CS540 Introduction to Artificial Intelligence

Lecture 11

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June 27, 2022

Coordination Game

Quiz

Exam Date

Admin

Exam Format

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Exam Formula Sheet

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Review Session

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Image Features Diagram

Motivation

One Dimensional Convolution

Definition

- The convolution of a vector $x = (x_1, x_2, ..., x_m)$ with a filter $w = (w_{-k}, w_{-k+1}, ...w_{k-1}, w_k)$ is:

$$a = (a_1, a_2, ..., a_m) = x * w$$

$$a_j = \sum_{t=-k}^{k} w_t x_{j-t}, j = 1, 2, ..., m$$

- w is also called a kernel (different from the kernel for SVMs).
- The elements that do not exist are assumed to be 0.

Two Dimensional Convolution

Definition

- The convolution of an $m \times m$ matrix X with a $(2k+1) \times (2k+1)$ filter W is:

$$A = X * W$$

$$A_{j,j'} = \sum_{s=-k}^{k} \sum_{t=-k}^{k} W_{s,t} X_{j-s,j'-t}, j, j' = 1, 2, ..., m$$

- The matrix W is indexed by (s, t) for $s = -k, -k+1, ..., k-1, k$ and $t = -k, -k+1, ..., k-1, k$.
- The elements that do not exist are assumed to be 0.

Convolution Diagram and Demo

Definition

Image Gradient

Definition

- The gradient of an image is defined as the change in pixel intensity due to the change in the location of the pixel.

$$\frac{\partial I(s,t)}{\partial s} \approx \frac{I\left(s+\frac{\varepsilon}{2},t\right)-I\left(s-\frac{\varepsilon}{2},t\right)}{\varepsilon}, \varepsilon = 1$$

$$\frac{\partial I(s,t)}{\partial t} \approx \frac{I\left(s,t+\frac{\varepsilon}{2}\right)-I\left(s,t-\frac{\varepsilon}{2}\right)}{\varepsilon}, \varepsilon = 1$$

Image Derivative Filters

Definition

- The gradient can be computed using convolution with the following filters.

$$w_x = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}, w_y = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$

Sobel Filter

Definition

- The Sobel filters also are used to approximate the gradient of an image.

$$W_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, W_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

Gradient of Images

Definition

- The gradient of an image I is $(\nabla_x I, \nabla_y I)$.

$$\nabla_x I = W_x * I, \nabla_y I = W_y * I$$

- The gradient magnitude is G and gradient direction Θ are the following.

$$G = \sqrt{\nabla_x^2 + \nabla_y^2}$$

$$\Theta = \arctan\left(\frac{\nabla_y}{\nabla_x}\right)$$

Gradient of Images Demo

Definition

Convolution Example

Quiz

Gradient Example

Quiz

Convolution Example 1

Quiz

Convolution Example 2

Quiz

SIFT

Discussion

- Scale Invariant Feature Transform (SIFT) features are features that are invariant to changes in the location, scale, orientation, and lighting of the pixels.

Histogram Binning Diagram

Discussion

HOG

Discussion

Classification

Discussion

- SIFT features are not often used in training classifiers and more often used to match the objects in multiple images.
- HOG features are usually computed for every cell in the image and used as features (in place of pixel intensities) in classification algorithms such as SVM.