



CS540 Introduction to Artificial Intelligence

Deep Learning I: Convolutional Neural Networks

University of Wisconsin-Madison

Announcements

- **Homeworks:**
 - HW 7 due in two weeks; provide feedback
- **Midterms are being graded**
- **Class roadmap:**

Tuesday, Mar 28	Deep Learning I
Thursday, Mar 30	Deep Learning II
Tuesday, April 4	Neural Network Review
Thursday, April 6	Search

Today's Goals

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- Build an understanding of convolutional neural networks.

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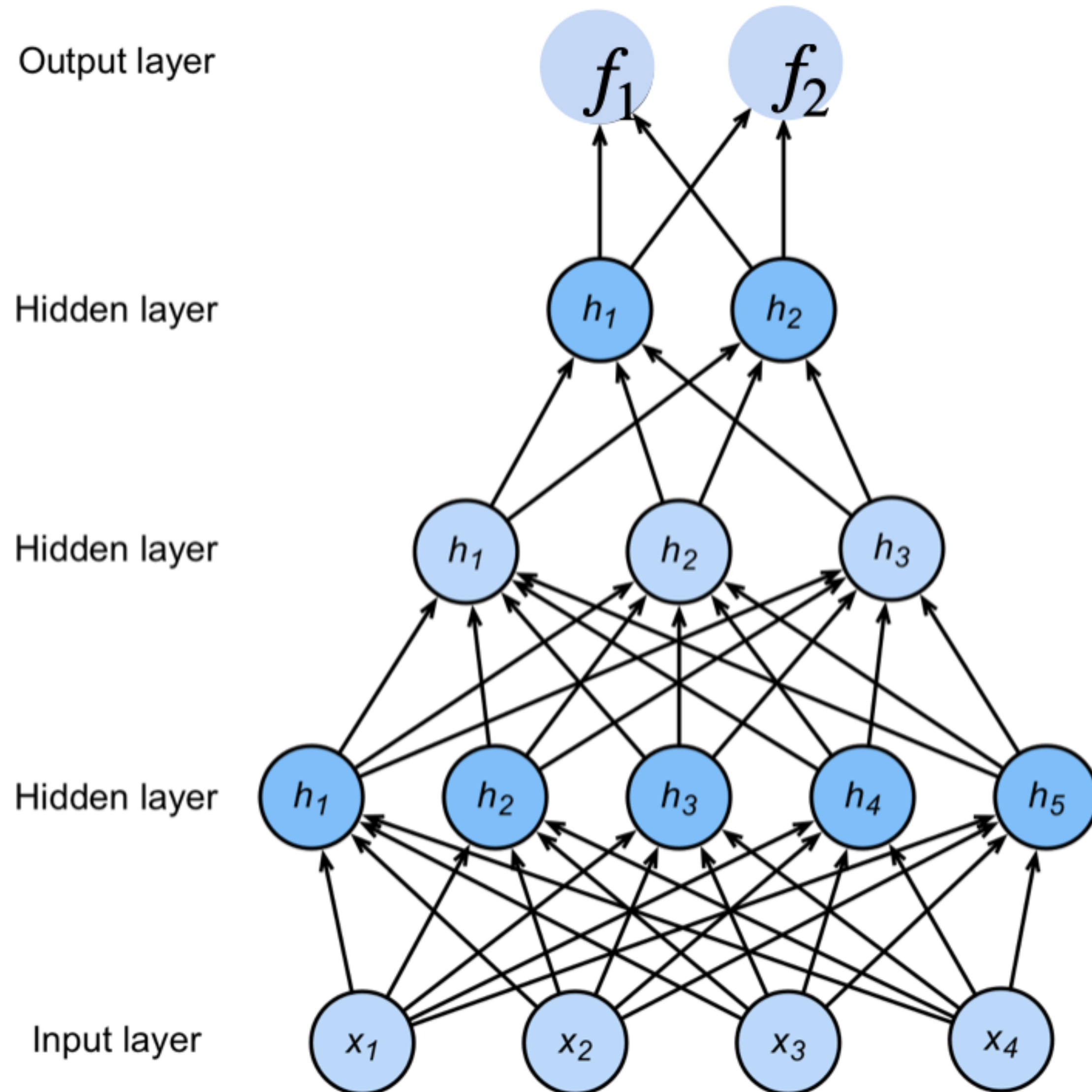
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 - Multiple input and output channels

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 - Padding and stride.
 - Multiple input and output channels
 - Pooling

Review: Deep Neural Networks



$$\mathbf{h}_1 = \sigma(\mathbf{W}^{(1)}\mathbf{x} + \mathbf{b}^{(1)})$$

$$\mathbf{h}_2 = \sigma(\mathbf{W}^{(2)}\mathbf{h}_1 + \mathbf{b}^{(2)})$$

$$\mathbf{h}_3 = \sigma(\mathbf{W}^{(3)}\mathbf{h}_2 + \mathbf{b}^{(3)})$$

$$\mathbf{f} = \mathbf{W}^{(4)}\mathbf{h}_3 + \mathbf{b}^{(4)}$$

$$\mathbf{p} = \text{softmax}(\mathbf{f})$$

**NNs are composition
of nonlinear
functions**

How to classify

Cats vs. dogs?

How to classify

Cats vs. dogs?



How to classify Cats vs. dogs?



Dual
12MP
wide-angle and
telephoto cameras

How to classify Cats vs. dogs?



Dual
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36M floats in a RGB image!

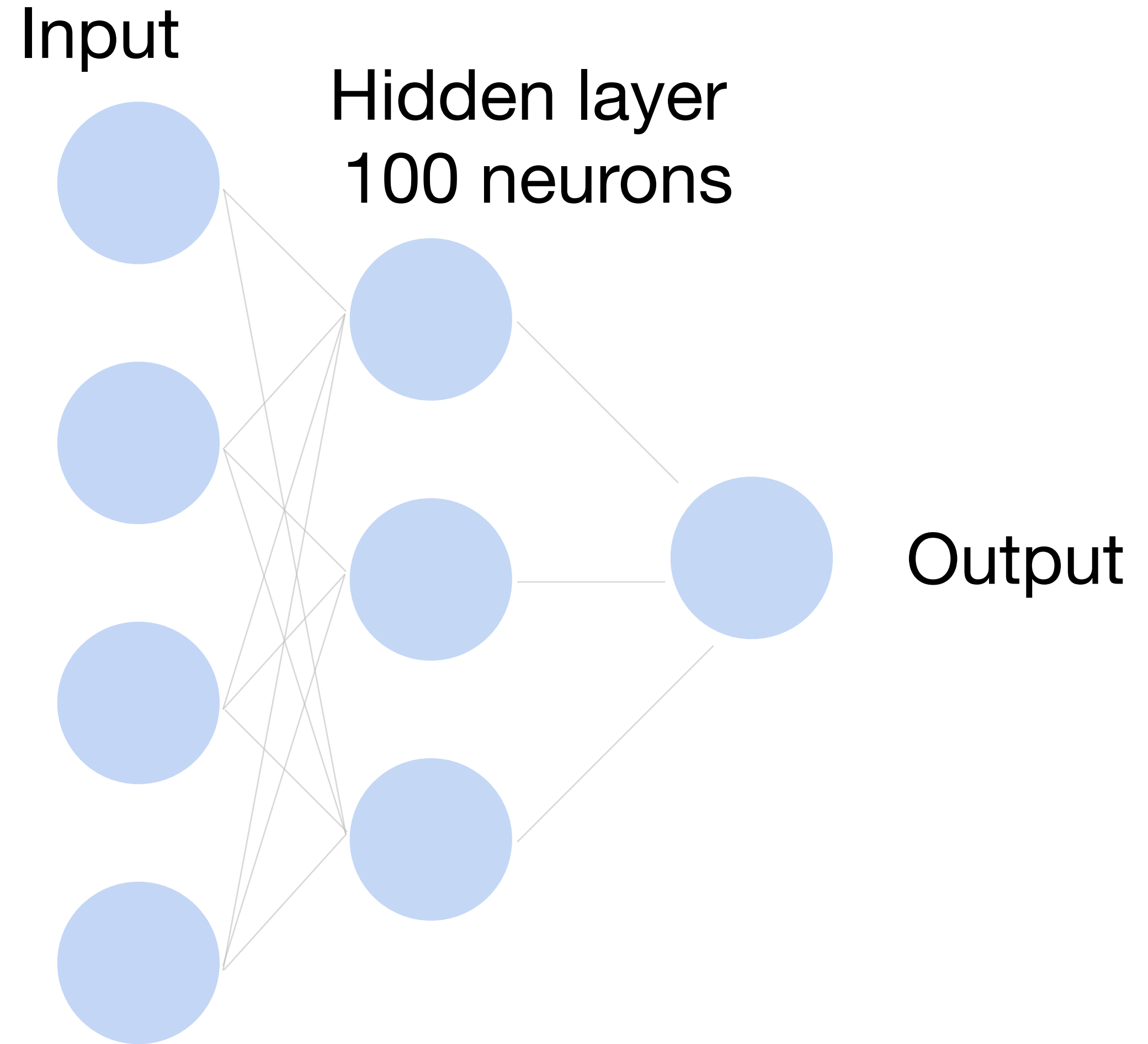
Fully Connected Networks

Cats vs. dogs?



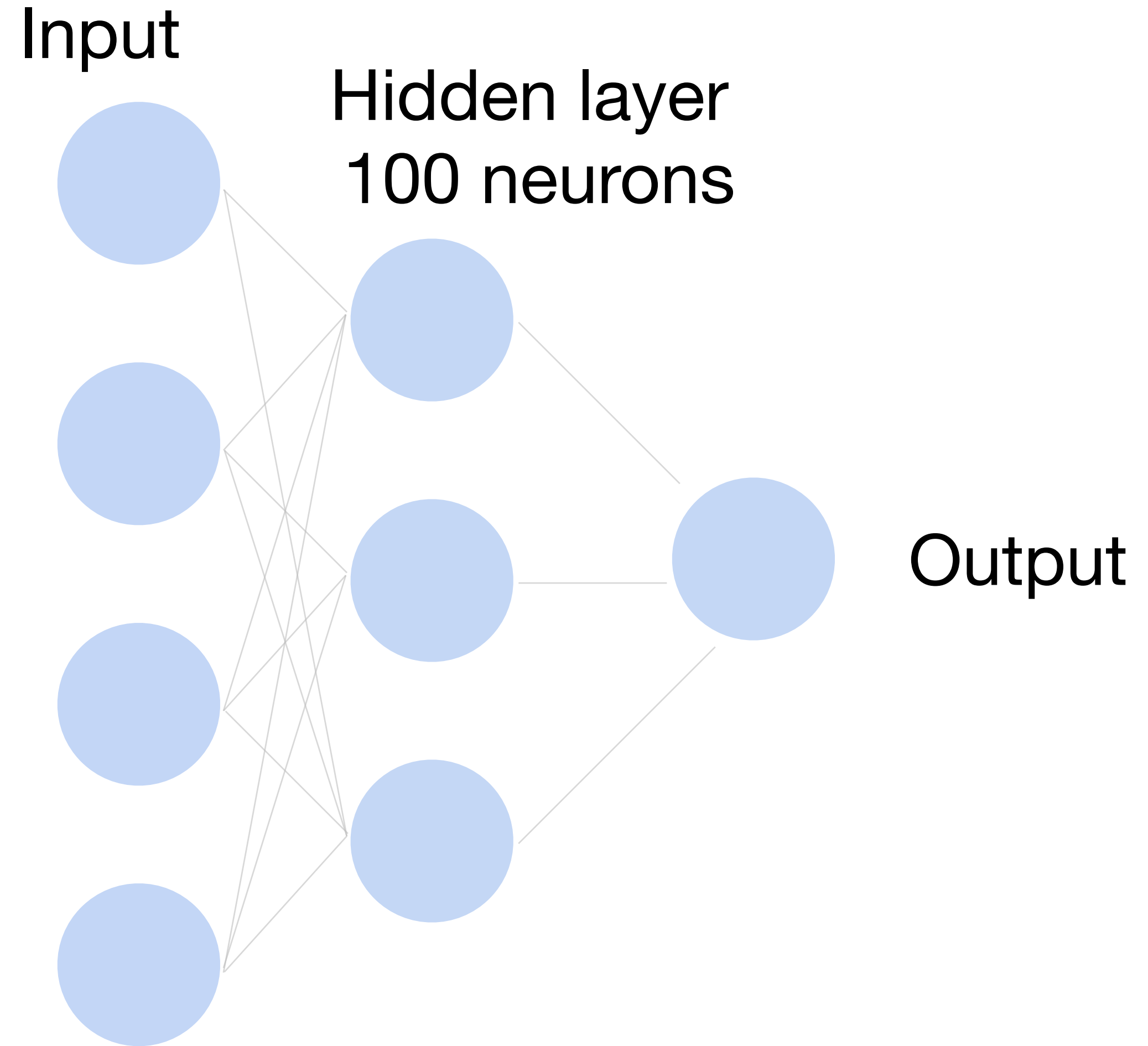
Fully Connected Networks

Cats vs. dogs?



Fully Connected Networks

Cats vs. dogs?



$\sim 36\text{M elements} \times 100 = \sim \mathbf{3.6B}$ parameters!

Convolutions come to rescue!

Where is
Waldo?



Why Convolution?

- Translation Invariance
- Locality



2-D Convolution

Input

0	1	2
3	4	5
6	7	8

Kernel

0	1
2	3

*

=

Output

19	25
37	43

$$0 \times 0 + 1 \times 1 + 3 \times 2 + 4 \times 3 = 19$$

2-D Convolution

Input

0	1	2
3	4	5
6	7	8

Kernel

0	1
2	3

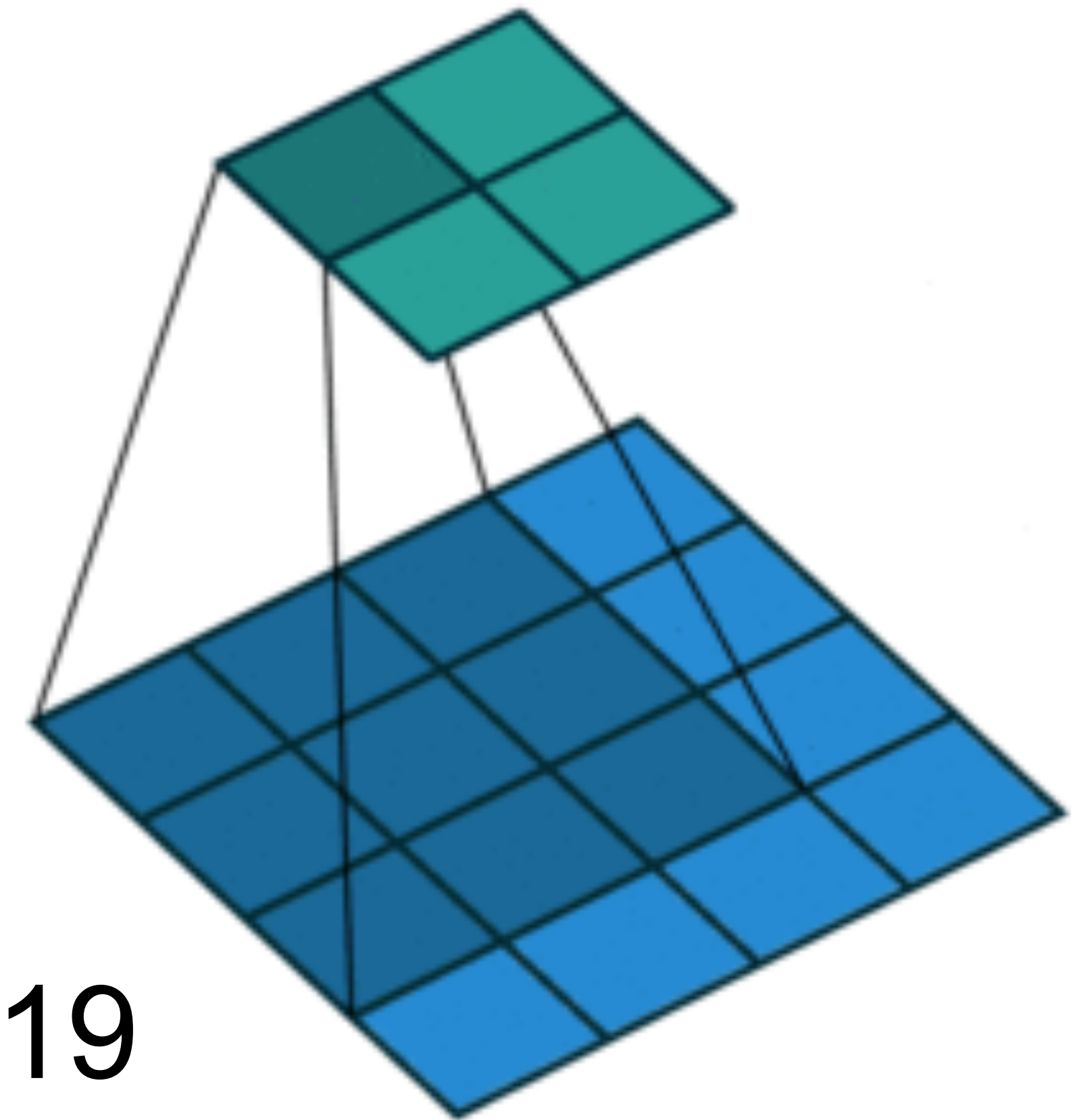
*

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2-D Convolution

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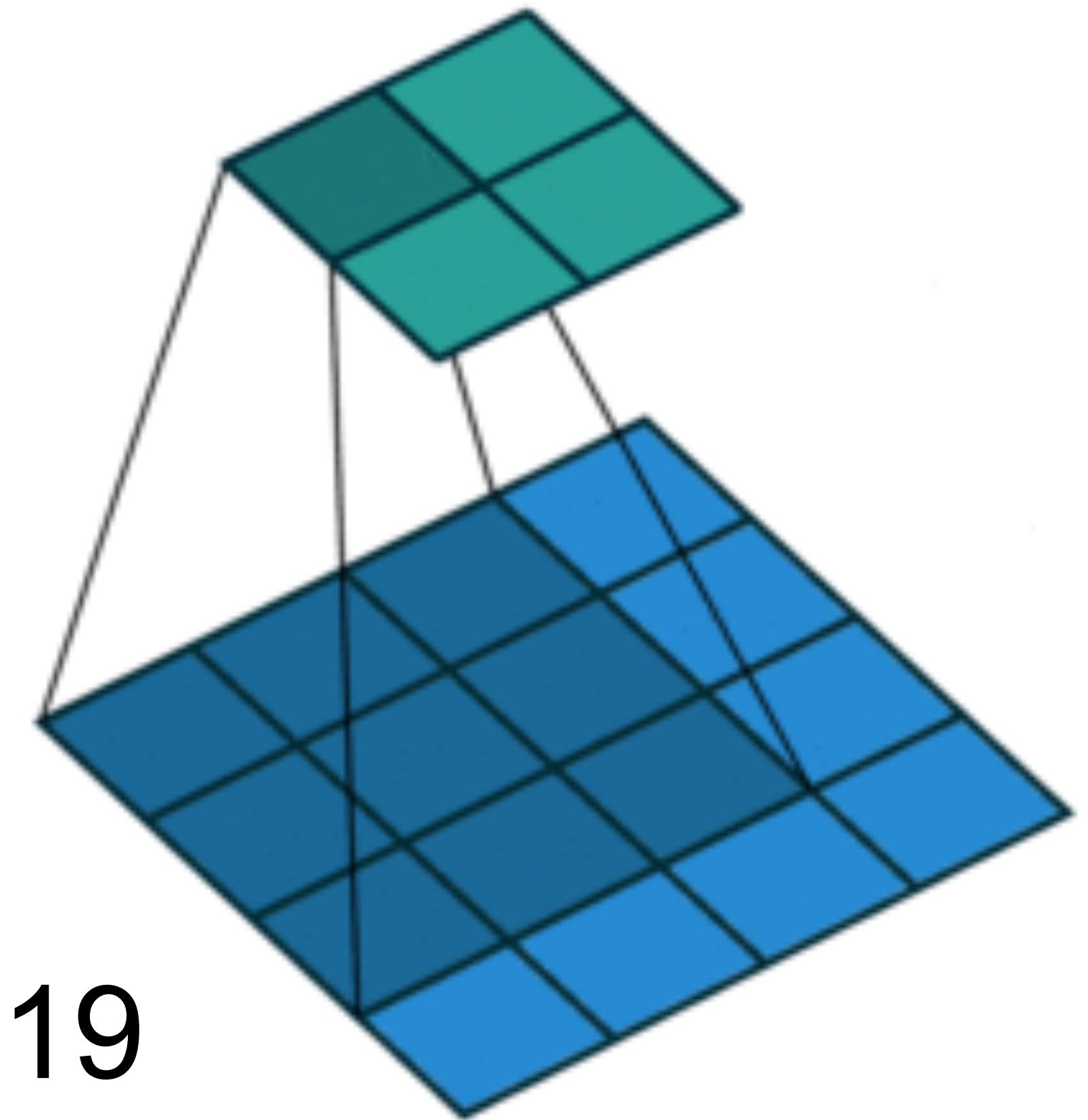
*

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Output

19	25
37	43

$$0 \times 0 + 1 \times 1 + 3 \times 2 + 4 \times 3 = 19$$



(vdumoulin@ Github)

2-D Convolution

Input

0	1	2
3	4	5
6	7	8

Kernel

0	1
2	3

*

=

Output

19	25
37	43

$$1 \times 0 + 2 \times 1 + 4 \times 2 + 5 \times 3 = 25$$

2-D Convolution

Input

0	1	2
3	4	5
6	7	8

*

Kernel

0	1
2	3

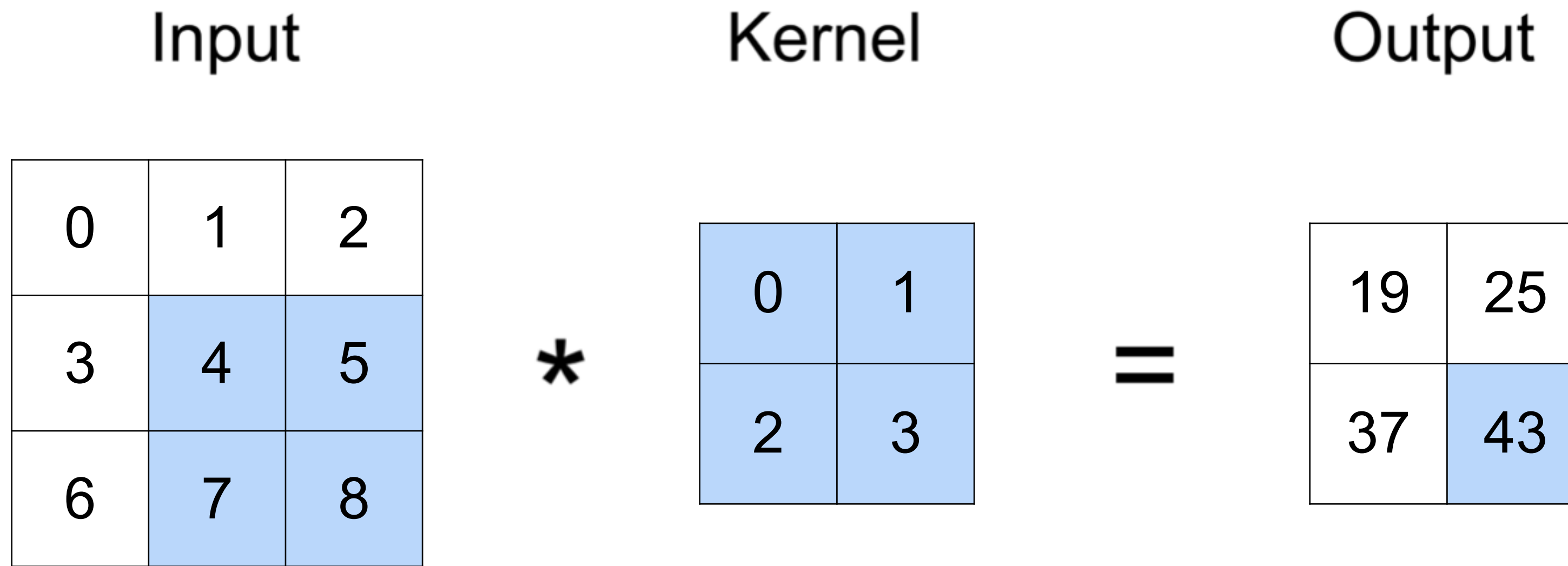
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Output

19	25
37	43

$$3 \times 0 + 4 \times 1 + 6 \times 2 + 7 \times 3 = 37$$

2-D Convolution



$$4 \times 0 + 5 \times 1 + 7 \times 2 + 8 \times 3 = 43$$

2-D Convolution Layer

0	1	2
3	4	5
6	7	8

 *

0	1
2	3

 =

19	25
37	43

- **X** : $n_h \times n_w$ input matrix
- **W** : $k_h \times k_w$ kernel matrix
- **Y** : $(n_h - k_h + 1) \times (n_w - k_w + 1)$ output matrix

$$Y = X * W$$

2-D Convolution Layer

0	1	2
3	4	5
6	7	8

 *

0	1
2	3

 =

19	25
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- **X** : $n_h \times n_w$ input matrix
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$$Y = X * W$$

Convolution operator not multiplication

2-D Convolution Layer

0	1	2
3	4	5
6	7	8

 *

0	1
2	3

 + 1 =

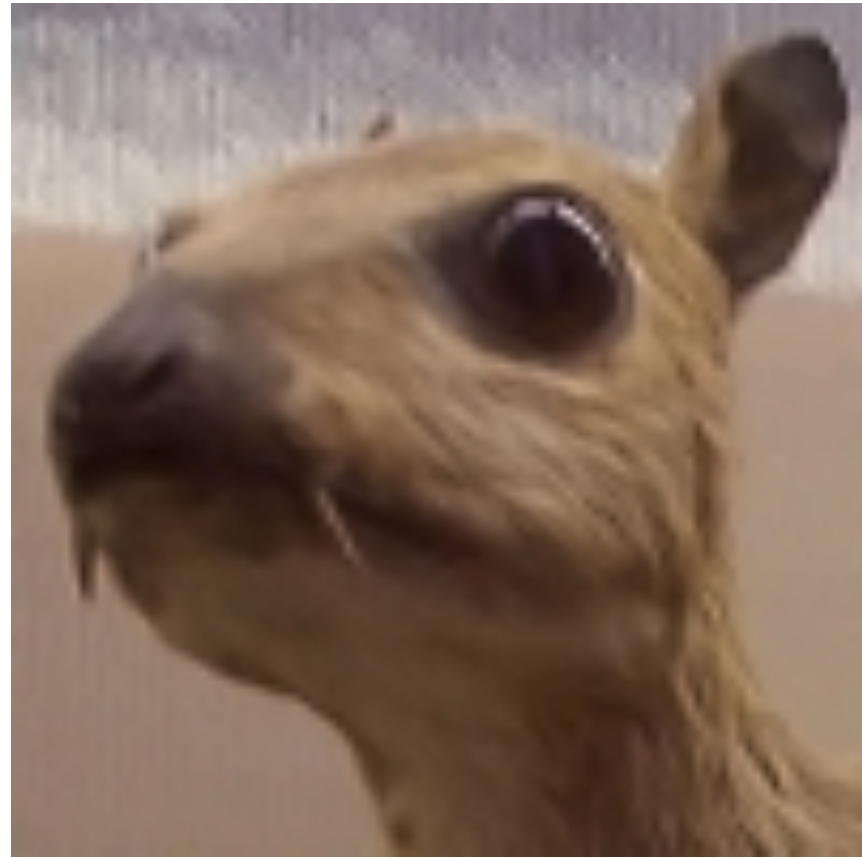
20	26
38	44

- **X** : $n_h \times n_w$ input matrix
- **W** : $k_h \times k_w$ kernel matrix
- **b** : scalar bias
- **Y** : $(n_h - k_h + 1) \times (n_w - k_w + 1)$ output matrix

$$Y = X * W + b$$

- **W** and b are learnable parameters

Examples



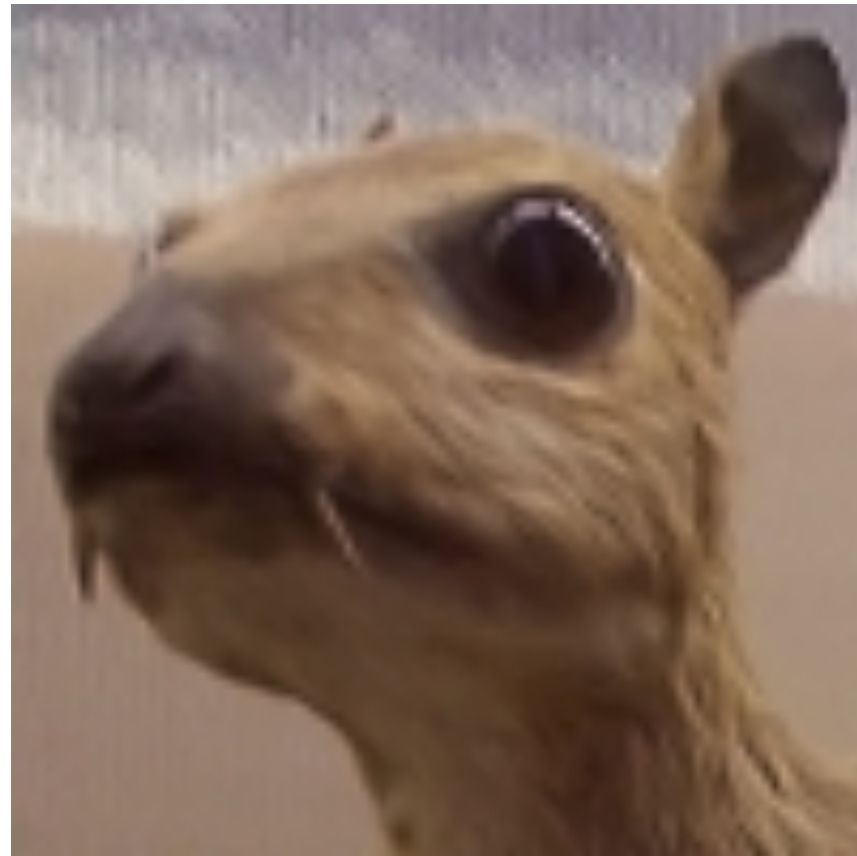
(wikipedia)

Examples

$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$



Edge Detection



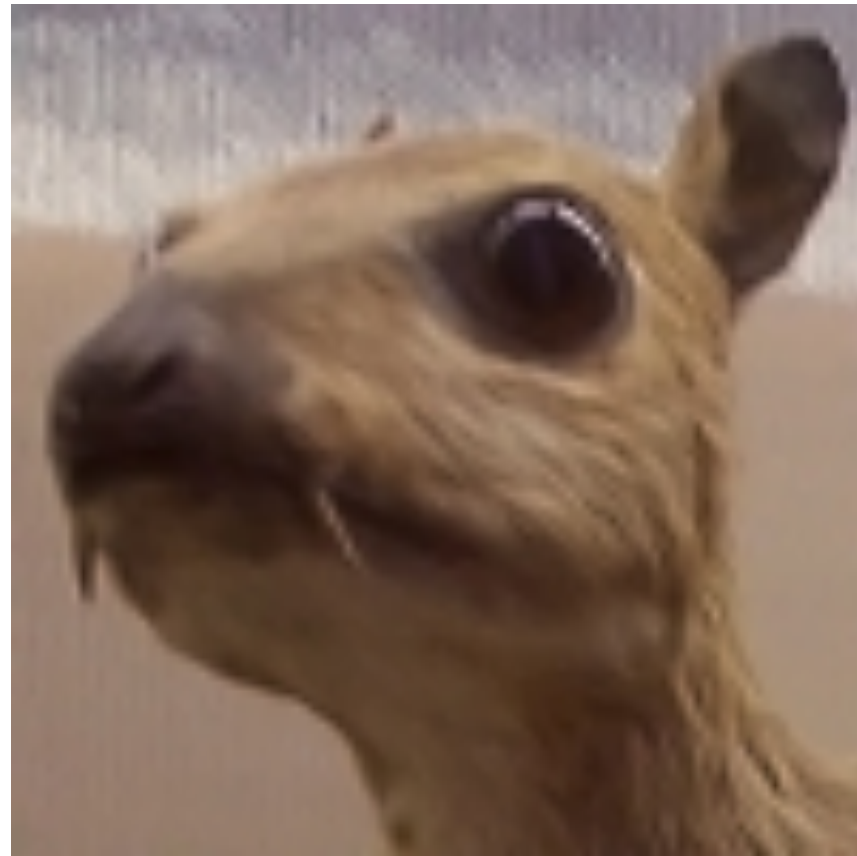
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Examples

$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

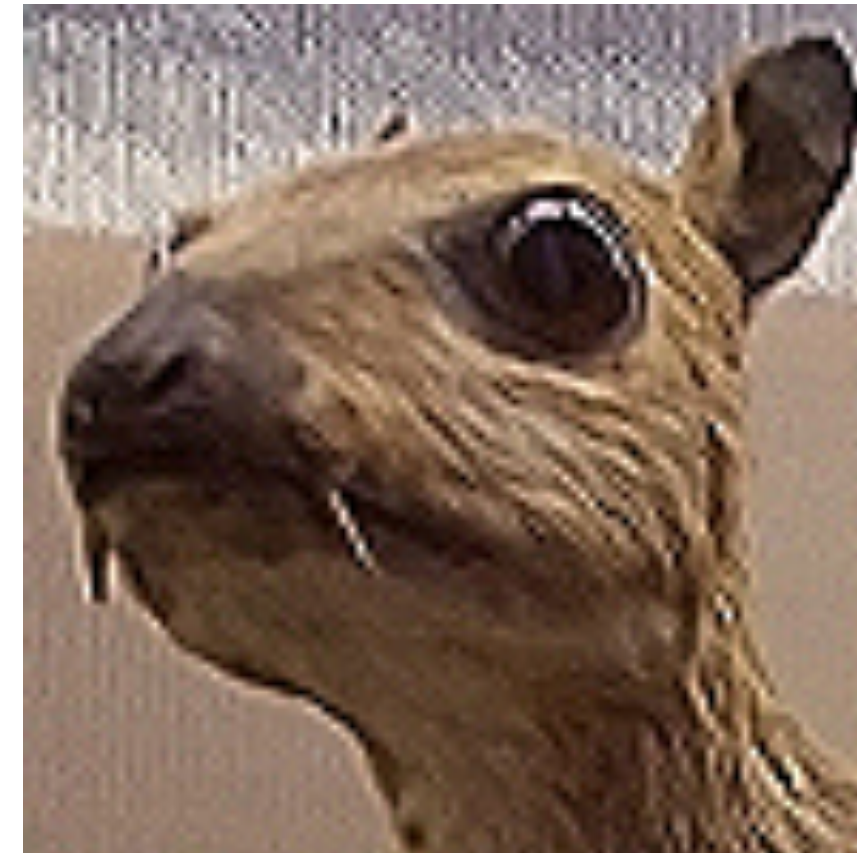


Edge Detection



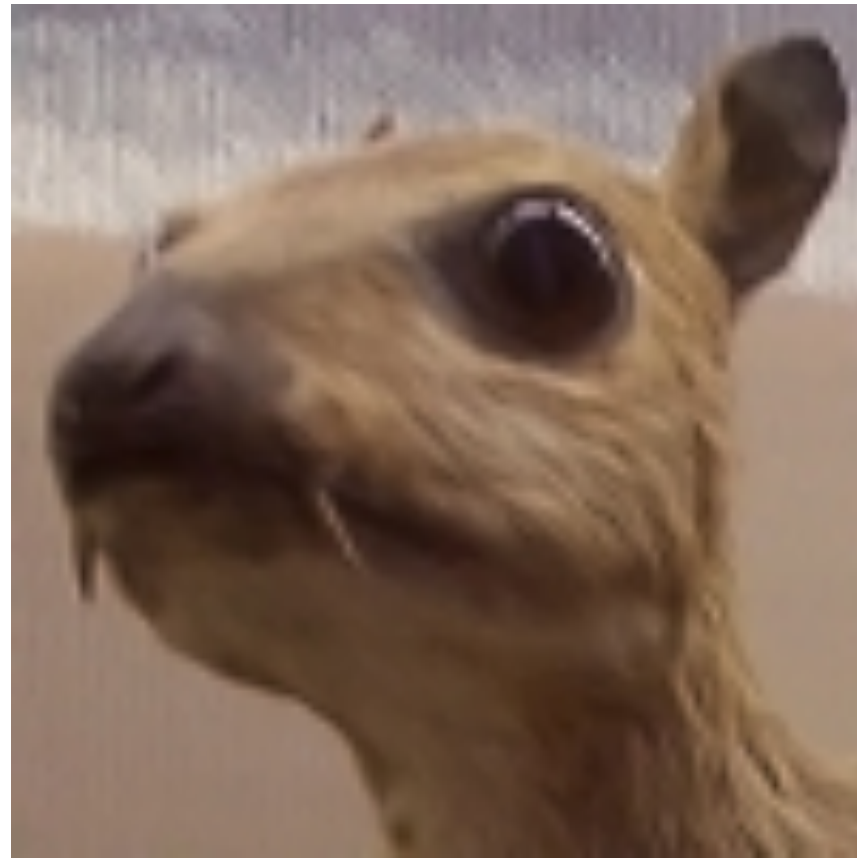
(wikipedia)

$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$



Sharpen

Examples



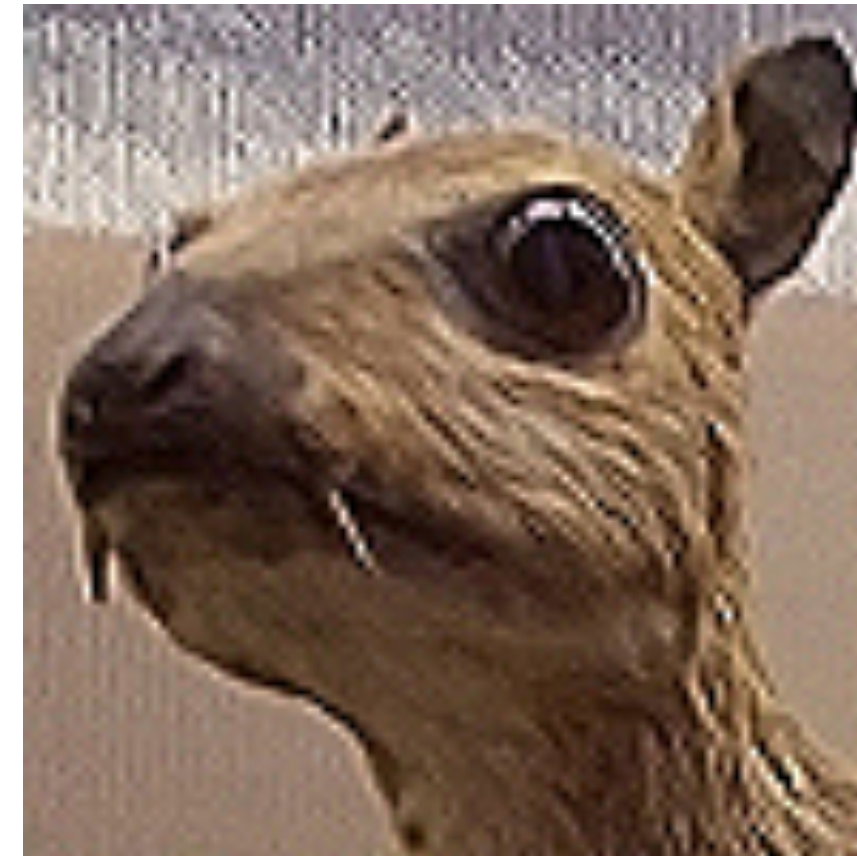
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$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$



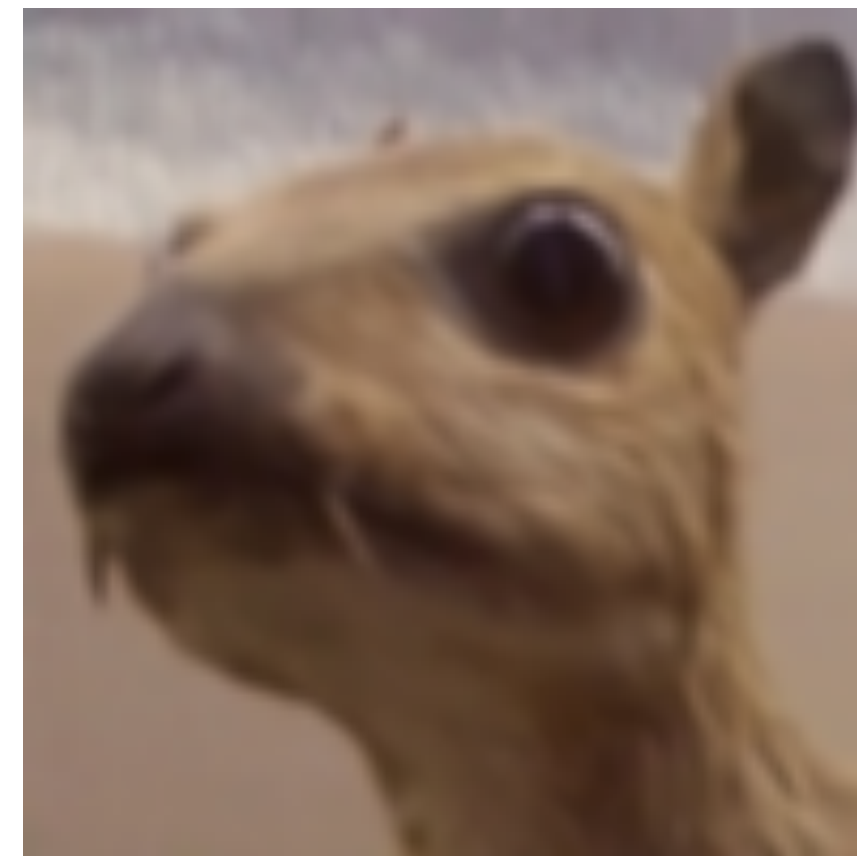
Edge Detection

$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$



Sharpen

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$



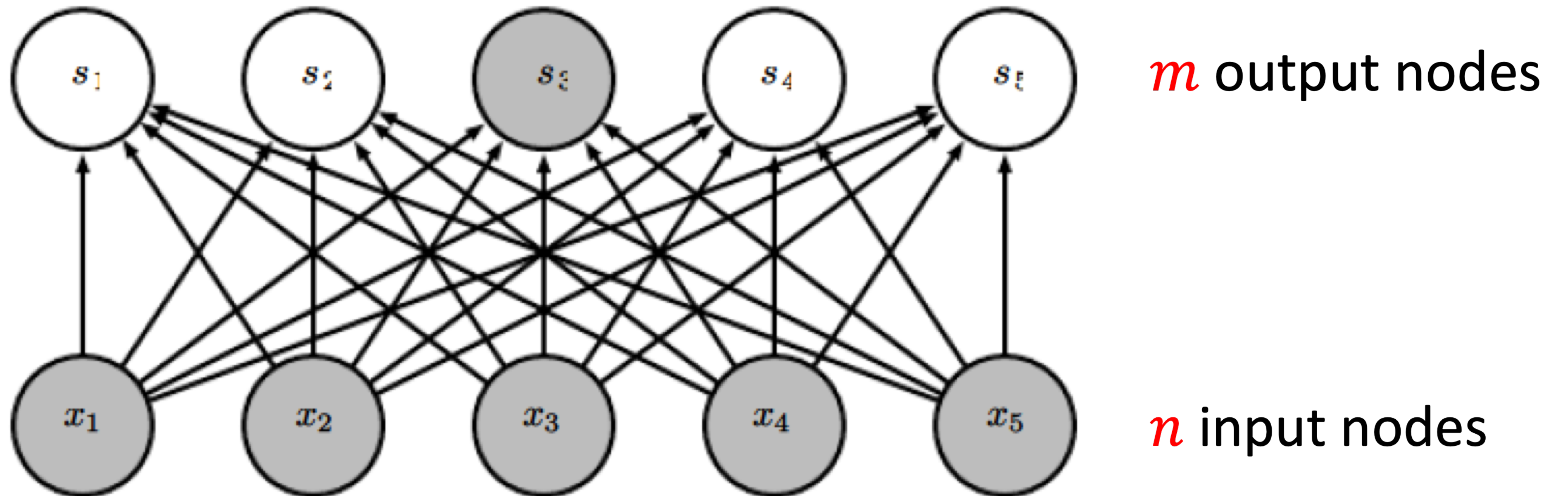
Gaussian Blur

Convolutional Neural Networks

- Convolutional networks: neural networks that use convolution in place of general matrix multiplication in at least one of their layers
- Strong empirical performance in applications – particularly computer vision.
- Examples: image classification, object detection.

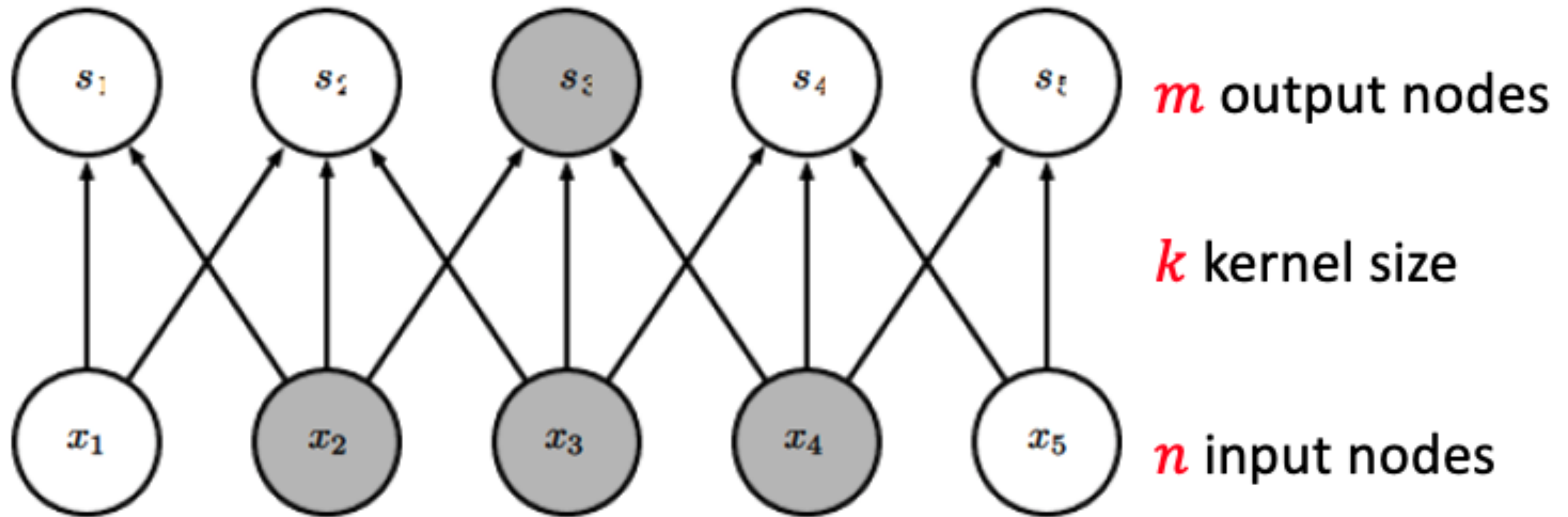
Advantage: sparse interaction

Fully connected layer, $m \times n$ edges



Advantage: sparse interaction

Convolutional layer, $\leq m \times k$ edges



Q1. Suppose we want to perform convolution as follows. What's the output?

0	1	2
3	4	5
6	7	8

*

0	1
1	-1

+ 1 = ?

A.

1	2
4	5

B.

1	2
3	4

C.

1	3
3	5

D.

0	1
3	4

Q1. Suppose we want to perform convolution as follows. What's the output?

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0	1
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+ 1

=

1	2
4	5

A.

1	2
4	5

B.

1	2
3	4

B.

1	3
3	5

$$\begin{aligned}
 0 \times 0 + 1 \times 1 + 3 \times 1 + 4 \times (-1) + 1 &= 1 \\
 1 \times 0 + 2 \times 1 + 4 \times 1 + 5 \times (-1) + 1 &= 2 \\
 3 \times 0 + 4 \times 1 + 6 \times 1 + 7 \times (-1) + 1 &= 4 \\
 4 \times 0 + 5 \times 1 + 7 \times 1 + 8 \times (-1) + 1 &= 5
 \end{aligned}$$

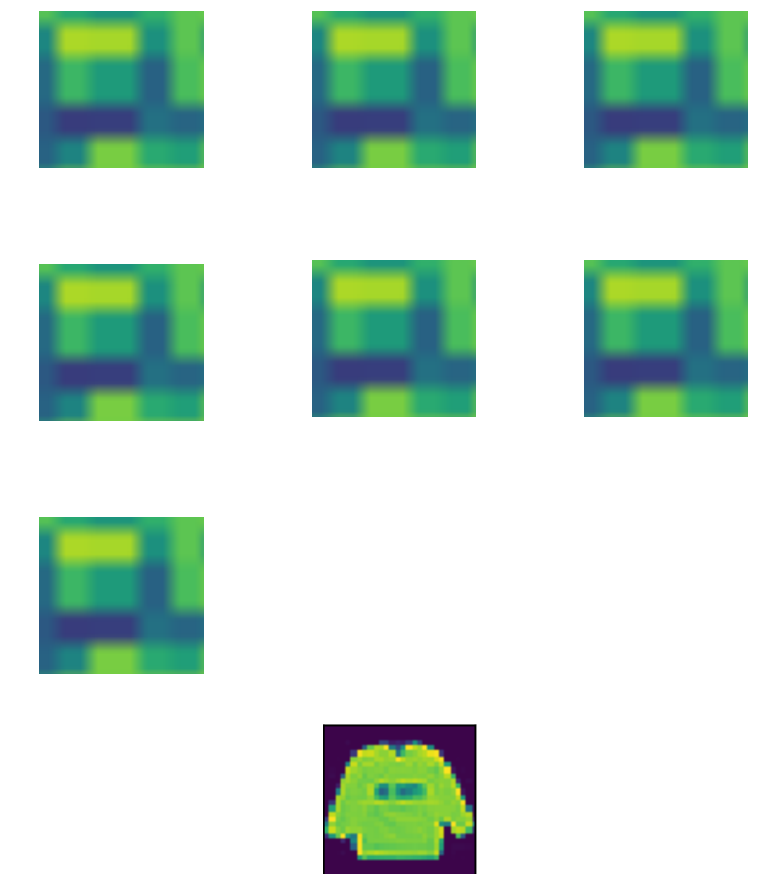
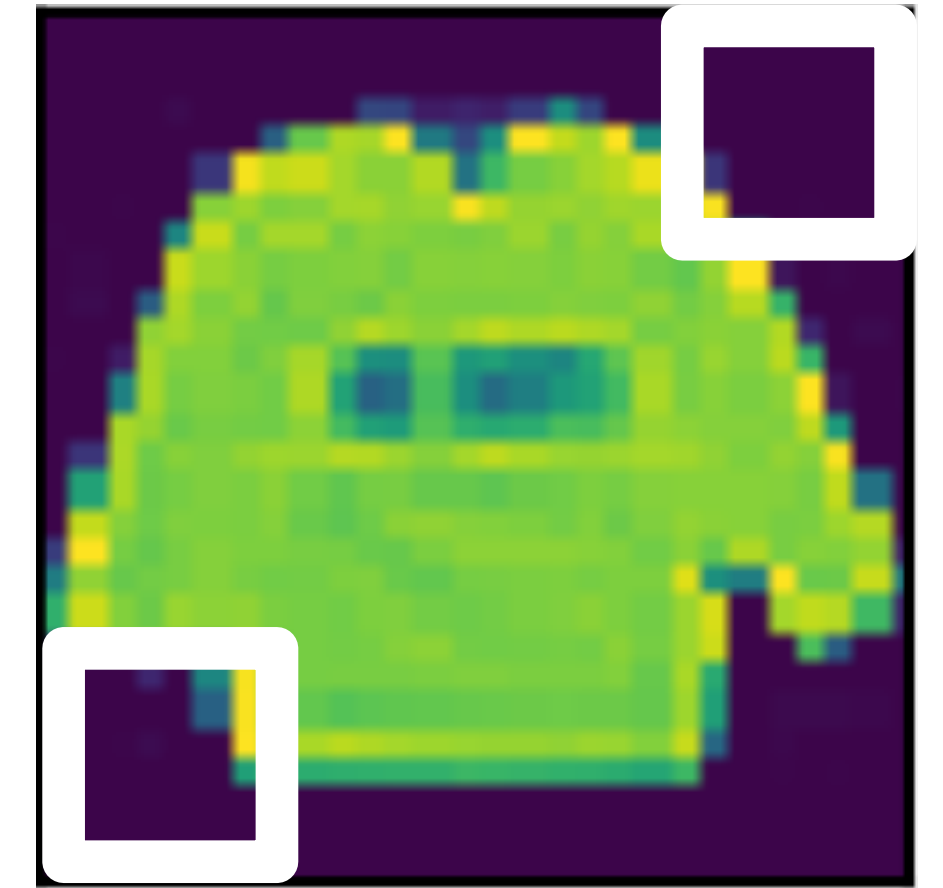
0	1
3	4



Padding and Stride

Padding

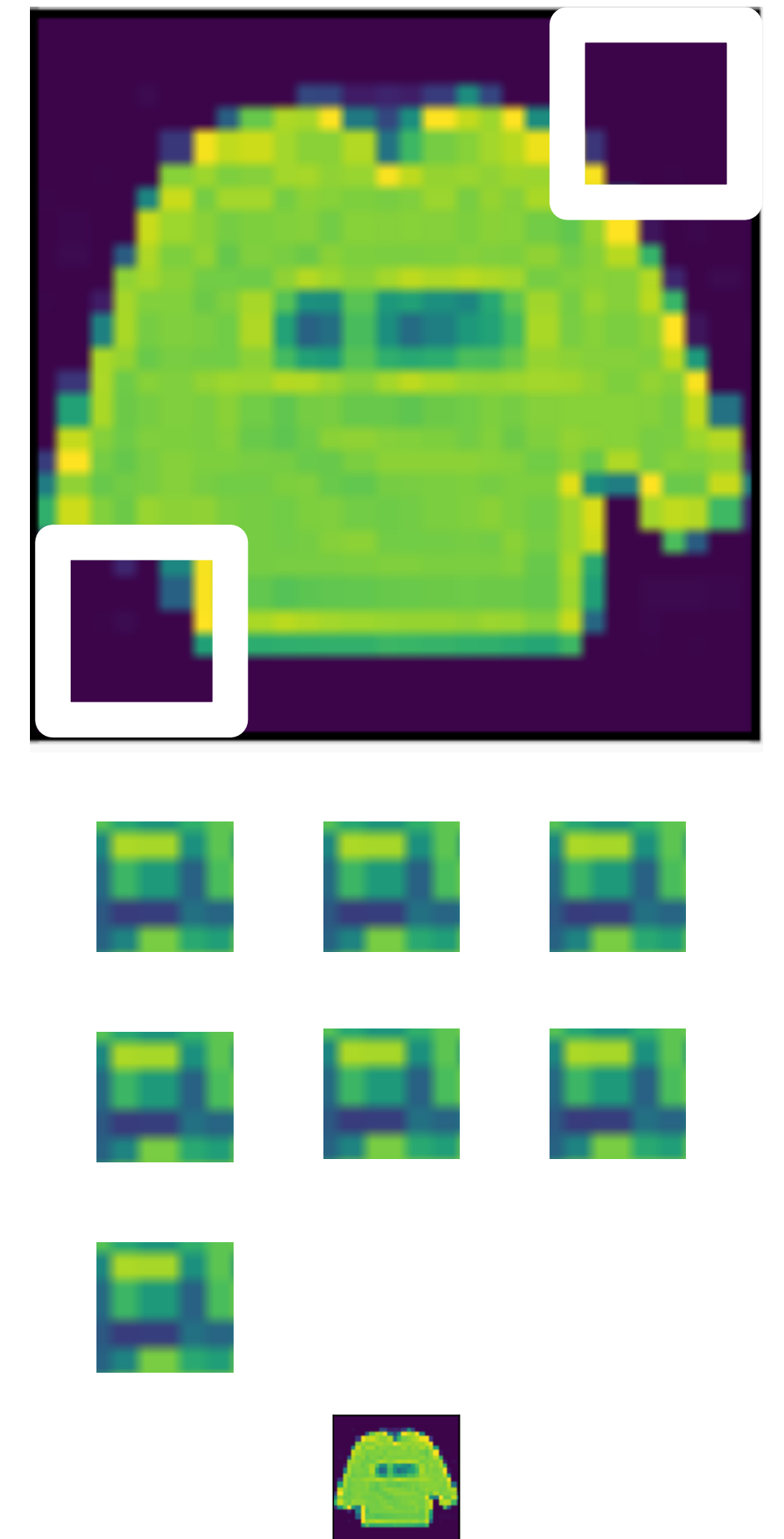
- Given a 32 x 32 input image
- Apply convolution with 5 x 5 kernel
 - 28 x 28 output with 1 layer
 - 4 x 4 output with 7 layers



Padding

- Given a 32 x 32 input image
- Apply convolution with 5 x 5 kernel
 - 28 x 28 output with 1 layer
 - 4 x 4 output with 7 layers
- Shape decreases faster with larger kernels
- Shape reduces from $n_h \times n_w$ to

$$(n_h - k_h + 1) \times (n_w - k_w + 1)$$



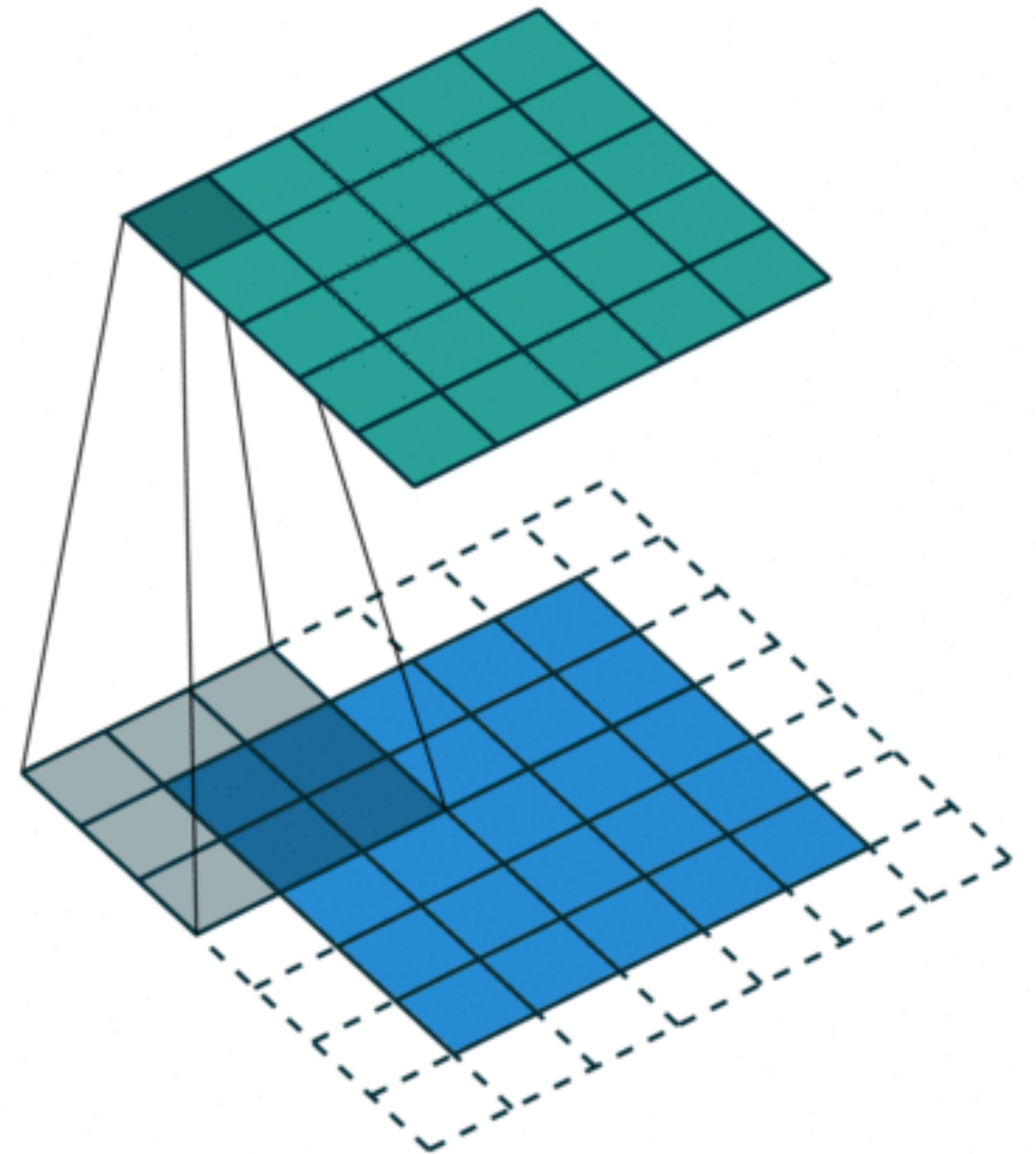
Convolutional Layers: Padding

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Padding adds rows/columns around input

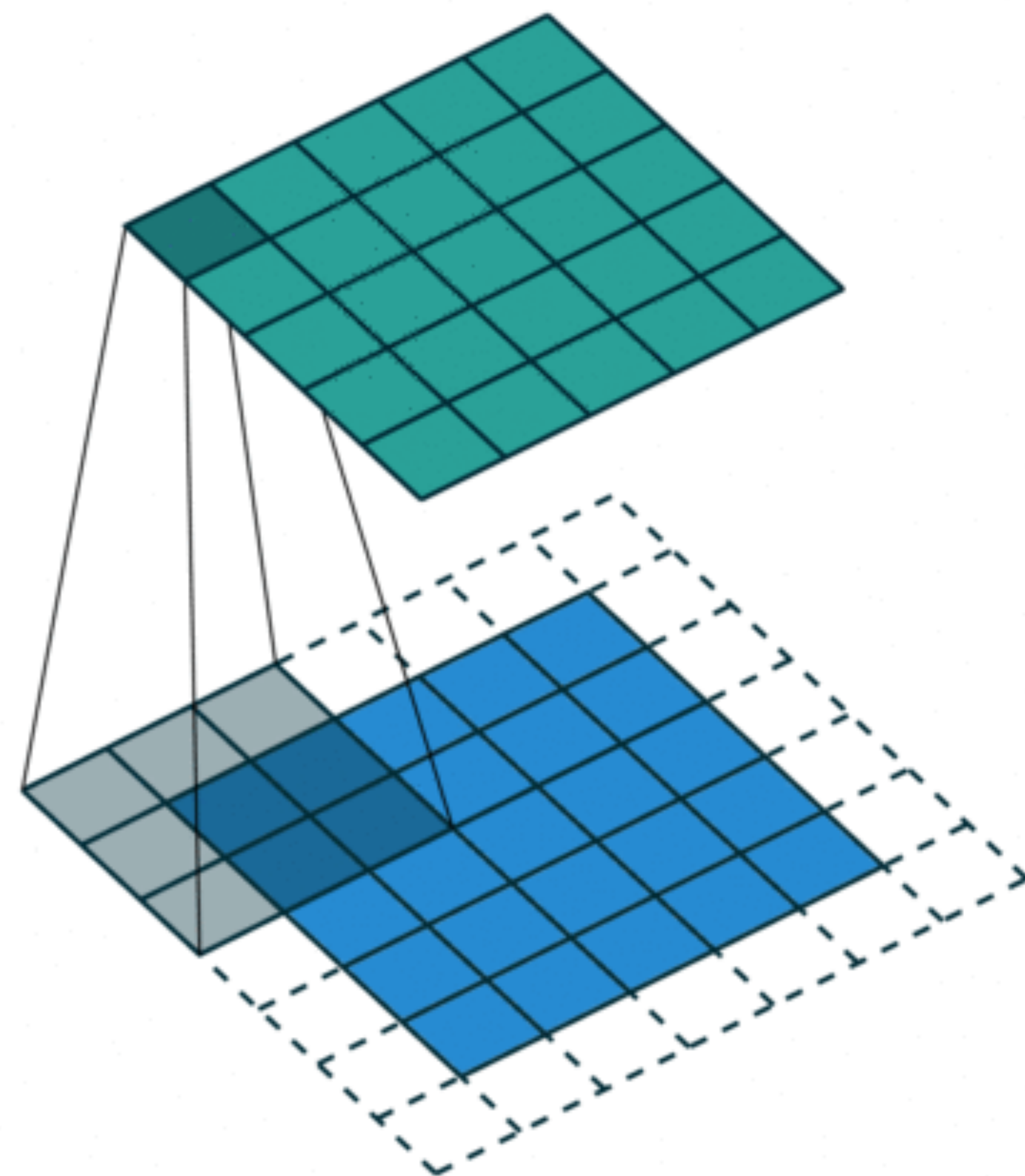
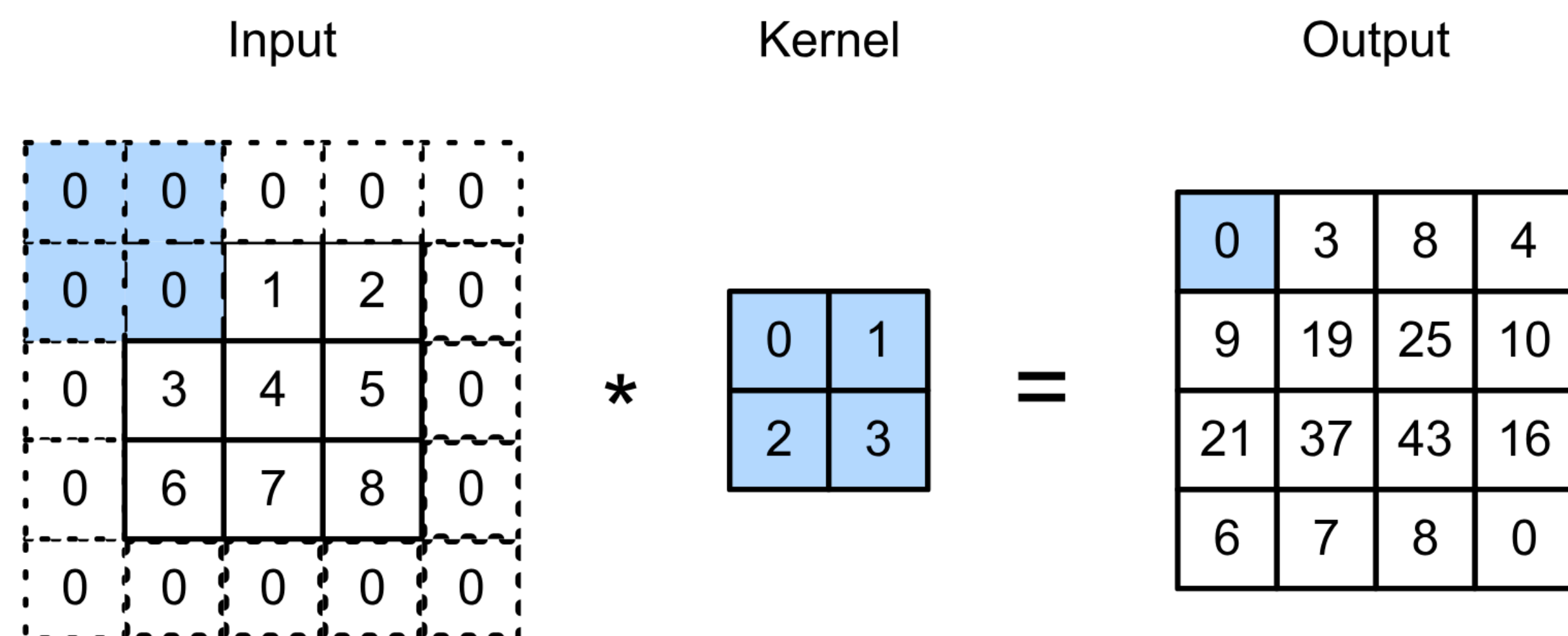
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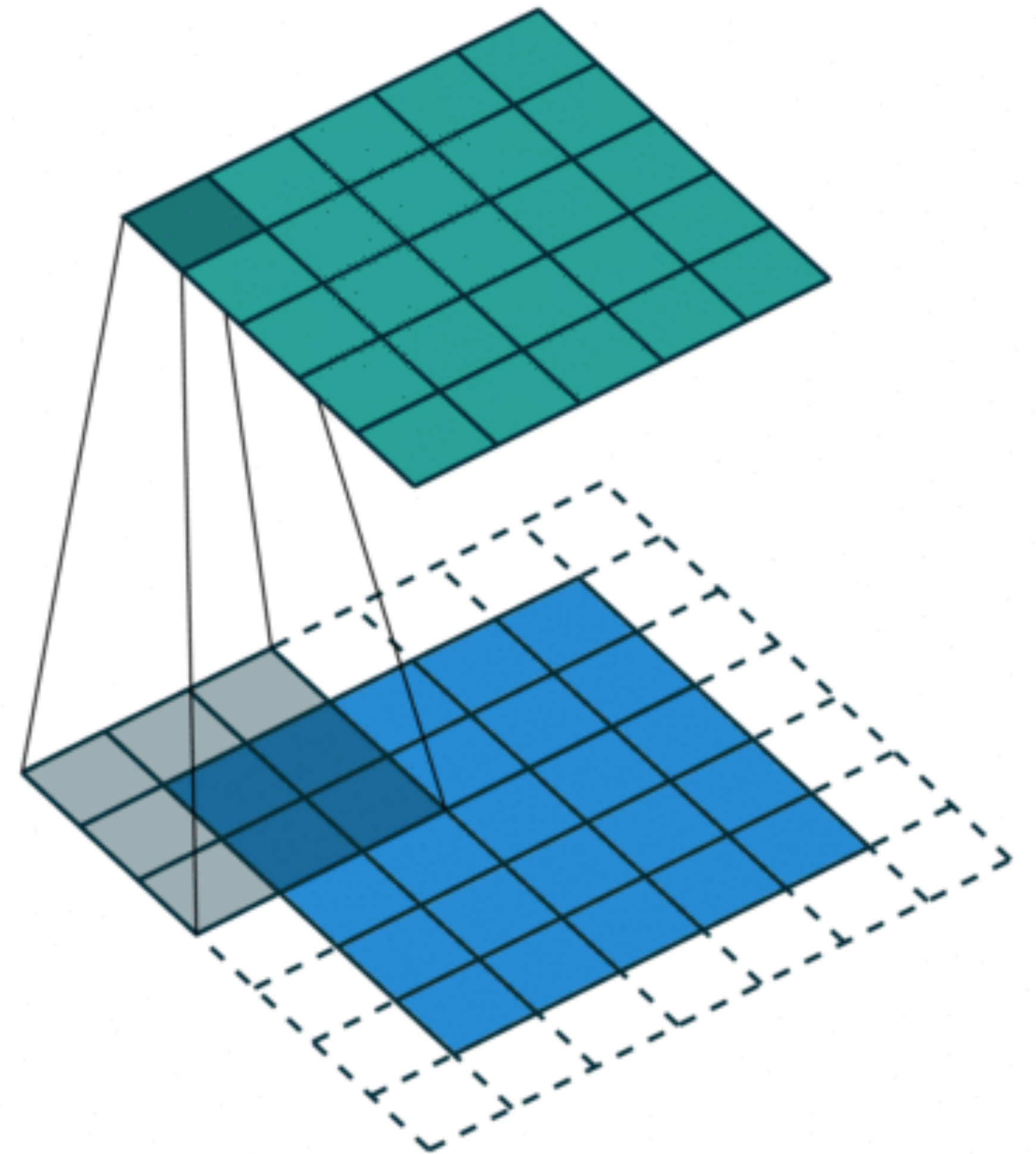
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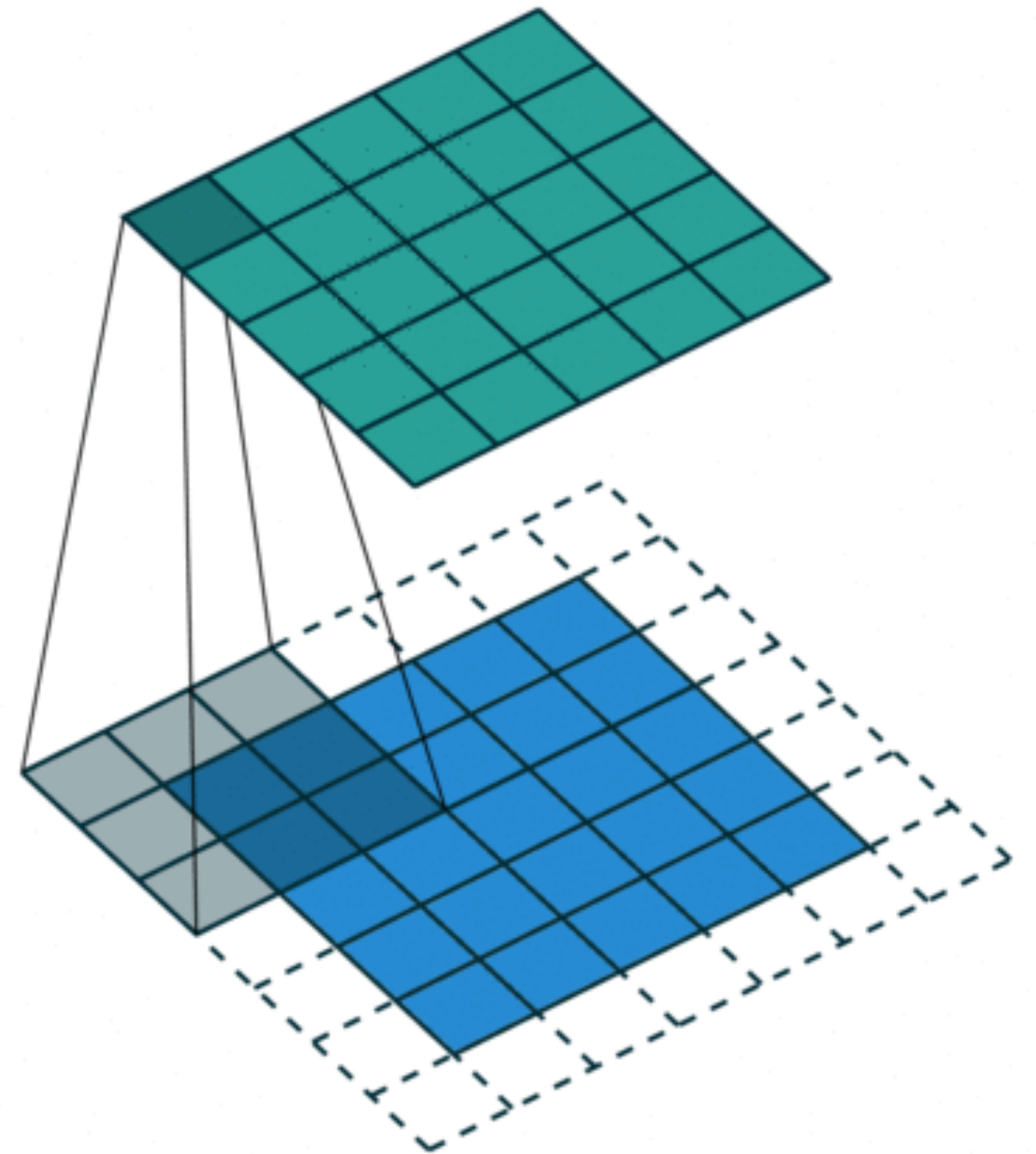
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Convolutional Layers: Padding

Padding adds rows/columns around input

- Why?

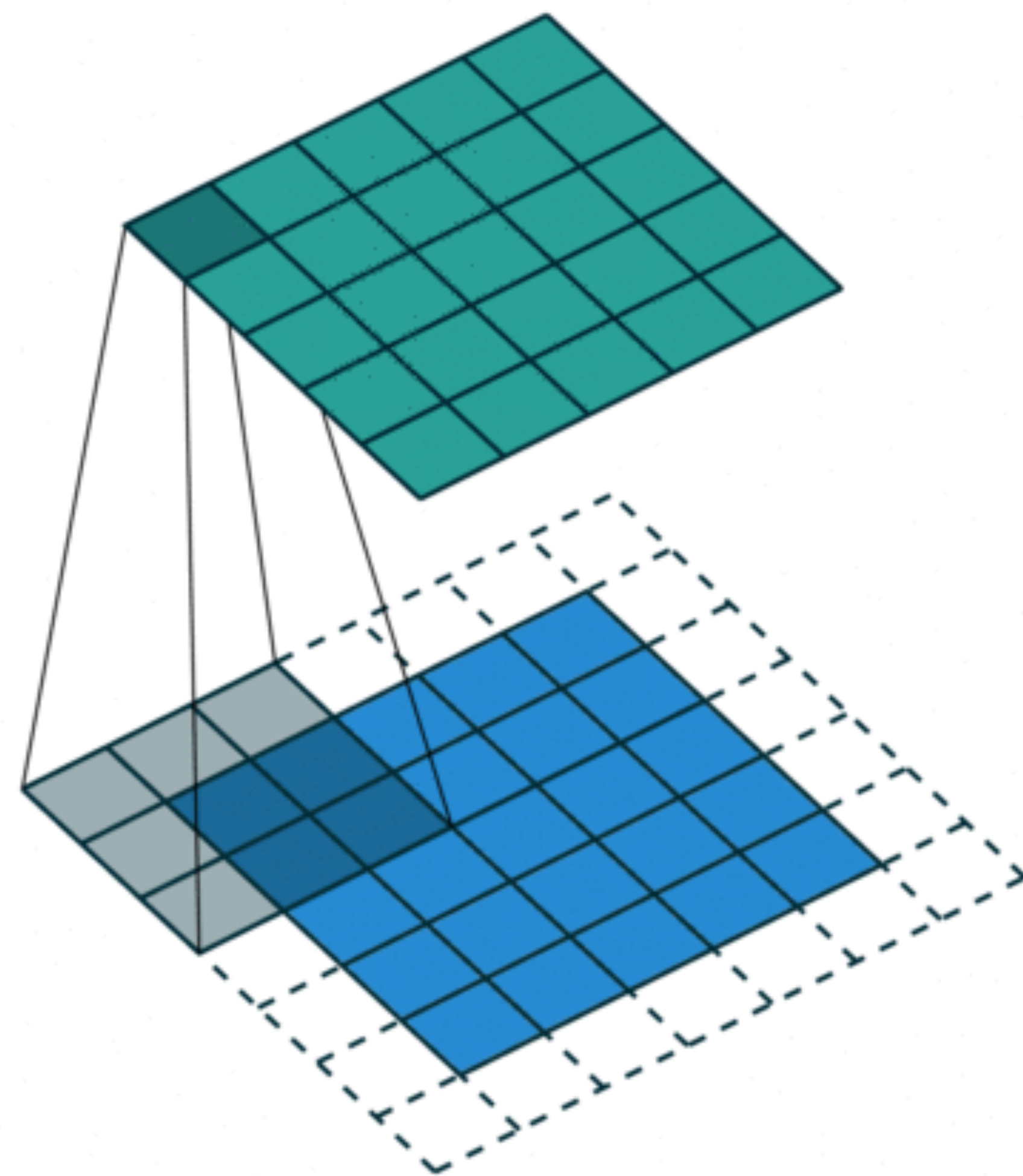


Convolutional Layers: Padding

Padding adds rows/columns around input

- Why?

1. Keeps **edge information**



Convolutional Layers: Padding

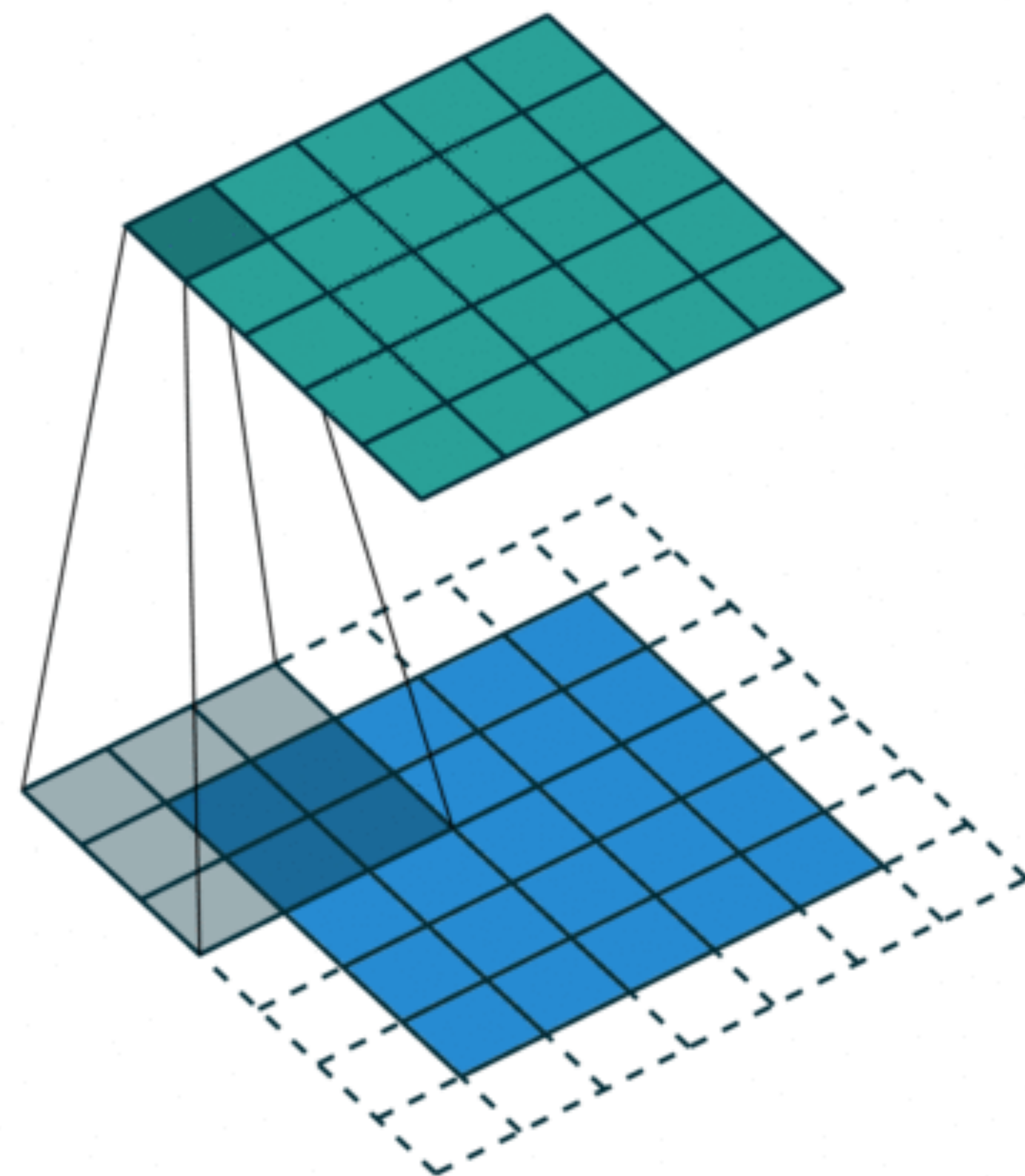
Padding adds rows/columns around input

- Why?

1. Keeps **edge information**

2. Preserves sizes / allows deep networks

- ie, for a 32x32 input image, 5x5 kernel, after 1 layer, get 28x28, after 7 layers, **only 4x4**



Convolutional Layers: Padding

Padding adds rows/columns around input

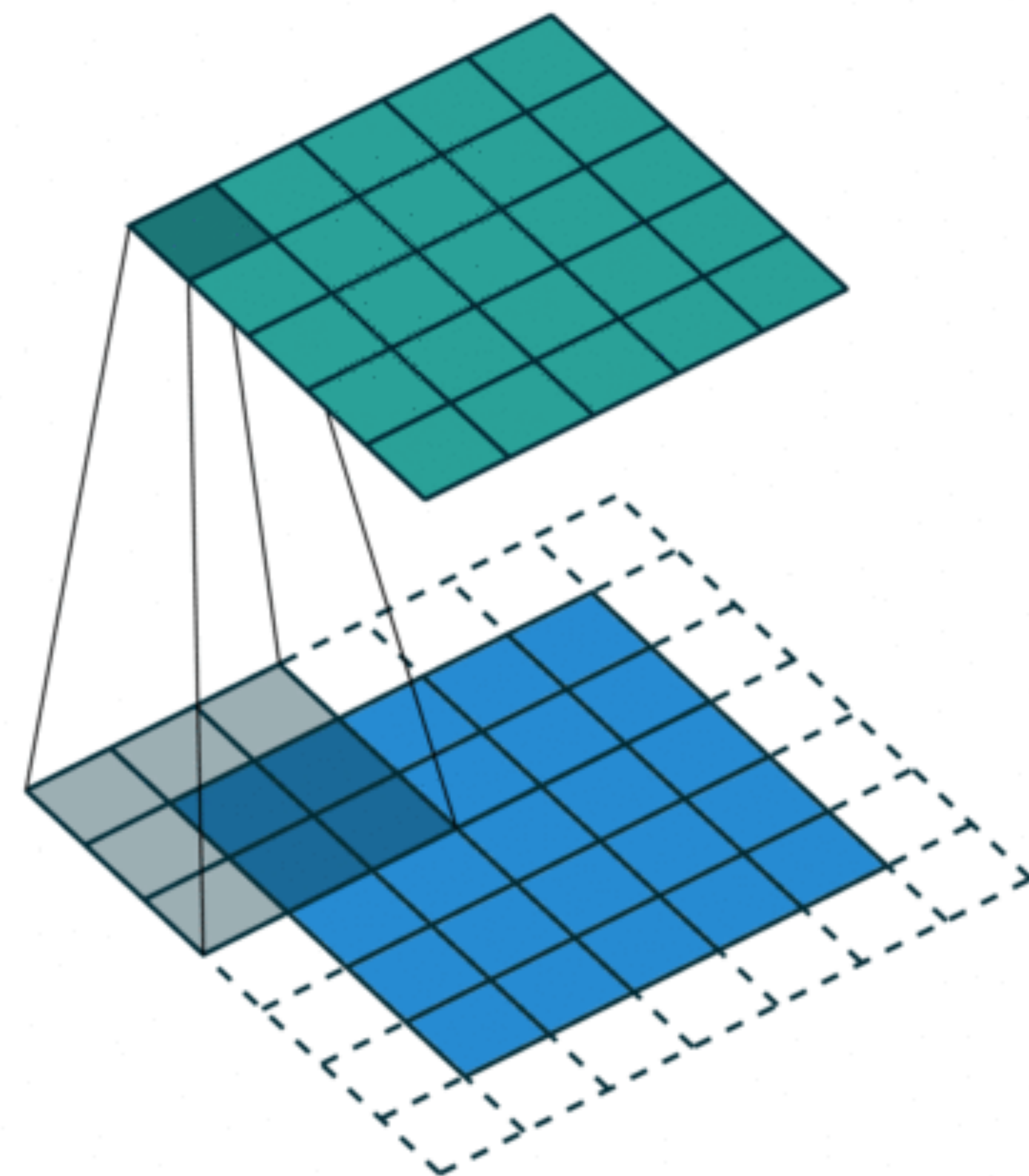
- Why?

1. Keeps **edge information**

2. Preserves sizes / allows deep networks

- ie, for a 32x32 input image, 5x5 kernel, after 1 layer, get 28x28, after 7 layers, **only 4x4**

3. Can combine different filter sizes



Convolutional Layers: Padding

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- Padding p_h rows and p_w columns, output shape is

Convolutional Layers: Padding

- Padding p_h rows and p_w columns, output shape is

$$(n_h - k_h + p_h + 1) \times (n_w - k_w + p_w + 1)$$

Convolutional Layers: Padding

- Padding p_h rows and p_w columns, output shape is

$$(n_h - k_h + p_h + 1) \times (n_w - k_w + p_w + 1)$$

- Common choice is $p_h = k_h - 1$ and $p_w = k_w - 1$

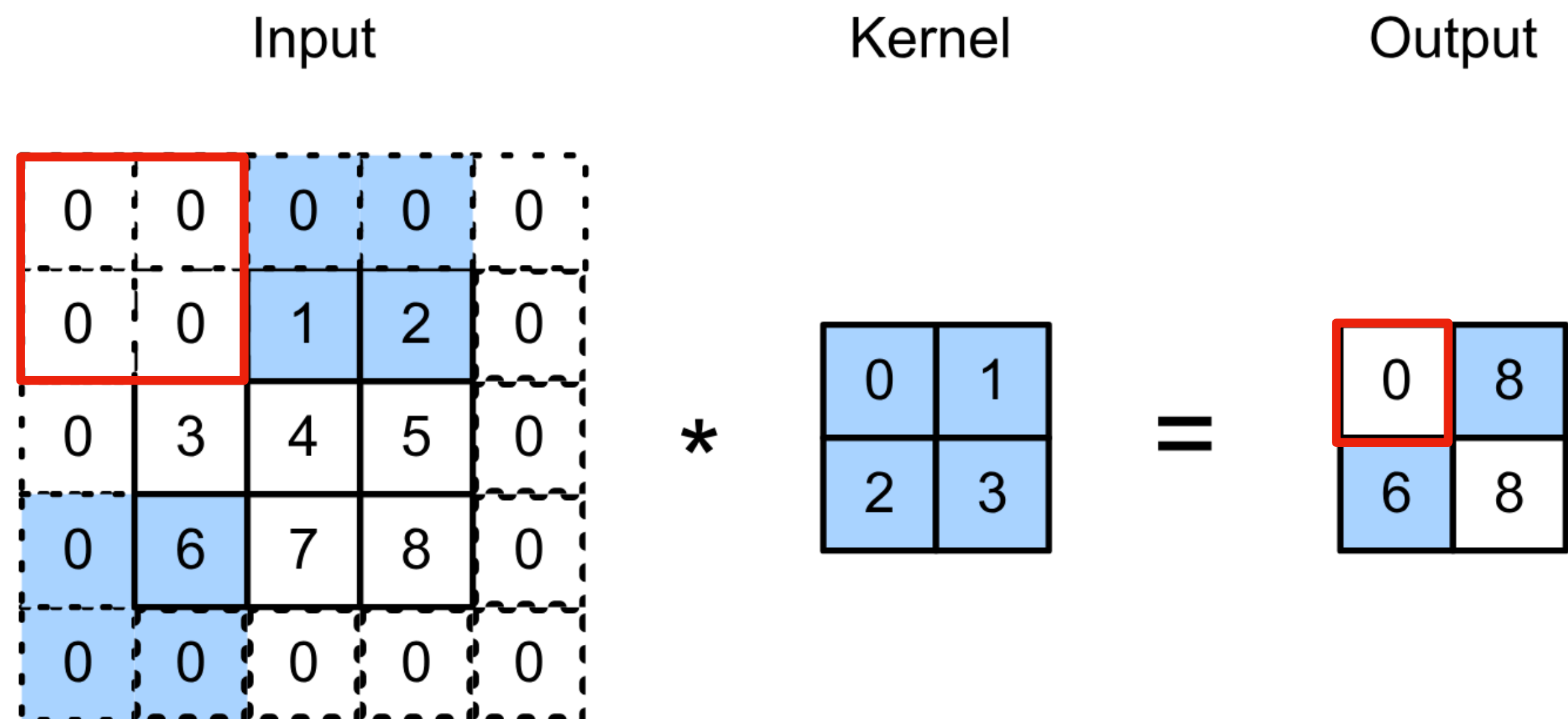
- Odd k_h : pad $p_h/2$ on both sides

- Even k_h : pad $\text{ceil}(p_h/2)$ on top, $\text{floor}(p_h/2)$ on bottom

Stride

- Stride is the #rows / #columns per slide

Example: strides of 3 and 2 for height and width



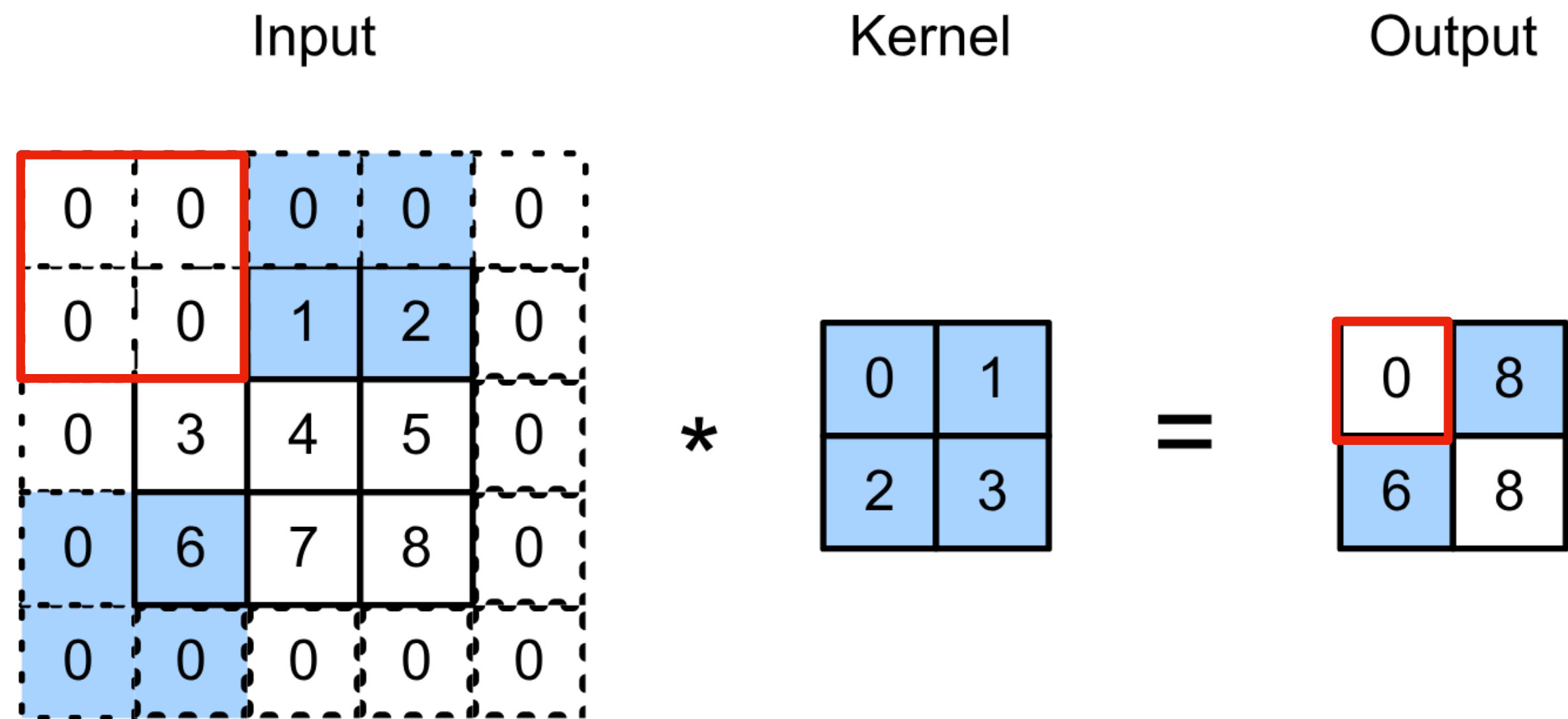
$$0 \times 0 + 0 \times 1 + 1 \times 2 + 2 \times 3 = 8$$

$$0 \times 0 + 6 \times 1 + 0 \times 2 + 0 \times 3 = 6$$

Stride

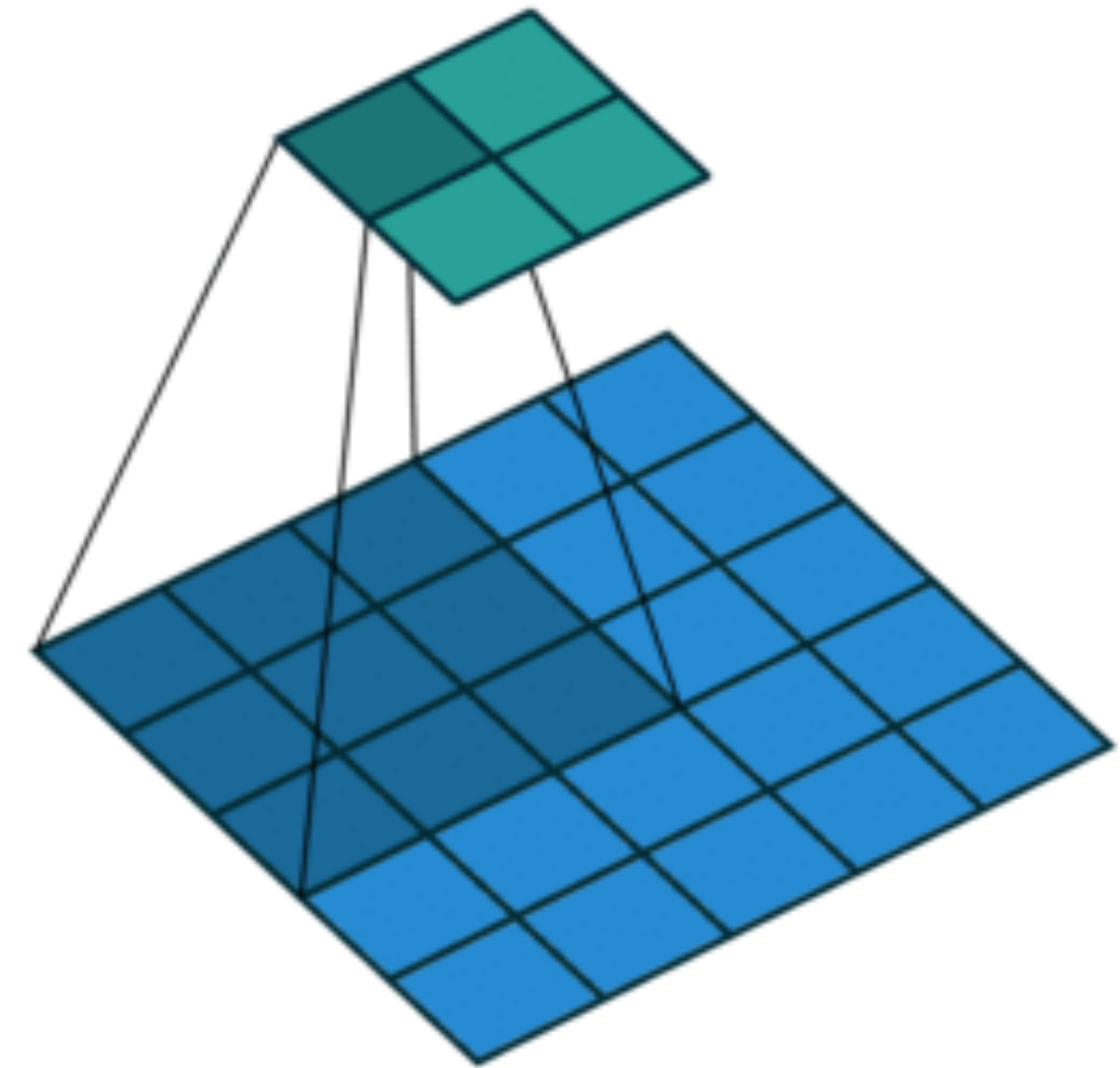
- Stride is the #rows / #columns per slide

Example: strides of 3 and 2 for height and width



$$0 \times 0 + 0 \times 1 + 1 \times 2 + 2 \times 3 = 8$$

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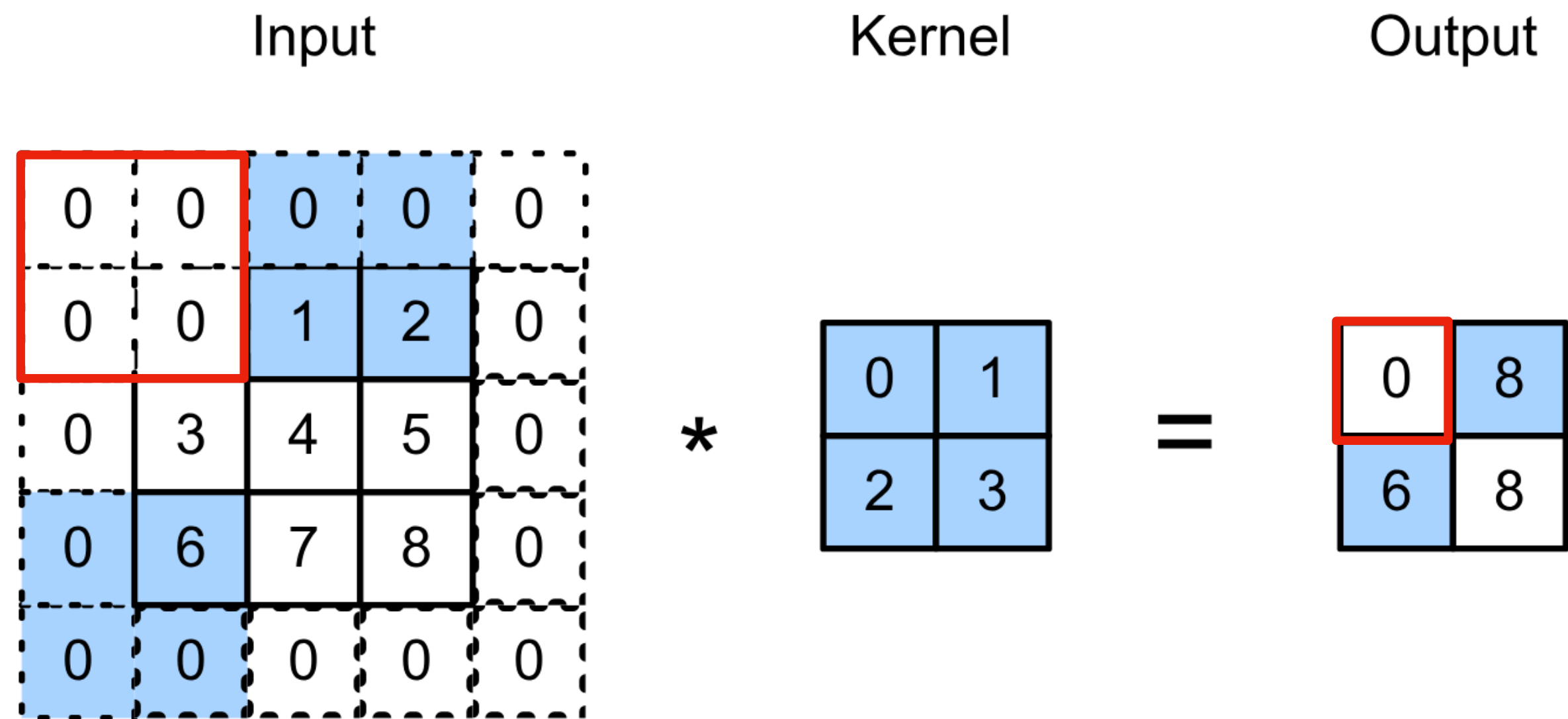


Stride 2,2

Stride

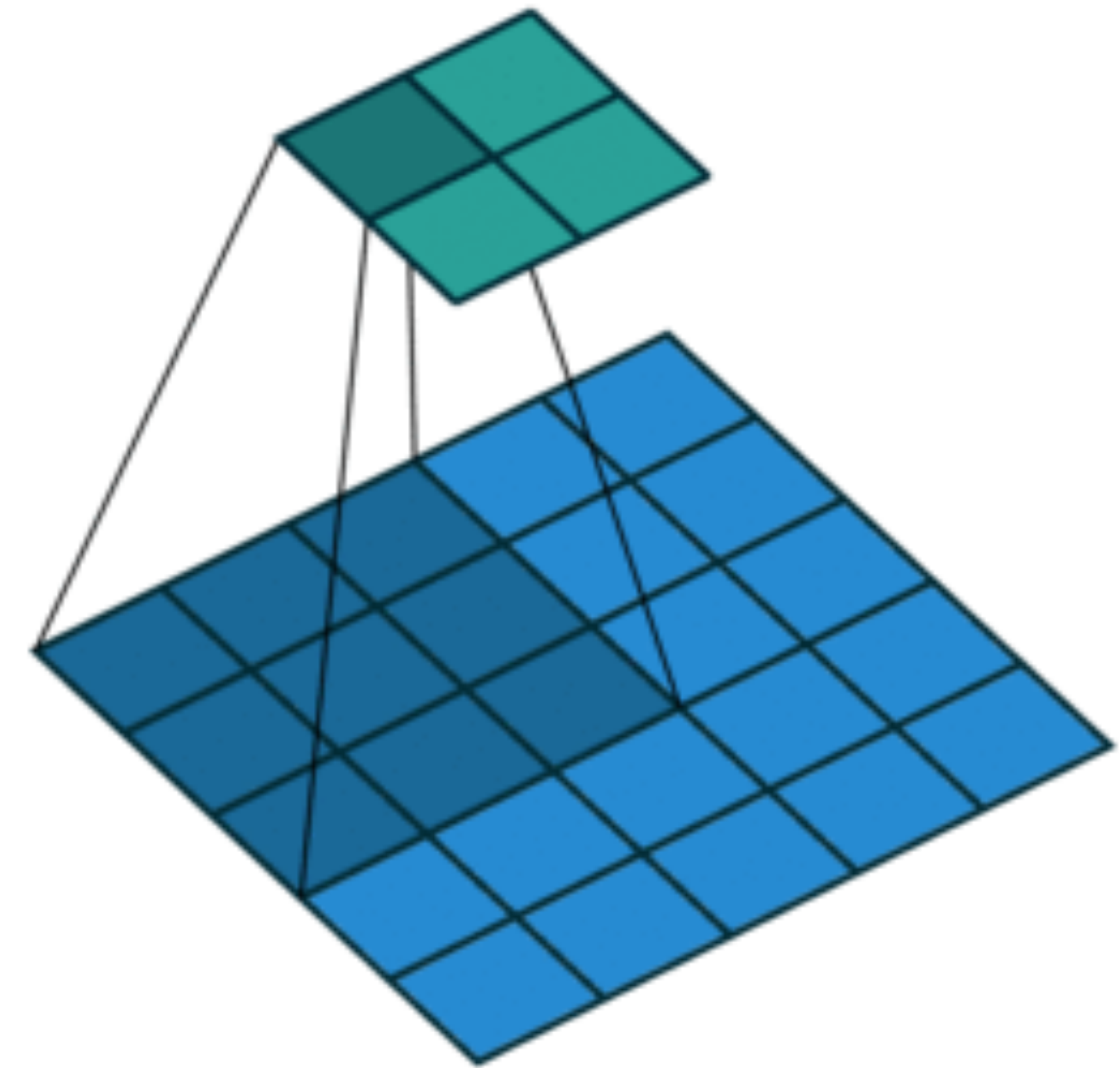
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Example: strides of 3 and 2 for height and width



$$0 \times 0 + 0 \times 1 + 1 \times 2 + 2 \times 3 = 8$$

$$0 \times 0 + 6 \times 1 + 0 \times 2 + 0 \times 3 = 6$$



Stride 2,2

Convolutional Layers: Stride

Convolutional Layers: Stride

- Given stride s_h for the height and stride s_w for the width, the output shape is

Convolutional Layers: Stride

- Given stride s_h for the height and stride s_w for the width, the output shape is

$$\lfloor (n_h - k_h + p_h + s_h) / s_h \rfloor \times \lfloor (n_w - k_w + p_w + s_w) / s_w \rfloor$$

Convolutional Layers: Stride

- Given stride s_h for the height and stride s_w for the width, the output shape is

$$\lfloor (n_h - k_h + p_h + s_h) / s_h \rfloor \times \lfloor (n_w - k_w + p_w + s_w) / s_w \rfloor$$

- Set $p_h = k_h - 1$, $p_w = k_w - 1$, then get

Convolutional Layers: Stride

- Given stride s_h for the height and stride s_w for the width, the output shape is

$$\lfloor (n_h - k_h + p_h + s_h) / s_h \rfloor \times \lfloor (n_w - k_w + p_w + s_w) / s_w \rfloor$$

- Set $p_h = k_h - 1$, $p_w = k_w - 1$, then get

$$\lfloor (n_h + s_h - 1) / s_h \rfloor \times \lfloor (n_w + s_w - 1) / s_w \rfloor$$

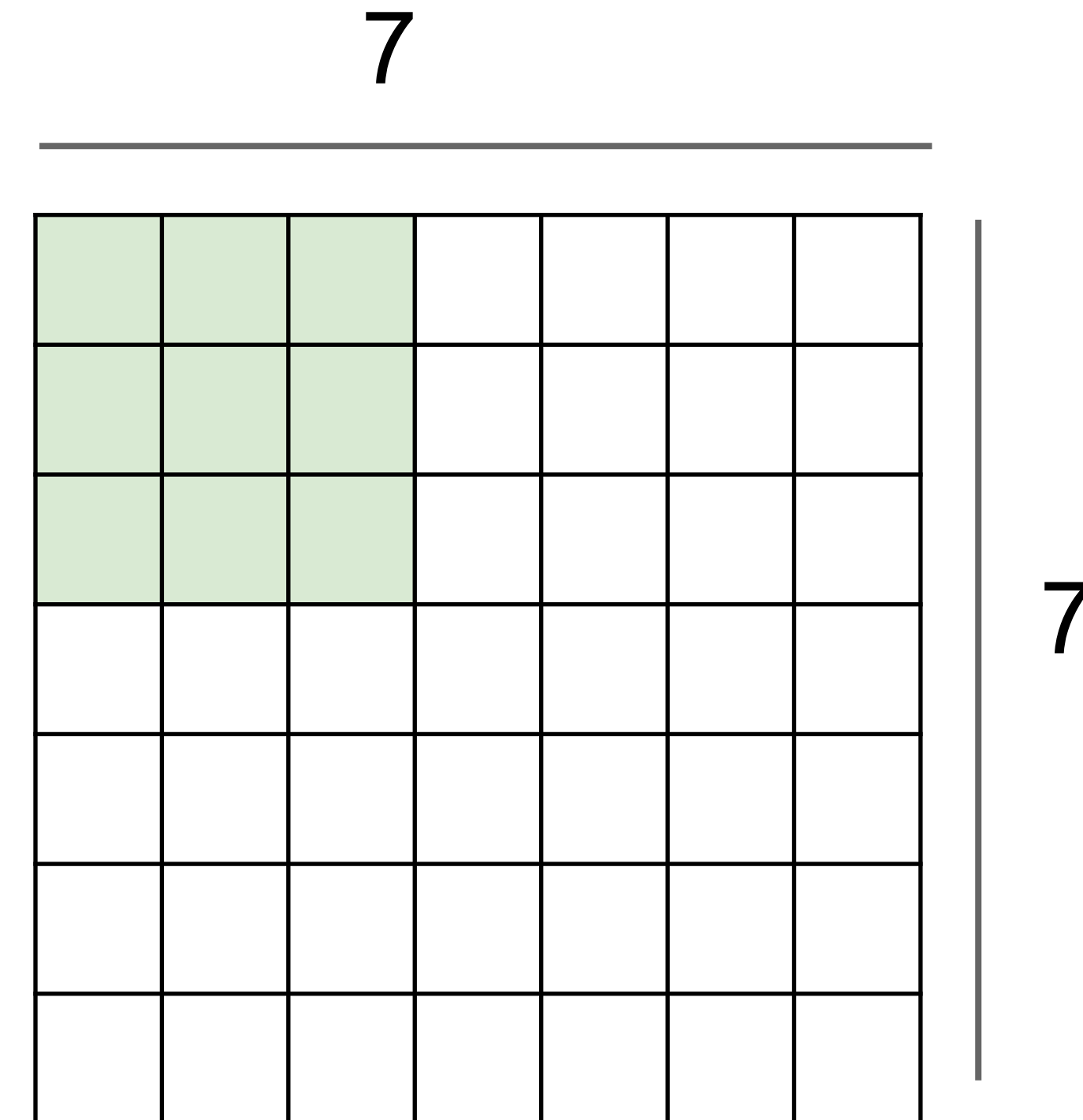
Q2. Suppose we want to perform convolution on a single channel image of size 7×7 (no padding) with a kernel of size 3×3 , and stride = 2. What is the dimension of the output?

A. 3×3

B. 7×7

C. 5×5

D. 2×2



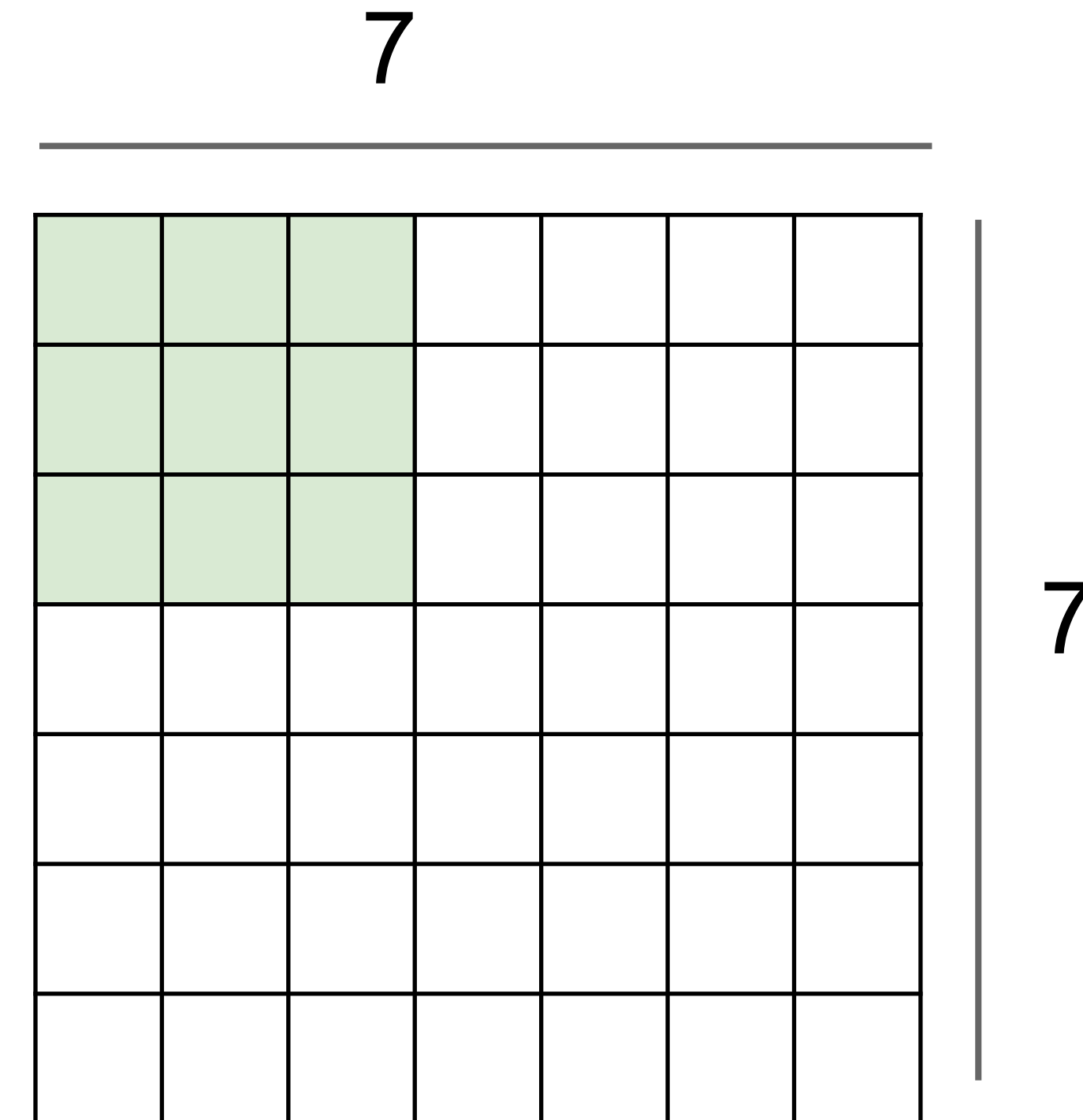
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$$\lfloor (n_h - k_h + p_h + s_h) / s_h \rfloor \times \lfloor (n_w - k_w + p_w + s_w) / s_w \rfloor$$



Multiple Input and Output Channels

Multiple Input Channels

- Color image may have three RGB channels
- Converting to grayscale loses information



Multiple Input Channels

- Color image may have three RGB channels
- Converting to grayscale loses information



Multiple Input Channels

- Have a kernel matrix for each channel, and then sum results over channels

Input

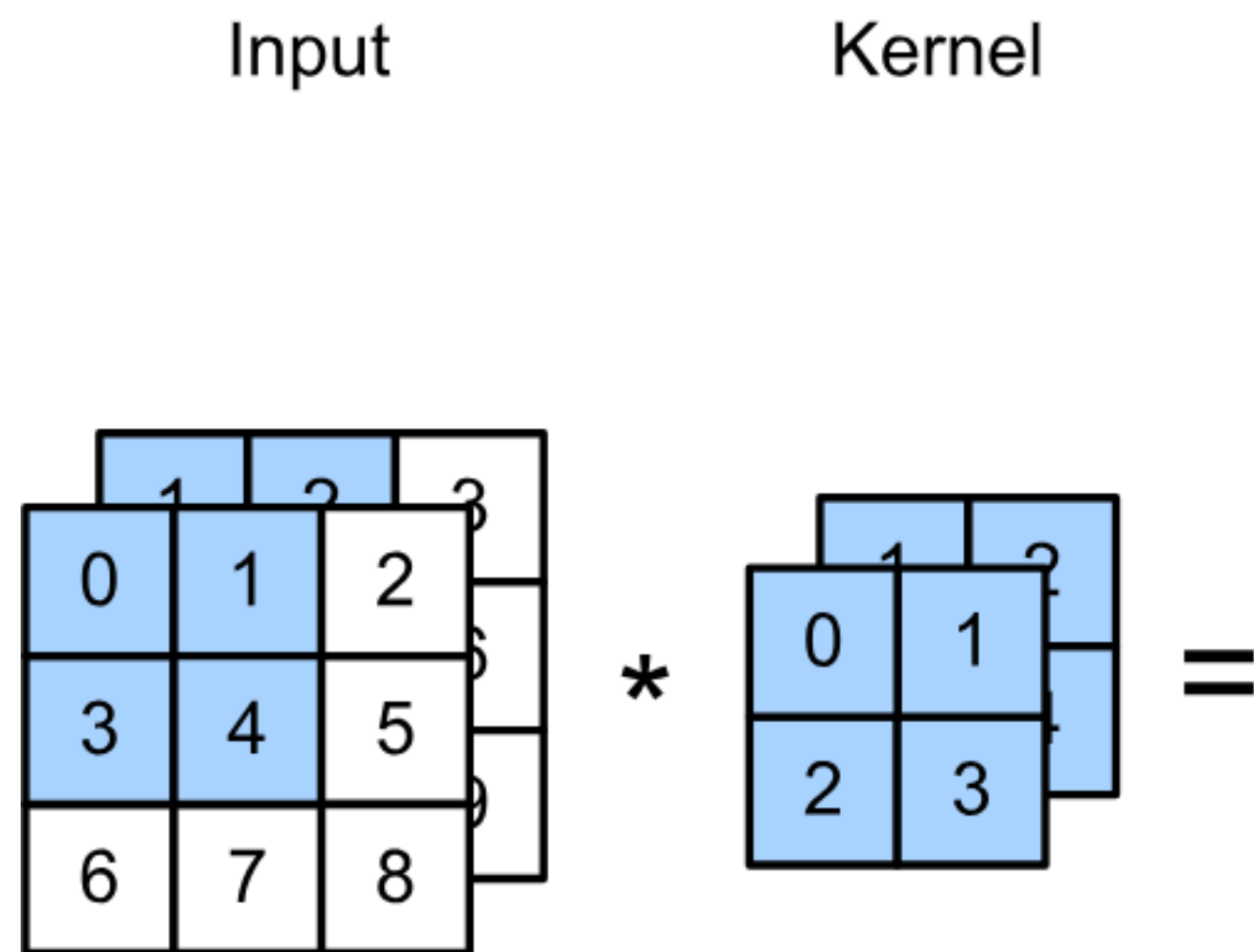
	1	2	3	
0	1	2		
3	4	5		
6	7	8		

*

=

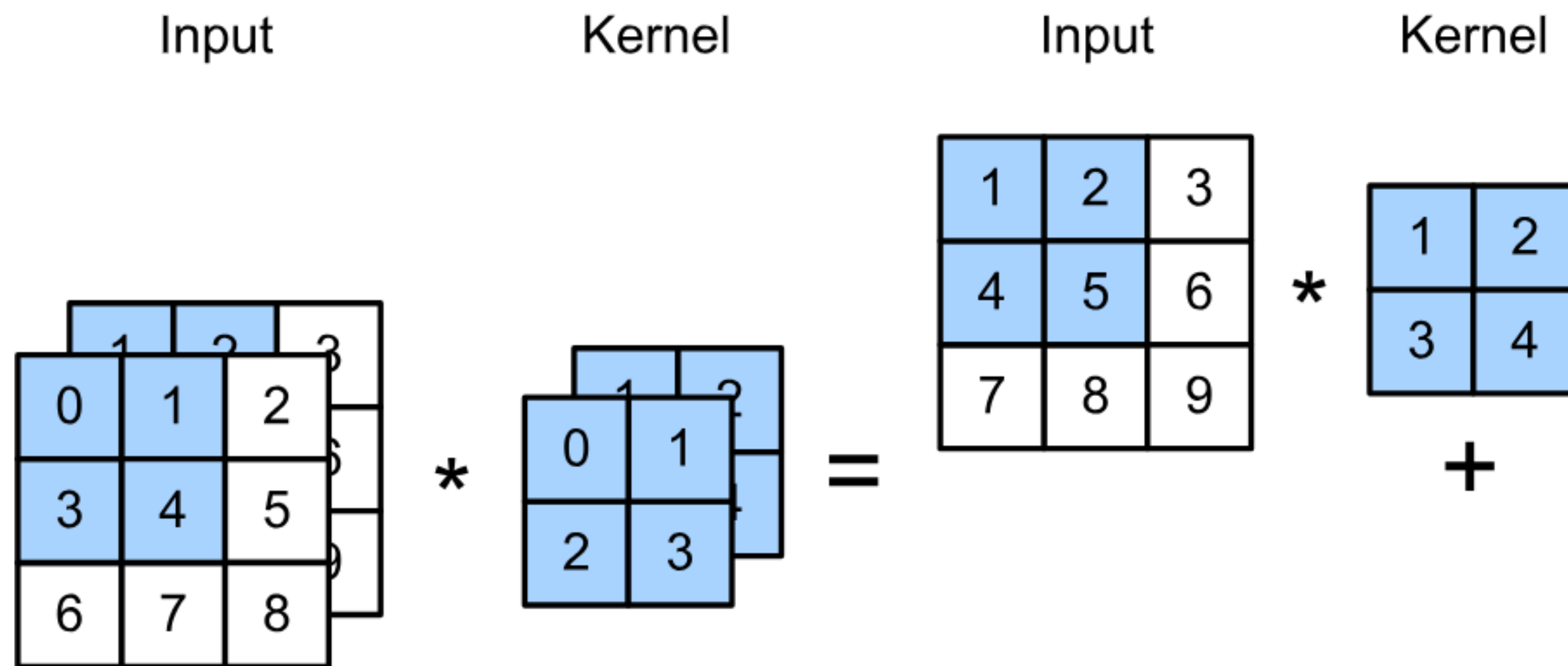
Multiple Input Channels

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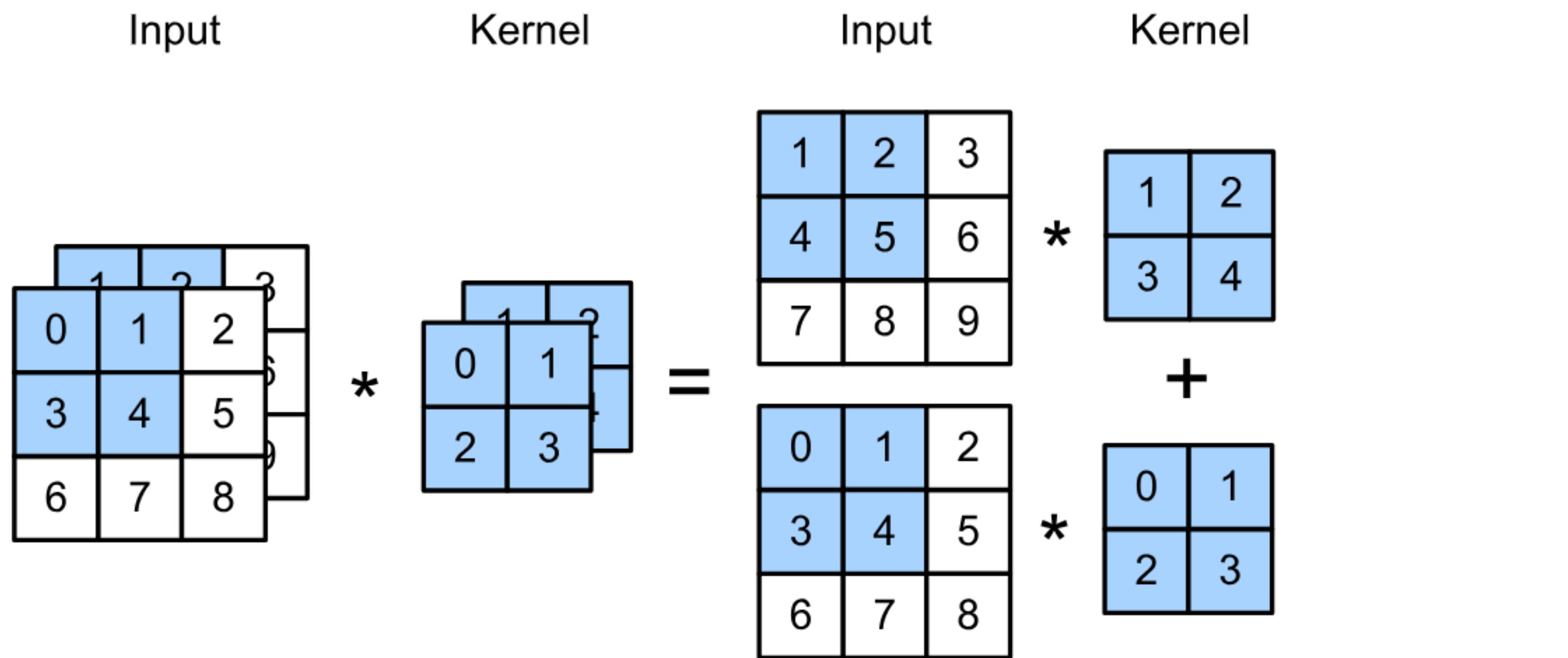
Multiple Input Channels

- Have a kernel matrix for each channel, and then sum results over channels



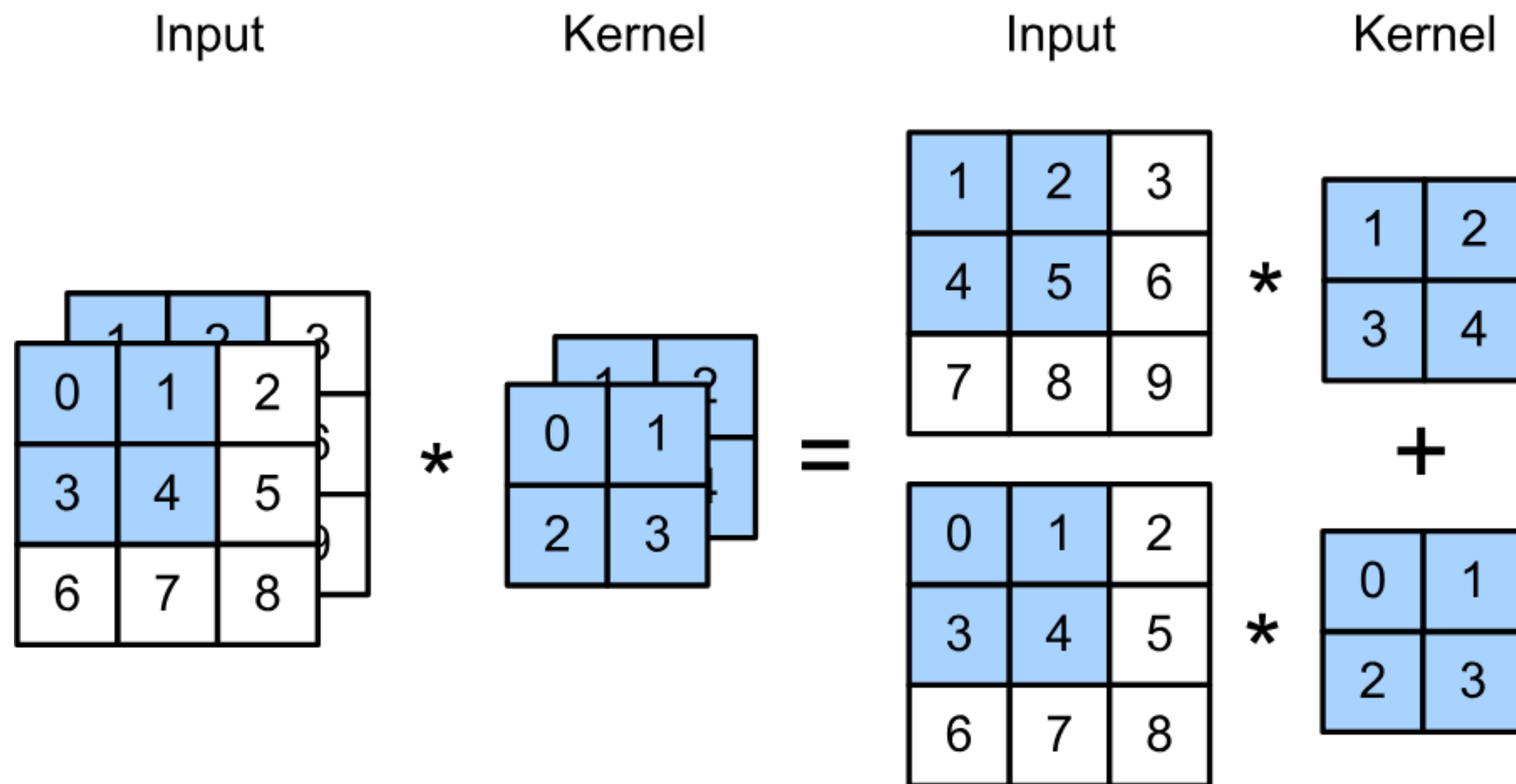
Multiple Input Channels

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Multiple Input Channels

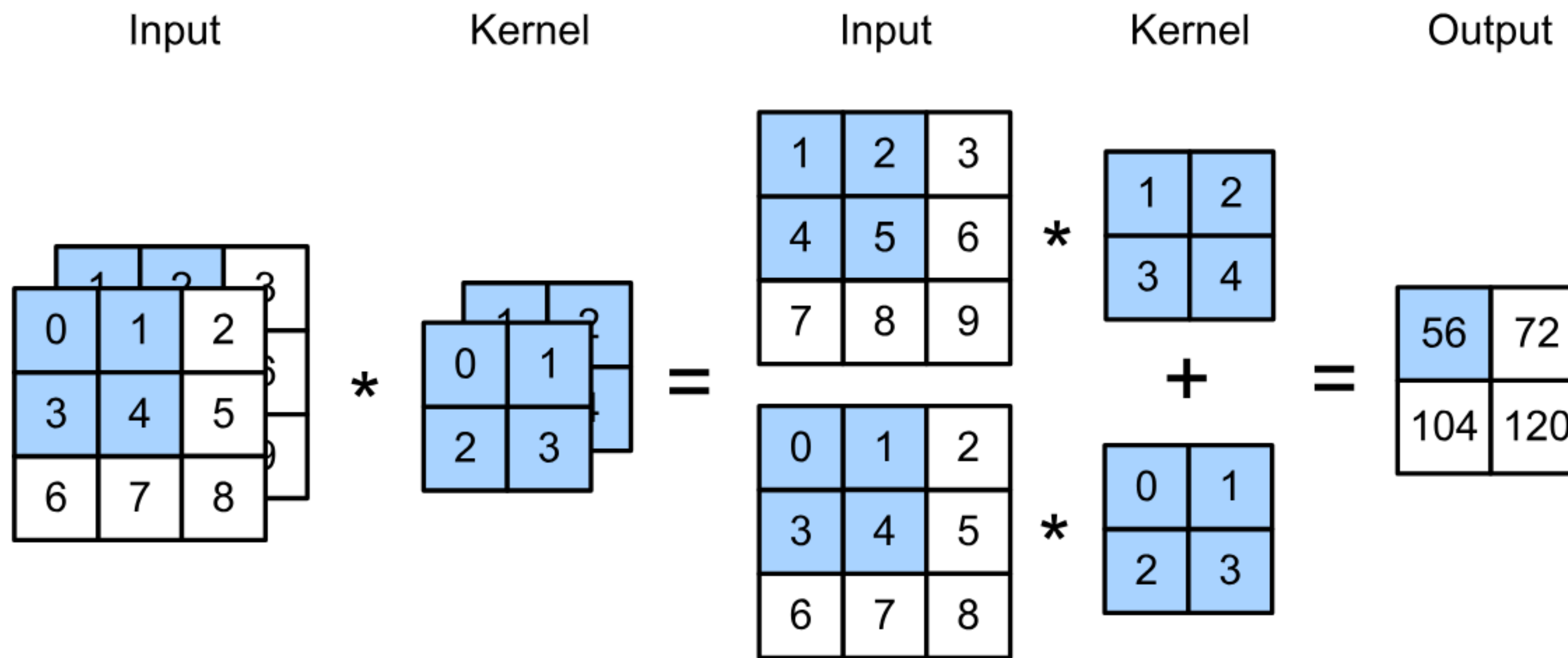
- Have a kernel matrix for each channel, and then sum results over channels



$$(1 \times 1 + 2 \times 2 + 4 \times 3 + 5 \times 4) \\ + (0 \times 0 + 1 \times 1 + 3 \times 2 + 4 \times 3) \\ = 56$$

Multiple Input Channels

- Have a kernel matrix for each channel, and then sum results over channels



$$(1 \times 1 + 2 \times 2 + 4 \times 3 + 5 \times 4) + (0 \times 0 + 1 \times 1 + 3 \times 2 + 4 \times 3) = 56$$

Convolutional Layers: Channels

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Convolutional Layers: Channels

- How to integrate multiple channels?
 - Have a kernel for each channel, and then sum results over channels

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Convolutional Layers: Channels

- How to integrate multiple channels?
 - Have a kernel for each channel, and then sum results over channels

$$\mathbf{X} : c_i \times n_h \times n_w$$

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Convolutional Layers: Channels

- How to integrate multiple channels?
 - Have a kernel for each channel, and then sum results over channels

$$\mathbf{X} : c_i \times n_h \times n_w$$

$$\mathbf{W} : c_i \times k_h \times k_w$$

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Convolutional Layers: Channels

- How to integrate multiple channels?
 - Have a kernel for each channel, and then sum results over channels

$$\mathbf{X} : c_i \times n_h \times n_w$$

$$\mathbf{W} : c_i \times k_h \times k_w$$

$$\mathbf{Y} : m_h \times m_w$$

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Convolutional Layers: Channels

- How to integrate multiple channels?
 - Have a kernel for each channel, and then sum results over channels

$$\mathbf{X} : c_i \times n_h \times n_w$$

$$\mathbf{W} : c_i \times k_h \times k_w$$

$$\mathbf{Y} : m_h \times m_w$$

$$\mathbf{Y} = \sum_{i=0}^{c_i} \mathbf{X}_{i,:,:} \star \mathbf{W}_{i,:,:}$$

“Slices” of tensors

Tensor: generalization of matrix to higher dimensions

Multiple Output Channels

- No matter how many inputs channels, so far we always get single output channel
- We can have **multiple 3-D kernels**, each one generates an output channel

Multiple Output Channels

- No matter how many inputs channels, so far we always get single output channel
- We can have **multiple 3-D kernels**, each one generates an output channel
- Input
- Kernels
- Output

Multiple Output Channels

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- Input $\mathbf{X} : c_i \times n_h \times n_w$
- Kernels
- Output

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- We can have **multiple 3-D kernels**, each one generates an output channel
- Input $\mathbf{X} : c_i \times n_h \times n_w$
- Kernels $\mathbf{W} : c_o \times c_i \times k_h \times k_w$
- Output

Multiple Output Channels

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- Kernels $\mathbf{W} : c_o \times c_i \times k_h \times k_w$
- Output $\mathbf{Y} : c_o \times m_h \times m_w$

Multiple Output Channels

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- We can have **multiple 3-D kernels**, each one generates an output channel

• Input $\mathbf{X} : c_i \times n_h \times n_w$

• Kernels $\mathbf{W} : c_o \times c_i \times k_h \times k_w$

• Output $\mathbf{Y} : c_o \times m_h \times m_w$

$$\mathbf{Y}_{i,:,:} = \mathbf{X} \star \mathbf{W}_{i,:,:,:}$$

Multiple Output Channels

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$$\mathbf{Y}_{i,:,:} = \mathbf{X} \star \mathbf{W}_{i,:,:,:}$$

for $i = 1, \dots, c_o$

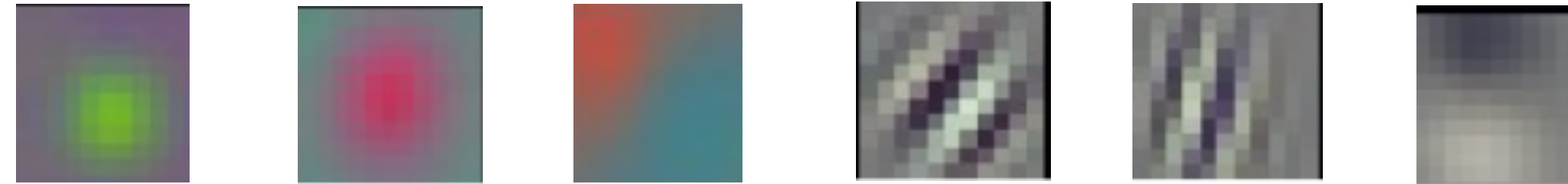
Multiple Input/Output Channels

- Each 3-D kernel may recognize a particular pattern



Multiple Input/Output Channels

- Each 3-D kernel may recognize a particular pattern



(Gabor filters)

Q3. Suppose we want to perform convolution on an RGB image of size 224×224 (no padding) with 64 kernels, each with height 3 and width 3. Stride = 1. Which is a reasonable estimate of the total number of scalar multiplications involved in this operation (without considering any optimization in matrix multiplication)?

A. $64 \times 3 \times 3 \times 222 \times 222$

B. $64 \times 3 \times 3 \times 222$

C. $3 \times 3 \times 222 \times 222$

D. $64 \times 3 \times 3 \times 3 \times 222 \times 222$

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C. $3 \times 3 \times 222 \times 222$

D. $64 \times 3 \times 3 \times 3 \times 222 \times 222$

For each kernel, we slide the window to 222×222 different locations. For each location, the number of multiplication is $3 \times 3 \times 3$. So in total $64 \times 3 \times 3 \times 3 \times 222 \times 222$

Q4. Suppose we want to perform convolution on a RGB image of size 224×224 (no padding) with 64 kernels, each with height 3 and width 3. Stride = 1. The convolution layer has bias parameters. Which is a reasonable estimate of the total number of learnable parameters?

A. $64 \times 222 \times 222$

B. $64 \times 3 \times 3 \times 222$

C. $3 \times 3 \times 3 \times 64$

D. $(3 \times 3 \times 3 + 1) \times 64$

Q4. Suppose we want to perform convolution on a RGB image of size 224×224 (no padding) with 64 kernels, each with height 3 and width 3. Stride = 1. The convolution layer has bias parameters. Which is a reasonable estimate of the total number of learnable parameters?

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Q4. Suppose we want to perform convolution on a RGB image of size 224×224 (no padding) with 64 kernels, each with height 3 and width 3. Stride = 1. The convolution layer has bias parameters. Which is a reasonable estimate of the total number of learnable parameters?

A. $64 \times 222 \times 222$

B. $64 \times 3 \times 3 \times 222$

C. $3 \times 3 \times 3 \times 64$

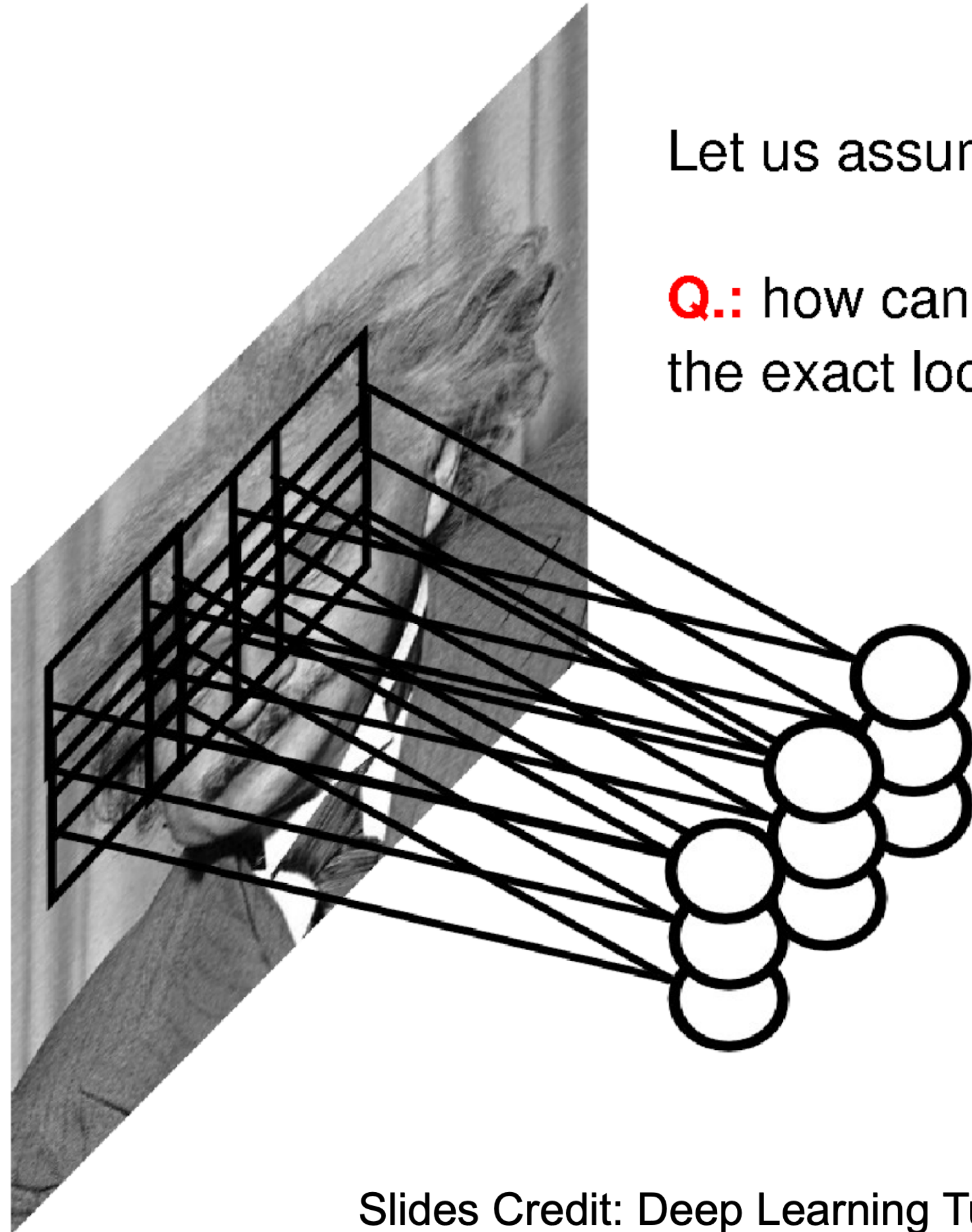
D. $(3 \times 3 \times 3 + 1) \times 64$

Each kernel is 3D kernel across 3 input channels, so has $3 \times 3 \times 3$ parameters. Each kernel has 1 bias parameter. So in total $(3 \times 3 \times 3 + 1) \times 64$



Pooling Layer

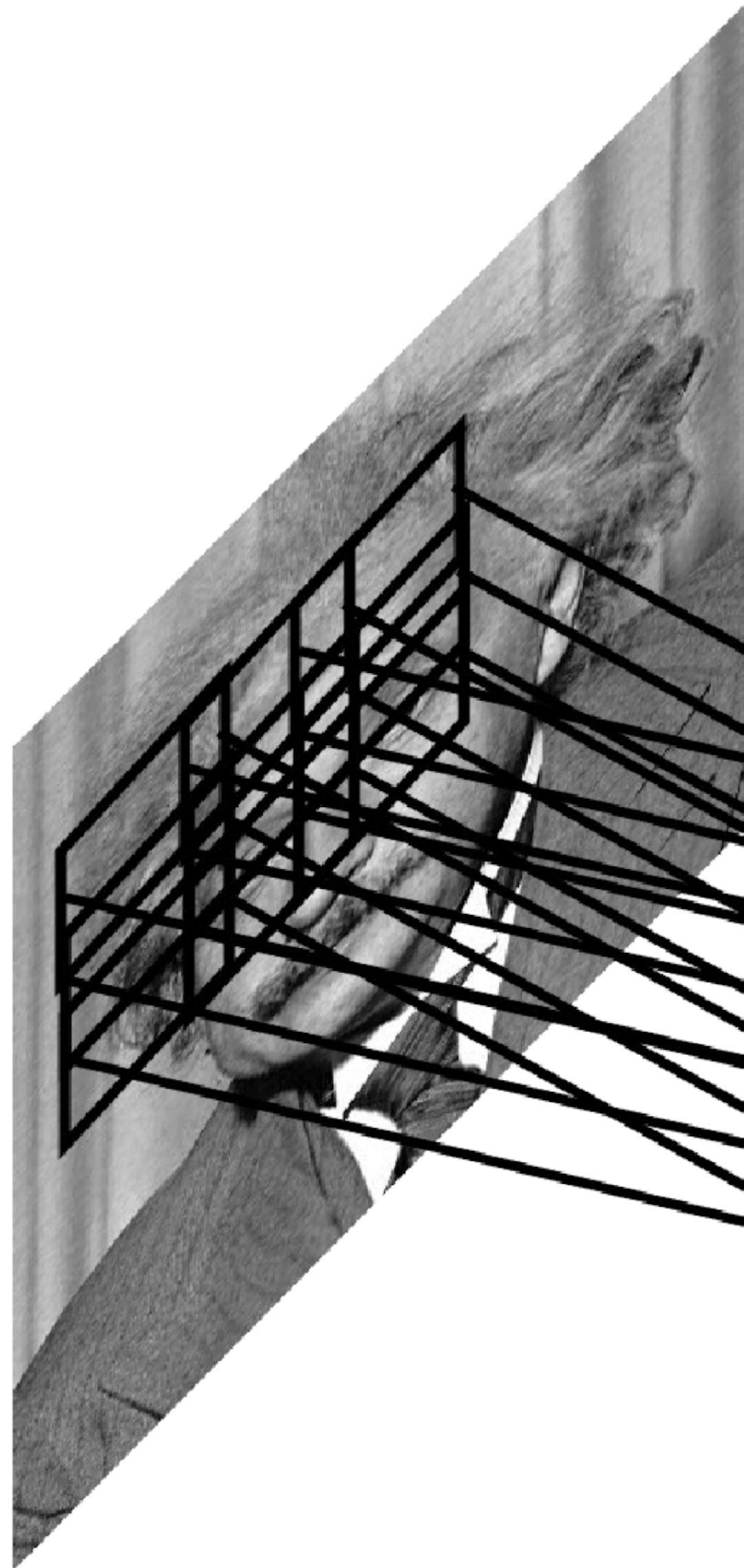
Pooling



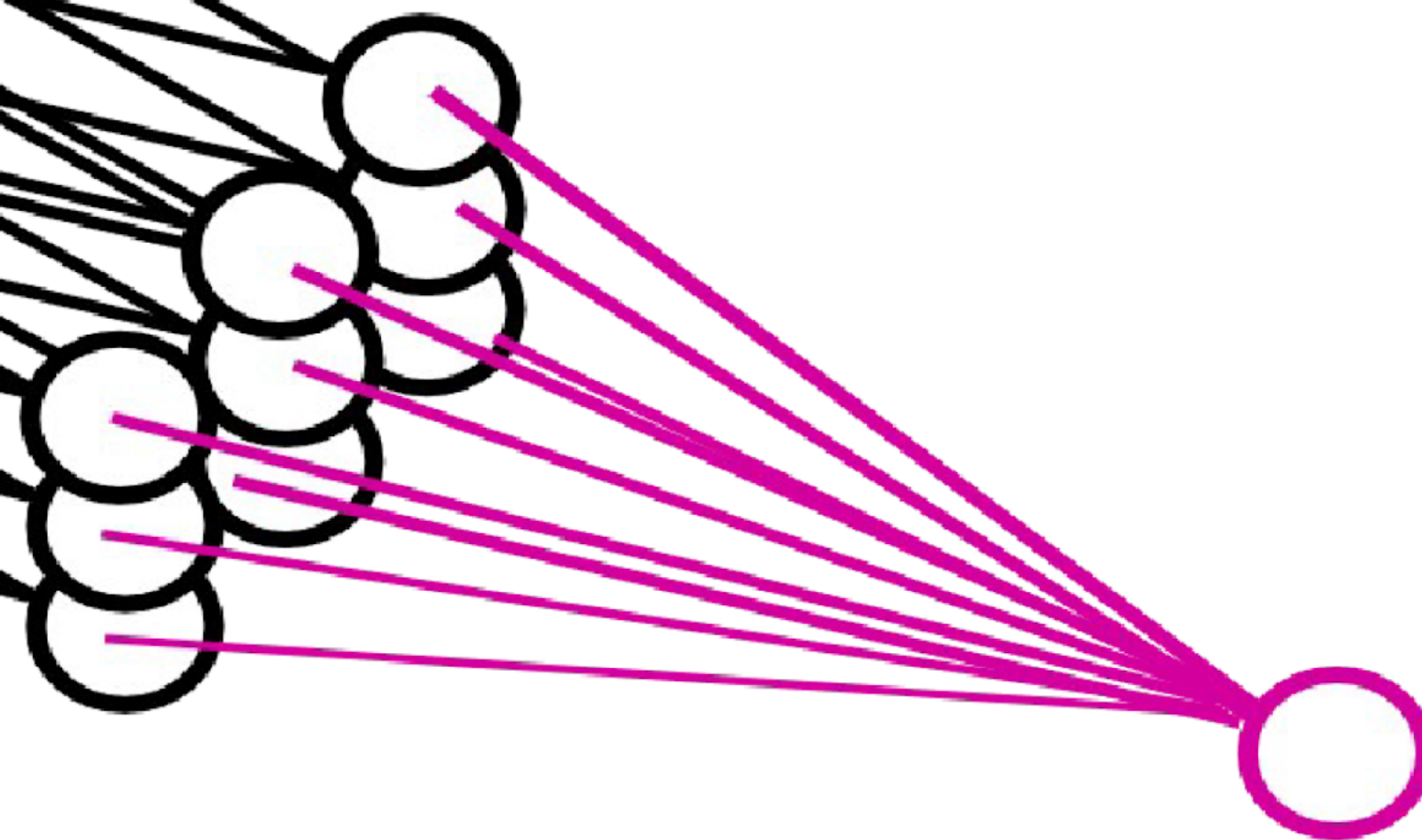
Let us assume filter is an “eye” detector.

Q.: how can we make the detection robust to the exact location of the eye?

Pooling

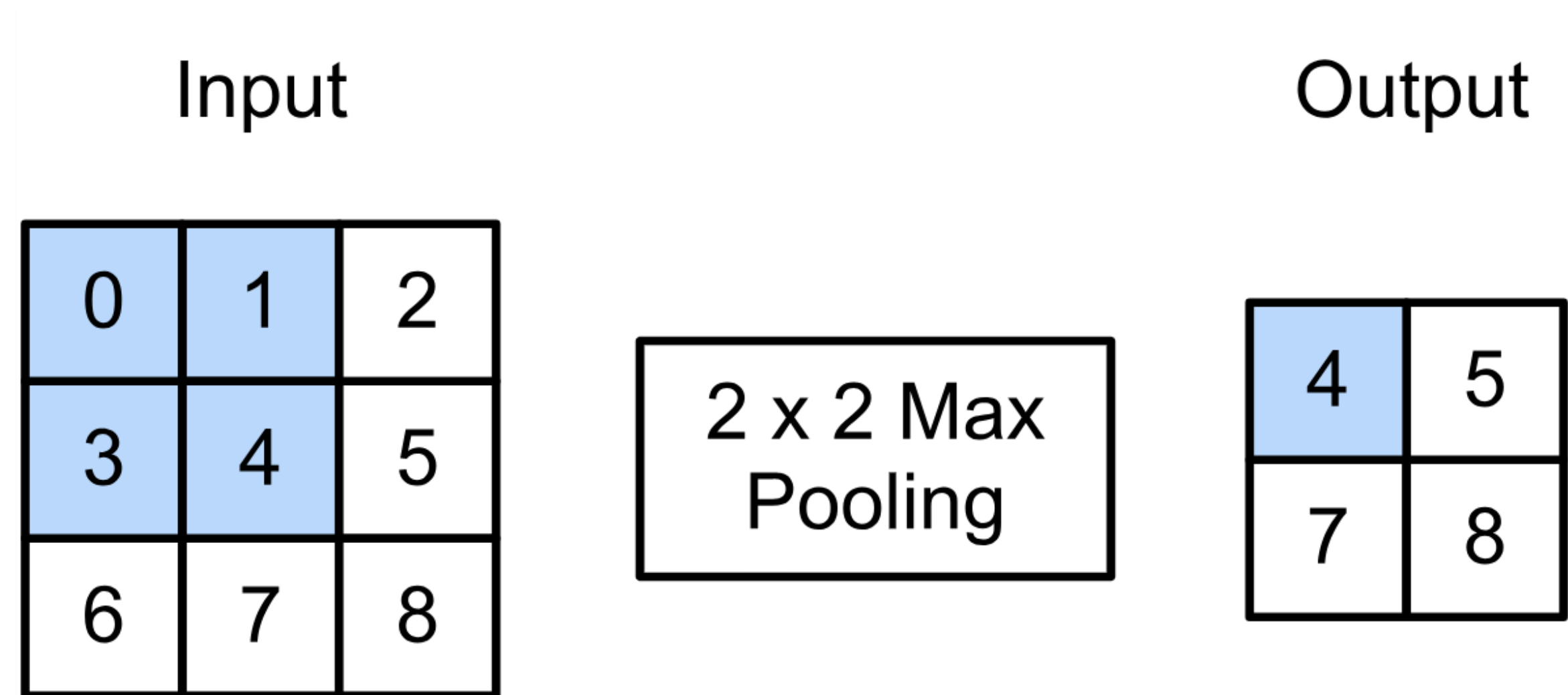


By “pooling” (e.g., taking max) filter responses at different locations we gain robustness to the exact spatial location of features.



2-D Max Pooling

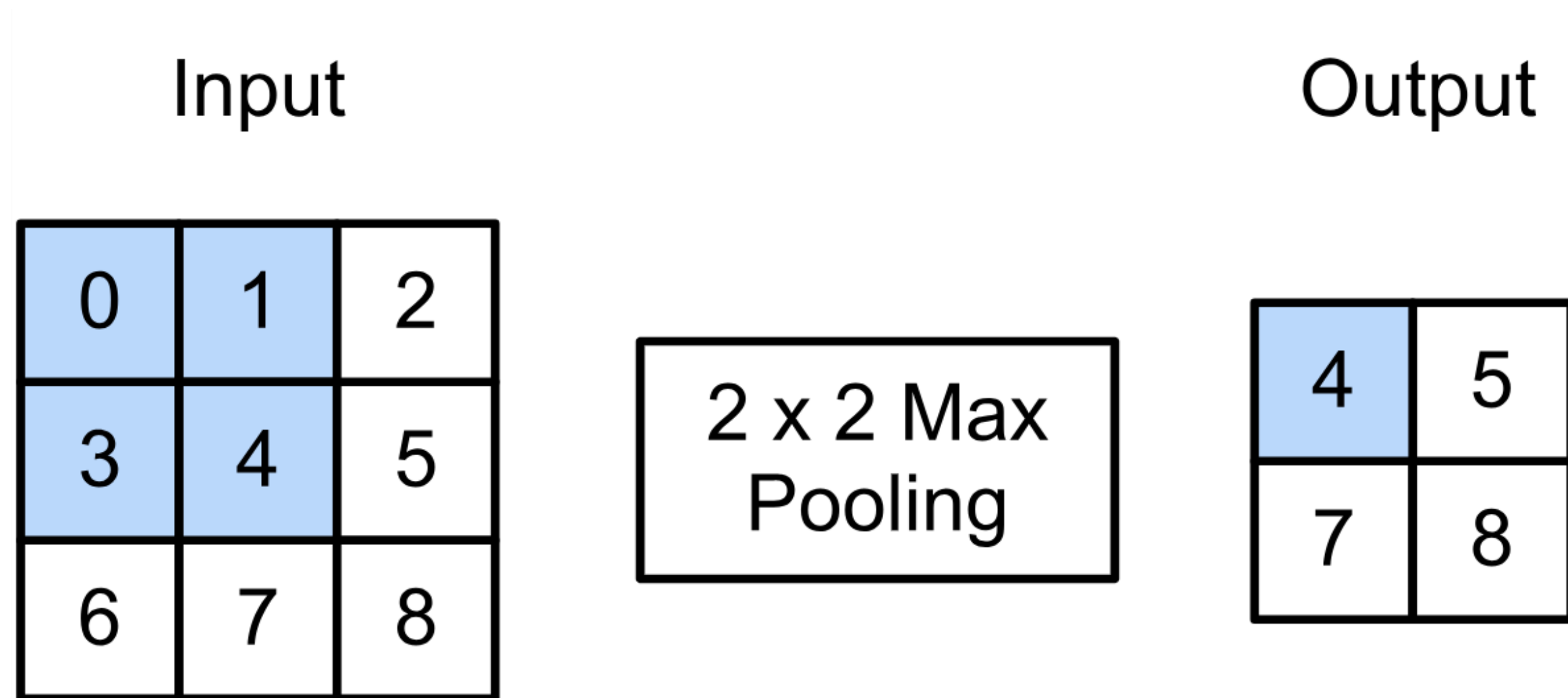
- Returns the maximal value in the sliding window



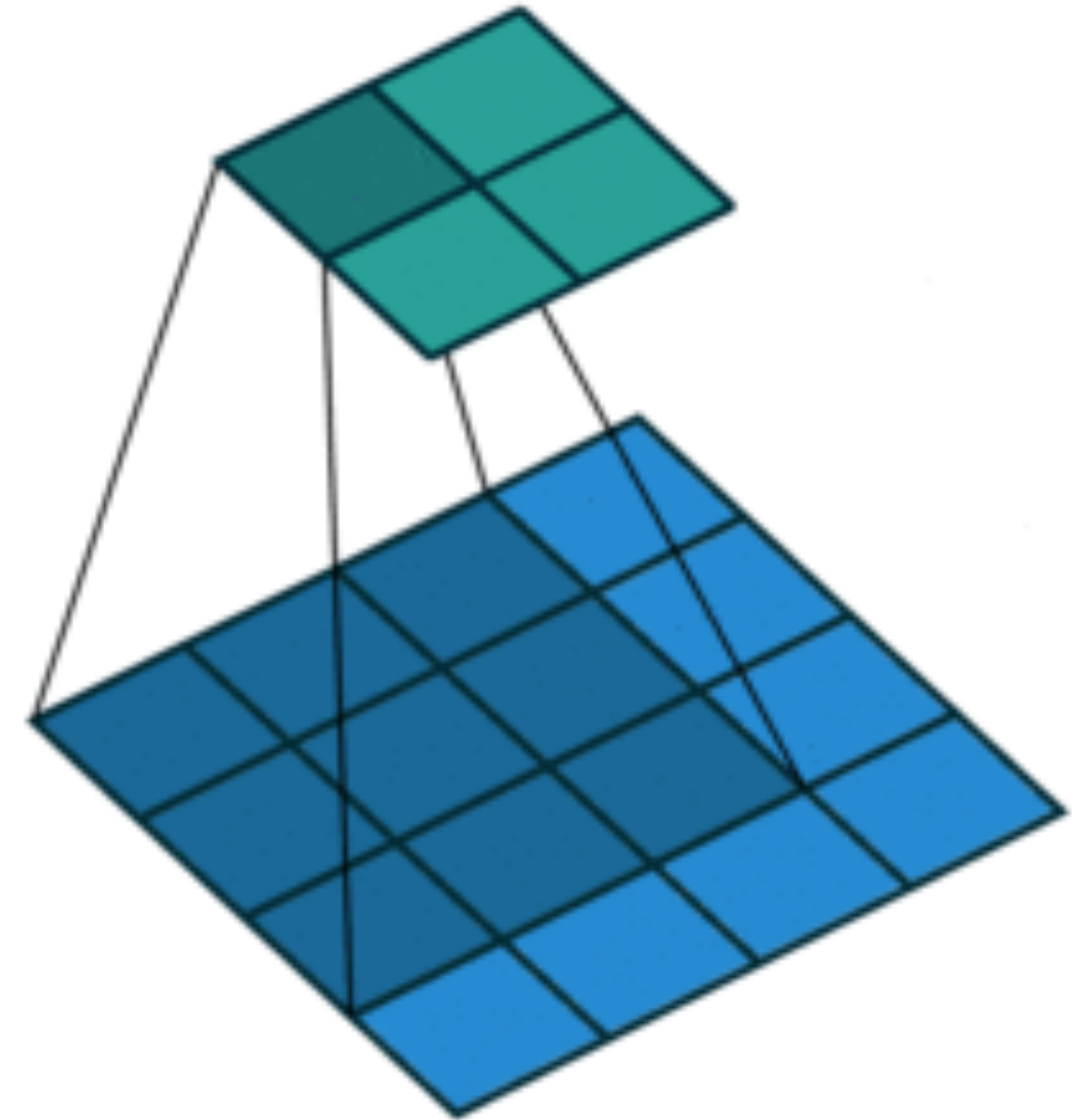
$$\max(0, 1, 3, 4) = 4$$

2-D Max Pooling

- Returns the maximal value in the sliding window

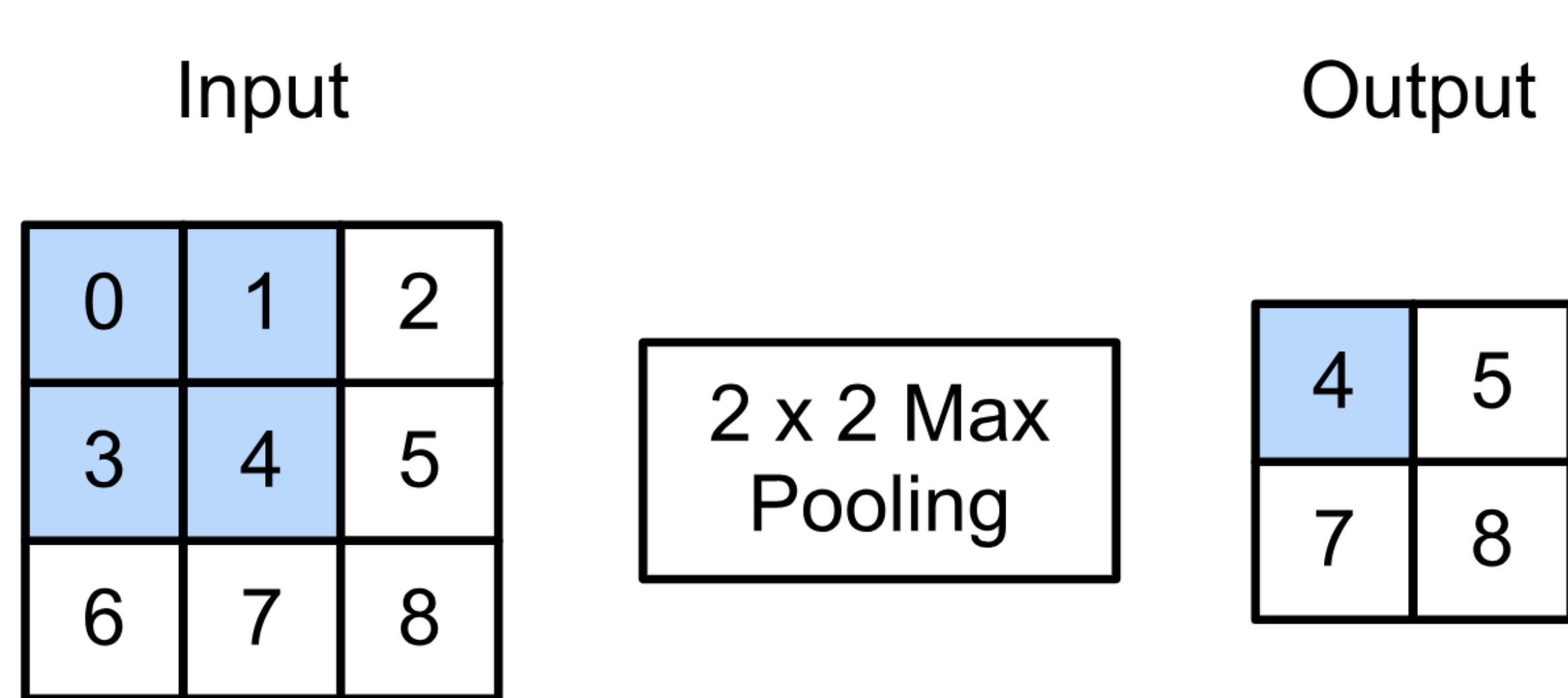


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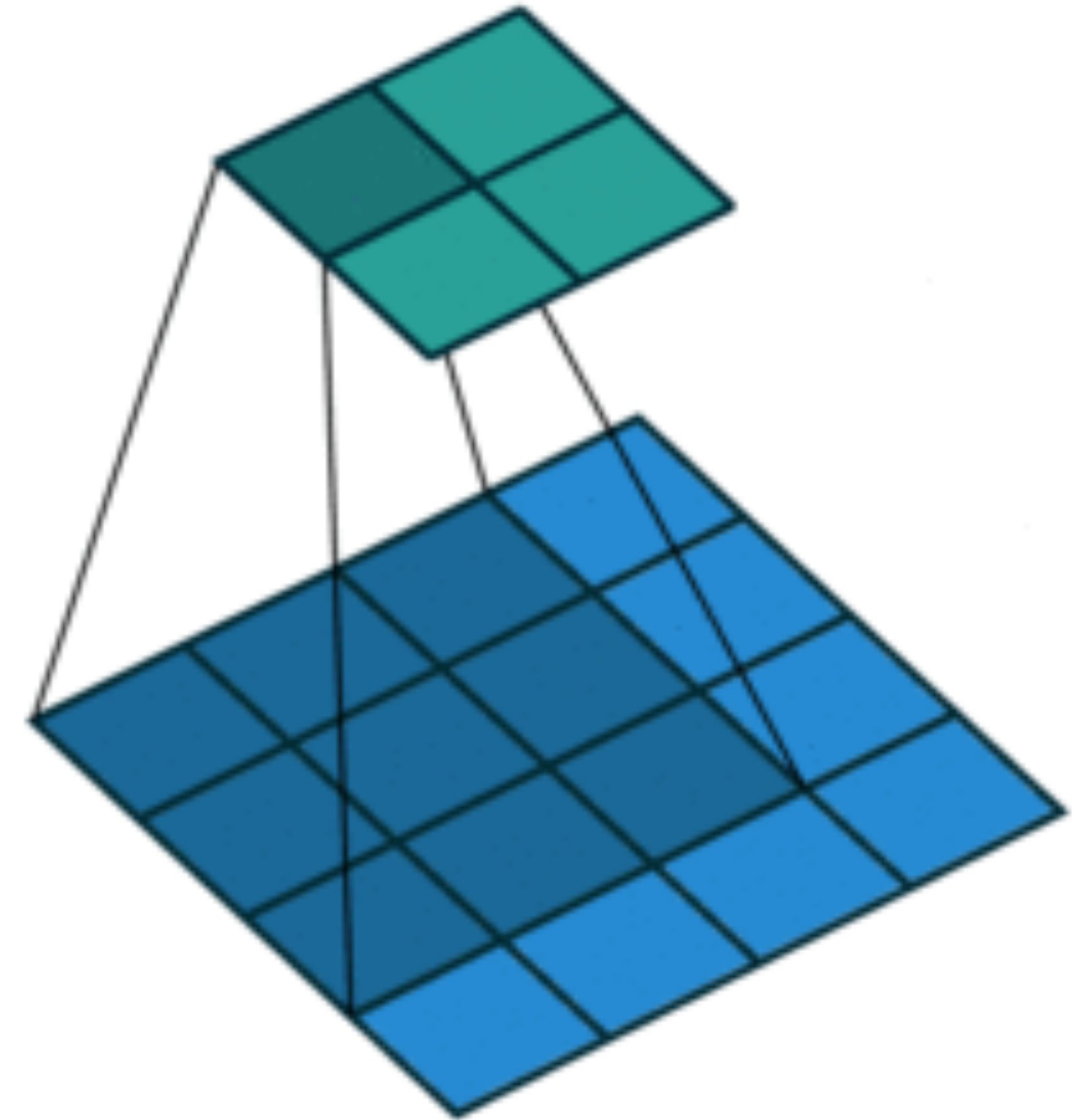


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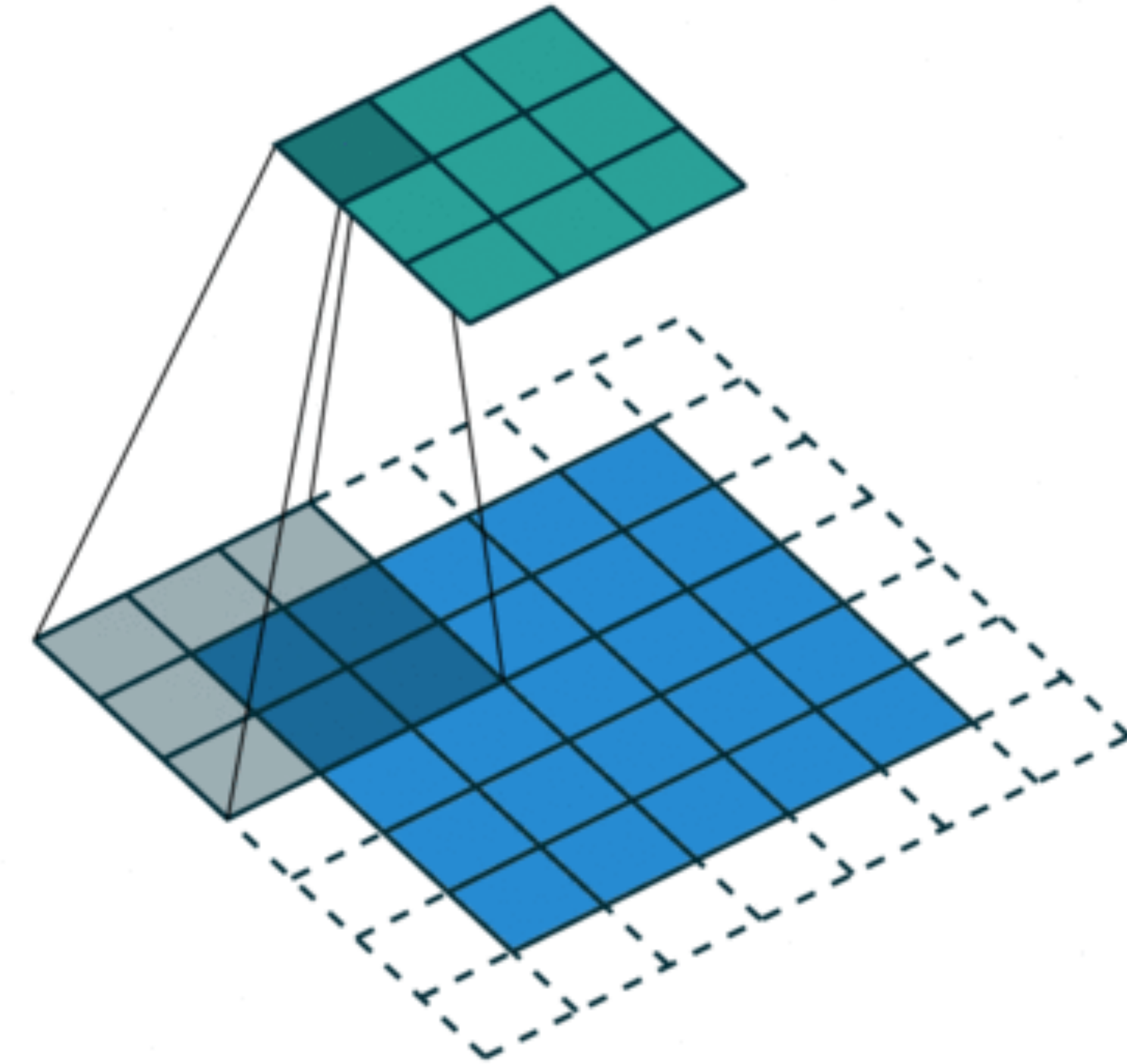
Padding, Stride, and Multiple Channels

- Pooling layers have similar padding and stride as convolutional layers
- No learnable parameters
- Apply pooling for each input channel to obtain the corresponding output channel

#output channels = #input channels

Padding, Stride, and Multiple Channels

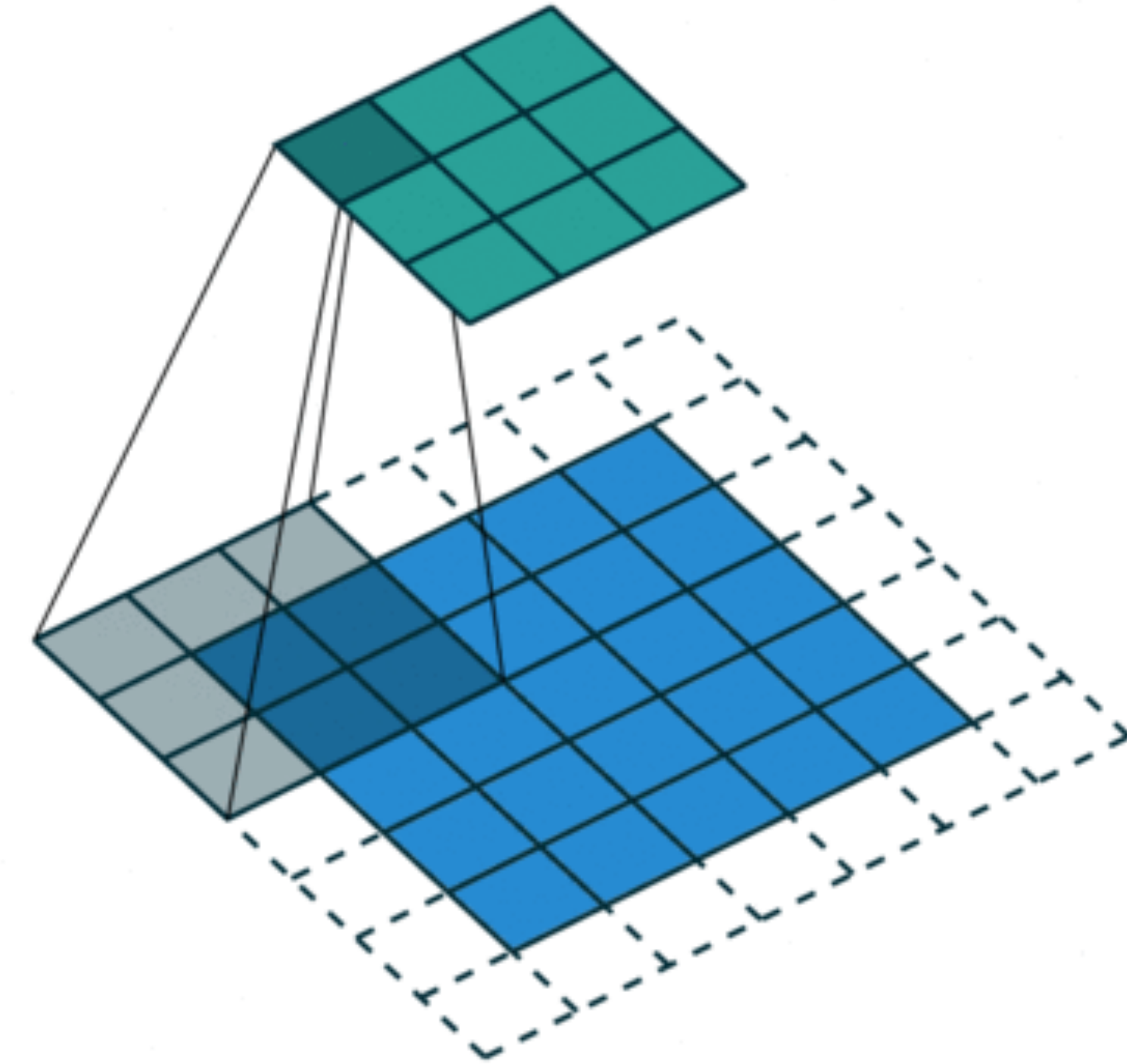
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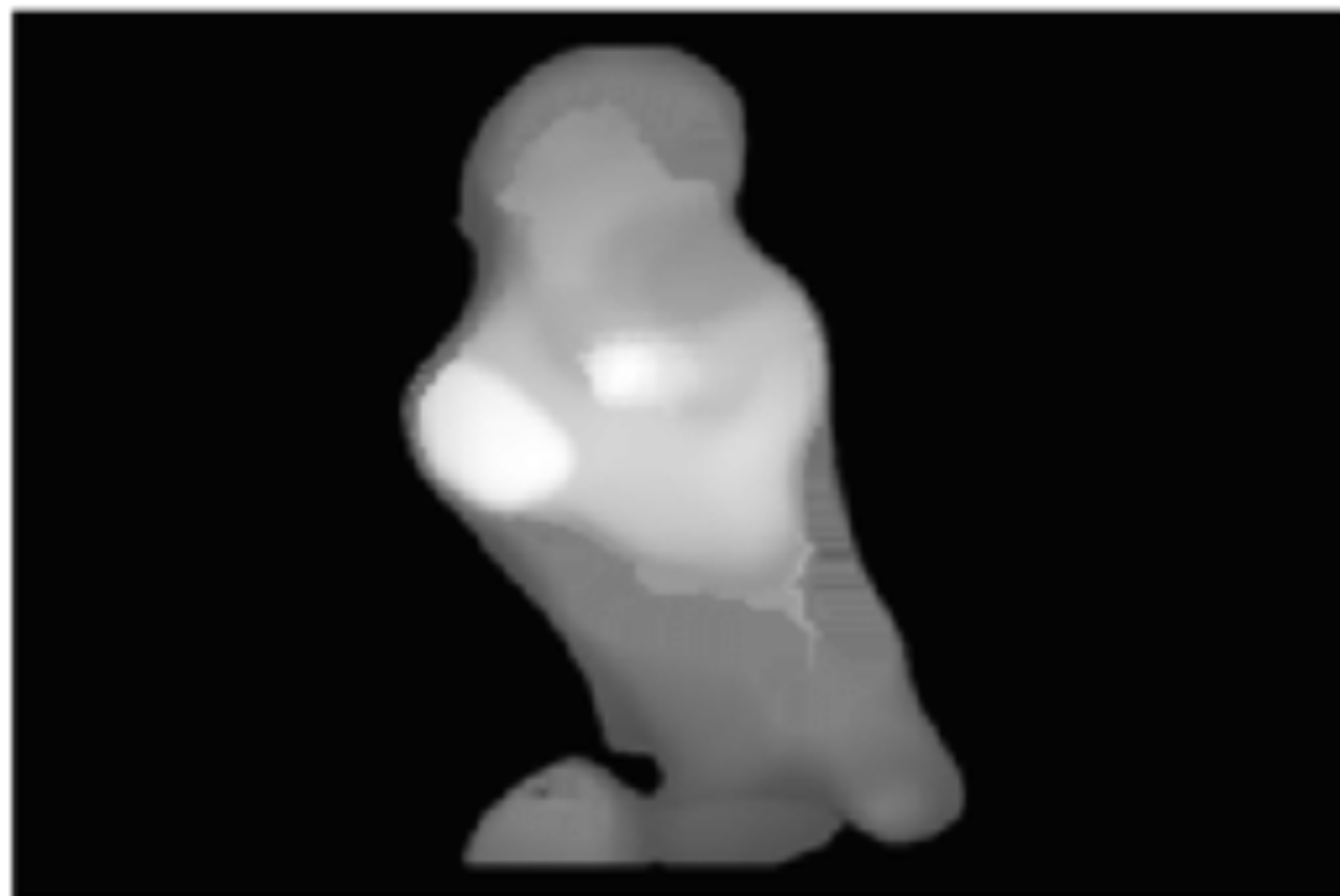


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Average Pooling

- Max pooling: the strongest pattern signal in a window
- Average pooling: replace max with mean in max pooling
 - The average signal strength in a window

Max pooling



Average pooling



Q5. Suppose we want to perform 2x2 average pooling on the following single channel feature map of size 4x4 (no padding), and stride = 2. What is the output?

A.

20	30
70	90

B.

16	8
20	25

C.

20	30
20	25

D.

12	2
70	5

12	20	30	0
20	12	2	0
0	70	5	2
8	2	90	3

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Q6. What is the output if we replace average pooling with 2 x 2 max pooling (other settings are the same)?

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Summary

Summary

- Intro of convolutional computations
 - 2D convolution
 - Padding, stride
 - Multiple input and output channels
 - Pooling



Acknowledgement:

Some of the slides in these lectures have been adapted from materials developed by Alex Smola and Mu Li:

<https://courses.d21.ai/berkeley-stat-157/index.html>