CS 564 Midterm Exam
Fall 2015
Answers and Grading Key

A: ER AND RELATIONAL MODELS [10%]

For the following questions, just answer (by circling) either True or False.

1. [2%] A multi-way relationship in ER can always be converted to a set of binary relationships.
   **TRUE**

2. [2%] It is possible to translate both a weak entity set and an ISA hierarchy in the ER model to the relational model.
   **TRUE**

3. [2%] The ER model has no mechanisms to capture keys that are not primary keys.
   **TRUE**

4. [2%] Given any ER diagram, there is always only one correct way to translate it to the relational model.
   **FALSE**

5. [2%] There are mechanisms to enforce referential integrity in SQL that cannot be depicted in the ER model.
   **TRUE**

B: NORMALIZATION AND DEPENDENCY THEORY [22%]

Consider a relation R with $2d$ attributes ($d$ is an integer $\geq 2$) that are named $A_1, A_2, \ldots, A_{2d}$. There is a set F of $2d$ FDs on R: $A_i \rightarrow A_{1+(i+1) \mod 2d}$, for $i = 1 \ldots 2d$. Here, $\mod$ is the modulo operator (remainder after integer division, e.g., $17 \mod 5 = 2$). For example, suppose $d = 2$, the attributes are $A_1, A_2, A_3, A_4$ and $F = \{ A_1 \rightarrow A_3, A_3 \rightarrow A_1, A_2 \rightarrow A_4, A_4 \rightarrow A_2 \}$. Answer the following questions.

1. [6%] Suppose $d = 2$. Obtain a lossless-join and dependency-preserving decomposition of R to BCNF using the algorithm given in class. Make sure you show the projections of F on to each relation in your decomposition.

   **ANSWER:**
\((A_1A_3, A_2A_4, A_1A_2)\) with respective projections \(\{A_1 \rightarrow A_3, A_3 \rightarrow A_1\}, \{A_2 \rightarrow A_4, A_4 \rightarrow A_2\},\) and \(\phi\).

2. [18%] For the following, \(d > 2\). Choose (by circling) the right option (only 1 is correct per question), and explain the reasoning behind your answer. If your answer is incorrect or your explanation is invalid/incomplete, no points will be awarded.

(a) [7%] What is the number of keys in \(R\)?

(i) 1  (ii) \(d\)  (iii) \(d + 2\)  (iv) \(2d\)  (v) \(d^2\)

ANSWER: (v) \(d^2\).

EXPLANATION:
All “odd” attributes determine each other. All “even” attributes determine each other. No odd attribute determines an even attribute and vice versa. Thus, to get a key, we need 1 odd and 1 even attribute (\(d\) choices each). Thus, the number of keys is \(d \times d = d^2\).

ALTERNATIVE VALID EXPLANATION:
Show that for, say, \(d = 3\), the number of keys is 9. Thus, only \(d^2\) is not incorrect among the listed options!

(b) [9%] In any possible lossless-join and dependency-preserving decomposition of \(R\) to BCNF, what is the number of relations with no non-trivial FDs in the projection of \(F^+\) on to it?

(i) 0  (ii) 1  (iii) 2  (iv) 3  (v) \(d\)

ANSWER: (ii) 1.

EXPLANATION:
Any relation that has 3 or more attributes will have either 2 odd or 2 even attributes, which means it will have non-trivial FDs. So, the only kind of relation that has no non-trivial FDs is that which has some key of \(R\) as its only attributes. Claim: there will be exactly 1 of such kind in the decomposition. If we have more than 1 of such kind, their join will be lossy. If we have none of such kind, the whole decomposition is lossy because no relation with only odd (or only even) attributes can contain a key of \(R\), and any relation that contains a key of \(R\) as a strict subset will violate BCNF.

ALTERNATIVE VALID EXPLANATION:
Show that for, say, \(d = 3\), the number of such relations in such a BCNF decomposition is 1. Thus, only (ii) is not incorrect among the given options!
Throughout this part, we will be using the following database schema:

**Product** (pid, name, brand, price, color)
**Sales** (pid, buyer, store, date)

Sales.pid is a foreign key referring to Product.pid.

1. [15%] Consider the following SQL query Q:

   ```
   SELECT brand 
   FROM Product 
   WHERE color = 'green' 
   GROUP BY brand 
   HAVING COUNT(*) < 3
   ```

   (a) [8%] Is the query Q equivalent to the query below? If yes, explain why. If not, provide a database instance that is a counterexample.

   ```
   SELECT DISTINCT brand 
   FROM Product p 
   WHERE (SELECT COUNT(*) 
   FROM Product q 
   WHERE q.brand = p.brand 
   AND q.color = 'green') < 3
   ```

   The query is not equivalent. If a brand sells no green product, this brand will be displayed, but the original query will not return this brand.

   (b) [7%] Is the query Q equivalent to the query below? If yes, explain why. If not, provide a database instance that is a counterexample.

   ```
   SELECT brand 
   FROM Product p 
   WHERE color = 'green' 
   AND (SELECT COUNT(*) 
   FROM Product q 
   WHERE q.brand = p.brand 
   AND q.color = 'green') < 3
   ```

   The query is not equivalent. If a brand sells two green products, the lack of DISTINCT means that the same brand will be displayed twice, but the original query will display it only once.

2. [15%] Express the following SQL query in both Relational Algebra and Tuple Relational Calculus:
SELECT DISTINCT name  
FROM Product p  
WHERE color = 'green'  
AND NOT EXISTS (SELECT *  
FROM Product q  
WHERE q.brand = p.brand  
AND q.price > 100)

Relational Algebra:
\[ \Pi_{\text{name}}(\sigma_{\text{color} = 'green'}(\text{Product}) \times (\Pi_{\text{brand}}(\text{Product}) - \Pi_{\text{brand}}(\sigma_{\text{price} > 100}(\text{Product})))) \]

Relational Calculus:
\[ \{ t \mid \exists p \in \text{Product}(p.color = 'green' \land p.name = t.name \land \neg \exists q \in \text{Product}(q.brand = p.brand \land q.price > 100) \} \]

3. [12%] Write one SQL query for each of the following:

   (a) [6%] For each brand, get the number of distinct products of that brand that were bought by John.

   SELECT p.brand, COUNT (DISTINCT p.pid)  
   FROM Product p, Sales s  
   WHERE s.buyer = "John" AND p.pid = s.pid  
   GROUP BY p.brand;

   (b) [6%] Get the date (or dates) for which the "Madison" store had the largest total sales (sum of the prices of all sold products).

   SELECT d.date  
   FROM (SELECT s.date, SUM(p.price) AS totalprice  
   FROM Product p, Sales s  
   WHERE s.store = "Madison" AND p.pid = s.pid  
   GROUP BY s.date ) AS d  
   WHERE d.totalprice = (SELECT MAX (d.totalprice)  
   FROM d);

4. [10%] For the following questions, just answer (by circling) either True or False.
(a) [2%] An *INSERT* statement in SQL can only add one tuple to the database. **FALSE**

(b) [2%] The following SQL query does not return any tuples where price is NULL.

SELECT * FROM Product WHERE price <> 100;

**TRUE**

(c) [2%] Suppose that we define the schema of Sales in SQL as follows:

```sql
CREATE TABLE Sales (  
pid INTEGER,  
buyer CHAR(20),  
seller CHAR(20),  
date DATE,  
FOREIGN KEY (pid) REFERENCES Product(pid)  
    ON UPDATE CASCADE);
```

When we update the pid of a product in Sales, the database will update the pid in the Product table. **FALSE**

(d) [2%] The following two queries are equivalent:

```sql
SELECT pid  
FROM Product  
ORDER BY price DESC  
LIMIT 1;

SELECT pid  
FROM Product  
WHERE price = (SELECT MAX (price) FROM Product);
```

**FALSE**

(e) [2%] The following is not a valid SQL query:

```sql
SELECT brand, MAX (price)  
FROM Product  
GROUP BY brand  
HAVING price > 100;
```

**TRUE**

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**D: DISKS AND BUFFER MANAGEMENT [16%]**
1. [6%] For the following questions, just answer (by circling) either True or False.

   (a) [2%] Most disks have multiple disk blocks within the same disk sector.
       TRUE

   (b) [2%] Sequential disk access is almost always slower than random disk access.
       FALSE

   (c) [2%] Given a disk block, either its “next” block or its “previous” block or both
       will always be on the same track as the given disk block.
       TRUE

2. [10%] In this question, you have to count the number of page I/Os (both reads and
       writes) for the given page access sequence and buffer replacement policy.

   There is only 1 query process. A page “Request” means the query process wants
   to read that page’s values for computations. A page “Modify” means the query
   process is modifying the values on that page. A page “Release” means the query
   process has finished using that page and notifies the buffer manager accordingly.

   The number of page frames in the buffer pool is 3. Initially, all buffer frames are
   free and clean, and none of the pages to be accessed are in RAM. Note that a buffer
   frame can be considered for replacement if and only if its pin count is 0. Also note
   that the dirty bit is set to 1 upon a “Modify” on a page.

   Access Sequence: Request A, Release A, Request B, Request C, Modify B, Modify

   What is the total number of page I/Os with LRU policy? Explain each page I/O in
   your answer.

   ANSWER: 6 pages I/Os.

   EXPLANATION:
   Buffer frames F1, F2, and F3. Initially, all of their pincount and dirtybit are 0.
   COUNTER tracks total I/O cost. Start with COUNTER = 0.
   Request A: I/O to read A into F1. Set F1.pincount = 1. COUNTER = 1.
   Release A. Set F1.pincount = 0.
   Request B: I/O to read B into F2. Set F2.pincount = 1. COUNTER = 2.
   Request C: I/O to read C into F3. Set F3.pincount = 1. COUNTER = 3.
   Modify B: Set F2.dirty = 1.
   Modify C: Set F3.dirty = 1.
Release B: Set F2.pincount = 0.
Request A: Available in F1. Set F1.pincount = 1.
Release A: Set F1.pincount = 0.
Request D: Need to find a frame with pincount 0 to replace. F1 or F2 can be used. LRU policy picks F2. But F2.dirty = 1. Thus, I/O to write (flush) B in F2 to disk. Set F2.dirtybit = 0. COUNTER = 4. I/O to read D into F2. Set F2.pincount = 1. COUNTER = 5.
Request B: Need to find a frame with pincount 0 to replace. F1 can be used. LRU policy picks F1. Since F1.dirty = 0, no need to flush. I/O to read B into F1. Set F1.pincount = 1. COUNTER = 6