

CS525 Open-Book Final Exam

Tuesday, May 14, 1996
12:25 p.m., 594 Van Hise

Answer all questions: 1, 2, 3a, 3b. If any question is missing from your sheets, inform the instructor.

Problems 1 and 2 can be solved by 2 pivots each.

Last Name (Print): _____

First Name: _____

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Grades

1. **Question 1:**—————
2. **Question 2:**—————
3. **Question 3:**—————
4. **Total:**—————

1. (10 points)

$$\begin{array}{ll} \text{minimize} & x_1^2 - x_1x_2 + \frac{x_2^2}{2} - 3x_1 + 2x_2 \\ \text{subject to} & -4x_1 + 3x_2 \geq -9 \\ & 5x_1 + 2x_2 \geq 1 \\ & x_1, x_2 \geq 0 \end{array}$$

Problem 1 Sheet

2. (10 points) Solve for all values of the parameter t in the interval $(-\infty, \infty)$. Fill in the summary table on the next page with three columns: parameter t range, minimum value $z(t)$ and solution point $x(t)$.

$$\begin{array}{ll} \text{minimize} & x_1 + x_2 + t\left(\frac{x_1}{2} - x_2\right) \\ \text{subject to} & x_1 - x_2 \geq -1 \\ & x_1 - 2x_2 \geq -4 \\ & x_1, x_2 \geq 0 \end{array}$$

3. (10 points) For each claim below, state first whether it is **true** or **false**. Then in no more than two or three sentences justify your answer. An unjustified “True” or “False” answer gets no credit.

(3a)(5 points) Let A be an $m \times n$ matrix. There exist $x \in R^n$ and $u \in R^m$ such that

$$Ax > 0, A'u = 0, 0 \neq u \geq 0$$

Check one: **True:** **False:**

(3b)(5 points) The LCP

$$0 \leq x \perp Mx + q \geq 0$$

always has a solution when M is a Z -matrix.

Check one: **True:** **False:**