

#### CS 540 Introduction to Artificial Intelligence Unsupervised Learning I

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Based on slides by Fred Sala

# Recap of Supervised/Unsupervised

#### Supervised learning:

- Make predictions, classify data, perform regression
- Dataset:  $(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_n, y_n)$

Features / Covariates / Input

Labels / Outputs

• Goal: find function  $f: X \to Y$  to predict label on **new** data







indoor

outdoor

# Recap of Supervised/Unsupervised

#### **Unsupervised** learning:

- No labels; generally won't be making predictions
- Dataset:  $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n$
- Goal: find patterns & structures that help better understand data.



Mulvey and Gingold

# Recap of Supervised/Unsupervised

Note that there are **other kinds** of ML:

- Mixtures: semi-supervised learning, self-supervised
  - Idea: different types of "signal"
- Reinforcement learning
  - Learn how to act in order to maximize rewards
  - Later on in course...



# Outline

- Intro to Clustering
  - Clustering Types, Centroid-based, k-means review
- Hierarchical Clustering
  - Divisive, agglomerative, linkage strategies

# **Unsupervised Learning & Clustering**

- Note that clustering is just one type of unsupervised learning (UL)
  - PCA is another unsupervised algorithm
- Estimating probability distributions also UL (GANs)
- Clustering is popular & useful!



StyleGAN2 (Kerras et al '20)

# **Clustering Types**

Several types of clustering

#### **Partitional**

- Centroid
- Graph-theoretic
- Spectral

#### **Hierarchical**

- Agglomerative
- Divisive

#### **Bayesian**

- Decision-based
- Nonparametric





- k-means is an example of partitional **center-based**
- Recall steps: **1.** Randomly pick k cluster centers



• 2. Find closest center for each point



• 3. Update cluster centers by computing centroids



• Repeat Steps 2 & 3 until convergence



# **Hierarchical Clustering**

Basic idea: build a "hierarchy"

- Want: arrangements from specific to general
- One advantage: no need for k, number of clusters.
- Input: points. Output: a hierarchy
  - A binary tree



Credit: Wikipedia

## Agglomerative vs Divisive

Two ways to go:

- Agglomerative: bottom up.
  - Start: each point a cluster. Progressively merge clusters
- Divisive: top down
  - Start: all points in one cluster. Progressively split clusters



Agglomerative. Start: every point is its own cluster



Get pair of clusters that are closest and merge



**Repeat:** Get pair of clusters that are closest and merge



**Repeat:** Get pair of clusters that are closest and merge



# Merging Criteria

Merge: use closest clusters. Define closest?

• Single-linkage

$$d(A, B) = \min_{x_1 \in A, x_2 \in B} d(x_1, x_2)$$

• Complete-linkage

$$d(A, B) = \max_{x_1 \in A, x_2 \in B} d(x_1, x_2)$$

• Average-linkage

$$d(A,B) = \frac{1}{|A||B|} \sum_{x_1 \in A, x_2 \in B} d(x_1, x_2)$$

We'll merge using single-linkage

- 1-dimensional vectors.
- Initial: all points are clusters



We'll merge using single-linkage





Continue...

$$d(C_1, C_2) = d(2, 4) = 2$$
  
 $d(C_2, \{7.25\}) = d(5, 7.25) = 2.25$ 



#### Continue...





We'll merge using complete-linkage

- 1-dimensional vectors.
- Initial: all points are clusters



Beginning is the same...



Now we diverge:





## When to Stop?

#### No simple answer:

Use the binary tree (a dendogram)

• Cut at different levels (g different heights/depth

