

MEMORY: TLBS, SMALLER PAGETABLES

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ADMINISTRIVIA

- Project 3 is due **Monday**
- Project 1 grades

AGENDA / LEARNING OUTCOMES

Memory virtualization

What are the challenges with paging ?

How we go about addressing them?

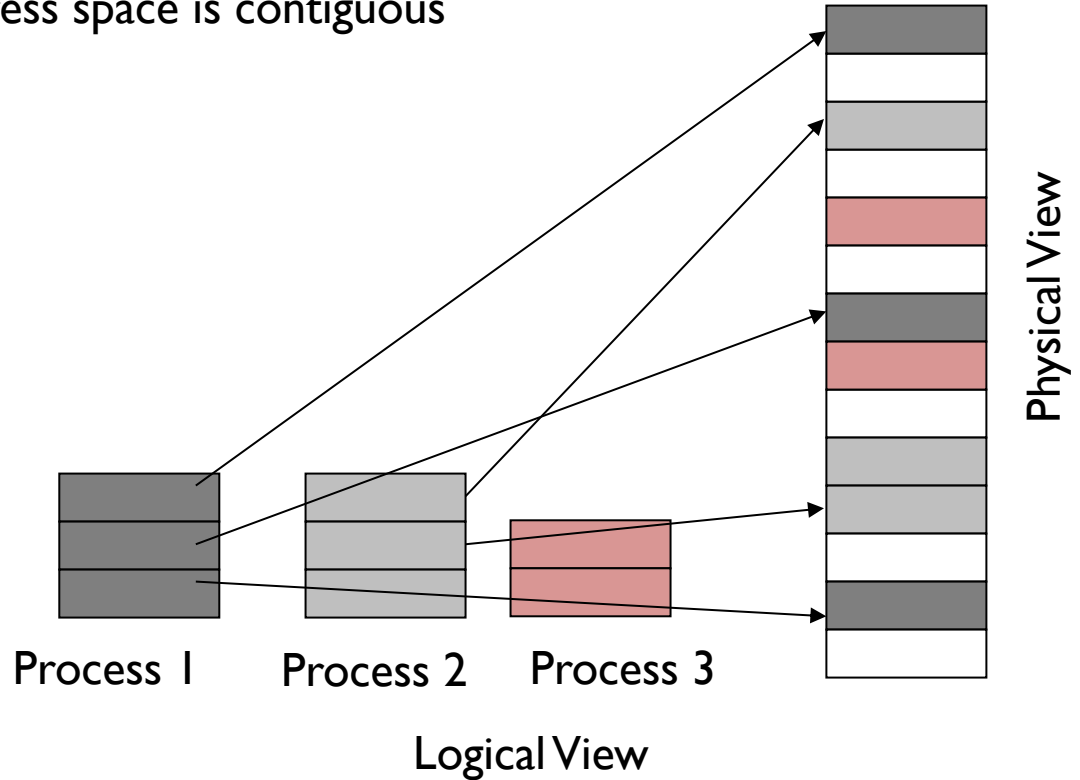
RECAP

PAGING

Goal: Eliminate requirement that address space is contiguous

Idea:
Divide address spaces and physical
memory into fixed-sized pages

Example page size: 4KB



PAGING TRANSLATION STEPS

For each mem reference:

1. extract **VPN** (virt page num) from **VA** (virt addr)
2. calculate addr of **PTE** (page table entry)
3. read **PTE** from memory
4. extract **PFN** (page frame num)
5. build **PA** (phys addr)
6. read contents of **PA** from memory

14 bit addresses

Assume PT is at phys addr 0x5000

Assume PTE's are 4 bytes

Assume 4KB pages – 12 bit offset

Simplified view
of page table

2
0
3
4

READ 0x1100

PROS/CONS OF PAGING

Pros

No external fragmentation

- Any page can be placed in any frame in physical memory

Fast to allocate and free

- Alloc: No searching for suitable free space
- Free: Doesn't have to coalesce with adjacent free space

Cons

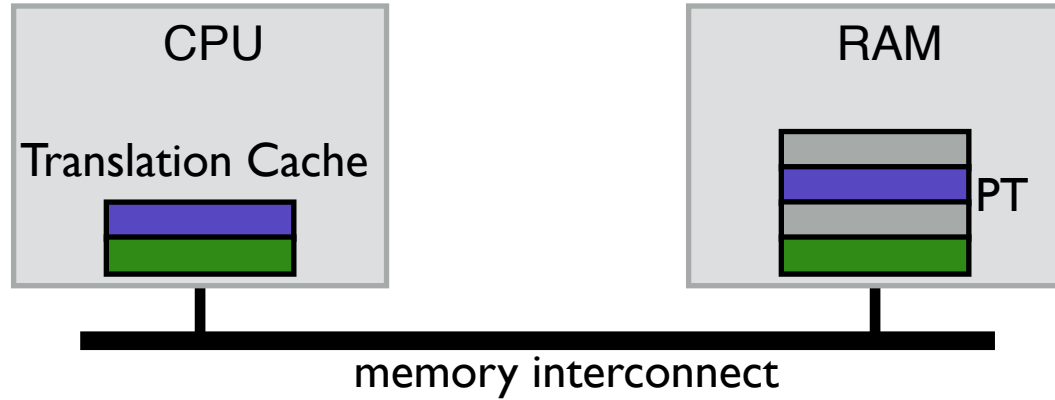
Additional memory reference

- MMU stores only base address of page table

Storage for page tables may be substantial

- Simple page table: Requires PTE for all pages in address space
- Entry needed even if page not allocated ?

STRATEGY: CACHE PAGE TRANSLATIONS



TLB Entry

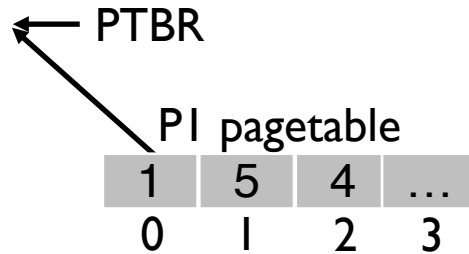
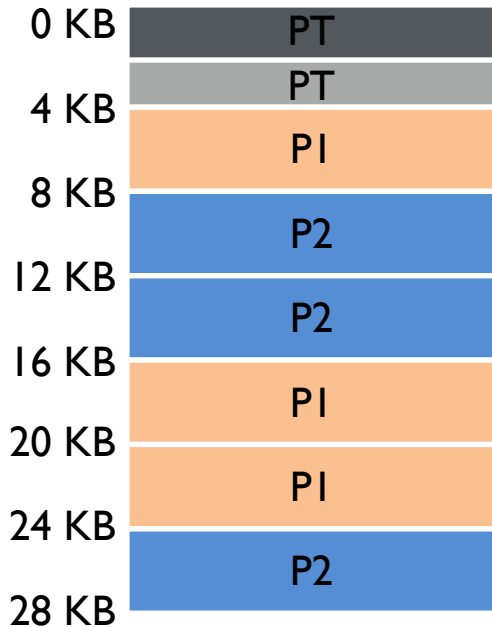
Tag (virtual page number)	Physical page number (page table entry)
---------------------------	---

Fully associative

Any given translation can be anywhere in the TLB

Hardware will search the entire TLB in parallel

TLB ACCESSES: SEQUENTIAL EXAMPLE



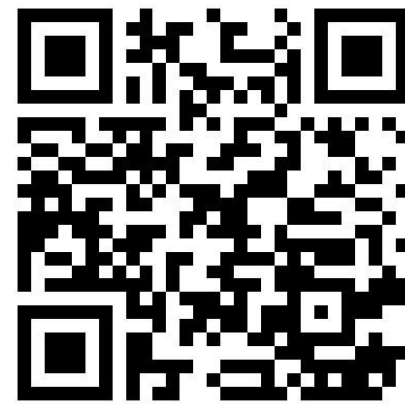
CPU's TLB

Valid	VPN	PPN
1	1	5

Virt	Phys
load 0x1000	load 0x0004
load 0x1004	load 0x5000
load 0x1008	(TLB hit) load 0x5004
load 0x100c	(TLB hit) load 0x5008
...	(TLB hit) load 0x500C
load 0x2000	...
load 0x2004	load 0x0008
	load 0x4000
	(TLB hit) load 0x4004

QUIZ 10: TLBS

<https://tinyurl.com/cs537-sp23-quiz10>



Consider a processor with 16-bit address space and 4kB page size.
Assume Page Table is at 0x2000 and each PTE is of 4 bytes.

VPN:0			
	0x0		
	0x0	Virtual Addresses	
PageTable	0x1	0x3000: load 0x5320, %eax	
	0x9	0x3004: load 0x4004, %ebx	
	0x7	0x3008: mul %ecx, %eax, %ebx	
	0x8	0x300C: store %ebx, 0x5324	
	0	0x3010: load 0x5328, %ebx	
	:		
VPN:15	0		

Memory accesses

Total

VPN:0

0x0
0x0
0x1
0x9
0x7
0x8
...

PageTable

Virtual Addresses

0x3000: load 0x5320, %eax

0x3004: load 0x4004, %ebx

0x3008: mul %ecx, %eax, %ebx

0x300C: store %ebx, 0x5324

0x3010: load 0x5328, %ebx

Memory accesses

TLB

Valid	VPN	PPN
0	2	6
0	7	23
0	2	5
0	3	2
0	1	89

TLB: POLICIES

How to we replace entries in the TLB?

How do we handle context switches?

PERFORMANCE OF TLB?

Miss rate of TLB: $\# \text{TLB misses} / \# \text{TLB lookups}$

$\# \text{TLB lookups?}$ number of accesses to a =

$\# \text{TLB misses?}$

= number of unique pages accessed

```
int sum = 0;
for (i=0; i<2048; i++) {
    sum += a[i];
}
```

Miss rate?

Would hit rate get better or worse
with smaller pages?

Hit rate?

WORKLOAD ACCESS PATTERNS

Workload A

```
int sum = 0;
for (i=0; i<2048; i++) {
    sum += a[i];
}
```

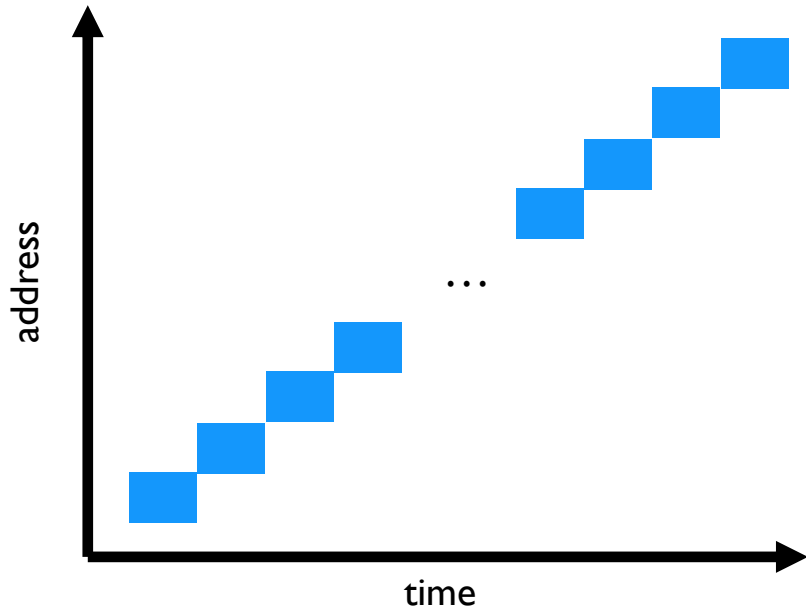
Workload B

```
int sum = 0;
srand(1234);
for (i=0; i<1000; i++) {
    sum += a[rand() % N];
}
srand(1234);
for (i=0; i<1000; i++) {
    sum += a[rand() % N];
}
```

WORKLOAD ACCESS PATTERNS

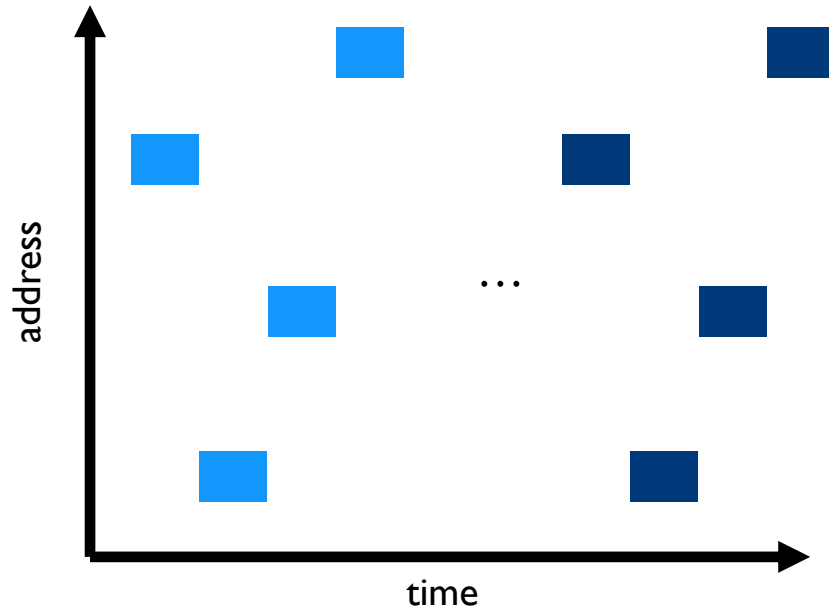
Spatial Locality

Sequential Accesses



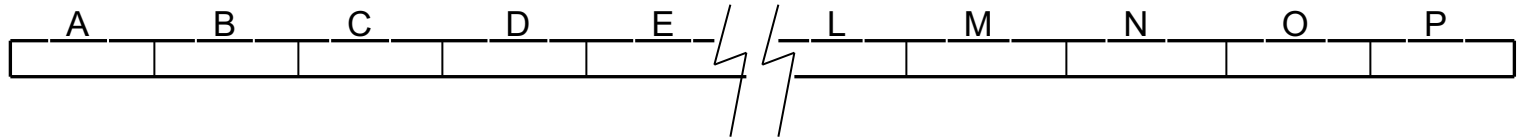
Temporal Locality

Repeated Random Accesses

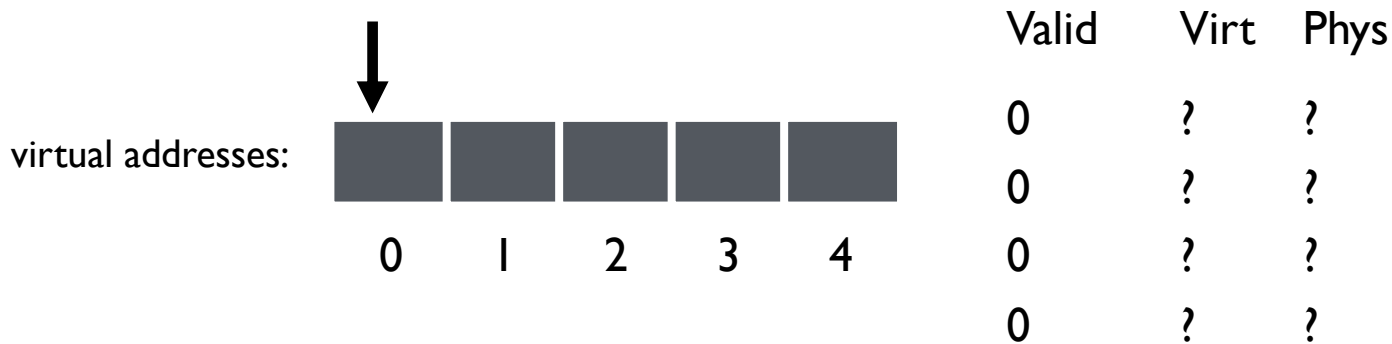


TLB REPLACEMENT POLICIES

LRU: evict Least-Recently Used TLB slot when needed



LRU TROUBLES



Workload repeatedly accesses same offset (0x01) across 5 pages (strided access), but only 4 TLB entries

What will TLB contents be over time?

How will TLB perform?

TLB REPLACEMENT POLICIES

LRU: evict Least-Recently Used TLB slot when needed

Random: Evict randomly chosen entry

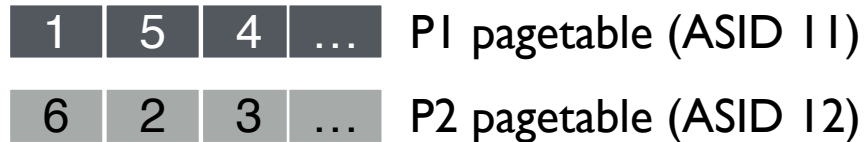
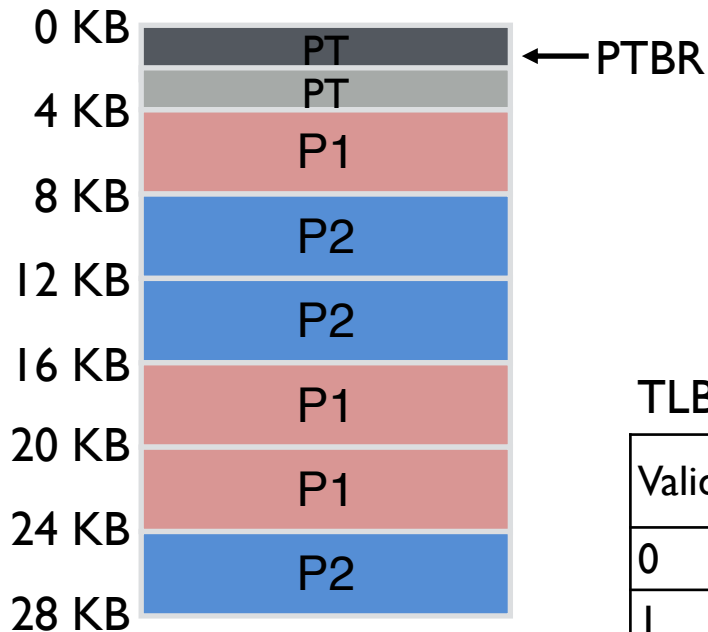
Sometimes random is better than a “smart” policy!

CONTEXT SWITCHES

What happens if a process uses cached TLB entries from another process?

1. Flush TLB on each switch
 - Costly → lose all recently cached translations
2. Track which entries are for which process
 - Address Space Identifier
 - Tag each TLB entry with an 8-bit ASID

TLB EXAMPLE WITH ASID



Virtual	Physical
load 0x1444 ASID: 12	
load 0x1444 ASID: 11	

TLB:

Valid	Virt	Phys	ASID
0	1	9	11
1	1	5	11
1	1	2	12
1	0	1	11

TLB PERFORMANCE

Context switches are expensive

Even with ASID, other processes “pollute” TLB

Architectures can have multiple TLBs

- 1 TLB for data, 1 TLB for instructions
- 1 TLB for regular pages, 1 TLB for “super pages”

HW AND OS ROLES

If H/W handles TLB Miss

CPU must know where pagetables are

- CR3 register on x86
- Pagetable structure fixed and agreed upon between HW and OS
- HW “walks” the pagetable and fills TLB

If OS handles TLB Miss:

“Software-managed TLB”

- CPU traps into OS upon TLB miss.
- OS interprets pagetables as it chooses
- Modify TLB entries with privileged instruction

TLB SUMMARY

Pages are great, but accessing page tables for every memory access is slow

Cache recent page translations → TLB

- MMU performs TLB lookup on every memory access

TLB performance depends strongly on workload

- Sequential workloads perform well
- Workloads with temporal locality can perform well

In different systems, hardware or OS handles TLB misses

TLBs increase cost of context switches

- Flush TLB on every context switch
- Add ASID to every TLB entry

QUIZ 11: MORE TLBS

<https://tinyurl.com/cs537-sp23-quiz11>



1. What problem(s) can be solved by using ASIDs ?
2. For a hardware-managed TLB miss, which of the following statements are true?
3. For a software-managed TLB miss, which of the following statements are true?

DISADVANTAGES OF PAGING

Additional memory reference to page table → Very inefficient

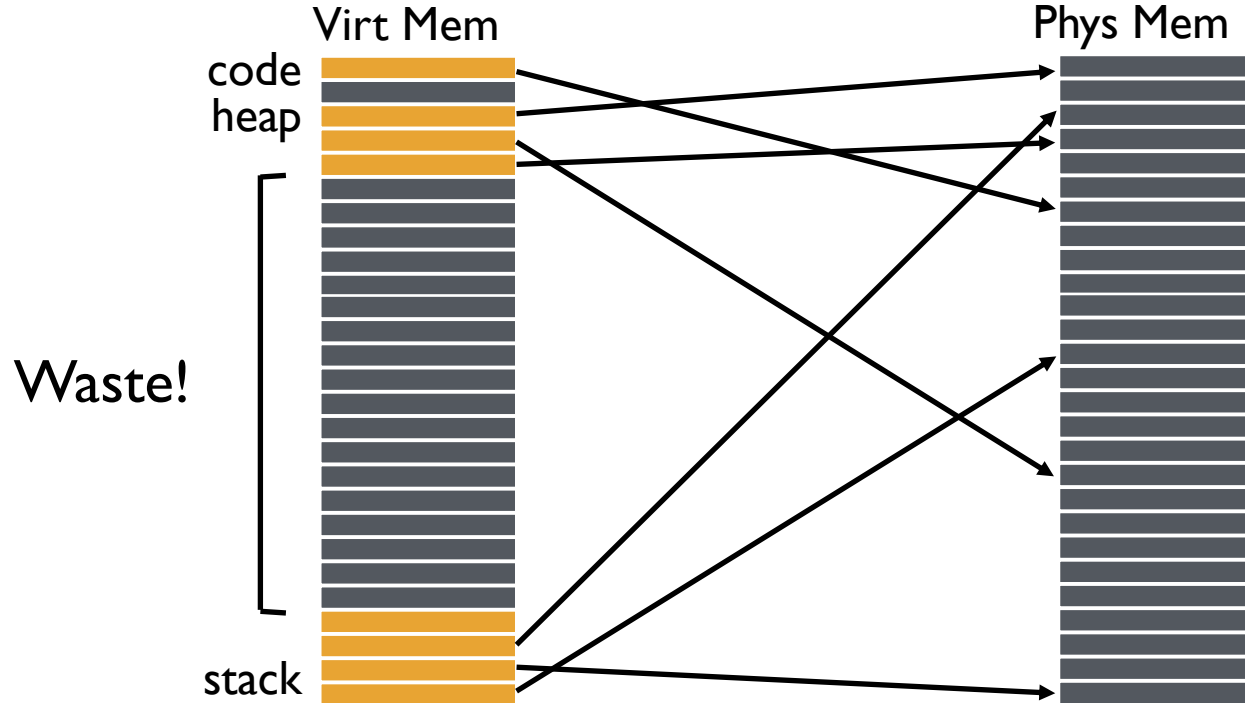
- Page table must be stored in memory
- MMU stores only base address of page table

Storage for page tables may be substantial

- Simple page table: Requires PTE for all pages in address space
Entry needed even if page not allocated ?

SMALLER PAGE TABLES

WHY ARE PAGE TABLES SO LARGE?



MANY INVALID PT ENTRIES

	PFN	valid	prot
	10		r-x
	-	0	-
	23		rw-
	-	0	-
	-	0	-
	-	0	-
	-	0	-
	...many more invalid...		
	-	0	-
	-	0	-
	-	0	-
	-	0	-
	28		rw-
	4		rw-

how to avoid storing these?

AVOID SIMPLE LINEAR PAGE TABLES?

Use more complex page tables, instead of just big array

Any data structure is possible with software-managed TLB

- Hardware looks for vpn in TLB on every memory access
- If TLB does not contain vpn, TLB miss
 - Trap into OS and let OS find vpn->ppn translation
 - OS notifies TLB of vpn->ppn for future accesses

OTHER APPROACHES

1. Multi-level Pagetables
 - Page the page tables
 - Page the pagetables of page tables...
2. Inverted Pagetables

MULTILEVEL PAGE TABLES

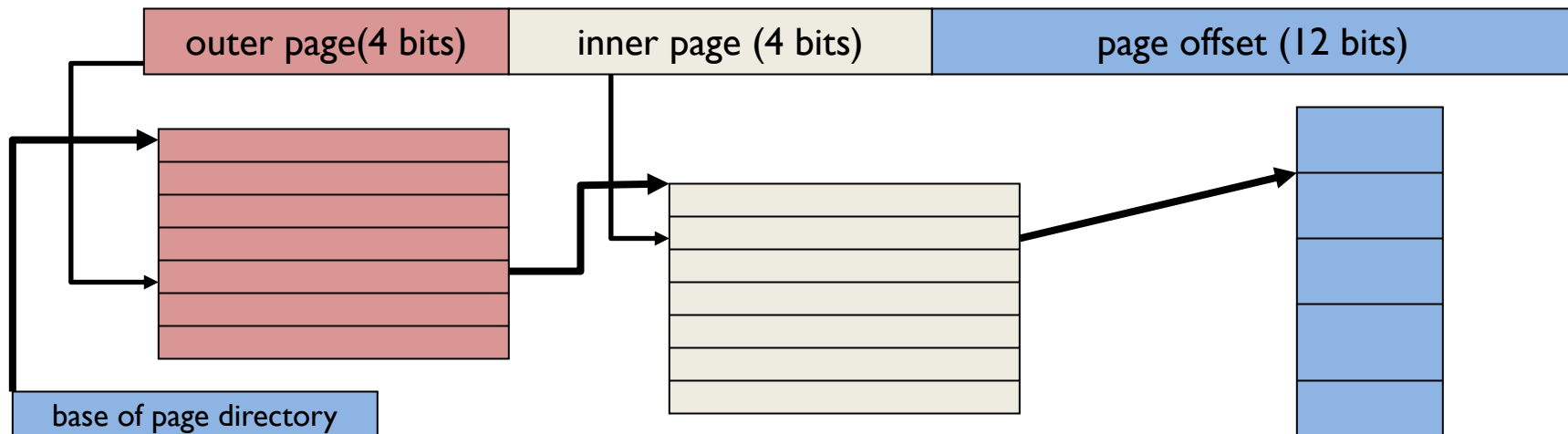
Goal: Allow page table to be allocated non-contiguously

Idea: Page the page tables

- Creates multiple levels of page tables; outer level “page directory”
- Only allocate page tables for pages in use
- Used in x86 architectures (hardware can walk known structure)

MULTILEVEL PAGE TABLES

20-bit address:



ADDRESS FORMAT FOR MULTILEVEL PAGING

30-bit address:



How should logical address be structured? How many bits for each paging level?

Goal?

– Each inner page table fits within a page

– PTE size * number PTE = page size

Assume PTE size = 4 bytes

Page size = 2^{12} bytes = 4KB

→ # bits for selecting inner page =

Remaining bits for outer page:

– $30 - \underline{\quad} - \underline{\quad} = \underline{\quad}$ bits

MULTILEVEL TRANSLATION EXAMPLE

page directory

PPN	valid
0x3	1
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
0x92	1

page of PT (@PPN:0x3)

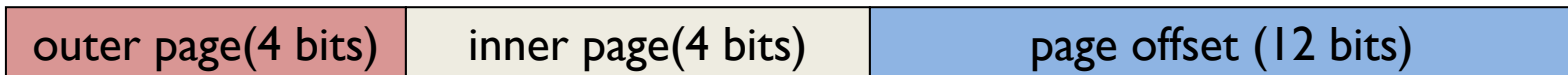
PPN	valid
0x10	1
0x23	1
-	0
-	0
0x80	1
0x59	1
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0

page of PT (@PPN:0x92)

PPN	valid
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
0x55	1
0x45	1

translate 0x01ABC

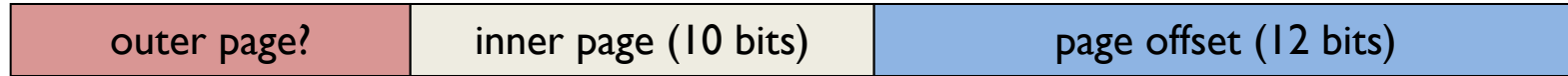
20-bit address:



PROBLEM WITH 2 LEVELS?

Problem: page directories (outer level) may not fit in a page

64-bit address:



Solution:

- Split page directories into pieces
- Use another page dir to refer to the page dir pieces.



How large is virtual address space with 4 KB pages, 4 byte PTEs,
(each page table fits in page)

4KB / 4 bytes → 1K entries per level

1 level:

2 levels:

3 levels:

FULL SYSTEM WITH TLBS

On TLB miss: lookups with more levels more expensive

Assume 3-level page table

Assume 256-byte pages

Assume 16-bit addresses

Assume ASID of current process is 211

ASID	VPN	PFN	Valid
211	0xbb	0x91	1
211	0xff	0x23	1
122	0x05	0x91	1
211	0x05	0x12	0

How many physical accesses for each instruction? (Ignore ops changing TLB)

(a) 0xAA10: movl 0x1111, %edi

(b) 0xBB13: addl \$0x3, %edi

(c) 0x0519: movl %edi, 0xFF10

INVERTED PAGE TABLE

Only store entries for virtual pages w/ valid physical mappings

Naïve approach:

Search through data structure $\langle \text{ppn}, \text{vpn} + \text{asid} \rangle$ to find match

Too much time to search entire table

Better:

Find possible matches entries by hashing $\text{vpn} + \text{asid}$

Smaller number of entries to search for exact match

Managing inverted page table requires software-controlled TLB

QUIZ 12

<https://tinyurl.com/cs537-sp23-quiz12>



Consider a virtual address space of 16KB with 64-byte pages.

1. How many bits will we have in our virtual address for this address space?
2. What is the total number of entries in the Linear Page Table for such an address space?
3. Consider a two-level page table now with a page directory. How many bits will be used to select the inner page assuming PTE size = 4 bytes?

QUIZ12

page directory

PPN	valid
0x3	1
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
0x92	1

page of PT (@PPN:0x3)

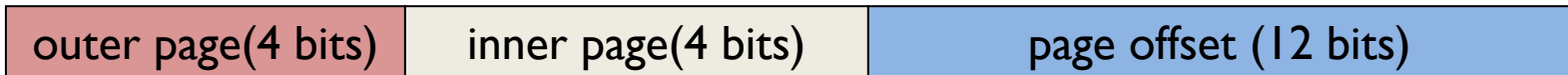
PPN	valid
0x10	1
0x23	1
-	0
-	0
0x80	1
0x59	1
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0

page of PT (@PPN:0x92)

PPN	valid
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
-	0
0x55	1
0x45	1

translate 0xFEED0

20-bit address:



SUMMARY: BETTER PAGE TABLES

Problem: Simple linear page tables require too much contiguous memory

Many options for efficiently organizing page tables

If OS traps on TLB miss, OS can use any data structure

- Inverted page tables (hashing)

If Hardware handles TLB miss, page tables must follow specific format

- Multi-level page tables used in x86 architecture
- Each page table fits within a page

NEXT STEPS

Project 3: In progress

Next class: Swapping!