Q1-1: You are presented with a dataset that has hidden/missing variables that influences your data. You are asked to use Expectation Maximization algorithm to best capture the data.

How would you define the **E** and **M** in Expectation Maximization?

- 1. Estimate the Missing/Latent Variables in the Dataset, Maximize the likelihood over the parameters in the model
- 2. Estimate the number of Missing/Latent Variables in the Dataset, Maximize the likelihood over the parameters in the model
- 3. Estimate likelihood over the parameters in the model, Maximize the number of Missing/Latent Variables in the Dataset
- 4. Estimate the likelihood over the parameters in the model, Maximize the number of parameters in the model

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## Q1-2: Select the correct statement.

- A. The EM algorithm is guaranteed to converge but may not reach a global optimum.
- B. The objective function optimized by the EM algorithm can also be optimized by a gradient descent algorithm which will find the global optimal solution, whereas EM finds its solution more quickly but may return only a locally optimal solution.

- 1. Both the statements are TRUE.
- 2. Statement A is TRUE, but statement B is FALSE.
- 3. Statement A is FALSE, but statement B is TRUE.
- 4. Both the statements are FALSE.

# Q1-2: Select the correct statement.

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- 2. Statement A is TRUE, but statement B is FALSE.
- 3. Statement A is FALSE, but statement B is TRUE.
- 4. Both the statements are FALSE.

For the second statement: The only false part is that the gradient descent algorithm will find the global optimal solution. Gradient descent can also get stuck in a local optima.

## Q2-1: Select the correct statement.

- A. The Chow-Liu algorithm not necessarily always choose edges from a complete graph.
- B. The algorithm tries to find a minimum spanning tree of a graph to minimize the negative loglikelihood of training data.
- C. Edge directions can be assigned randomly in the Chow-Liu algorithm.

- 1. True, True, True
- 2. False, False, True
- 3. True, False, True
- 4. False, False, False

# Q2-1: Select the correct statement.

- A. The Chow-Liu algorithm not necessarily always choose edges from a complete graph.
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- 1. True, True, True
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- 3. True, False, True
- 4. False, False, False



- 2. The algorithm tries to find a maximum spanning tree of a graph to minimize the negative log-likelihood of training data.
- 3. Any directions for edges: Once we pick a node, and edges going away from this node, so that it remains a tree.

Q2-2: Which of the following can NOT be the sequence of edges added, in that order, to a maximum spanning tree using Kruskal's algorithm?

- 1. (c f), (a c), (e f), (b d), (b c)
- 2. (c f), (a c), (e f), (c e), (b d)
- 3. (c f), (a c), (e f), (b d), (d e)
- 4. All of the above are valid.



Q2-2: Which of the following can NOT be the sequence of edges added, in that order, to a maximum spanning tree using Kruskal's algorithm?



(c - f), (a - c), (e - f), (c - e), (b - d) form a cycle.

## Q3-1: Select the correct statement.

- A. Sparse Candidate Algorithm (SCA) is an iterative algorithm.
- B. SCA consists of 2 parts: Restrict Phase and Maximize Phase.
- C. SCA will always lead to a global optimal solution.

- 1. True, True, True
- 2. True, False, True
- 3. True, True, False
- 4. False, True, False

## Q3-1: Select the correct statement.

- A. Sparse Candidate Algorithm (SCA) is an iterative algorithm.
- B. SCA consists of 2 parts: Restrict Phase and Maximize Phase.
- C. SCA will always lead to a global optimal solution.

- 1. True, True, True
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- 3. True, True, False
- 4. False, True, False

SCA can lead to sub-optimal solution.

Q3-2: Recall for Bernoulli distribution: Let X ~ Bern( $\theta$ ), x  $\in$  {0, 1}, 0 <  $\theta$  < 1. Then,  $p_{\theta}(x) = \theta^{x}(1 - \theta)^{1-x}$  and E[X] =  $\theta$ . Consider two bernoulli distributions  $p_{\theta 1}(X)$  and  $p_{\theta 2}(X)$ . Calculate the KL divergence:  $KL(p_{\theta 1}(X) || p_{\theta 2}(X))$ .

- 1.  $\theta_1 \log[\theta_1/\theta_2] + (1 \theta_1) \log[(1 \theta_1)/(1 \theta_2)]$
- 2.  $\theta_2 \log[\theta_1/\theta_2] + (1 \theta_2) \log[(1 \theta_1)/(1 \theta_2)]$
- 3.  $(1 \theta_1) \log[\theta_1/\theta_2] + \theta_1 \log[(1 \theta_1)/(1 \theta_2)]$
- 4.  $(1 \theta_2) \log[\theta_1/\theta_2] + \theta_2 \log[(1 \theta_1)/(1 \theta_2)]$

$$D_{KL}(P(X) || Q(X)) = \sum_{x} P(x) \log \frac{P(x)}{Q(x)}$$

Q3-2: Recall for Bernoulli distribution: Let X ~ Bern( $\theta$ ), x  $\in$  {0, 1}, 0 <  $\theta$  < 1. Then,  $p_{\theta}(x) = \theta^{x}(1 - \theta)^{1-x}$  and E[X] =  $\theta$ . Consider two bernoulli distributions  $p_{\theta 1}(X)$  and  $p_{\theta 2}(X)$ . Calculate the KL divergence:  $KL(p_{\theta 1}(X) || p_{\theta 2}(X))$ .

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- 3.  $(1 \theta_1) \log[\theta_1/\theta_2] + \theta_1 \log[(1 \theta_1)/(1 \theta_2)]$
- 4.  $(1 \theta_2) \log[\theta_1/\theta_2] + \theta_2 \log[(1 \theta_1)/(1 \theta_2)]$

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Log-Likelihood Ratio (LLR)
= \log[p_{\theta_1}(X)/p_{\theta_2}(X)]
= \log[\theta_1^X(1 - \theta_1)^{1-X} / \theta_2^X(1 - \theta_2)^{1-X}]
= X \log[\theta_1/\theta_2] + (1 - X) \log[(1 - \theta_1)/(1 - \theta_2)]
```

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\begin{split} & \mathsf{KL}(\mathsf{p}_{\theta 1}(\mathsf{x}) \mid\mid \mathsf{p}_{\theta 2}(\mathsf{x})) = \mathsf{E}_{\theta 1}(\mathsf{LLR}) \\ & = \mathsf{E}_{\theta 1}[\mathsf{X}] \log[\theta_1/\theta_2] + (1 - \mathsf{E}_{\theta 1}[\mathsf{X}]) \log[(1 - \theta_1)/(1 - \theta_2)] \\ & = \theta_1 \log[\theta_1/\theta_2] + (1 - \theta_1) \log[(1 - \theta_1)/(1 - \theta_2)] \end{split}
```