

CS 536 Announcements for Thursday, February 13, 2025

Programming Assignment 2 – due Tuesday, February 18

Homework 2 – is available

Last Time

- why regular expressions aren't enough
- CFGs
 - formal definition
 - examples
 - language defined by a CFG
- parse trees
- Makefiles
- ambiguous grammars
- grammars for expressions
 - precedence
 - associativity
- grammars for lists

Today

- syntax-directed translation
- abstract syntax trees
- implementing ASTs

end of Midterm 1 material

CFG review

```
prog → BEGIN stmts END
stmts → stmts SEMICOLON stmt
      | stmt
stmt → ID ASSIGN expr
expr → expr PLUS term
     | term
term → term TIMES factor
     | factor
factor → expon POW factor
      | expon
expon → INTLIT
      | LPAREN expr RPAREN
```

precedence
low
↓
high

Overview of CFGs



CFGs for language definition

- the CFGs we've discussed can generate/define languages of valid strings

start by building parse tree
& end with some valid string $w \in L(G)$

CFGs for language recognition

start with string w
& end with yes/no answer depending on whether $w \in L(G)$

CFGs for parsing

start with string w
& end with parse tree for w if $w \in L(G)$
↳ generally use AST instead of parse tree
- need to translate sequence of tokens (w)

Syntax-directed translation (SDT)

= translating from a sequence of tokens into a sequence of actions/other form based on underlying syntax

could be: AST, value, type, etc.

To define a syntax-directed translation

Augment CFG with **translation rules** (at most 1 rule per production)

↳ LHS → RHS

- define translation of LHS non-terminal as a function of
 - constants
 - translations of RHS non-terminals
 - values of token (terminals) on RHS

To translate a sequence of tokens using SDT *

- build parse tree
- use translation rules to compute translation of each non-terminal in parse tree
bottom-up ← handle child ren of node before node
- translation of sequence of tokens is the translation of the parse tree's root non-terminal (ie, start symbol)

The **type** of the translation can be anything: numeric, string, set, tree, ...

* Note: above is how to understand the translation, not how a compiler actually does it

Example: grammar for language of binary numbers

CFG

$b \rightarrow 0$

$b \rightarrow 1$

$b \rightarrow b0$

$b \rightarrow b1$

translation rules

$b.trans = 0$

$b.trans = 1$

$b_1.trans = b_2.trans * 2$

$b_1.trans = b_2.trans * 2 + 1$

SDT to compute the decimal equivalent of a binary number

Example: input string 10110

Parse tree:

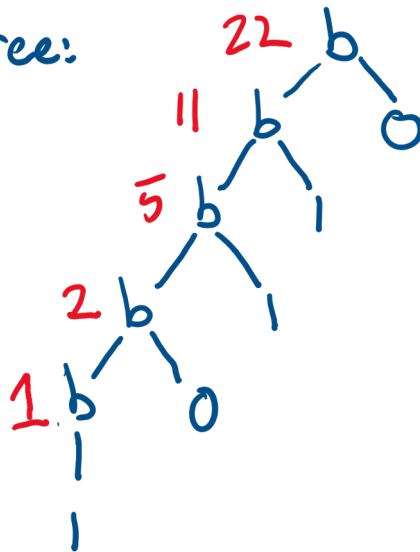
steps

④

③

②

①



Translation is 22

Example: grammar for language of variable declarations

CFG

$\text{declList} \rightarrow \epsilon$
 $\text{declList} \rightarrow \text{decl declList}_2$
 $\text{decl} \rightarrow \text{type ID ;}$
 $\text{type} \rightarrow \text{INT}$
 $\text{type} \rightarrow \text{BOOL}$

Translation rules

$\text{declList.trans} = ""$
 $\text{declList}_1.\text{trans} = \text{decl.trans} + "" + \text{declList}_2.\text{trans}$
 $\text{decl.trans} = \text{ID.value}$

string concatenation

Write a syntax-directed translation for the CFG given above so that the translation of a sequence of tokens is a string containing the ID's that have been declared.

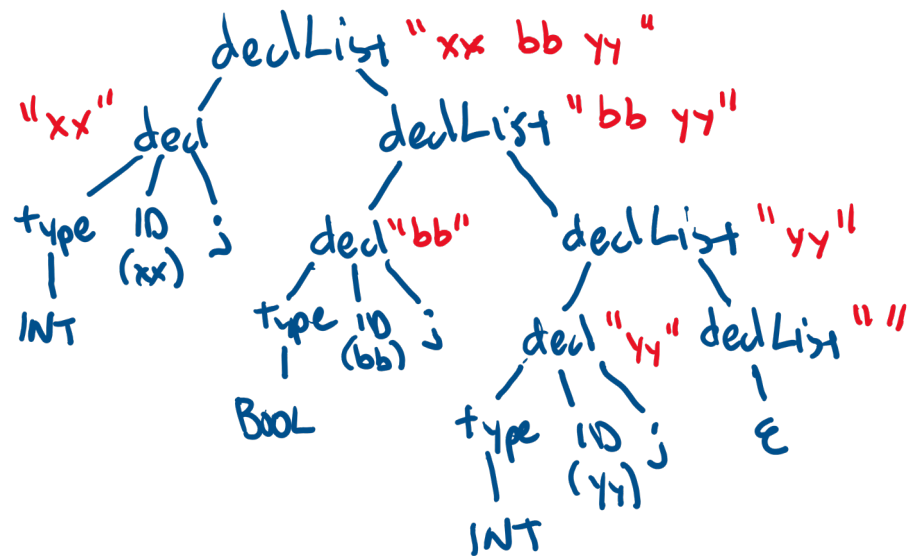
Example input

int xx ;
 bool bb ;
 int yy ;

Output

$"bb xx yy"$
 (in any order)

Parse tree



Translation is
 $"xx bb yy"$

Example: grammar for language of variable declarations

CFG

declList $\rightarrow \epsilon$
 | decl declList

decl \rightarrow type ID ;

type \rightarrow INT
 | BOOL

Translation rules

declList.trans = ""
 declList₁.trans = decl.trans + " " + declList₂.trans

decl.trans = type.trans ? ID.value : "" *

type.trans = true
 type.trans = false

Modify the previous syntax-directed translation so that only declarations of type `int` are added to the output string.

Example input

int xx;
 bool bb;
 int yy;

Output

"xx yy"
 (in any order)

- Note:
- 1) different non-terms can have different types as their translation
 - 2) translation rules can be conditional

* $x = a ? b : c;$ equiv to if (a)
 x = b;
 else
 x = c;

SDT for parsing

Previous examples showed SDT process assigning different types to the translation

- translate tokenized stream to an integer value
- translate tokenized stream to a string

For parsing, we'll need to translate a **tokenized stream** to an **abstract-syntax tree (AST)**

Abstract syntax trees

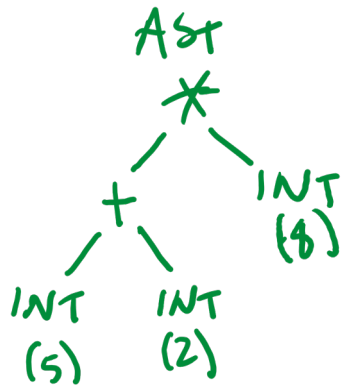
AST = condensed form of parse tree

- operators are internal nodes (not leaves)
- chains of productions are collapsed
- lists are flattened
- syntactic details are omitted
↳ eg ; parens

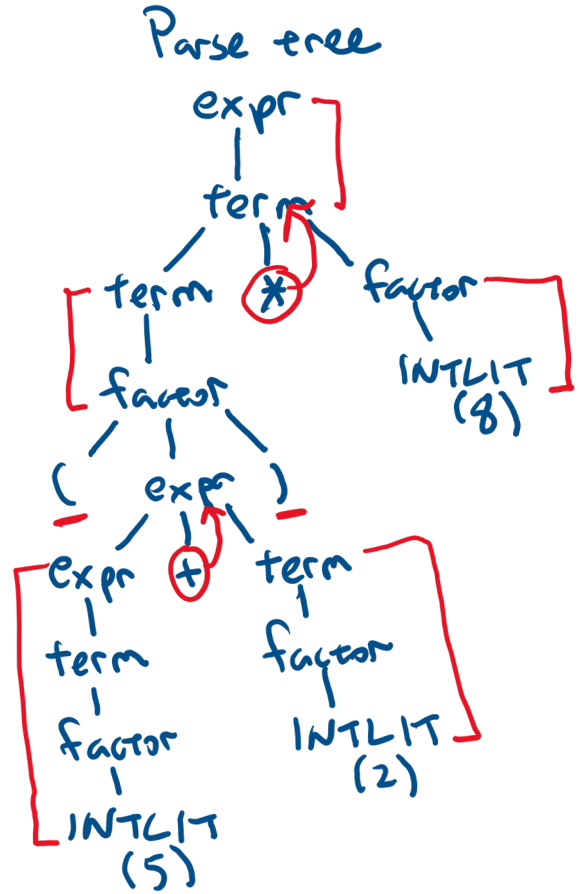
AST Example

CFG

- expr → expr PLUS term
| term
- term → term TIMES factor
| factor
- factor → INTLIT
| LPAREN expr RPAREN



(5+2)*8



Resume
at 7:30

SDT review

SDT = translating from a sequence of tokens into a sequence of actions/other form, based on underlying syntax

To define a syntax-directed translation

- augment CFG with **translation rules** $lhs \rightarrow rhs$
 - define translation of LHS non-terminal as a function of:
 - constants $2, " "$
 - translations of RHS non-terminals $rhs.trans$
 - values of terminals (tokens) on RHS $TOKEN.value$

contains terms,
non-terms, ϵ

To translate a sequence of tokens using SDT (conceptually)

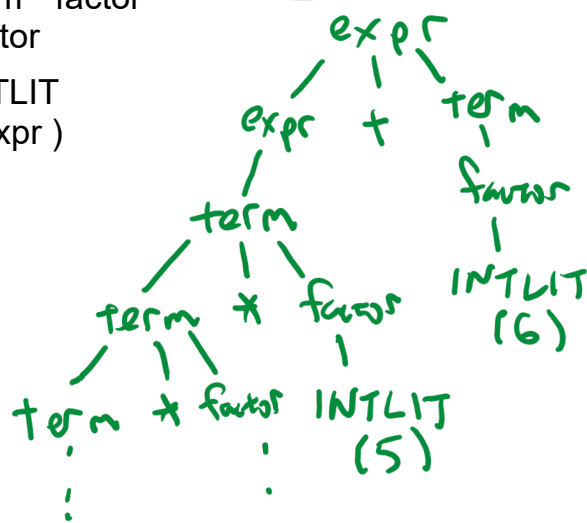
- build parse tree
- use translation rules to compute translation of each non-terminal (bottom-up)
- translation of sequence of tokens = translation of parse tree's root non-terminal

For parsing, we'll need to translate tokenized stream to **abstract-syntax tree (AST)**

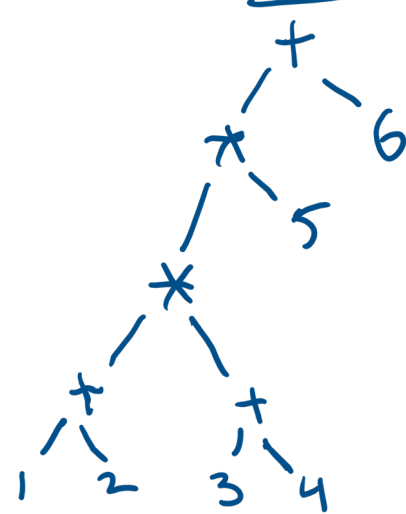
Example $(1+2) * (3+4) * 5 + 6$

expr \rightarrow expr + term
 | term
 term \rightarrow term * factor
 | factor
 factor \rightarrow INTLIT
 | (expr)

Parse tree



AST



translation rule:

$expr.trans = \text{MkPlusNode}(expr_2.trans, term.trans)$

AST for parsing

We've been showing the translation in two steps:

token stream \rightarrow parse tree \rightarrow AST then throw away parse tree

In practice we'll do

token stream \rightarrow AST

Why have an AST?

- captures essential structure
- easier to work with

$expr \rightarrow expr + term$

AST implementation

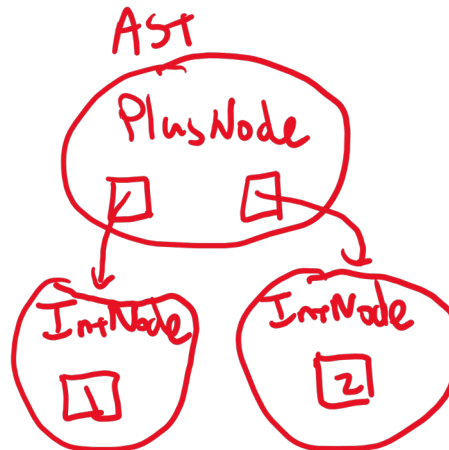
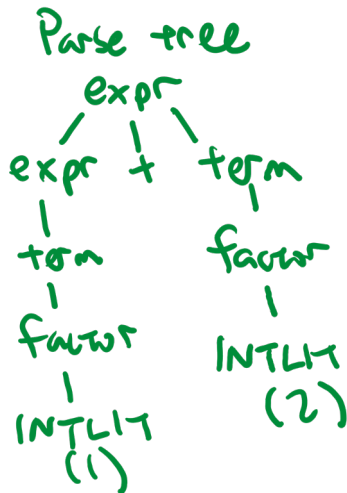
$expr, trans = MkPlusNode(expr_2.trans, term.trans)$

Define a class for each kind of AST node

Create a new node object in some rules

- new node object is the value of LHS.trans
- fields of node object come from translations of RHS non-terminals

Given $1+2$



```
class PlusNode {
  InNode left;
  InNode right;
}
class InNode {
  int value;
}
```

Need class hierarchy
& make subclasses of ExpNode

```
class PlusNode extends ExpNode {
```

```
  ExpNode left;
  ExpNode right;
```

→ put into ExpNode

```
}
class InNode extends ExpNode {
  int value;
}
```

Translation rules to build ASTs for expressions

CFG

expr \rightarrow expr + term

| term

term \rightarrow term * factor

| factor

factor \rightarrow INTLIT

| (expr)

Translation rules

expr₁.trans = *new PlusNode(expr₂.trans, term.trans)*

expr.trans = *term.trans*

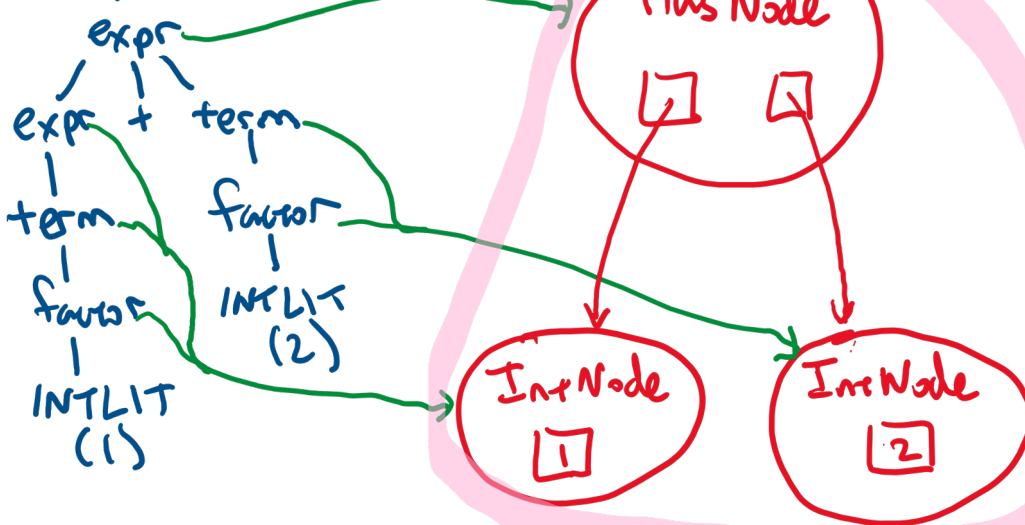
term₁.trans = *new TimesNode(term₂.trans, factor.trans)*

term.trans = *factor.trans*

factor.trans = *new IntNode(INTLIT.value)*

factor.trans = *expr.trans*

Example 1+2



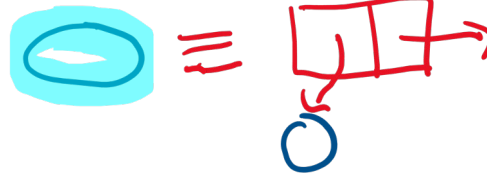
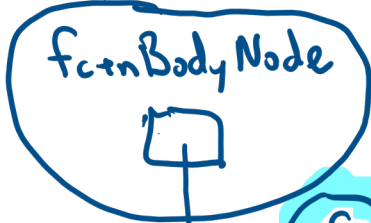
ASTs for non-expressions

Example

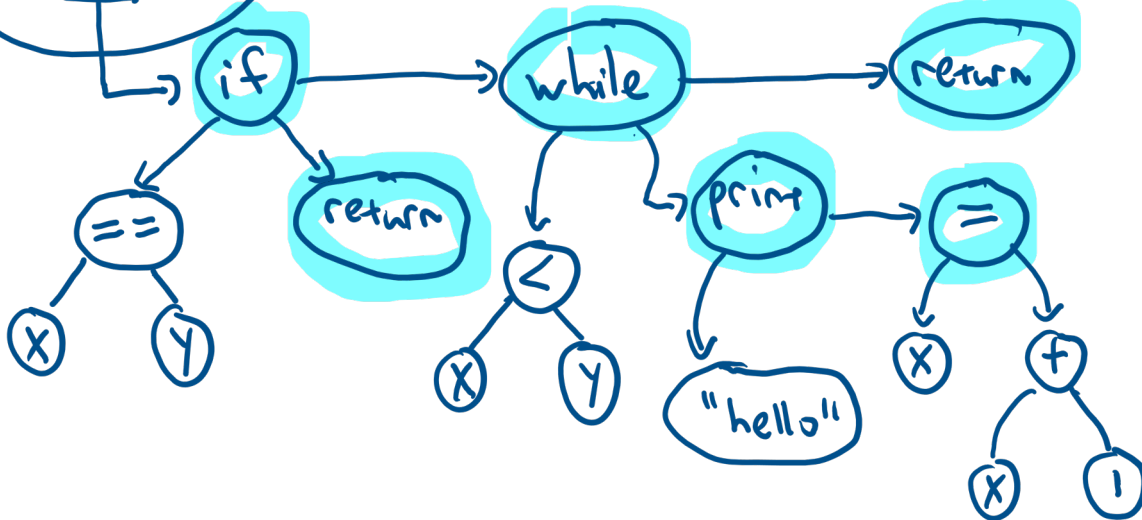
```
void foo(int x, int y) {  
  if (x == y) {  
    return;  
  }  
  while (x < y) {  
    cout << "hello";  
    x = x + 1;  
  }  
  return;  
}
```



AST for function body



ie linked list



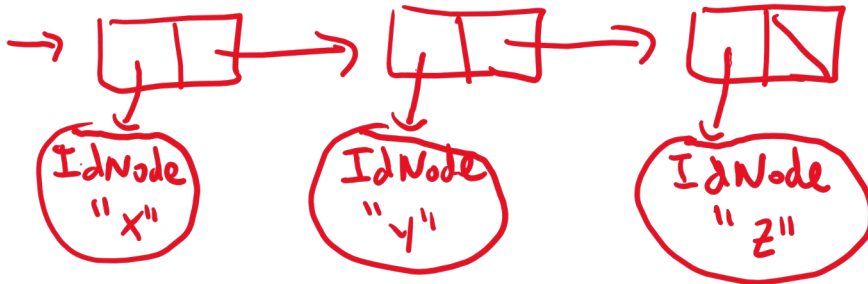
ASTs for lists

CFG

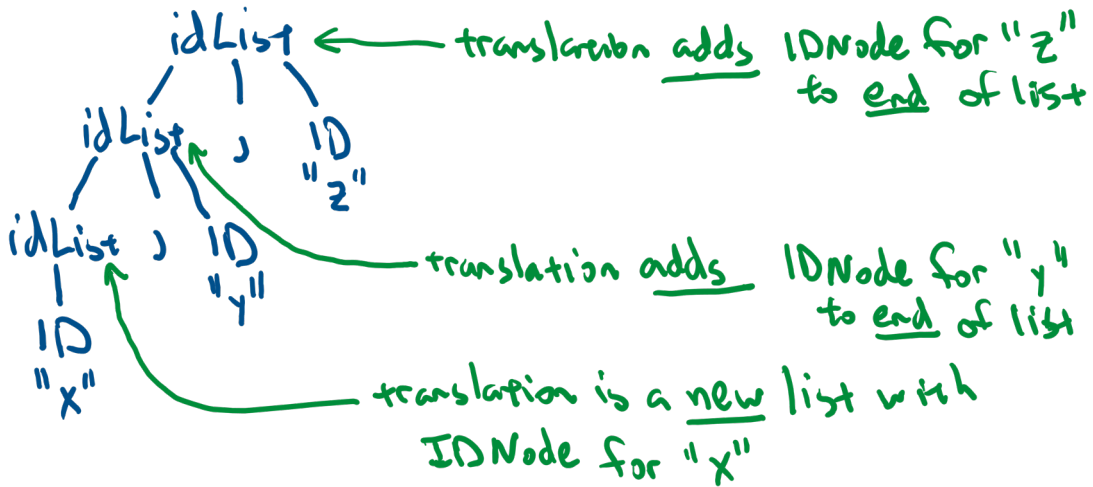
idList → idList COMMA ID
 | ID

Input x, y, z

Want AST to be



Parse tree



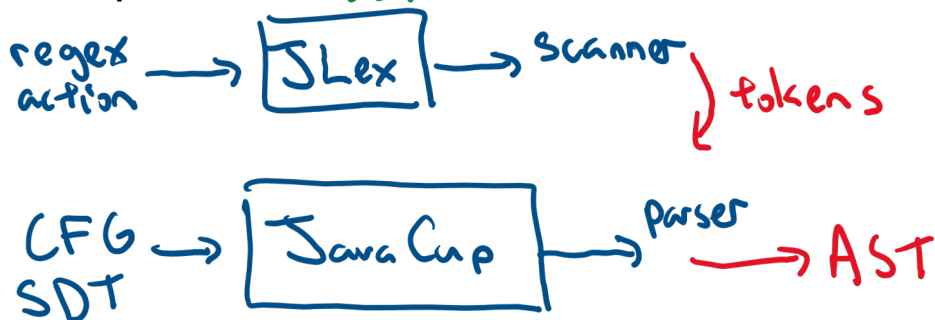
The bigger picture

Scanner

- **Language abstraction:** regular expressions
- **Output:** token stream
- **Tool:** JLex
- **Implementation:** interpret DFA using table (for δ), recording `most_recent_accepted_position` & `most_recent_token`

Parser

- **Language abstraction:** CFG
- **Output:** AST (by way of a syntax-directed translation)
- **Tool:** Java CUP ← next time
- **Implementation:** ??? ← next time



Next Time

- Java CUP
- approaches to parsing
- bottom-up parsing
- CFG transformations
- CYK algorithm