

CS 839: Foundation Models Models I

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Announcements

•Announcement:

Homework 1 is released

•Class roadmap:

Thursday Sept. 19	Models I
Tuesday Sept. 24	Models II
Thursday Sept. 26	Prompting I
Tuesday Oct. 1	Prompting II
Thursday Oct. 3	Specialization

Mostly Language Models

Outline

•From Last Time

• Finish up SSMs, a little bit more on decoders

Encoder-only Models

•Example: BERT, architecture, multitask training, fine-tuning

Decoder-only Models

•Example: GPT, architecture, basic functionality

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State-Space Model: Discrete Form

Step 2: let's make this a discrete function

State Input \downarrow \downarrow \downarrow $x_k = \overline{A}x_{k-1} + \overline{B}u_k$ Output \rightarrow $y_k = \overline{C}x_k$

- Ignored D
- •Can create approximations of A,B,C through discretizing.
- •Looks a lot like an RNN! (or, a linear version of one)

State-Space Model: Convolutional Form

Step 3: let's unroll the recursion

$$\begin{aligned} x_0 &= \overline{B}u_0 & x_1 = \overline{AB}u_0 + \overline{B}u_1 & x_2 = \overline{A}^2\overline{B}u_0 + \overline{AB}u_1 + \overline{B}u_2 \\ y_0 &= \overline{CB}u_0 & y_1 = \overline{CAB}u_0 + \overline{CB}u_1 & y_2 = \overline{CA}^2\overline{B}u_0 + \overline{CAB}u_1 + \overline{CB}u_2 \end{aligned}$$

$$y_k = \overline{CA}^k \overline{B} u_0 + \overline{CA}^{k-1} \overline{B} u_1 + \dots + \overline{CAB} u_{k-1} + \overline{CB} u_k$$

In general, $y = \overline{K} * u.$

•This is a **convolution**!

State-Space Model: Convolutional Form

Step 3: let's unroll the recursion

• Convolution
$$y_k = \overline{CA}^k \overline{B} u_0 + \overline{CA}^{k-1} \overline{B} u_1 + \dots + \overline{CAB} u_{k-1} + \overline{CB} u_k$$
$$y = \overline{K} * u.$$

- •But a weird one. It's a very **long** convolution.
 - Kernel as long as the input sequence (say, L).
 - Naively, is this better than attention?
 - Let's do **something else** instead.

Interlude: Time & Frequency Domains

Back to Signals and Systems class,

- •Convolution in the time-domain is element-wise multiplication in the frequency domain
- •So low-complexity.
- •But, need to convert to frequency domain
- •Solution: **FFT.** O(L log L) (and also for iFFT, to invert back).
- •So, can compute fast and use during training!

$$y_k = \overline{CA}^k \overline{B} u_0 + \overline{CA}^{k-1} \overline{B} u_1 + \dots + \overline{CAB} u_{k-1} + \overline{CB} u_k$$

 $y = \overline{K} * u.$

Back to SSM Picture

Back to the formula

$$x_k = \overline{A}x_{k-1} + \overline{B}u_k$$
$$y_k = \overline{C}x_k$$

- •Just directly making all of these trainable parameters doesn't work so well.
 - Similar issues as in RNNs: stuff blowing up
 - Instead, various models propose approaches
- S4 (Structured State Space Models) Gu et al' 22
 - Build A with a special fixed transition matrix that is good at memorization
 - Couple with a particular parametrization to get the discretization.

Using SSMs as Layers

Back to the formula

 $x_k = \overline{A}x_{k-1} + \overline{B}u_k$ $y_k = \overline{C}x_k$

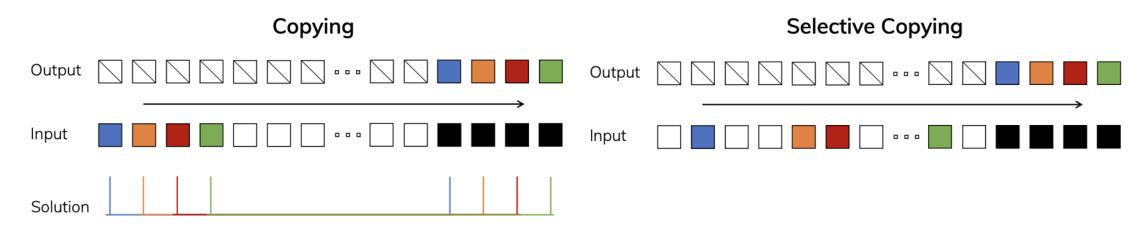
S4 (Structured State Space Models) Gu et al' 22

- Special A state transition matrix
- Special parametrization/choice of trainable parameters
- How to actually use these? Need to define a layer,
 - Stack H of them together (similar to conv layers, multihead attn)
 - Mix with linear layer, place activation function at the end

S4 Results: The Good and the Bad

Models like S4 can address very long sequences

- "S4 solves the Path-X task, an extremely challenging task that involves reasoning about LRDs over sequences of length ... 16384.
 All previous models have failed..."
- •But, can struggle with "selective" tasks.



S4 Results: The Good and the Bad

Solution: need some type of context-aware approach

•Mamba Model

• Gu and Dao '23, "Mamba: Linear-Time Sequence Modeling with Selective State Spaces"

Algorithm 1 SSM (S4)	Algorithm 2 SSM + Selection (S6)
Input: <i>x</i> : (B, L, D)	Input: $x : (B, L, D)$
Output: <i>y</i> : (B, L, D)	Output: $y : (B, L, D)$
1: \mathbf{A} : (D, N) \leftarrow Parameter	1: $A : (D, N) \leftarrow Parameter$
\triangleright Represents structured $N \times N$ matrix	\triangleright Represents structured $N \times N$ matrix
2: \boldsymbol{B} : (D, N) \leftarrow Parameter	2: \boldsymbol{B} : (B, L, N) $\leftarrow s_{\boldsymbol{B}}(\boldsymbol{x})$
3: $C : (D, N) \leftarrow Parameter$	3: $C: (B, L, N) \leftarrow s_C(x)$
4: Δ : (D) $\leftarrow \tau_{\Delta}$ (Parameter)	4: $\Delta : (B, L, D) \leftarrow \tau_{\Delta}(Parameter + s_{\Delta}(x))$
5: $\overline{A}, \overline{B}$: (D, N) \leftarrow discretize(Δ, A, B)	5: $\overline{A}, \overline{B} : (B, L, D, N) \leftarrow \text{discretize}(\Delta, A, B)$
6: $y \leftarrow SSM(\overline{A}, \overline{B}, C)(x)$	6: $y \leftarrow SSM(\overline{A}, \overline{B}, C)(x)$
Time-invariant: recurrence or convolution	► Time-varying: recurrence (<i>scan</i>) only
7: return y	7: return y

Lots of Related Approaches & Variations

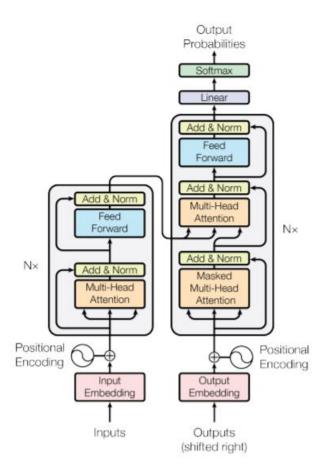
- •Linear attention. "Transformers are RNNs: Fast Autoregressive Transformers with Linear Attention". Katharopoulos et al, '20
- •**RWKV**. "RWKV: Reinventing RNNs for the Transformer Era", Peng et al '23

We'll see more as we go!

Back To Transformers: Model Architecture

- Initial goal for an architecture: encoder-decoder
 - Get rid of recurrence
 - Replace with **self-attention**

- •Architecture
 - The famous picture you've seen
 - Centered on self-attention blocks



Vaswani et al. '17

Interlude: Encoder-Decoder Models

Translation tasks: natural encoder-decoder architectureIntuition:

oms. Oh, do let us go in a caravan."

Mrs. Russell shook her head. "I know it sounds lovely, darling; but we to get a caravan? It would cost at least fifty pounds to buy one, en if we had one, Daddy couldn't get away this summer. No, we take up our minds to do without a holiday this year; but I'll tell you wha I do: we'll all go to Southend for the day, as we did last year, and r lunch and tea with us and have a splendid picnic."

Multilitie, where wouldn't be any lanway late and we should a

"Then we can bathe again," said Bob; " but, oh! I do wish I could ha ny and ride," he added unexpectedly. "You don't know how I long ny," he continued, sighing deeply as he remembered the blissful holi ten a friend let him share his little Dartmoor pony and ride occasional "Southend is nothing but houses and people," cried Phyllis; " it's no b an this place; and oh! Mummie, I do so *long* for fields and flowers imals," she added pitcously; and she shook her long brown hair forv hide the tears in her eyes.

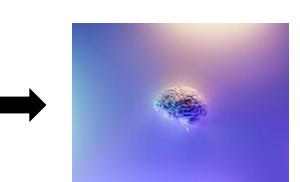
"Never mind, darling, you shall have them one day," answered issell with easy vagueness.

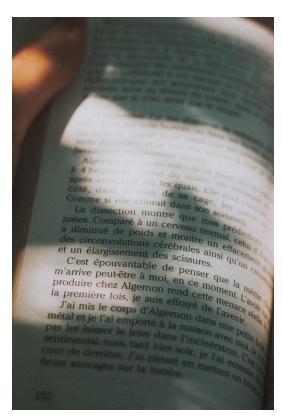
This really was not very comforting, and it was the most fortunate thing st at that moment a car stopped at the door.

"Uncle Edward!" shouted Bob, rushing from the room. Phyllis bru e tears so hastily from her eyes that she arrived at the front door almo on as he did, and both flung themselves on the tall, kindly-looking man st g beside the car.

"Uncle Edward! Uncle Edward!" they cried. "You've come at e've been longing to see you. Oh, how glad we are you're here!" Now the delightful thing was that their uncle seemed just as pleased to em as they were to see him, and returned their hugs and greetings with most cordiality. They were just on the point of dragging him into use, hanging one on each arm, when he said: "Stop, not so fast. There me things to fetch in from the car."

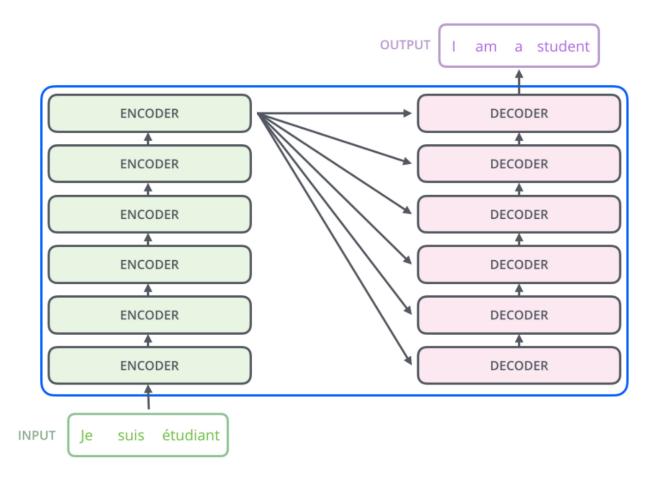
So saying he began diving into the back of it and bringing out, not or itcase, but various parcels, which he handed out one by one. "That's the pair of chickens I've prought for your mother" said he has





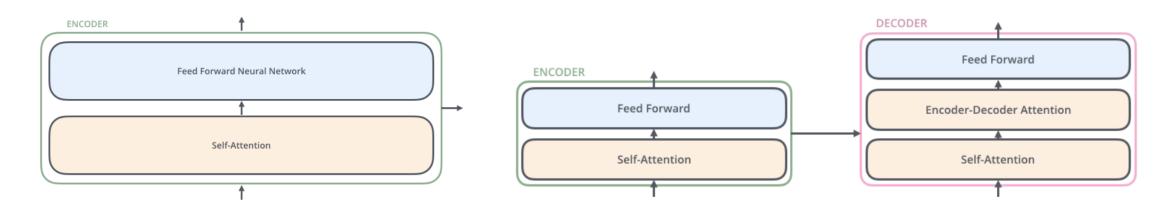
Transformers: Architecture

- •Sequence-sequence model with stacked encoders/decoders:
 - For example, for French-English translation:



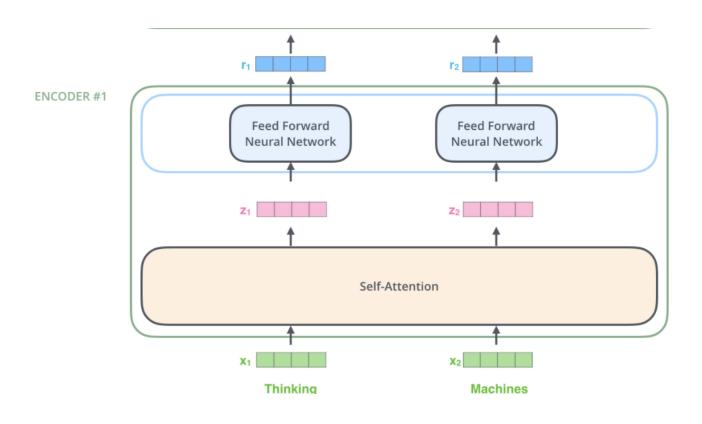
Transformers: Architecture

- •Sequence-sequence model with **stacked** encoders/decoders:
 - What's inside each encoder/decoder unit?
 - Focus on encoder first: **pretty simple**! 2 components:
 - Self-attention block
 - Fully-connected layers (i.e., an MLP)
 - Captures 1) interactions 2) processing (separately!)



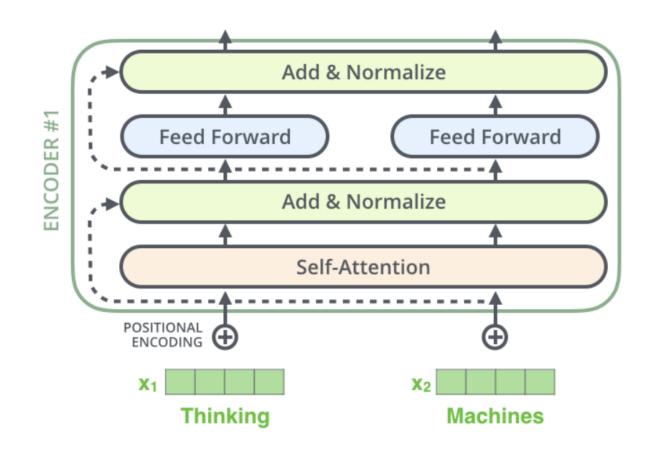
Transformers: Inside an Encoder

- •Let's take a look at the encoder. Two components:
 - 1. Self-attention layer (covered this)
 - •2. "Independent" feedforward nets for each head



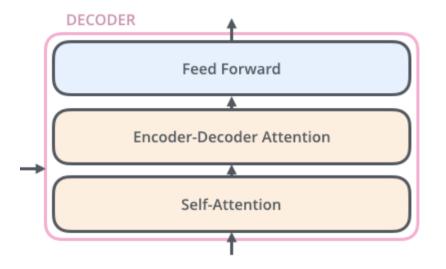
Transformers: More Tricks

- Recall a big innovation for ResNets: residual connections
 - And also layer normalizations
 - Apply to our encoder layers



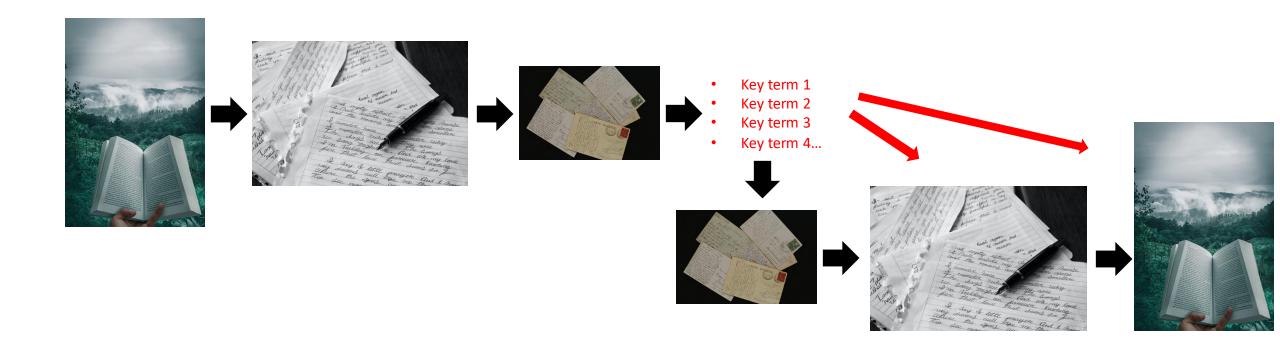
Transformers: Inside a Decoder

- •Let's take a look at the decoder. Three components:
 - 1. Self-attention layer (covered this)
 - 2. Encoder-decoder attention (same, but K, V come from encoder)
 - •3. "Independent" feedforward nets for each head



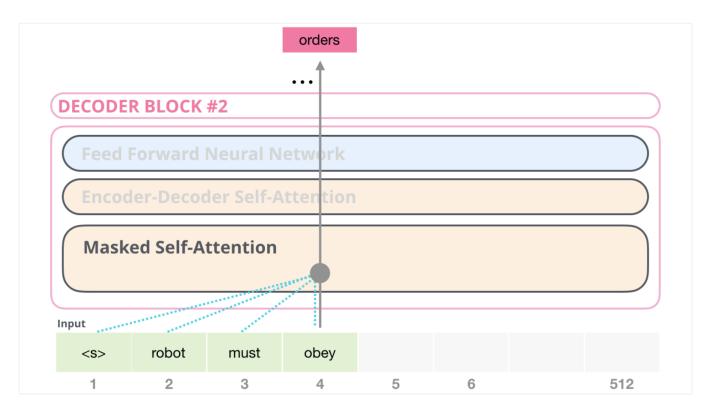
Transformers: Cross-Attention

- Why encoder-decoder attention ?
 - Recall: same as before, but K, V come from encoder
 - Actually more traditional, but... intuition:



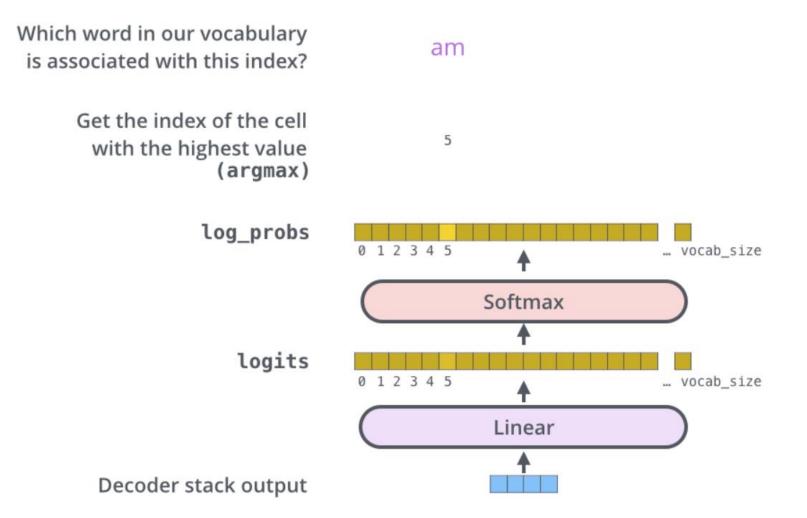
Transformers: Decoder Masking

- •One more interesting bit!
 - At the decoder level, self-attention changes a bit:
 - Masked instead: block *future* words from being attended to



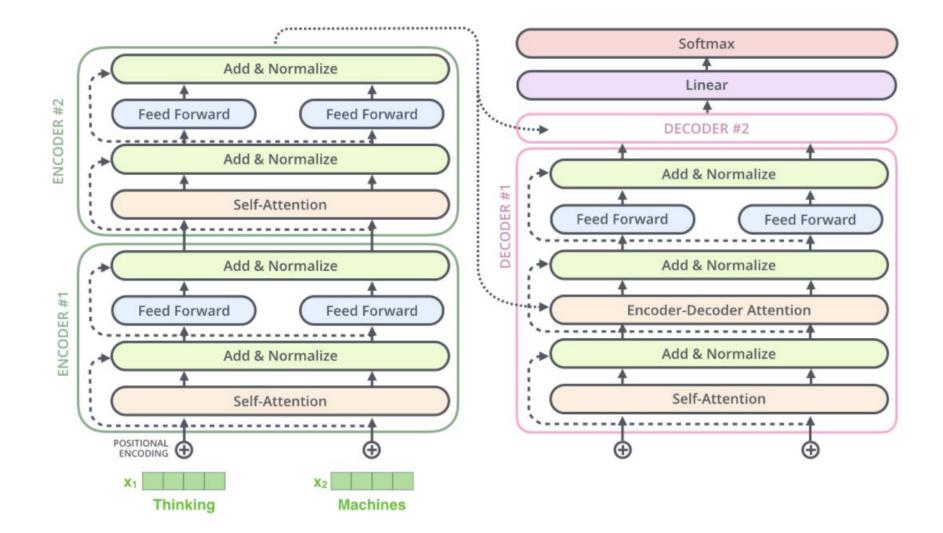
Transformers: Outputs

• Finally, let's see the final layer and outputs



Transformers: Putting it All Together

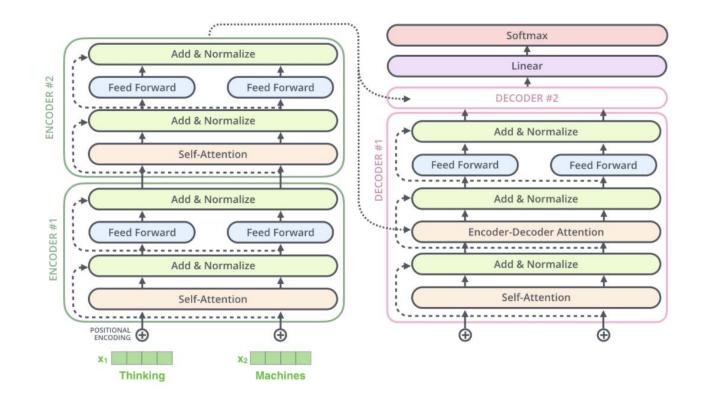
•What does the full architecture look like?

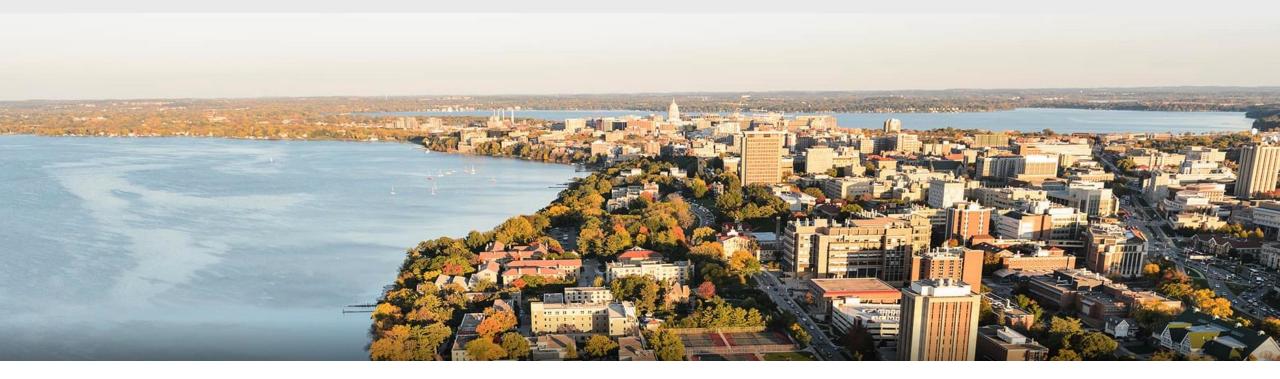


Transformers: Training

• Data: standard datasets (WMT English-German)

- •~5 million pairs for this dataset
- Nothing very special: Adam optimizer





Break & Questions

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From Last Time Finish up SSMs, a little bit more on decoders

Encoder-only Models

•Example: BERT, architecture, multitask training, fine-tuning

Decoder-only Models

• Example: GPT, architecture, basic functionality

Why Encoder-Decoder?

Wanted two things for translation:

- 1) **Outputs** in natural language
- 2) Tight alignment with **input**

What happens if we relax these?1. Encoder-only models2. Decoder-only models

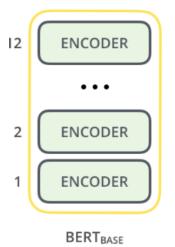


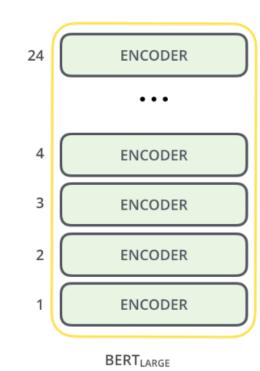
Encoder-Only Models: BERT

Let's get rid of the first part

• 1) **Outputs** in natural language

- 2) Tight alignment with **input**
- Rip away decoders
 - Just stack encoders







Interlude: Contextual Embeddings

- **Q**: Why is it called "BERT"?
 - A: In a sense, follows up ELMo

•Story:

- 2013: "Dense" word embeddings (Word2Vec, Glove)
- Downside: fixed representations per word
 - "Bank": building or riverside?
- Need: contextual representations
 - Using language model-like techniques
 - 2018: ELMo, BERT
 - ELMo: uses LSTMs, BERT uses transformers



Highlights

1. Nearest neighbors

The Euclidean distance (or cosine similarity) between two word vectors provides an effective method for measuring the linguistic or semantic similarity of the corresponding words. Sometimes, the nearest neighbors according to this metric reveal rare but relevant words that lie outside an average human's vocabulary. For example, here are the closest words to the target word *frog*:



https://nlp.stanford.edu/projects/glove/

Interlude: Contextual Embeddings

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BERT acronym:

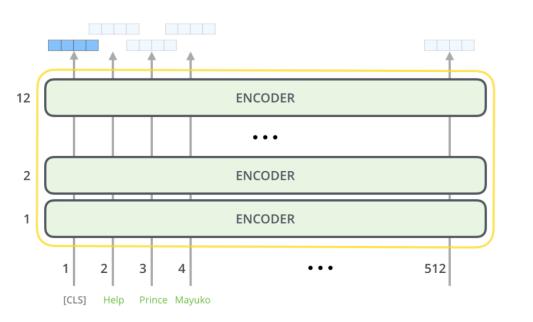
- Bidirectional Encoder Representations from Transformers.
- ERT should make sense,
- Bidirectional: no causal masks, look at both sides of a word!
- Captured in self-attention block

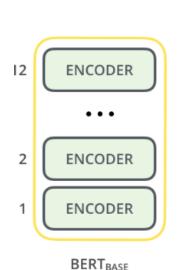


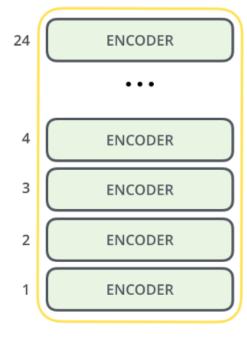
BERT: Forward Pass

BERT architecture

- Rip away decoders
 - Just stack encoders





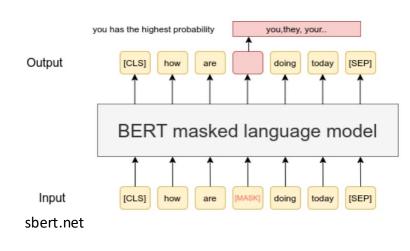


BERTLARGE

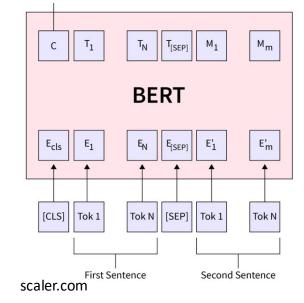
BERT: Training

Training is more interesting!

- Pretraining. Then fine-tuning on task of interest
- Back to self-supervised learning!
- •Two tasks for **pretraining**.



1. Masked Language Modeling



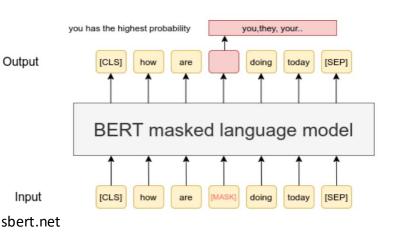
2. Next Sentence Prediction

BERT: Training Task 1

Masked Language Modeling Task

• Use [MASK] token for word to be predicted

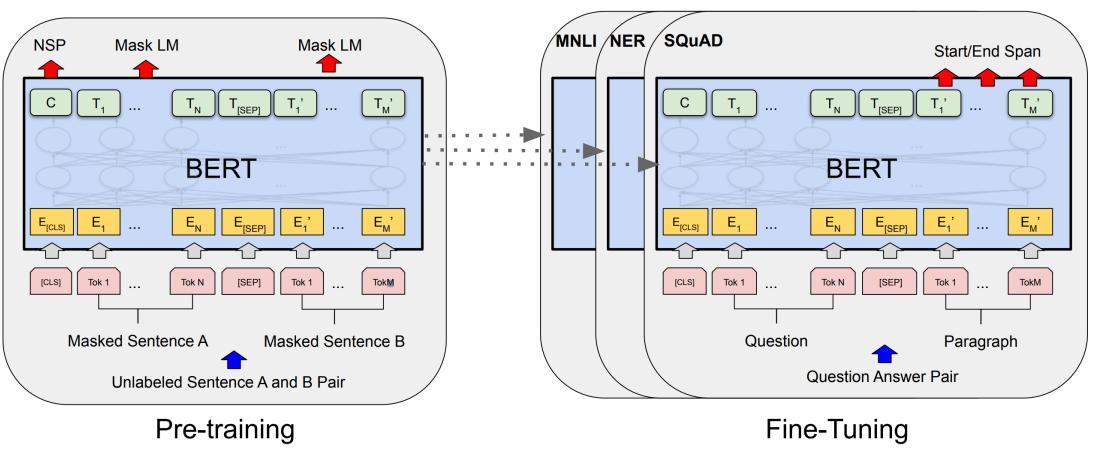
- •Which words to mask?
 - Original paper: 15% of words at random
 - But... of these
 - 10% of the time, no [MASK], flip word randomly
 - 10% of the time leave word unchanged



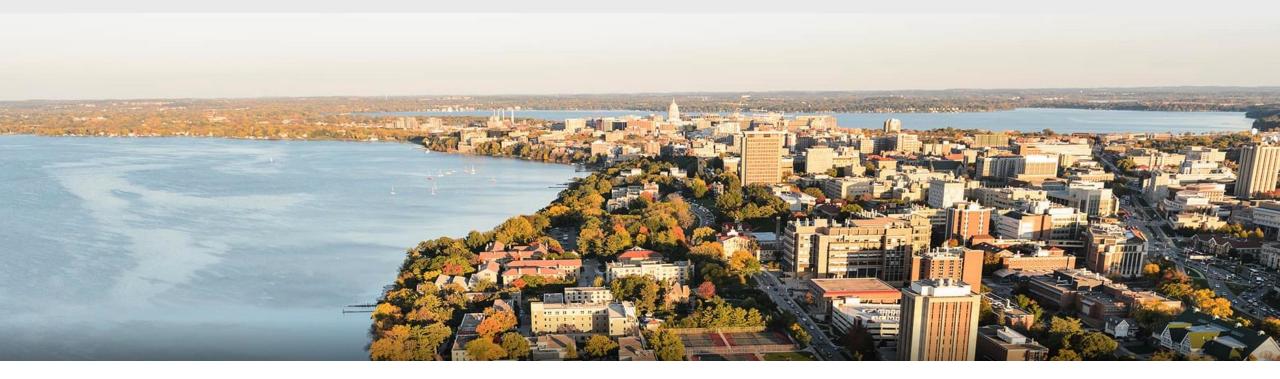
BERT: Training

Training is more interesting,

• Pretraining. Then fine-tuning on task of interest



Devlin et al



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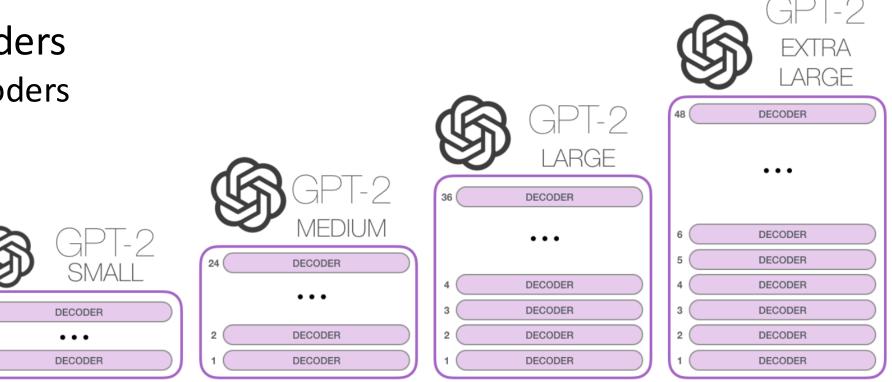
Decoder-only Models

•Example: GPT, architecture, basic functionality

Decoder-Only Models: GPT

Let's get rid of the first part 1) Outputs in natural language 2) Tight alignment with input

- Rip away encoders
 - Just stack decoders



Model Dimensionality: 768

Model Dimensionality: 1024

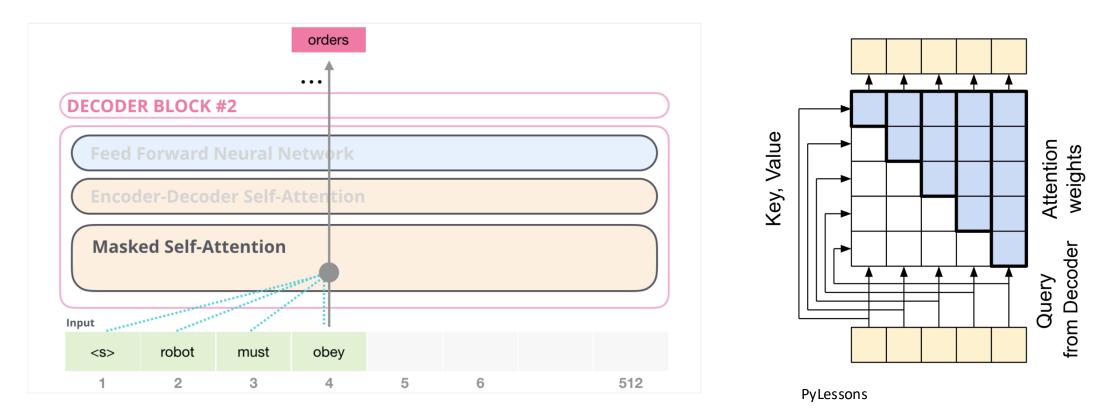
Model Dimensionality: 1280

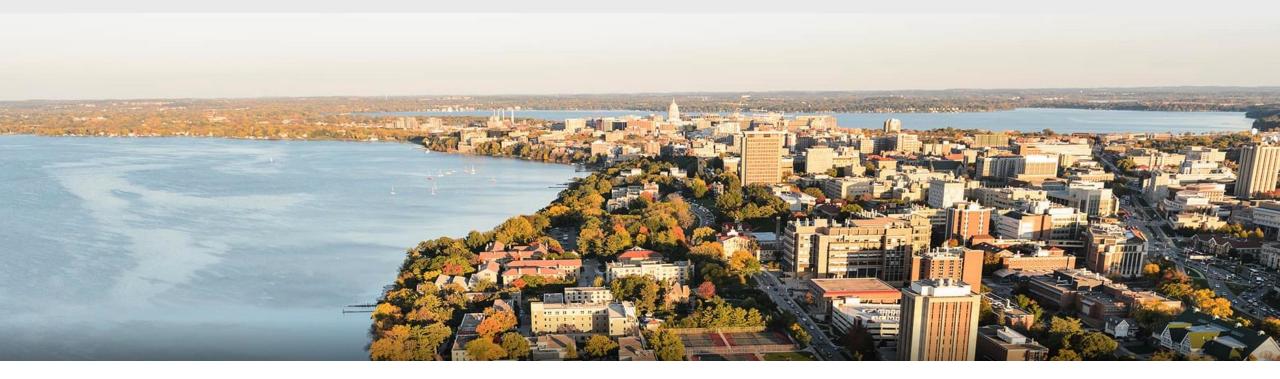
Model Dimensionality: 1600

Decoder-Only Models: GPT

Rip away encoders

- Just stack decoders
- Use causal masking! NB: not a *mask token* like in BERT





Thank You!