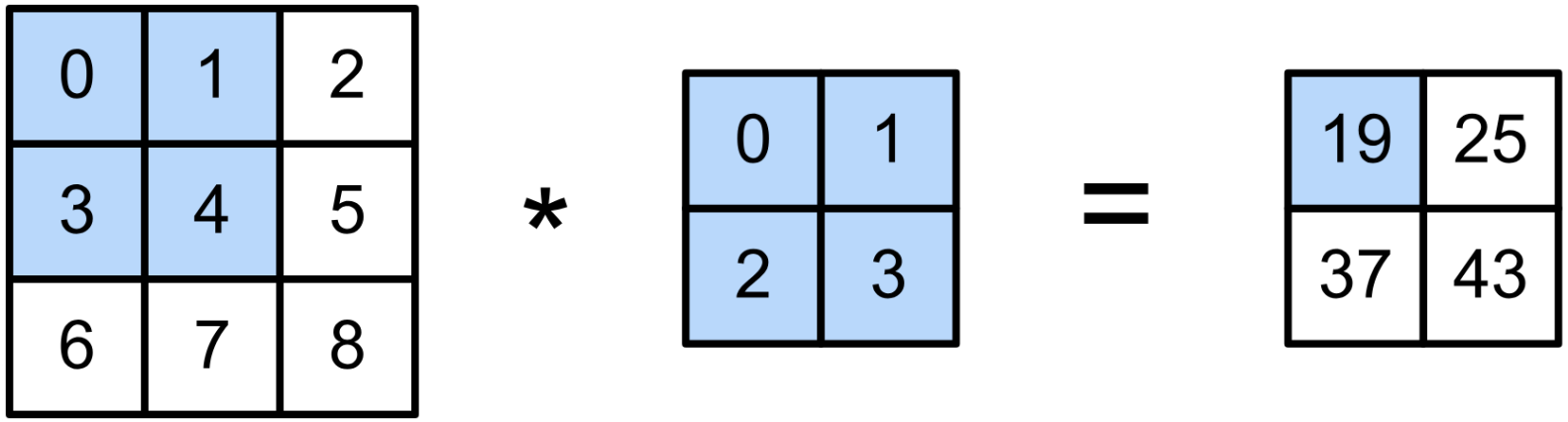


Training Neural Networks

- Algorithm:
  - Get $D = \{(x^{(1)}, y^{(1)}), \ldots, (x^{(n)}, y^{(n)})\}$
  - Initialize weights
  - Until stopping criteria met,
    - For each training point $(x^{(i)}, y^{(i)})$
    - Compute: $f_{\text{network}}(x^{(d)})$ ← **Forward Pass**
    - Compute gradient: $\nabla L^{(i)}(w) = \left[\frac{\partial L^{(d)}}{\partial w_0}, \frac{\partial L^{(d)}}{\partial w_1}, \ldots, \frac{\partial L^{(d)}}{\partial w_m}\right]^T$ ← **Backward Pass**
    - Update weights: $w \leftarrow w - \alpha \nabla L^{(i)}(w)$

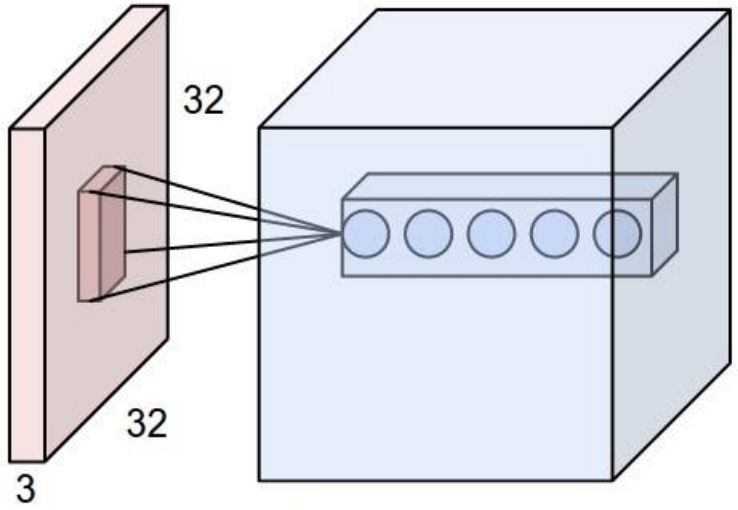
Neural Networks: Convolution Layers

- Notation:
  - *X:* n_h x n_w input matrix
  - *W:* k_h x k_w kernel matrix
  - *b* : bias (a scalar)
  - *Y*: () x () output matrix
- As usual *W*, *b* are learnable parameters



Neural Networks: Convolution NNs

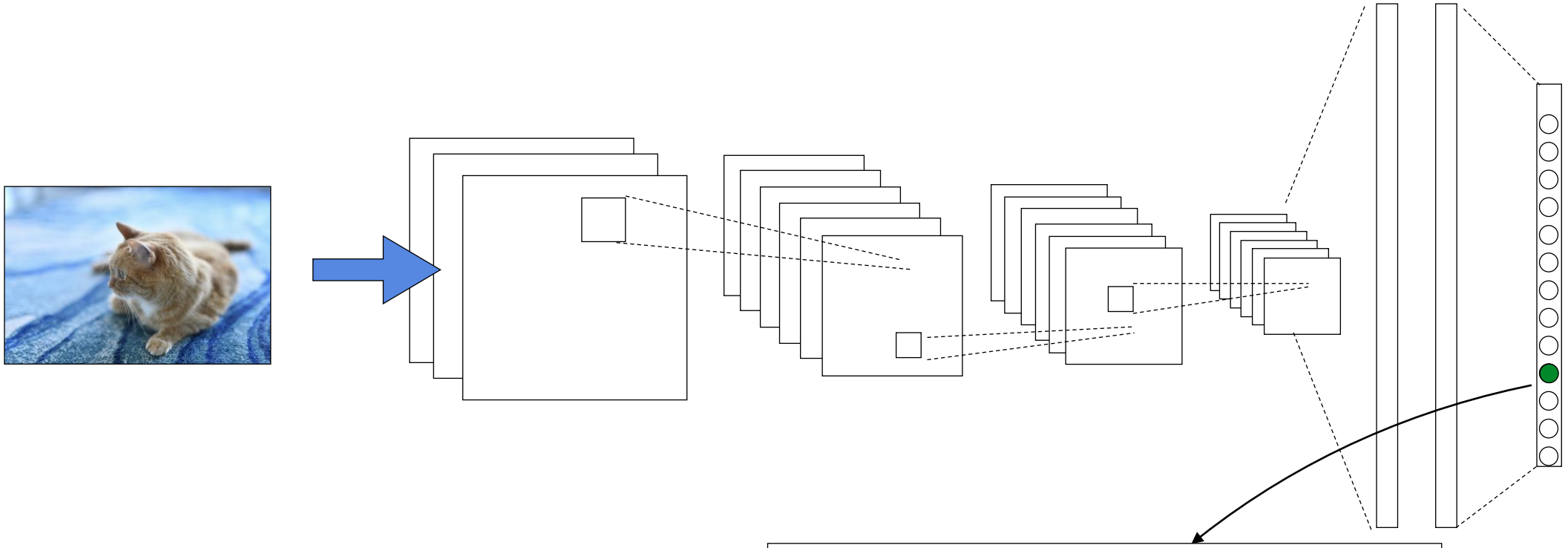
- Properties
  - Input: volume c_i x n_h x n_w (channels x height x width)
  - Hyperparameters: # of kernels/filters c_o, size k_h x k_w, stride s_h x s_w, zero padding p_h x p_w
  - Output: volume c_o x m_h x m_w (channels x height x width)
  - Parameters: k_h x k_w x c_i per filter, total $(k_h$ x k_w x $c_i)$ x c_o



Stanford CS 231n

Training a CNN

- Q: so we have a bunch of layers. How do we train?
- A: same as before. Apply softmax at the end, use backprop.

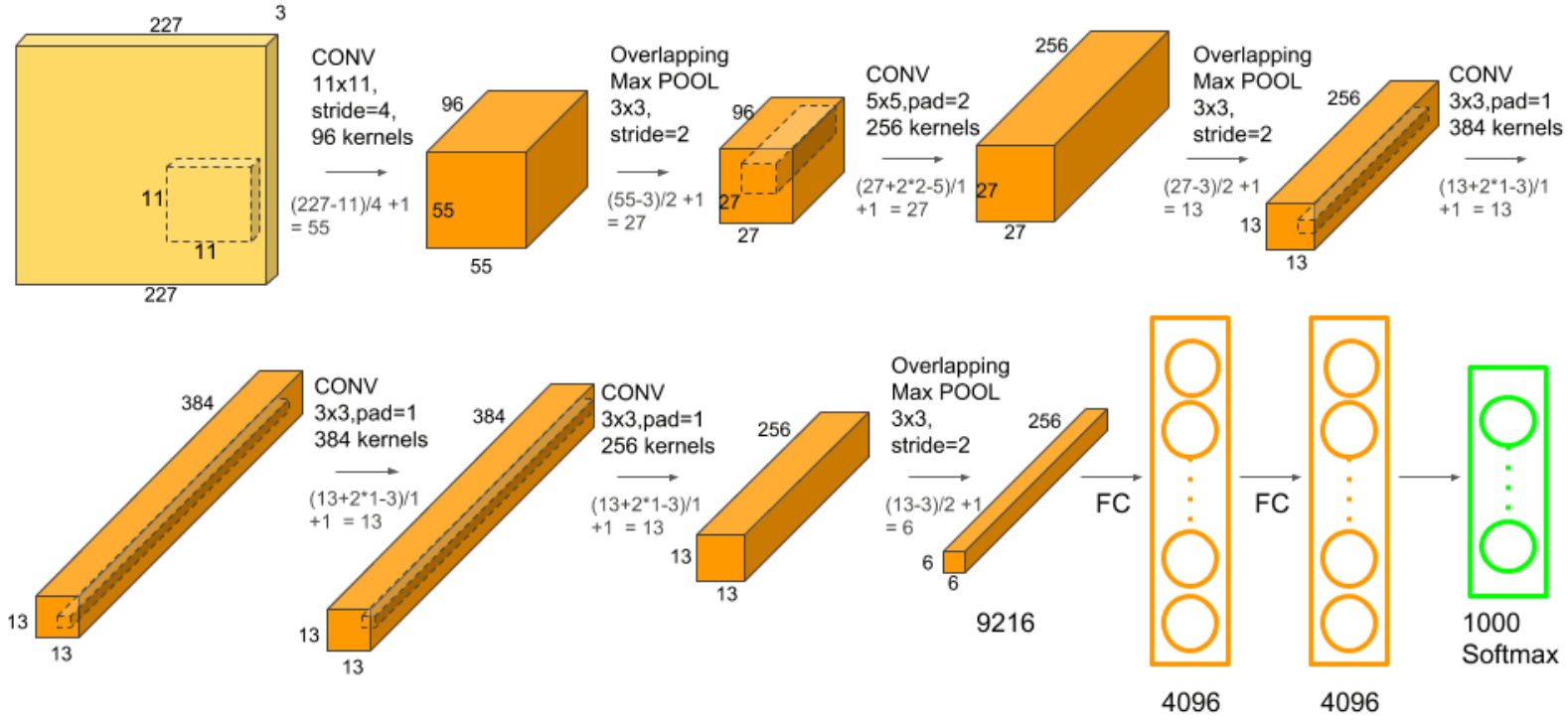


$$p_i(\boldsymbol{x}) = \frac{\exp\left(f_i(\boldsymbol{x})\right)}{\sum_{j=1}^{N} \exp\left(f_j(\boldsymbol{x})\right)},$$

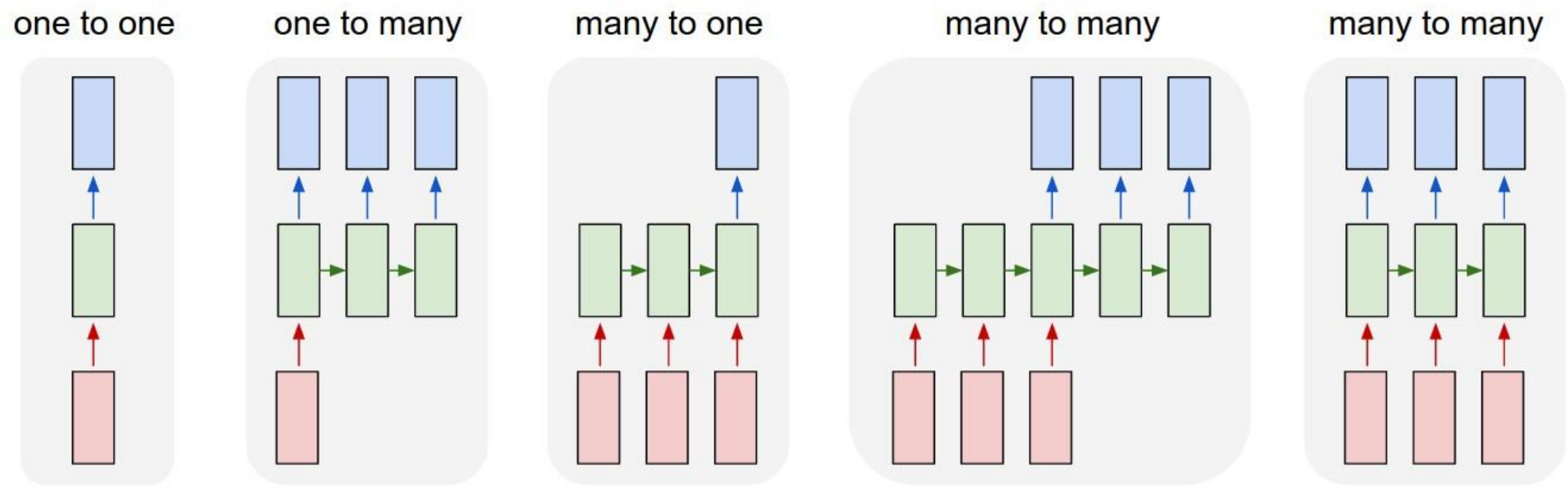
softmax

CNN Architectures: AlexNet

- First of the major advancements: AlexNet
- Wins 2012 ImageNet competition
- Major trends: deeper, bigger LeNet



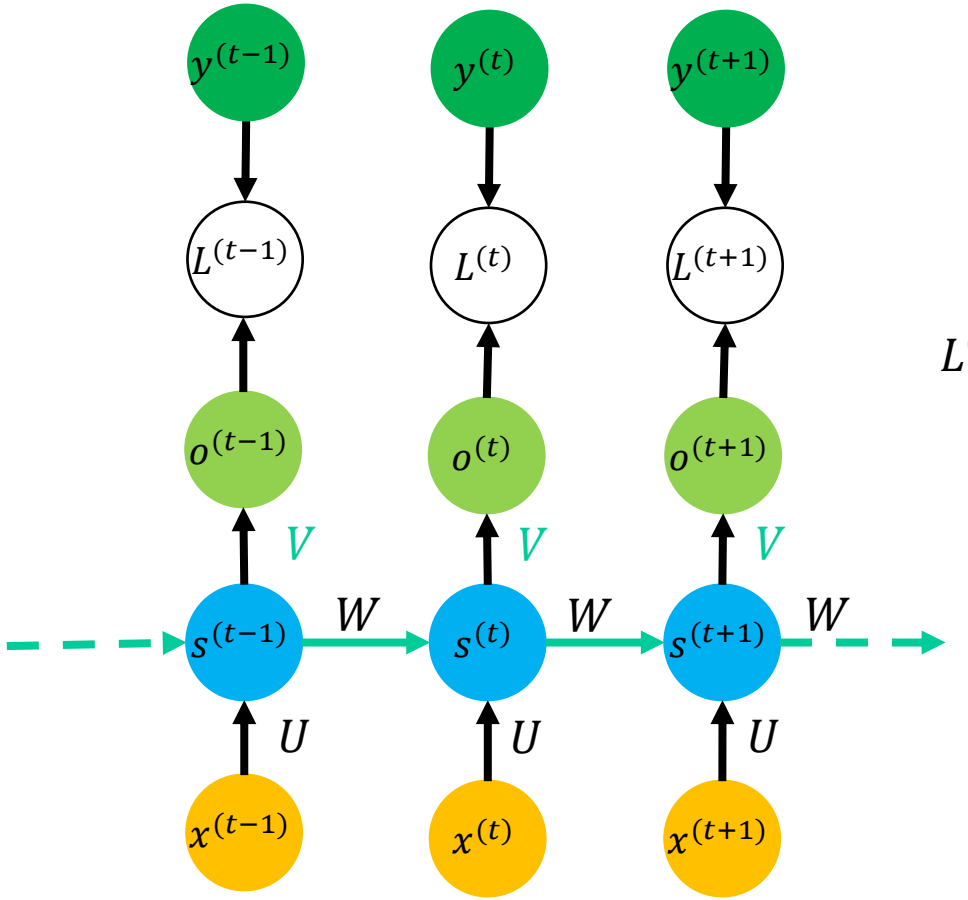
Tasks We Can Handle with NNs?



- Mostly talked about (1) so far
  - Others: need a new kind of model

Neural Networks: Simple RNNs

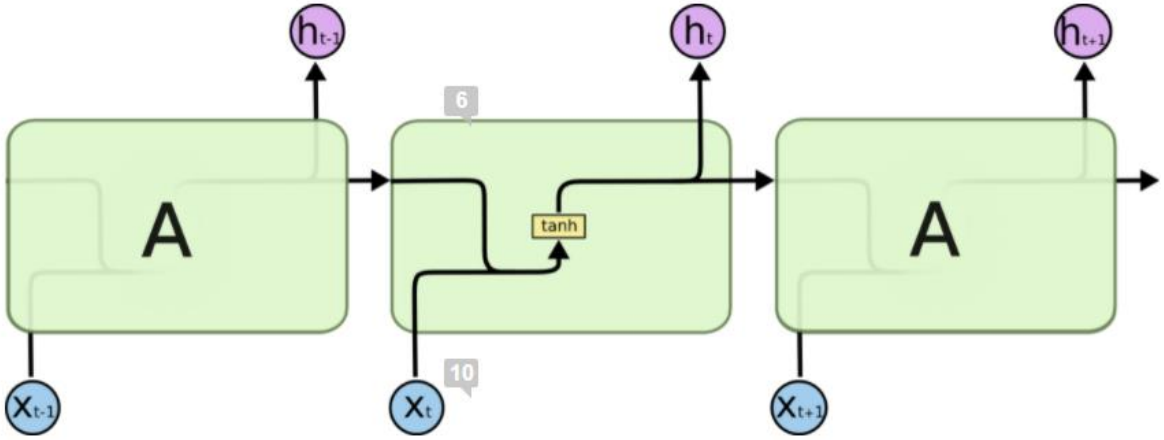
- Classical RNN variant:



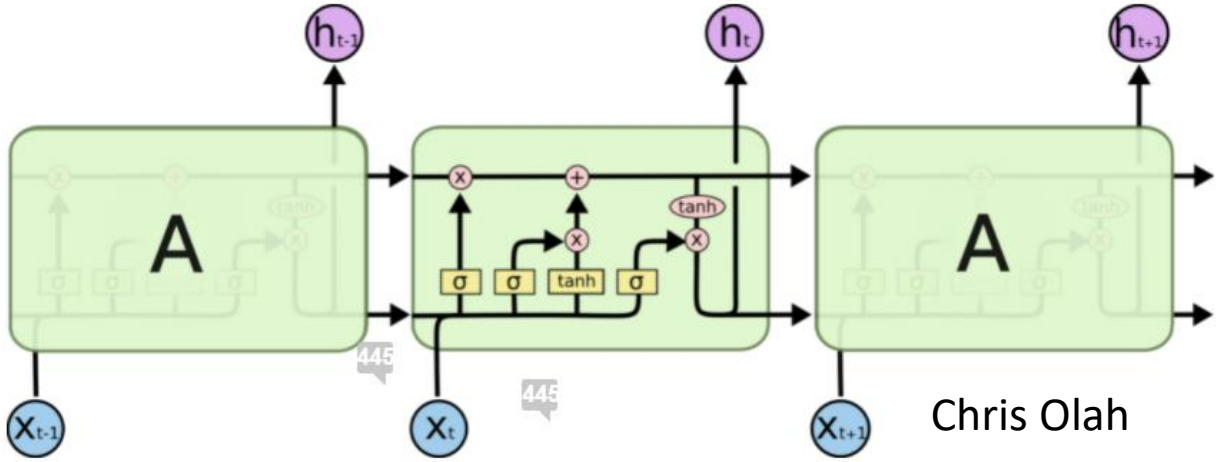
$$a^{(t)} = b + Ws^{(t-1)} + Ux^{(t)}$$
$$s^{(t)} = \tanh\left(a^{(t)}\right)$$
$$o^{(t)} = c + Vs^{(t)}$$
$$\hat{y}^{(t)} = \text{softmax}\left(o^{(t)}\right)$$
$$L^{(t)} = \text{CrossEntropy}(y^{(t)}, \hat{y}^{(t)})$$

Neural Networks: LSTMs

- RNN: can write structure as:



- Long Short-Term Memory: deals with problem. Cell:



Chris Olah

Data Augmentation

Augmentation: transform + add new samples to dataset

- Transformations: based on domain
- Idea: build **invariances** into the model
  - **Ex**: if all images have same alignment, model learns to use it
- Keep the label the same!

Data Augmentation: Examples

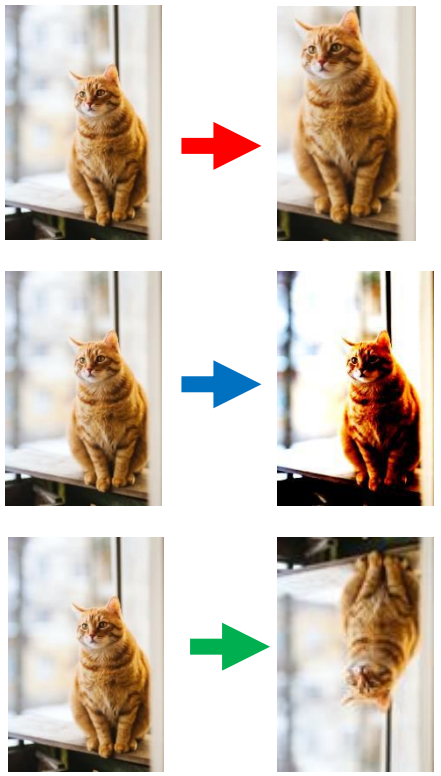
Examples of transformations for images

- **Crop** (and zoom)
- **Color** (change contrast/brightness)
- **Rotations+** (translate, stretch, shear, etc)

Many more possibilities. Combine as well!

Q: how to deal with this at **test time**?

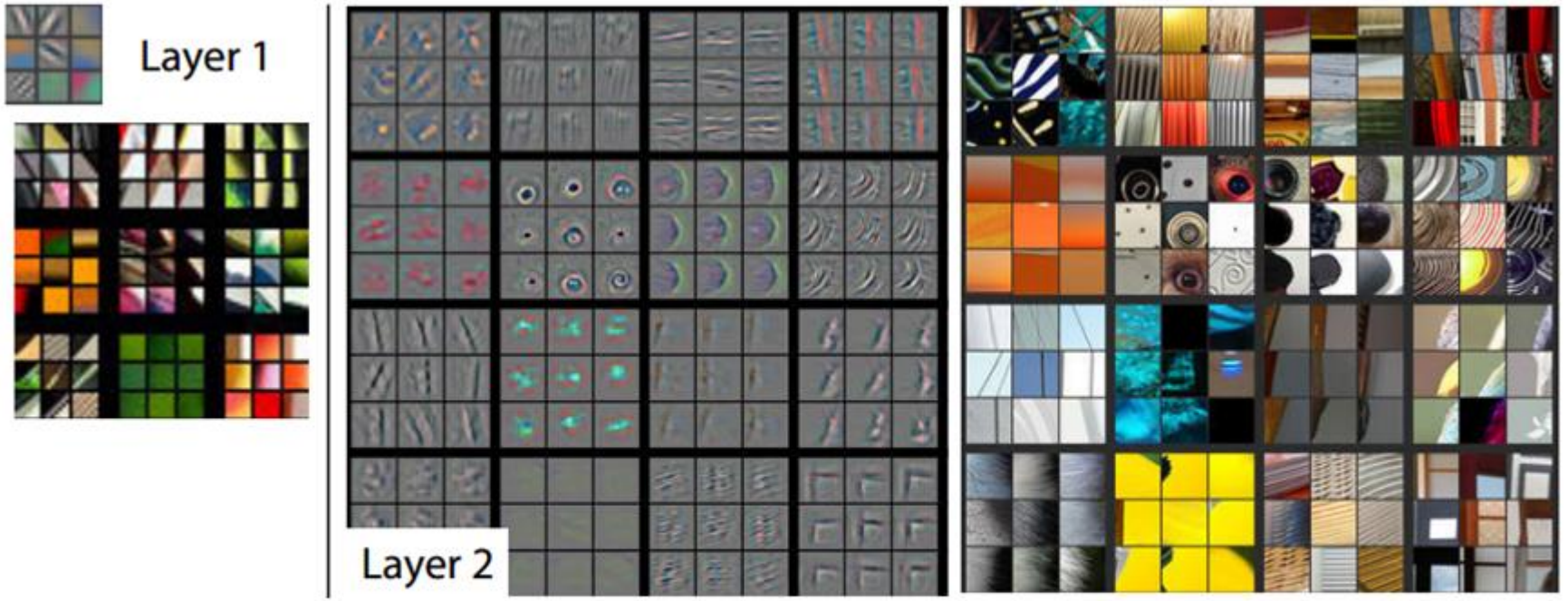
- A: transform, test, average



Break & Questions

Representations

- Basic idea in ML is to discover useful representations
  - I.e., higher level features that are discriminative
  - These are not necessarily present in raw data…



Visualizations of Layer 1 and 2. Each layer illustrates 2 pictures, one which shows the filters themselves and one that shows what part of the image are most strongly activated by the given filter. For example, in the space labled Layer 2, we have representations of the 16 different filters (on the left)

Desphande

Where to Get Representations**?**

- Deep learning:
  - Automatically obtain good features, but
  - **Downside**: Need lots of labeled data

- Pre-trained models:
  - E.g., ResNets trained on ImageNet. Use last layer (pre-prediction)
  - **Downside**: pre-trained task may not match our goal task

- Generative model encoders:
  - **Downside**: may not relate to semantics we care about

Representations from **Self Supervision**

- There's lots of information in our dataset already
  - Of course, specific to our task

- Need to create tasks from unlabeled data: "Pretext tasks"
  - Ex: predict stuff you already know

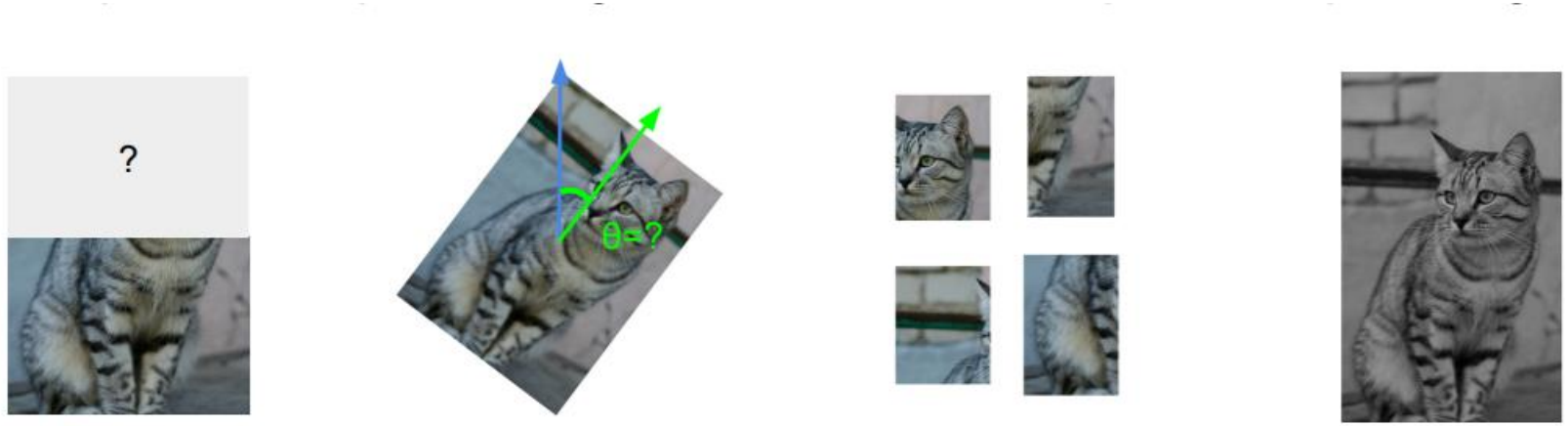


image completion | rotation prediction | "jigsaw puzzle" | colorization

Using the Representations

- Don’t care specifically about our performance on self-task
- Use the learned network as a feature extractor
- Once we have labels for a particular task, train
  - A small amount of data