

Introduction to Computer Networks

# Computer Networks: Performance Analysis

<https://pages.cs.wisc.edu/~mgliu/CS640/S25/index.html>

Ming Liu

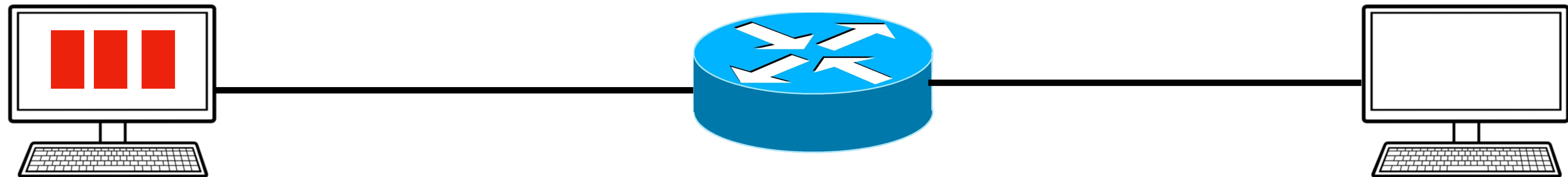
mgliu@cs.wisc.edu

# Outline

- Last
  - Computer networks: hardware infrastructure
  - Computer networks: software system
- Today
  - Delay
  - Throughput
  - RTT and BDP
- Announcements
  - Lab1 will be released this Thursday
  - No class on Thursday

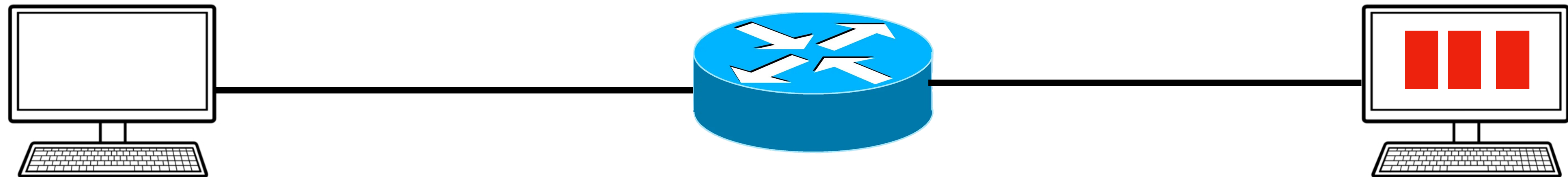
# Packet-Switched Networks

- Packet communication path
  - Host 1 → Router A → Router B → ... → Host 2

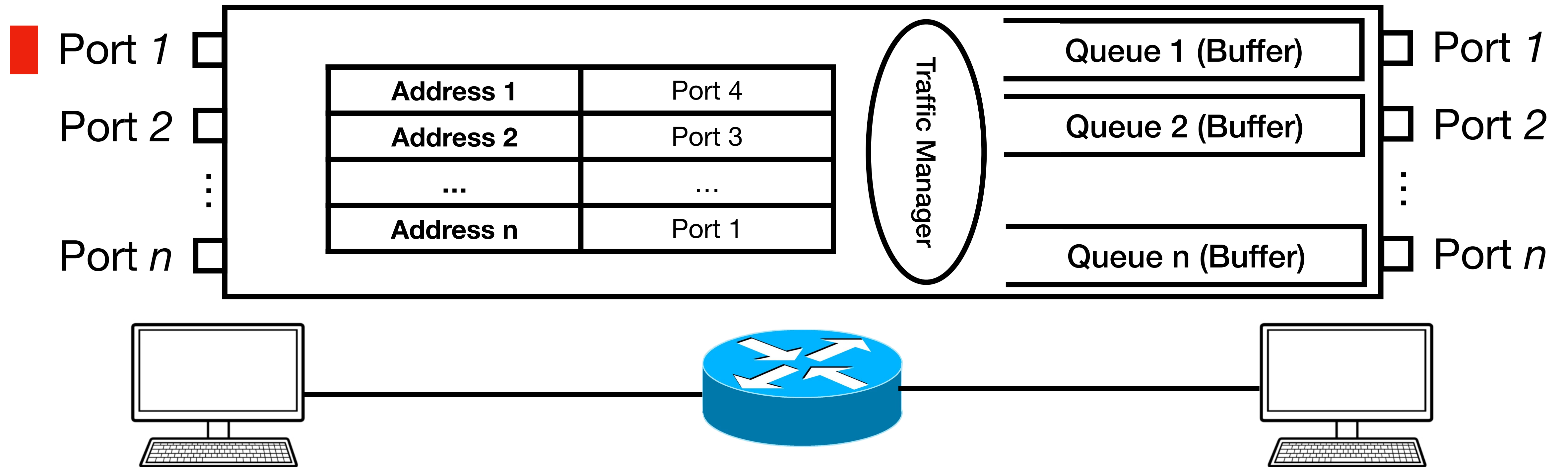


# Packet-Switched Networks

- Packet communication path
  - Host 1 → Router A → Router B → ... → Host 2
- Delay
  - The total amount of time transfers N bits across the packet path
  - Four types of delay

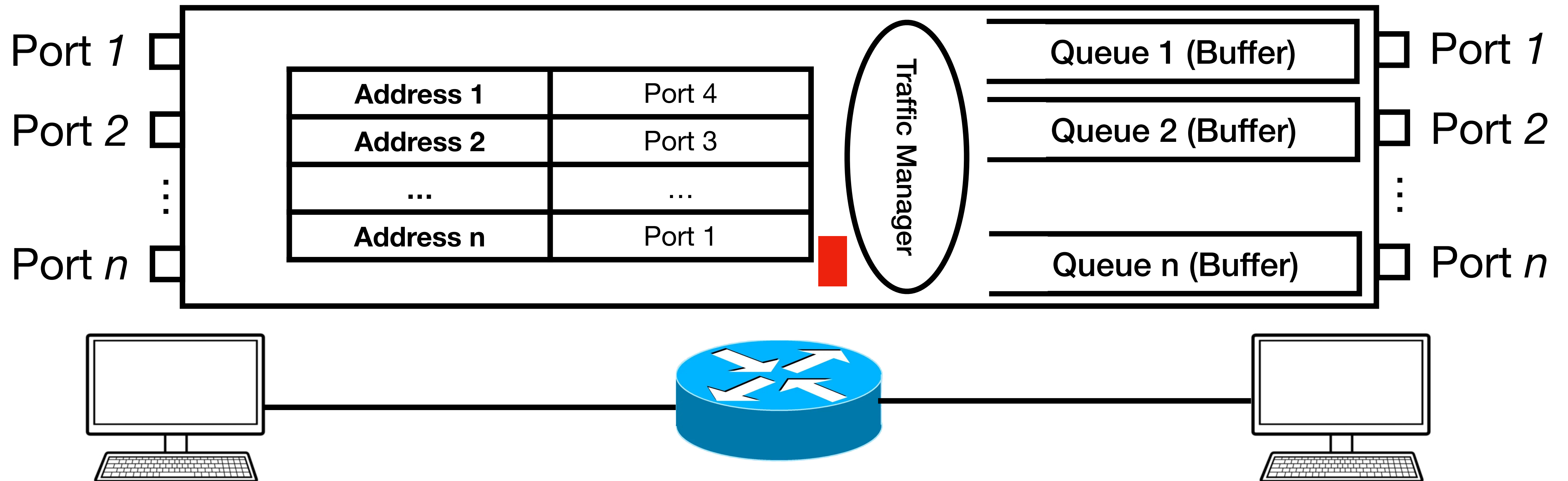


# Processing Delay ( $T_{proc}$ )

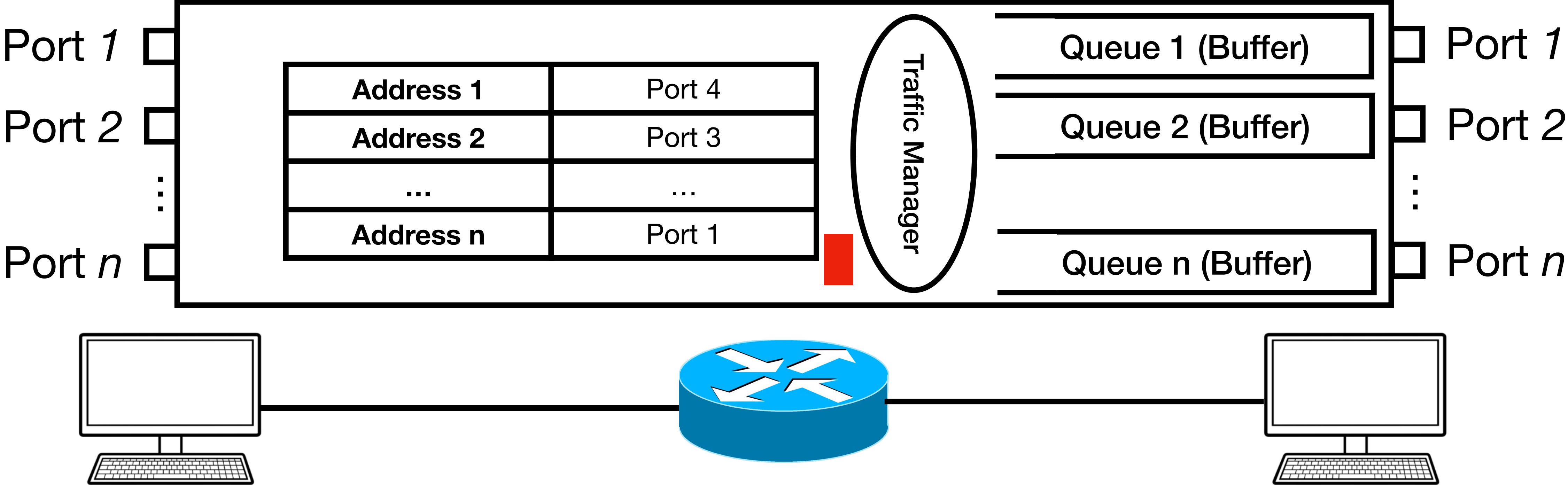


# Processing Delay ( $T_{proc}$ )

- The time required to examine the packet header and determine where to forward
  - Including checking bit-level errors
  - Microsecond

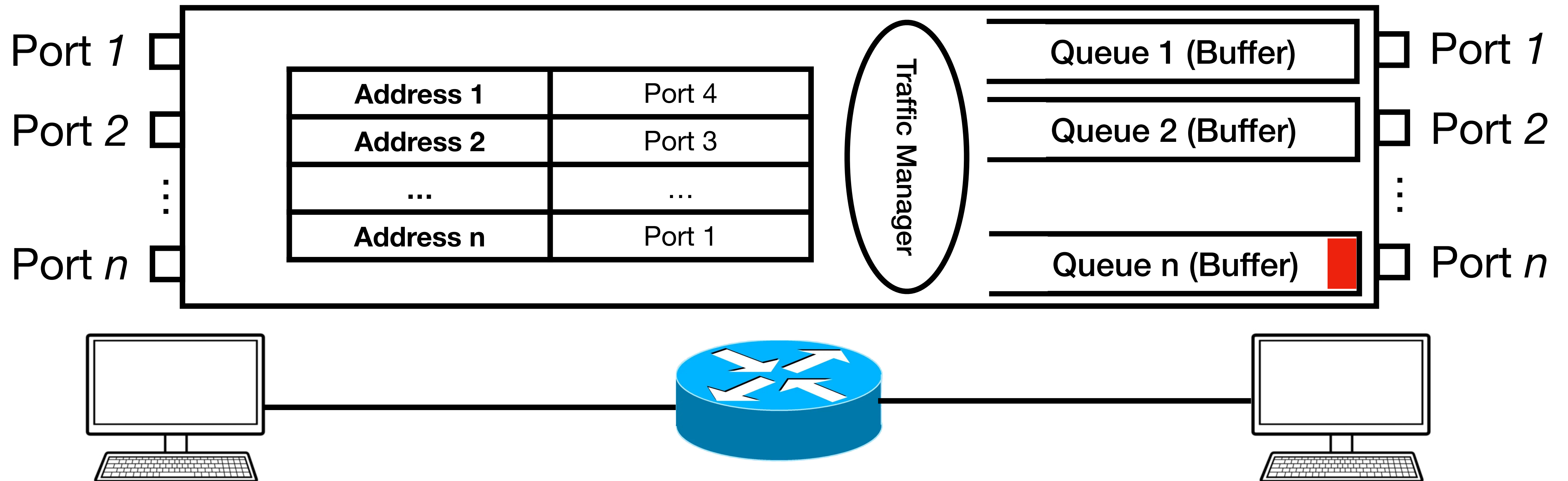


# Queueing Delay ( $T_{\text{queue}}$ )



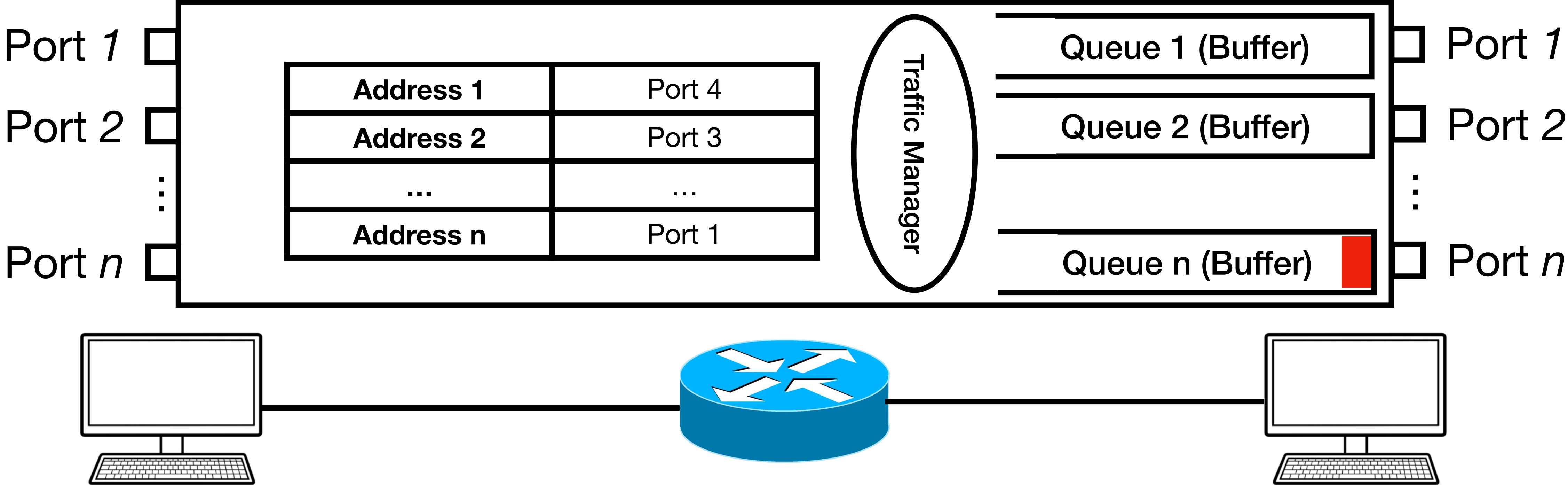
# Queueing Delay ( $T_{\text{queue}}$ )

- The time it takes to wait to be transmitted
  - Depend on the number of earlier-arriving packets
  - Microsecond~Millisecond



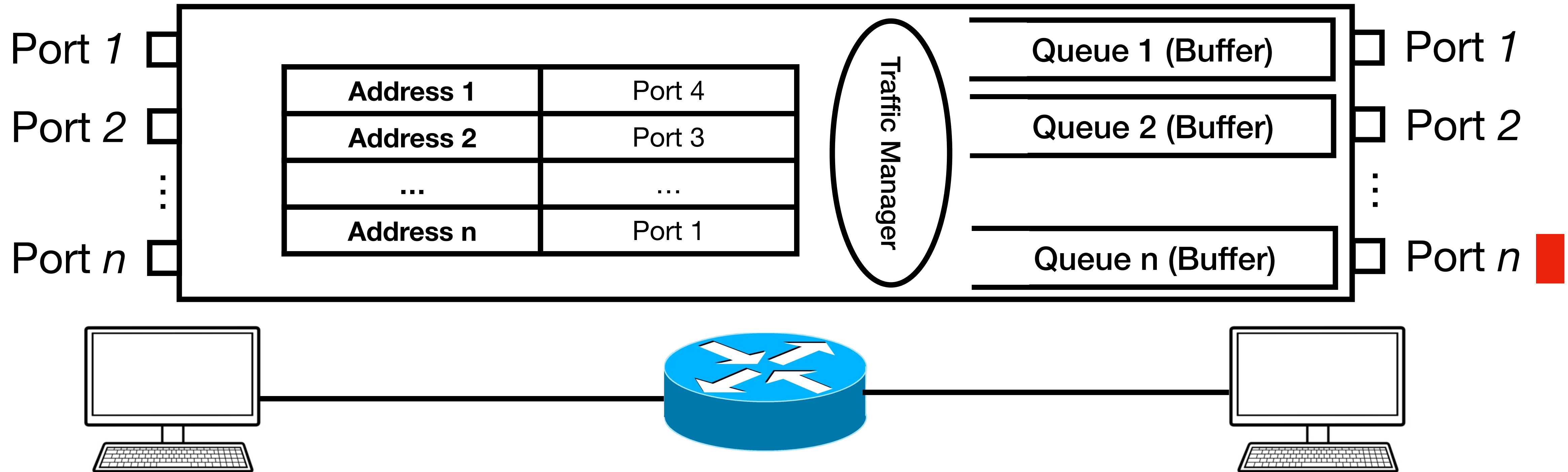


# Transmission Delay ( $T_{trans}$ )



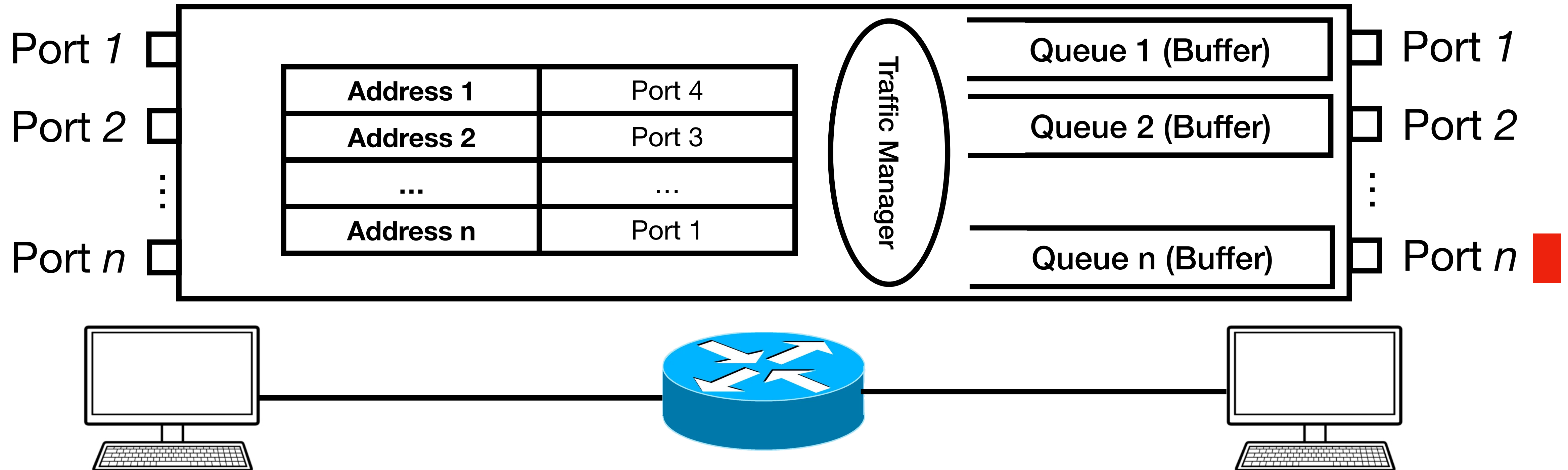
# Transmission Delay ( $T_{trans}$ )

- The time it takes to transmit through the communication ports
  - First-come-first-served manner
  - Depend on the packet length and transmission rate

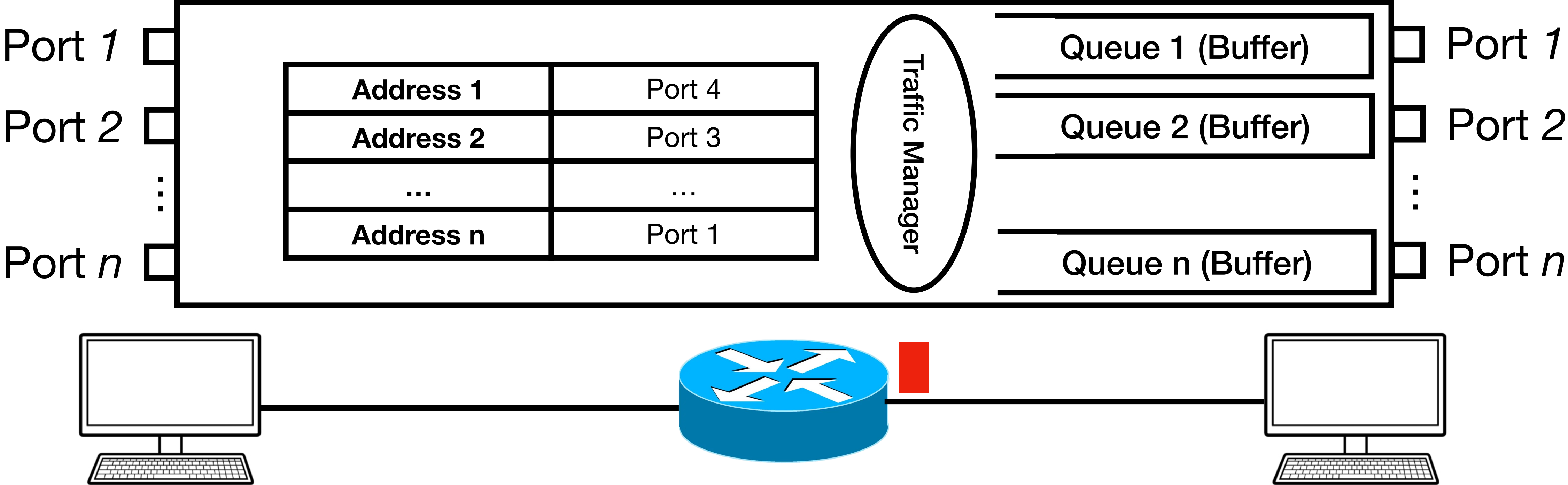


# Transmission Delay Calculation

- Packet length (L bits) and Transmission Rate (R bits/sec)
  - Transmission Delay =  $L/R$
  - Suppose  $L=1\text{KB}$ ,  $R = 10\text{Mbps}/100\text{Mbps}$ , what is the transmission delay?

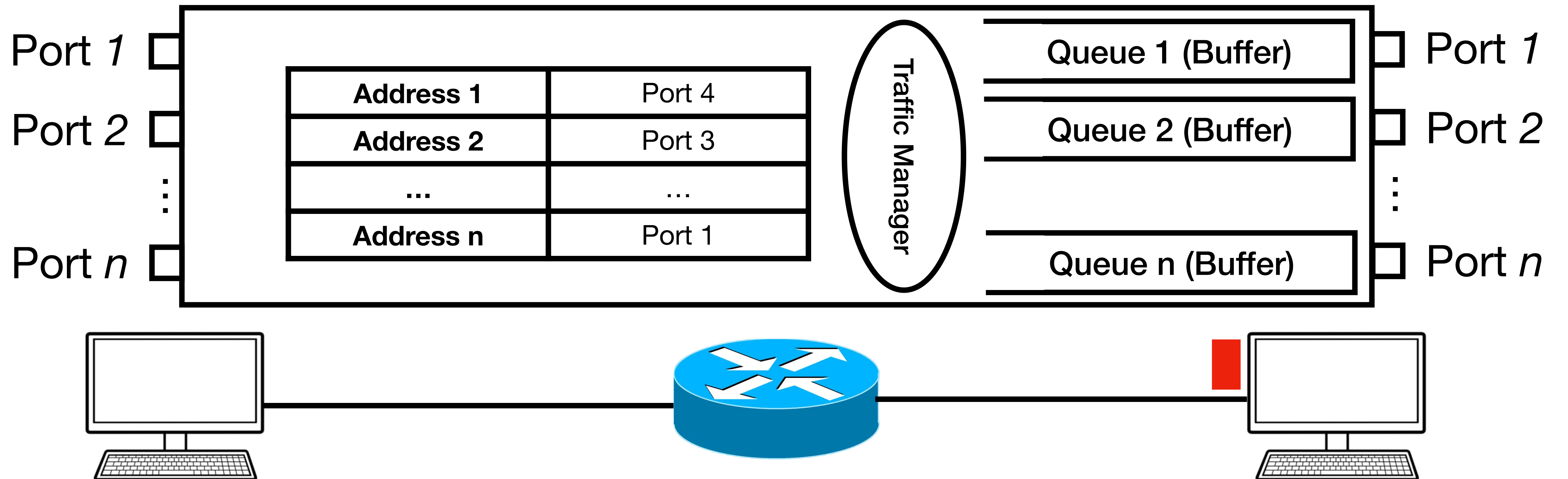


# Propagation Delay ( $T_{prop}$ )



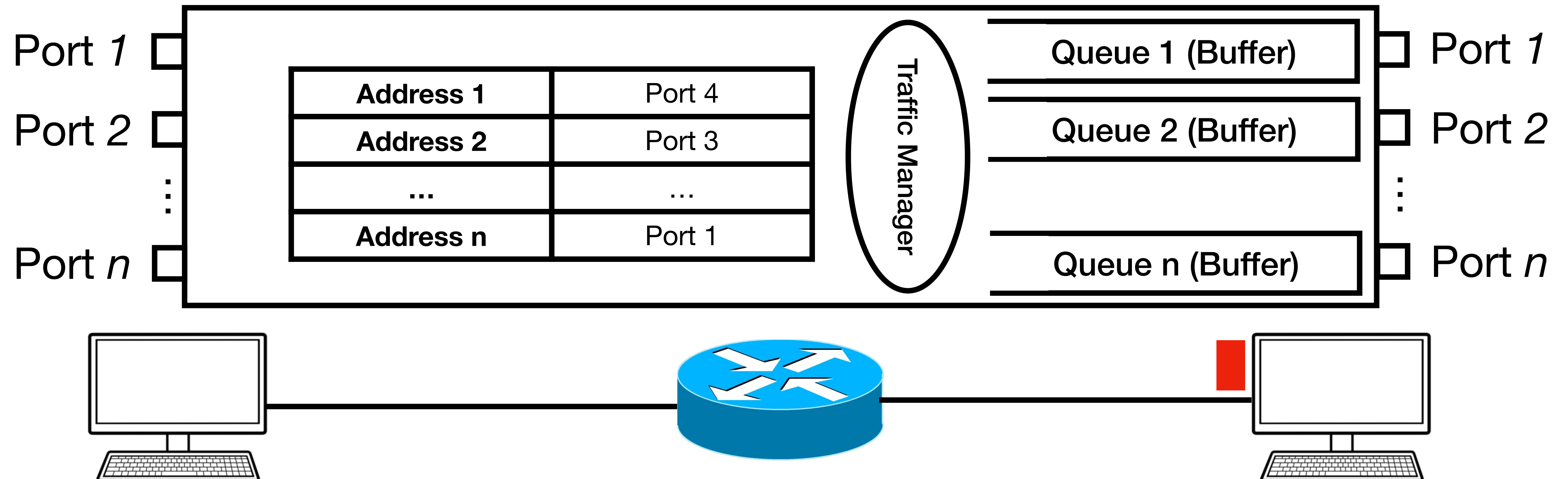
# Propagation Delay ( $T_{prop}$ )

- The time required to propagate over the communication link
  - Depend on the physical media (e.g., fiber optics, copper wire, etc.)
  - $2 \times 10^8 \sim 3 \times 10^8$  meters/second



# Propagation Delay Calculation

- Distance (d) and propagation speed (s)
  - Propagation delay =  $d/s$
  - Distance matters!



# Transmission Delay v.s. Propagation Delay

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  - Distance (d) = 3m and propagation speed (s) =  $3^8$  m/s
  - What is the transmission delay and propagation delay?



# Transmission Delay v.s. Propagation Delay

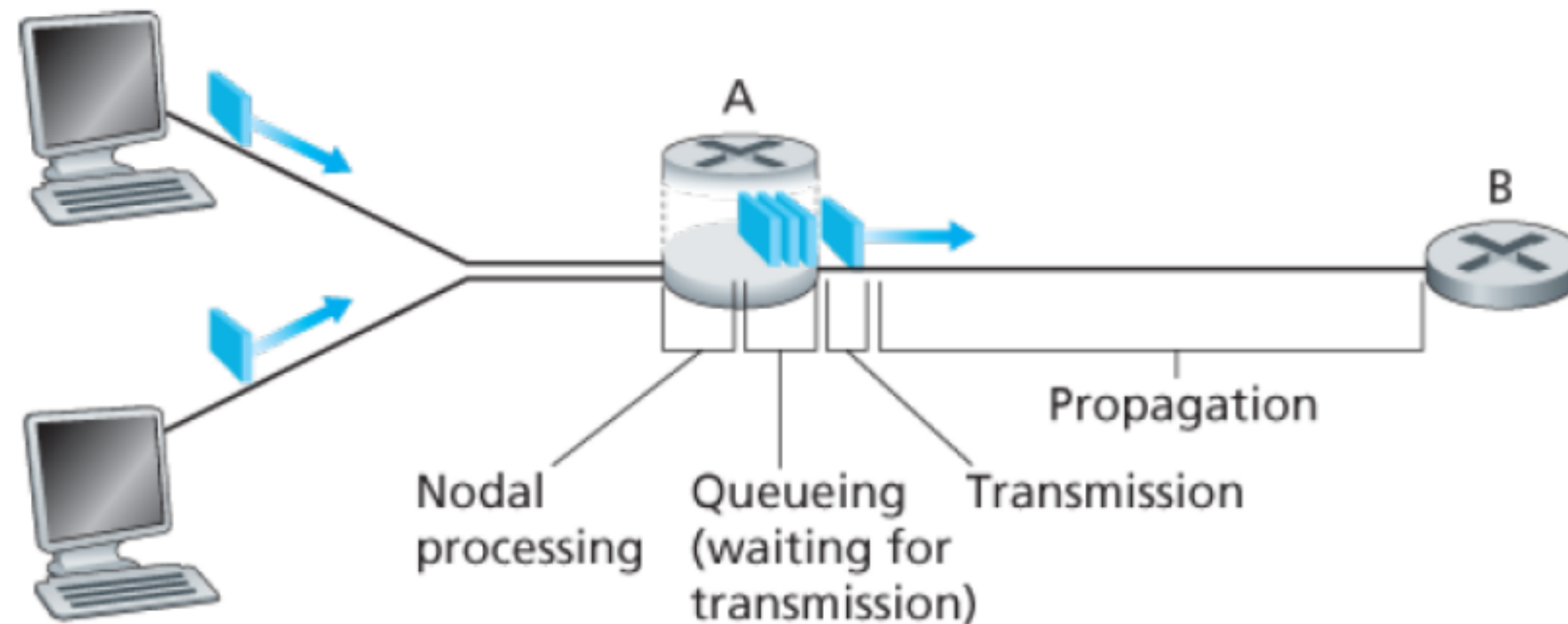
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  - What is the transmission delay and propagation delay?
  - If we increase the transmission rate to 1Gbps, what happens?
  - If we increase the distance to 3km, what happens?

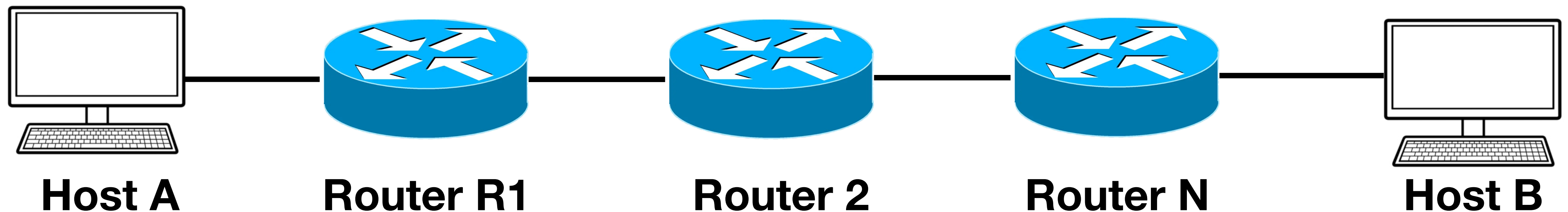
# Total (Nodal) Delay

- $T_{\text{total}} = T_{\text{proc}} + T_{\text{queue}} + T_{\text{trans}} + T_{\text{prop}}$ 
  - Per-node, also called total nodal delay



# End-to-End Delay

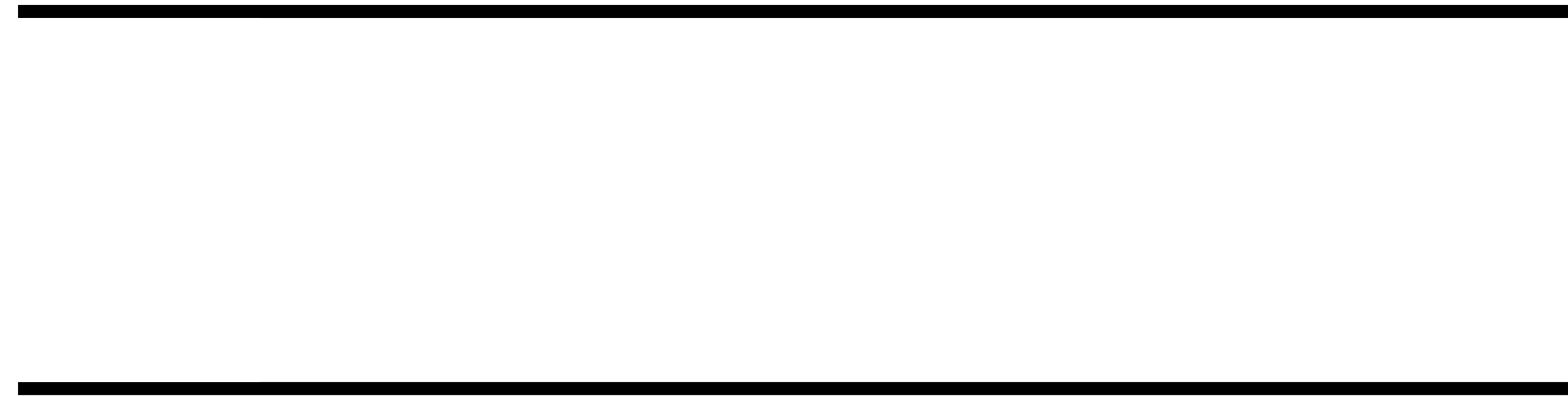
- Suppose
  - Host A can send a packet infinitely fast
  - Host B can receive a packet infinitely fast
- What is the end-to-end delay for a packet from host A to host B?
  - $T_{\text{end-to-end}} = N (T_{\text{proc}} + T_{\text{queue}} + T_{\text{trans}} + T_{\text{prop}}) + T_{\text{prop}}$



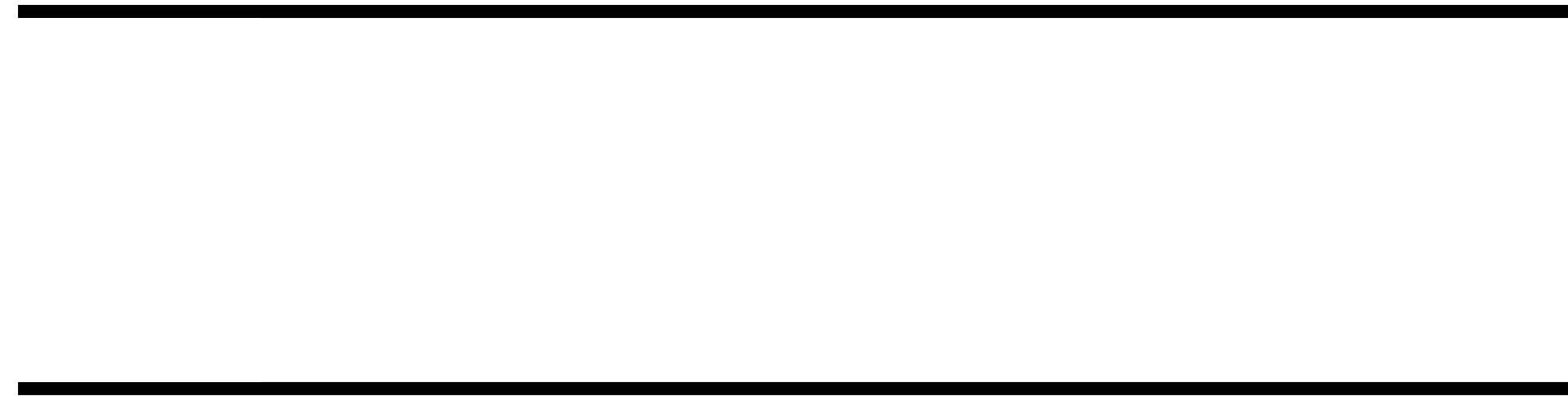
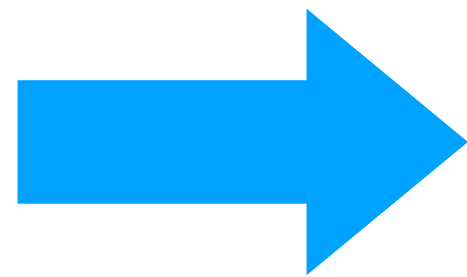
# Queueing Delay

- The most complicated and interesting one
  - Varying packet to packet and scenario to scenario
- Statistical metrics
  - Average queueing delay
  - Variance of queueing delay
  - Tail queueing delay
  - The probability that the queueing delay exceeds some value

# When the Queue is built up?

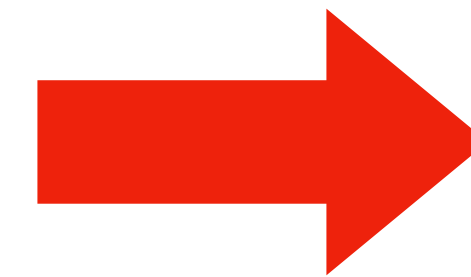
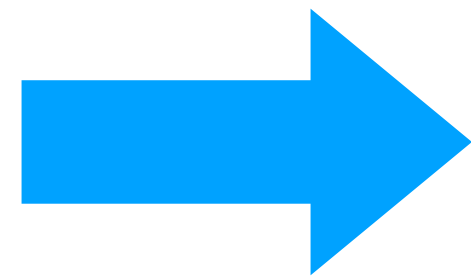


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- Packet arrival rate **a**
- Unit: packets/second

- Transmission rate **R**
- Unit: bits/second



# When the Queue is built up?

- Given time  $T$ , incoming traffic load  $>$  outgoing traffic load
  - Incoming traffic load =  $\sum_{i=1}^N pkt\_size_i$
  - Out going traffic load =  $R * T$



- Packet arrival rate **a**
- Unit: packets/second

- Transmission rate **R**
- Unit: bits/second

# Traffic Intensity

- We define the ratio  $(\lambda a/R)$  as the traffic intensity
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**Design your system so that the traffic intensity is no greater than 1!**

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  - Suppose all packets consist of  $L$  bits
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**Can we see queueing when  $\lambda a/R \leq 1$ ?**

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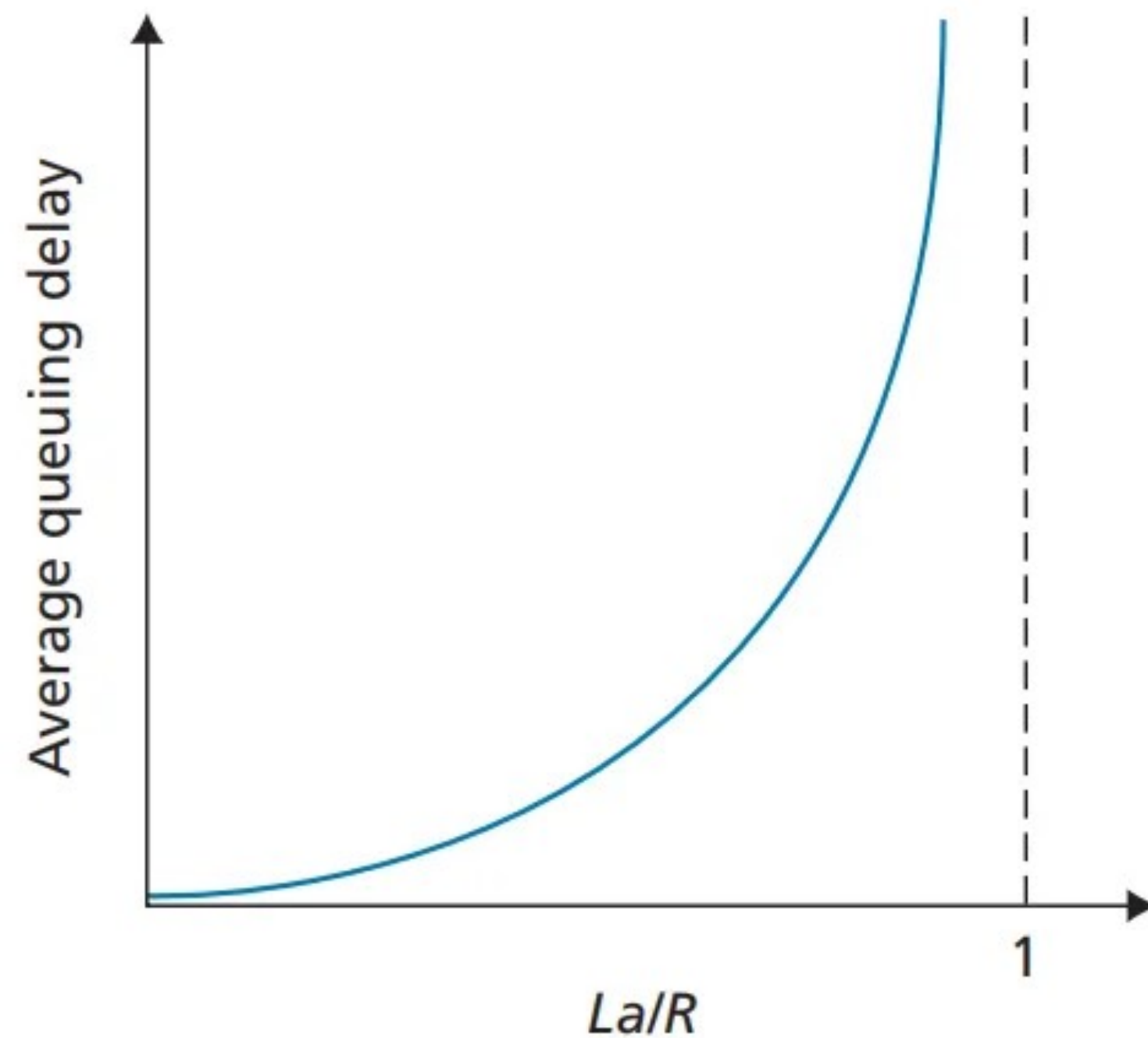
# Traffic Arrival process

- Suppose one packet arrives every  $L/R$  seconds
  - No queueing
- Suppose  $N$  packets arrive every  $(L/R)N$  seconds
  - The 1st packet has no queueing delay,  $T_{\text{queue}} = 0$
  - The 2nd packet has to wait for the 1st one,  $T_{\text{queue}} = L/R \times 1$
  - The 3rd packet has to wait for the 1st and 2nd ones,  $T_{\text{queue}} = L/R \times 2$
  - The  $n$ th packet has to wait for the  $(n-1)$  ones,  $T_{\text{queue}} = L/R \times (n-1)$



# Traffic Intensity Curve

- Close to 1, the average queueing delay increases
  - A small percentage increase causes a significant delay increase
  - In reality, queue is fixed-sized ==> **Packet Loss**

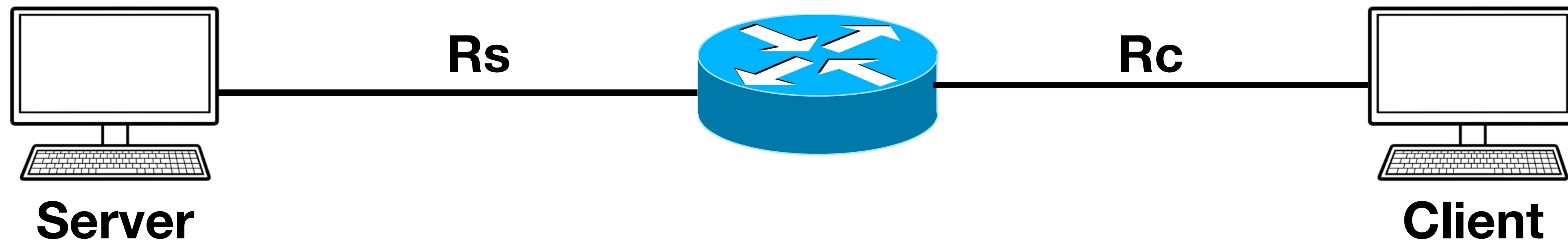


# Throughput

- Bandwidth: the number of bits transmitted per second at a communication port and link
  - bps, Kbps, Mbps, Gbps, Tbps, ...
- Throughput: the number of bits transmitted from A to B
  - A and B can be host, switch, etc.
  - bps, Kbps, Mbps, Gbps, Tbps, ...

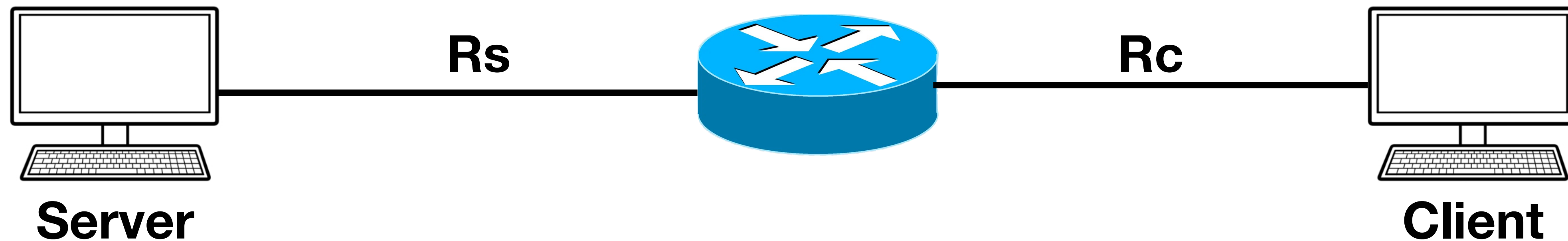
# A Simple Throughput Example

- A file transferring from a server to a client



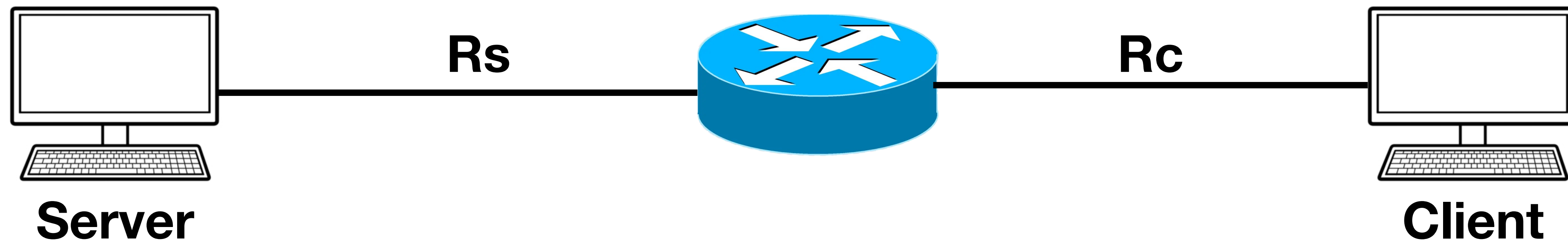
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- A file transferring from a server to a client
  - If  $R_s < R_c \implies$  The client receives the file at  $R_s$
  - If  $R_s > R_c \implies$  The client receives the file at  $R_c$ , but router is queued



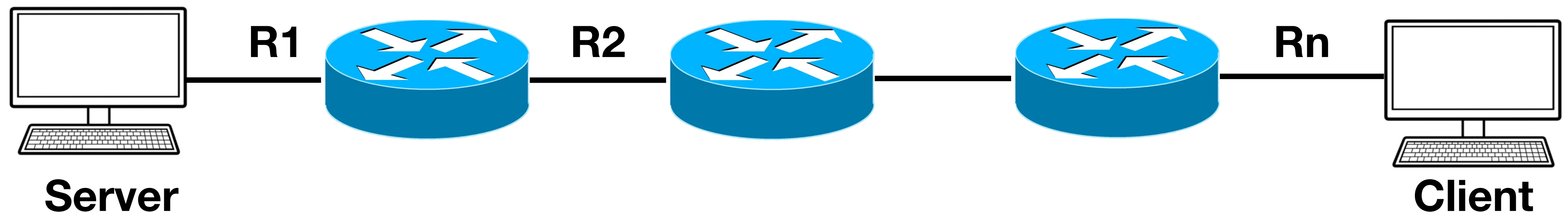
# A Simple Throughput Example

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  - If  $R_s > R_c \implies$  The client receives the file at  $R_c$ , but router is queued
- Throughput =  $\min \{R_s, R_c\}$ 
  - Depend on the bottleneck link
- A log file = 32M bits,  $R_s = 2\text{Mbps}$ ,  $R_c = 1\text{Mbps}$ 
  - Transfer time is 32 seconds



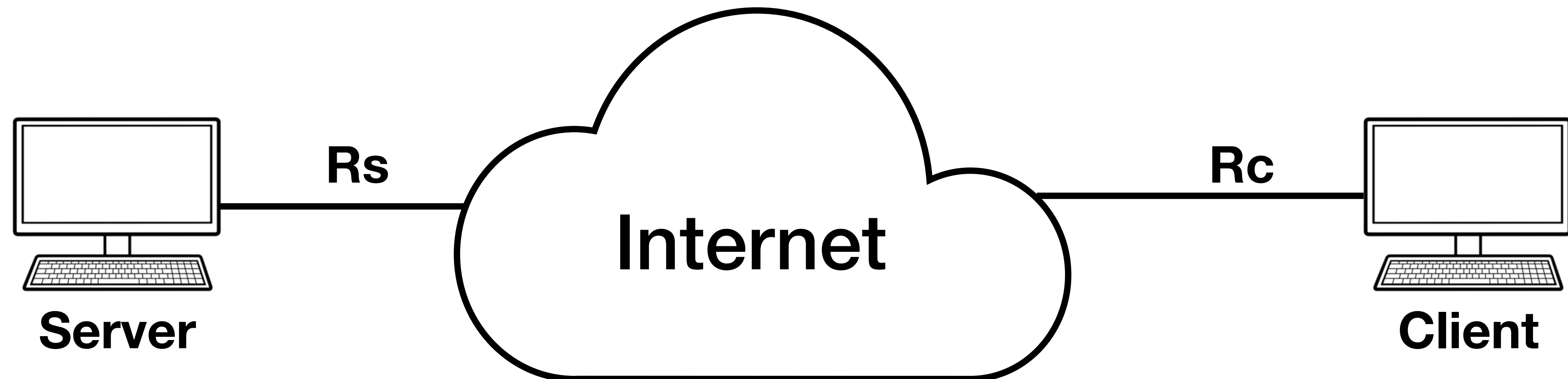
# Another Throughput Example

- Communication path: server -> a list of routers -> Client
- Throughput =  $\min \{R_1, R_2, R_3, \dots, R_n\}$ 
  - Depend on the bottleneck link



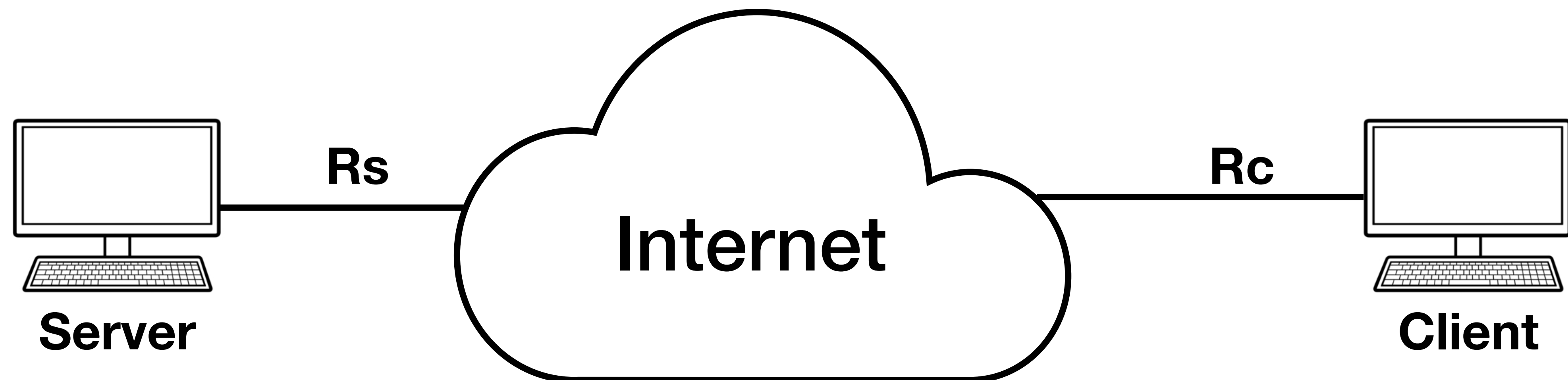
# Throughput in a Shared Network

- Impossible to know the communication path details
- What is the throughput to transfer a file from a server to a client?



# Throughput in a Shared Network

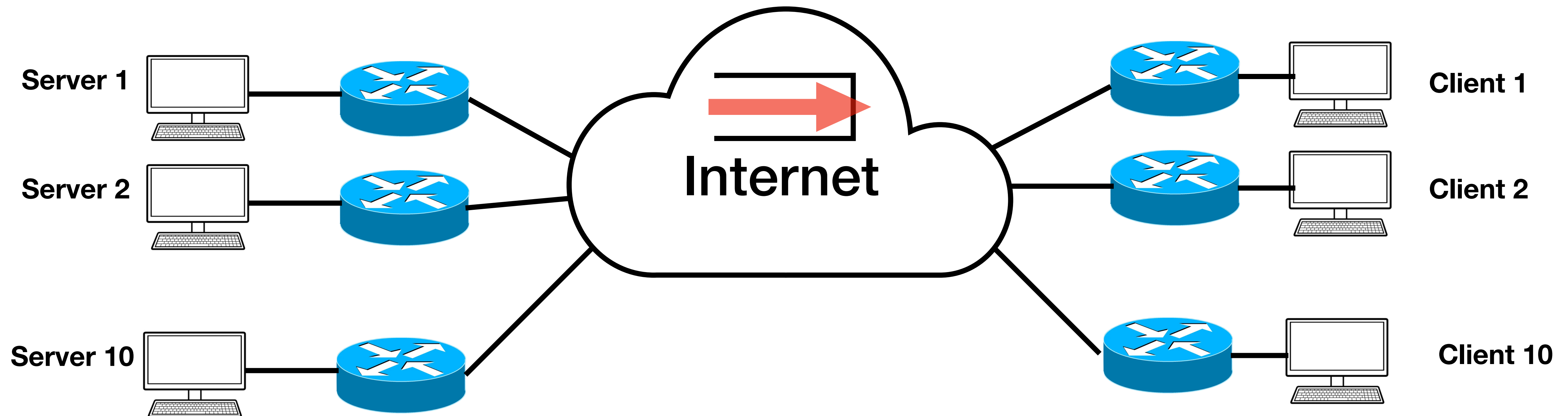
- Impossible to know the communication path details
- What is the throughput to transfer a file from a server to a client?
  - Actual Throughput = File Size / Total Transfer Time
  - Actual Throughput  $\leq \min \{R_s, R_c\}$





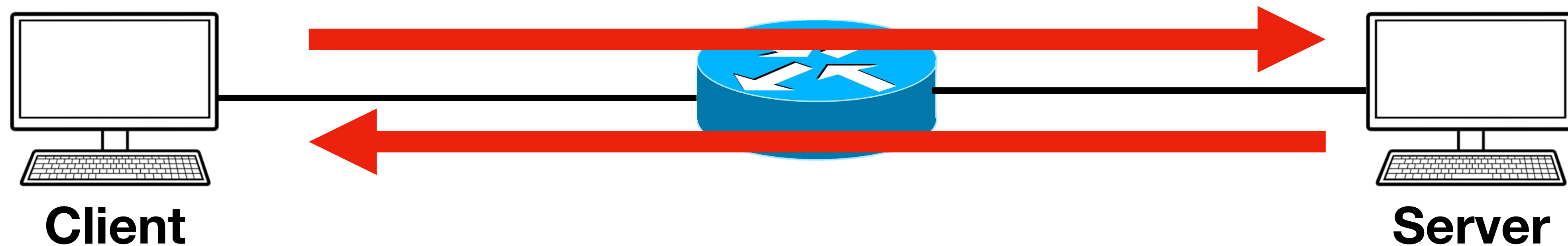
# Throughput under Concurrent Transmissions

- Throughput also depends on intervening traffic



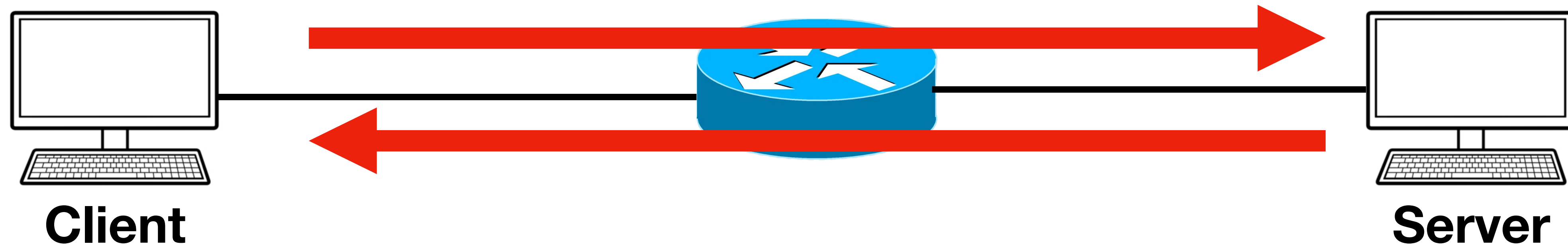
# RTT (Round-Trip Time)

- The time it takes to send a request from a client to a server and receive the response back
  - $RTT = \text{Total delay (Client} \rightarrow \text{Server)} + \text{Total Delay (Server} \rightarrow \text{Client)}$



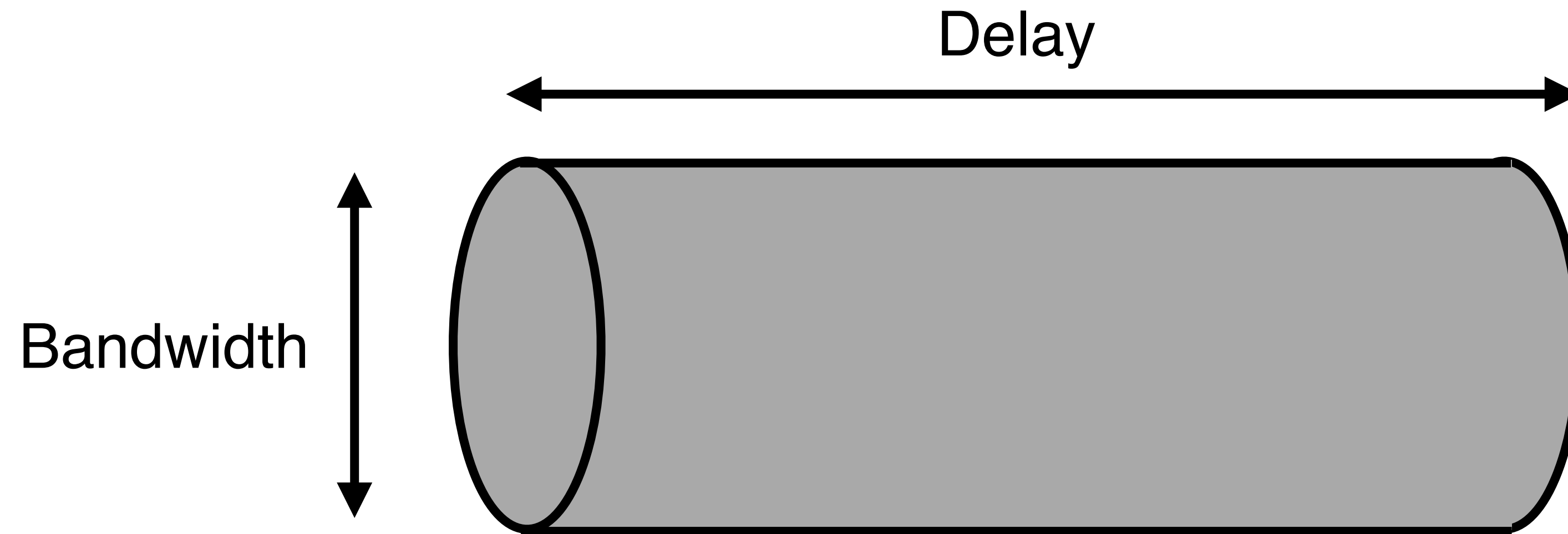
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- RTT is application-dependent
  - Web browsing: page download time (time to retrieve the first object)
  - Cloud gaming: interactive latency
  - Video conferencing and streaming: Time to First Frame
  - LLM: Time to first token



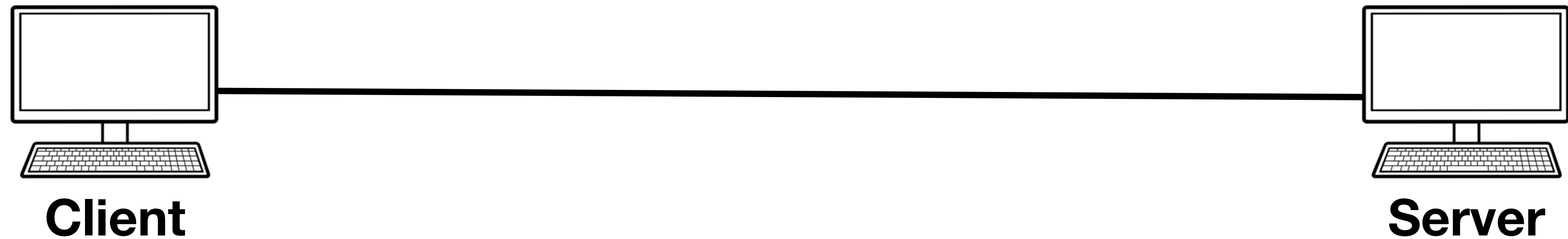
# BDP (Bandwidth-Delay Product)

- The volume of a data pipe for one transmission
  - Bandwidth \* Delay
  - The number of bits have left the sender and are yet to reach the receiver



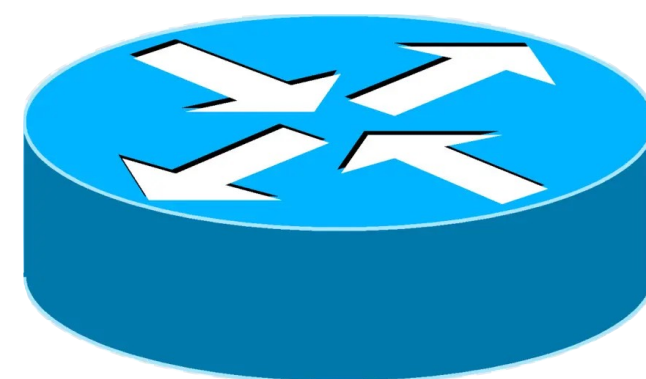
# BDP of a Communication Link

- Delay=Propagation delay  $\implies$  Link BDP
  - The number of bits over the wire



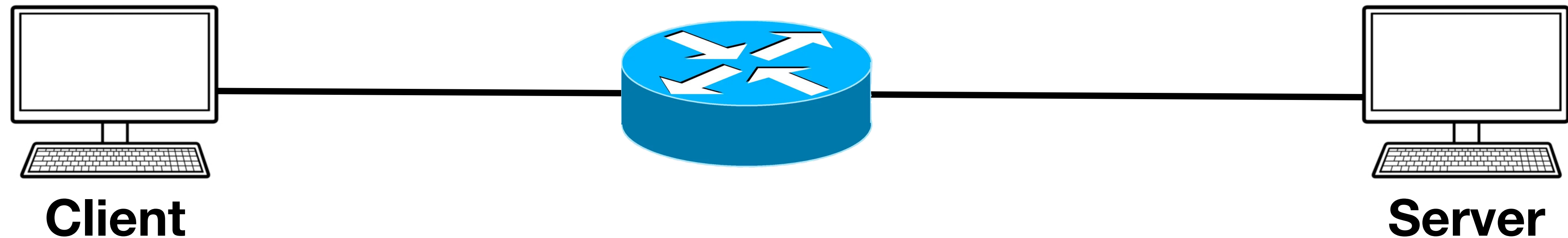
# BDP of a Router

- Delay=Propagation delay  $\implies$  Link BDP
  - The number of bits over the wire
- Delay=Processing + Queueing + Transmission  $\implies$  Router BDP
  - The number of bits a router can hold



# BDP of Client $\rightarrow$ Server

- Delay=Propagation delay  $\Rightarrow$  Link BDP
  - The number of bits over the wire
- Delay=Processing + Queueing + Transmission  $\Rightarrow$  Router BDP
  - The number of bits a router can hold
- Delay=Total delay  $\Rightarrow$  End-to-End BDP
  - The number of bits that stay in-flight between two hosts



# Summary

- Today
  - Computer networks: performance analysis
- Next lecture
  - Physical Layer: Encoding