

**CS/ECE 252: INTRODUCTION TO COMPUTER ENGINEERING  
COMPUTER SCIENCES DEPARTMENT  
UNIVERSITY OF WISCONSIN – MADISON**

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Midterm Examination 1  
In Class (50 minutes)  
Monday, October 1, 2007  
Weight: 15%

**CLOSED BOOK, NOTE, CALCULATOR, PHONE, & COMPUTER.**

The exam has **four** two-sided pages.

Plan your time carefully, since some problems are longer than others.

NAME: \_\_\_\_\_

SECTION: \_\_\_\_\_

ID# \_\_\_\_\_

<b>Problem Number</b>	<b>Maximum Points</b>	<b>Graded By</b>
1	4	EH
2	3	EH
3	3	NEJ
4	4	NEJ
5	4	SR
6	4	SJ
7	4	GJ
8	4	SJ/SR/NEJ
Total	30	

**Problem 1 (4 points)**

a) What is the largest (most positive) integer that can be represented as an *unsigned* integer using 13 bits?

$$1111111111111_2 = (2^{13} - 1)_d = 8191_d$$

Full credit for any one of  $(2^{13} - 1)_d$  or  $8191_d$

b) What is the largest (most positive) integer that can be represented as a *two's complement* integer using 13 bits?

$$0111111111111_2 = (2^{12} - 1)_d = 4095_d$$

Full credit for any one of  $(2^{12} - 1)_d$  or  $4095_d$

**Problem 2 (3 points)**

Consider bitwise logical operations: Compute (1101 AND 0111) OR (NOT 0011)

$$(1101 \text{ AND } 0111) \text{ OR } (\text{NOT } 0011) = (0101) \text{ OR } (1100) = 1101$$

**Problem 3 (3 points)**

Convert the number **-84** (base ten) into two's complement representation with 8 bits.

$$+84_{\text{d}} = 01010100_{\text{b}}$$

$$-84_{\text{d}} = 10101011_{\text{b}} + 1_{\text{b}} = 10101100_{\text{b}}$$

**Problem 4 (4 points)**

Consider the 8-bit binary bit pattern **10010010**. What is its decimal (base ten) value if the bit pattern is interpreted as:

- a) An unsigned integer?

$$10010010_{\text{b}} = 128 + 16 + 2 = 146_{\text{d}}$$

- b) A two's complement integer?

$$10010010_{\text{b}} = -(01101101 + 1)_{\text{b}} = -(01101110)_{\text{b}} = -(64 + 32 + 8 + 4 + 2)_{\text{d}} = -110_{\text{d}}$$

**Problem 5 (4 points)**

- a) Add the following 5-bit two's complement binary numbers: **01111 + 01101**. Express your answer in 5-bit two's complement. Please indicate if there was an overflow.

**11100 - There is overflow.**

- b) Add the following 5-bit two's complement binary numbers: **11110 + 01111**. Express your answer in 5-bit two's complement. Please indicate if there was an overflow.

**01101 - There is no overflow.**

**Problem 6 (4 points)**

- a) Convert the ASCII string "**F4n**" into binary. (See attached ASCII table. Only convert the characters between the quotation marks.)

**"F4n" = 0x46347E = 01000110 00110100 01111110 (00000000 at end OK)**

- b) Convert the binary value **0010010001101011** into an ASCII string.

**0010010001101011 = 0x246B = "\$k"**

**Problem 7 (4 points)**

a) What is the base ten (decimal) value represented by binary 110.101 ?

$$\begin{aligned} 110.101 &= 1 \times (2^2) + 1 \times (2^1) + 0 \times (2^0) + 1 \times (2^{-1}) + 0 \times (2^{-2}) + 1 \times (2^{-3}) \\ &= 4 + 2 + 0 + 1/2 + 0 + 1/8 \\ &= 6 \frac{5}{8} \text{ (or } 53/8, 6.625, \text{ etc.)} \end{aligned}$$

b) The bits for an IEEE floating point number are allocated as follows:

sign (1 bit)	exponent (8 bits)	fraction (23 bits)
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$$\text{where } N = (-1)^S \times 1.\text{fraction} \times 2^{\text{exponent}-127}$$

Convert 1 10000001 110000000000000000000000 to decimal.

$$N = (-1)^1 \times (1.11)_b \times 2^{129-127} = -1 \times (1.11)_b \times 2^2 = -(111)_b = -7$$

**Problem 8 - Circle the correct answer (2 points each)**

**I. Which of the following is a universal computing device?**

- a. A 16-button(0-9, period, =/+/-/x/÷) calculator
- b. A laptop computer running Windows XP
- c. An ultrafast supercomputer
- d. All of the above
- e. **Both (b) and (c)**

**II. When referring to an algorithm, definiteness means:**

- a. **Each step must be precisely defined**
- b. The algorithm's variables must not overflow a fixed number of bits
- c. The number of unknowns and equations is the same
- d. None of the above

## ASCII Table

<i>Character</i>	<i>Hex</i>	<i>Character</i>	<i>Hex</i>	<i>Character</i>	<i>Hex</i>	<i>Character</i>	<i>Hex</i>
nul	00	sp	20	@	40	`	60
soh	01	!	21	A	41	a	61
stx	02	"	22	B	42	b	62
etx	03	#	23	C	43	c	63
eot	04	\$	24	D	44	d	64
enq	05	%	25	E	45	e	65
ack	06	&	26	F	46	f	66
bel	07	'	27	G	47	g	67
bs	08	(	28	H	48	h	68
ht	09	)	29	I	49	i	69
lf	0A	*	2A	J	4A	j	6A
vt	0B	+	2B	K	4B	k	6B
ff	0C	,	2C	L	4C	l	6C
cr	0D	-	2D	M	4D	m	6D
so	0E	.	2E	N	4E	n	6E
si	0F	/	2F	O	4F	o	6F
dle	10	0	30	P	50	p	70
dc1	11	1	31	Q	51	q	71
dc2	12	2	32	R	52	r	72
dc3	13	3	33	S	53	s	73
dc4	14	4	34	T	54	t	74
nak	15	5	35	U	55	u	75
syn	16	6	36	V	56	v	76
etb	17	7	37	W	57	w	77
can	18	8	38	X	58	x	78
em	19	9	39	Y	59	y	79
sub	1A	:	3A	Z	5A	z	7A
esc	1B	;	3B	[	5B	{	7B
fs	1C	<	3C	\	5C		7C
gs	1D	=	3D	]	5D	}	7D
rs	1E	>	3E	^	5E	~	7E
us	1F	?	3F	_	5F	del	7F

**Scratch Sheet (in case you need additional space for some of your answers)**