

M16

Q 1, 11, 12, 13

Q 9, 4, 2, 8

Q1

10 persons

A(1)\B(9)	Y(≥ 1 report) $1-(1-q)^9$	N $(1-q)^9$
Y (p)	5-3	5-3
N (1-p)	5	0

(p=q)

Expected reward of A: $p \cdot 2 + (1-p) \cdot 5 \cdot (1-(1-q)^9)$

$$dA/dp = 2 - 5(1-(1-q)^9) = -3 + 5 \cdot (1-q)^9 = 0 \Rightarrow (1-q)^9 = 3/5$$

$$(1-q)^{10} = (3/5)^{(10/9)}$$

Q11

-7. (-4, -3, -2, 8, 10)

$x > -1$ (-4+3)

Q12

$+ (+2)$	$- (+1)$	$+ (+2)$
$- (-1)$	$- (-4)$	$- (+1)$
$- (-2)$	$- (-1)$	$+ (+2)$

Q13

- 19 R F

N firm to R

From N firm who pollute the river: $15*N \rightarrow 10*(N-1)+60$

From 19-N firm who build filter: $10*N+60 \rightarrow 15*(N+1)$

$$15*N \leq 10*(N-1)+60. \quad 5N \leq 50$$

$$10*N+60 \leq 15*(N+1). \quad 45 \leq 5N$$

$$N = 9 \text{ or } N = 10$$

Q9

A \ B	I	II	III	IV
I	3, -10	11, -8	7, -7	6, -5
II	7, -3	13, -3	13, -6	8, -2
III	0, -9	7, -4	5, -11	3, -8
IV	8, -1	11, -6	12, -9	5, 2

For player A, action 2 is strictly better than action 1
For player B, action 4 is strictly better than action 3

Q4

Row \ Col	L	R
U (p)	9,5	9,0
D (1-p)	9,0	0,10

If the C player choose L, Row do not care about p

If the C player choose R \rightarrow Row will have $p = 1 \rightarrow$ C player choose L

When will C player choose L?

Expect reward for C(C choose L with 100%) = $p*5$

Expect reward for C(C choose R with 100%) = $(1-p)*10$

$R(\text{C choose L}) \geq R(\text{C choose R})$

$P*5 \geq (1-P)*10$

$P \geq 2/3$

$P \leq 1$

Q2

- 266
- Long (266-N): 1. $1 \rightarrow (N+1)/19$
- Direct (N): $n/19$. $N/19 \rightarrow 1$

- $1 \leq (N+1)/19$ $18 \leq N$
- $N/19 \leq 1$. $M \leq 19$

- $N = 18$ or $N = 19$
- $266 - N$

Q8

Romeo \ Juliet	Bach (q)	Stravinsky (1-q)
Bach (p)	6, 3 (pq)	0, 0 (p(1-q))
Stravinsky (1-p)	0, 0. ((1-p)q)	3, 6 ((1-p)(1-q))

First P

Second Q

First cannot find better P conditioned on Q

Second cannot find better Q conditioned on P

Expected reward for R player: $p \cdot q \cdot 6 + (1-p) \cdot (1-q) \cdot 3$

Expected reward for C player: $p \cdot q \cdot 3 + (1-p) \cdot (1-q) \cdot 6$

$dR's \text{ Reward}(p)/dp = q \cdot 6 - (1-q) \cdot 3 = 0. \quad q=1/3$

$dC's \text{ Reward}(q)/dq = p \cdot 3 - (1-p) \cdot 6 = 0. \quad p=2/3$

$$2/9 \cdot 6 + 2/9 \cdot 3 = 2$$

$$w * x + b = [w, b] * [x, 1]. \text{ Who wio}$$

$$X \rightarrow x * w_1 + b_1 = [x, 1] * w_{ih} \rightarrow \text{sigmoid} \rightarrow \text{hidden (28)}$$

$$\text{hidden (28)} \rightarrow \text{hidden} * w_2 + b_2 = [\text{hidden}, 1] * w_{ho} \rightarrow \text{value} [-\text{inf}, +\text{inf}]$$

$$(\text{value} - \Rightarrow 0; \text{value} + \Rightarrow 1) \rightarrow \text{sigmoid} \rightarrow \text{pre} \in [0, 1] \quad y \in \{0, 1\} \quad (\text{value} < 0.5 \Rightarrow 0, \text{value} > 0.5 \Rightarrow 1)$$

$$\text{Loss} = \text{Loss}(\text{pre}, y) = \text{crossentropy}$$

$$\text{Gradient } d \text{ loss} / d w_1$$

$$D \text{ loss} / d b_1$$

$$\text{Sigmoid}(x) = \text{return } 1 / (1 + e^{-x})$$

$$\text{Sigmoid} \rightarrow \text{function return } [0, 1] \rightarrow 0, 1$$

$$[-\text{inf}, +\text{inf}]$$