## \# Exam 3

Name or ID: $\qquad$

## Question 1

[1 points] Given the following confusion matrix, what is the precision for class Dragon?

| Class $\backslash$ Predict | Cat | Dog | Dragon |
| :--- | :--- | :--- | :--- |
| Cat | 40 | 10 | 0 |
| Dog | 10 | 20 | 10 |
| Dragon | 0 | 0 | 30 |

$\square 3 / 4$
$\square 1 / 2$
$\square 1$
$\square 1 / 4$

Question 2
$\square$ [1 points] What is matrix. $\operatorname{argmax}(\operatorname{axis}=1)$, where matrix = numpy. $\operatorname{array([[1,~2,~3],~[4,~5,~}$ 6]])?
$\checkmark[2,2]$
$\square[1,1,1]$
$\square[2,2,2]$
$\square$ $[3,3]$

## Question 3

[1 points] There are 4 documents, and 3 of these documents contain the token "Groot". In document 1, there are 10 tokens in total, and 5 of them are "Groot". What is the bag of words feature (without normalization) of document 1 feature "Groot"?


5



10

Question 4
[1 points] What is a valid simplification of numpy. linalg. solve ( $X, X @ y$ ), assuming the code runs without error (and numerical instability)?

[1 points] The shape of $A$ is $(3,2)$, the shape of $B$ is $(3,3)$, and the shape of $C$ is $(4,3)$. What is the shape of A @ B @ C?
?
$(3,3)$
$(4,2)$
(Error)
$(2,4)$

## Question 6

[1 points] If $x 0$ has two columns, and $x=$ sklearn.preprocessing.PolynomialFeatures(2).fit_transform( x 0 ) is used as the design matrix, how many weights (include coefficients and biases or intercepts) will a linear regression estimate?

[1 points] af has 10 columns and 5 rows. After applying $p=\operatorname{PCA}(3)$ and $p$.fi t(df), what is the shape of p. components_? Note: the rows of p. components_ are the principal components.
$(3,10)$
$(3,5)$
$(5,3)$
$(10,3)$

Question 8
[1 points] Given points [[1], [2], [3], [4]] and starting centroids [0] and [7], what are the centroids after the first iteration of assigning points and updating centroids, using the iterative K-Means Clustering algorithm with Manhattan distance?

$[0,7]$
$\square[1,3]$
$[2,4]$
$\square$ [1.5, 3.5]

## Question 9

[1 points] The gradient vector dw at [w1, w2, w3, w4] $=[-1,1,2,-2]$ is $[2,-2,-1,1]$, if gradient descent $w=w-$ alpha * dw is used, which variable will increase by the largest amount in the next iteration?

w1

## Question 10

[1 points] Suppose $d x y=$ skimage.filters.sobel(img) produces the $d x y$ matrix in the following table. To highlight the edge pixels in the original image in green, image[ $\mathrm{dxy}>\mathrm{t}]=[0,255,0]$ is used, and 2 pixels are highlighted. Which value of $t$ is used?

| 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 |
| 0 | 0.5 | 0.75 | 0 |
| 0 | 0 | 0 | 0 |

[^0]Question 11
$\square$ [1 points] One-vs-one support vector machines are trained and produce the following the confusion matrix. How many training items are used in training the " 0 vs 2 " support vector machine?

| Count | Predict 0 | Predict 1 | Predict 2 |
| :--- | :--- | :--- | :--- |
| Class 0 | 10 | 20 | 10 |
| Class 1 | 0 | 10 | 0 |
| Class 2 | 10 | 0 | 10 |

$\square$
70

6010
$\square$
40
$\square$ Question 12
[1 points] The 3-fold cross validation accuracy for four different neural networks is summarized below. Which model is the most preferred one based on cross validation accuracy?

| Network | Fold 1 accuracy | Fold 2 accuracy | Fold 3 accuracy |
| :--- | :--- | :--- | :--- |
| $W$ | 0.5 | 0.5 | 0.5 |
| $X$ | 0.6 | 0.8 | 1 |
| $Y$ | 0.7 | 0.8 | 0.9 |
| $Z$ | 0.8 | 0.8 | 0.8 |



$\square \mathrm{W}$
Z
[1 points] What is the optimal solution [x1, x2] to the linear program max x1 + 2 * x2 subject to x1 $+\mathrm{x} 2<=1$ and $\mathrm{x} 1>=0 \times 2>=0$ ?
$\square$ $[1,1]$
$\square$ $[0,0]$
$[1,0]$
$[0,1]$

## Question 14

[1 points] Suppose the standard form of a linear program max c @ x subject to A @ x <= band x$\rangle=$ 0 has len $(c)=5, A$. shape $=(3,5)$, and $\operatorname{len}(b)=3$. What is the number of dual variables len $(y)$ ? Note: the dual problem is min $b$ @ $y$ subject to $A$ ' @ $y>=c$ and $y>=0$ where ' means transpose.


1
$\checkmark 3$
15
$\square$
5
[1 points] Suppose all the random vectors generated from a multivariate normal distribution are on the same line, using numpy. random.multivariate_normal([0, 0], [[1, c], [c, 4]], 1000). What is the value of $c$ ?


0

Question 16
[1 points] Consider a Markov chain with the following transition matrix with three states [0, 1,2 ]. What is the probability a sequence $[0,0,2]$ is observed (given it starts with 0 )?

| From $\backslash$ To | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0.5 | 0.5 |
| 2 | 0.5 | 0 | 0.5 |

$\square$ 0.25
0.5


## Question 17

[1 points] For a logistic regression $1 r$, if $1 r$.predict_proba( $x$ ) for some item $x$ is $[0.3,0.5,0.2$ ], what is lr.predict ( $x$ ) for the same $x$ ?


1


Question 18
[1 points] What is the complete linkage Manhattan distance between c1 = [[5], [4], [0]] and c2 = [[2], [1]]? Note: c1 is a cluster with 3 points and c2 is a cluster with 2 points.
$\square$
2
$\square$
3
1
4

## Question 19

[1 points] Given the principal components $u 1=[0,0,1], u 2=[1,0,0], u 3=[0,1,0]$, and the PCA (principal component analysis) features of an item $x$ is $y=[-1,0,1]$, what is $x$ ?$[-1,0,1]$
$[1,1,1]$
$[0,1,-1]$
$\square[1,0,-1]$

Question 20
[1 points] If you think any of the questions are not clear or incorrect, please explain here; otherwise, enter "none". Please do not leave the answer blank:
none

END OF EXAM

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[^0]:    0.8
    $\square 0.25$
    $\square$
    $\square$ 0.7

