# HW6, CS769 

Nathanael Fillmore

Due April 11, 2008

## 1 Page Rank

Question 1. After one step, the walker will be at page 2,11 , 21 , or 31 , each with probability $1 / 4$.
Question 2. After one step, the walker will be at page 2, 11, 21, or 31, each with probability $0.2275=$ $9 / 10 * 1 / 4+1 / 10 * 1 / 40$, or at any other page, each with probability $0.0025=1 / 10 * 1 / 40$.

Question 3. The PageRank $r$ for each page $u$ is:

| $u$ | $r$ | $u$ | $r$ | $u$ | $r$ | $u$ | $r$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.0032 | 11 | 0.0236 | 21 | 0.0485 | 31 | 0.0486 |
| 2 | 0.0039 | 12 | 0.0243 | 22 | 0.0399 | 32 | 0.0399 |
| 3 | 0.0039 | 13 | 0.0249 | 23 | 0.0347 | 33 | 0.0345 |
| 4 | 0.0039 | 14 | 0.0255 | 24 | 0.0316 | 34 | 0.0312 |
| 5 | 0.0039 | 15 | 0.0262 | 25 | 0.0300 | 35 | 0.0292 |
| 6 | 0.0039 | 16 | 0.0271 | 26 | 0.0295 | 36 | 0.0282 |
| 7 | 0.0040 | 17 | 0.0285 | 27 | 0.0300 | 37 | 0.0279 |
| 8 | 0.0044 | 18 | 0.0307 | 28 | 0.0316 | 38 | 0.0283 |
| 9 | 0.0065 | 19 | 0.0342 | 29 | 0.0347 | 39 | 0.0294 |
| 10 | 0.0143 | 20 | 0.0397 | 30 | 0.0400 | 40 | 0.0157 |

This was computed as follows:

```
% P was defined earlier
b = ones (40,1)/40 % uniform distribution
alpha = 0.9
M = alpha*P + (1-alpha)*b*ones(40,1)'
[V,D] = eig(M)
r = V(:,1)
r = r/sum(r)
```


## Question 4.



Pages 21 and 31 have the same PageRank (almost). This is because they have the same number of pages linking to them, and the linking pages are also ranked similarly. Page 11 is ranked lower. Why? Pages 21 and 31 are linked to by $1-10$ as well as 20,22 and 30,32 respectively; page 11 is linked to by $1-10$ as well as 12 (since 10 already links to it). Thus in effect page 11 has one less link than pages 21 and 31 do. Additionally, page 11 is near the $1-10$ range, which has more outgoing links than the other pages; hence the incoming neighbor links 11 does have are worth less than those of 21 and 31.

## 2 Latent Semantic Indexing

## Question 6.



This was computed as follows:

```
load cs.dat;
X = spconvert(cs);
X = X';
[U,S,V] = svds(X);
U_hat = U(:,1:2);
S_hat = S(1:2,1:2);
```

V_hat = V(:,1:2);
X_hat = S_hat*V_hat';
plot(X_hat(1,:), X_hat(2,:), 'o')

## 3 Latent Dirichlet Allocation

Question 7.


Question 8.

| topic | words |
| :---: | :---: |
| 000 | \# java pdf 100 jasmin 4 programming \#\# cs 97 |
| 001 | madison wi research sciences wisconsin 608 department dayton science 1210 |
| 002 | class player frames will week use no package if all |
| 003 | was pictures jerel $\mathrm{n} \# \mathrm{t}$ one some back me but last |
| 004 | picture camera canon last first next atlantic\#city previous am 30 |
| 005 | was me \#a href\# \#font font first tenaya n\#t \#\#\# |
| 006 | madison wisconsin parallel links $\mathrm{j} \#$ usa $\mathrm{m} \#$ computing performance information |
| 007 | br \#a href\# http \#td td \#tr tr var class\# |
| 008 | june rest $200629 \# 30$ cloud created bbgallerycloud n parallel sorting |
| 009 | learning xml machine other which one also reinforcement neural its |
| 010 | systems \# database will project management material course minibase class |
| 011 | class ff \# if points will array which 2 |
| 012 | \# 5 series 0 assignment 2 time analysis 4 models |
| 013 | science department madison research wisconsin wisconsin\#madison sciences 2007 statistics wi |
| 014 | program profiling path warts new paths qpt research cache systems |
| 015 | statistics stat 2006 fall statistical 608 madison spring department 301 |
| 016 | 31 new image function if press e keypress keypresslistener next0 |
| 017 | \# image $2 \mathrm{c} \# \#$ will library your system standard |
| 018 | \# cs cs\#wisc\#edu email algorithms os\#9 theory list group |
| 019 | 0 learning 2007 style\# semi\#supervised machine uw zhu cs width\# |
| 020 | week project what 2007 \# top clustering report information which |
| 021 | $00 \# 00$ phase $0 \# 0000$ number rate first process proxy cache |
| 022 | memory code not x chapter time program p class int |
| 023 | \#a li href\# br http p href pdf postscript \# |
| 024 | was david but me madison wisconsin web parter about if |
| 025 | discussion stat statistics model analysis y\# 2 spring fall \# |
| 026 | was me about $\mathrm{n} \# \mathrm{t}$ do he so but what \#\#\# |
| 027 | research systems learning doan arpaci\#dusseau information a\# c\# anhai pdf |
| 028 | discussion \# pdf homework 2 office 349 exam |
| 029 | ph 5 \#h5 devise user li puzzle program will our |
| 030 | wisconsin memory research architecture parallel more systems mark david hill |
| 031 | var false null \# images parentindexpageurl firstindexpageurl lastindexpageurl u not |
| 032 | \# 2007 b paper \# \# t\# research abstract program |
| 033 | but do so was $\mathrm{n} \# \mathrm{t}$ not me if \#\#\# did |
| 034 | \# td \#td 2 all 3 photo e \# center |
| 035 | function name value days savecookie readcookie album web next index |
| 036 | here \#\#\# homepage me web if click your links am |
| 037 | courier new \#font your font program which function face\# file |
| 038 | picture last next previous first \#06 hawaii animation class simulation |
| 039 | cs document\#write \# me introduction dot ece about classes math |
| 040 | he theory his will complexity program science some cai may |
| 041 | cache web proxy sharing query protocol traces server client summary |
| 042 | è â width\# \#p p center align\# 0 i̊a \#td |
| 043 | condor linux project software computing code our if system your |
| 044 | analysis 2005 newton statistics 00 hours a\# statistical methods 2006 |
| 045 | server go last results updated configuration client back mn about |
| 046 | \#\#\# java www\#cs\#wisc\#edu\#\#koconnor 2000 here some was 2 naming out |
| 047 | systems networks advanced prof\# research fall network project system pdf |
| 048 | not do $\mathrm{n} \# \mathrm{t}$ was your but me so one all |
| 049 | http mangasarian 2005 mining \# research l\# pdf olvi wisconsin |

Some of the topics seem sensible, for example topic 001 has to do with the mailing address of the CS department. Topic 007 has is all from inside html tags. Topic 004 combines photography with navigation, presumably because of photo galleries. Some of the topics are strange, for example topic 000 finds a connection between "java", "pdf", "100", and "\#\#"-I guess from course webpages?

## Question 9.

| user | best topic-weight pairs |
| :--- | :--- |
| jerryzhu | $(17,905.6575810603),(19,877.37349511399998)$ |
| shavlik | $(9,1853.0155380872)$ |
| miron | $(7,84.293074253699999),(43,67.275698118700006),(1,33.477841889099999)$ |
| sohi | $(30,153.01553808720001)$ |
| pb | $(47,1477.0950339067001),(28,297.93604226769997)$ |

