CS540 Introduction to Artificial Intelligence Lecture 18

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Based on lecture slides by Jerry Zhu, Yingyu Liang, and Charles Dyer

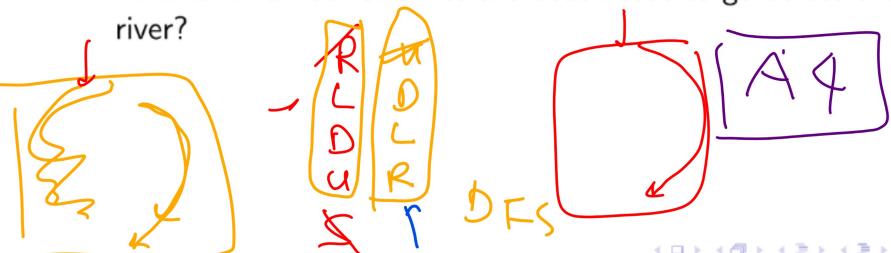
August 1, 2022

River Crossing Problem

Quiz



 Three married couples (husbands and wifes) need to cross the river. The boat requires at least one person to operate and holds no more than two people. No woman can be in the presence of another man unless her husband is also present (this is called the Jealous Husband Problem). What is the minimum number of times the boat needs to go across the



Homework Admin

7-dy M9 next

- M8 to M11 and P4 to P5 due dates all moved by one week: sorry about the delay in getting them ready on time.
 - M9 and M10 are ready, you should be able to do both after today's lecture.
 - P5 is updated (please refresh the page), you should be able to solve all questions after today's lecture.
- X3 to X5 videos not finished yet: I will try to post them later this week.

Summary

Discussion

- Search:
 - Uniformed: Breadth first search \rightarrow Add states at the end \rightarrow Remove states from the front \rightarrow Complete + Optimal.
 - Uniformed: Depth first search \rightarrow Add states to the front Remove states to the front \rightarrow Incomplete + Not optimal.
 - Uniformed: Itervative deepening search \rightarrow DFS with depth $\frac{Opt}{Sol_n}$ Sol_n

initial

State

ncitom

- Informed: Uniform cost search.
- Informed: Best first greedy search.
- Informed: A search.
- Informed: A star search.

Uniformed vs. Informed Search Motivation

- Uninformed search means only the goal G and the successor functions s' are given.
- Informed search means which non-goal states are better is also known.

Heuristic Diagram Motivation

Uniform Cost Search Description

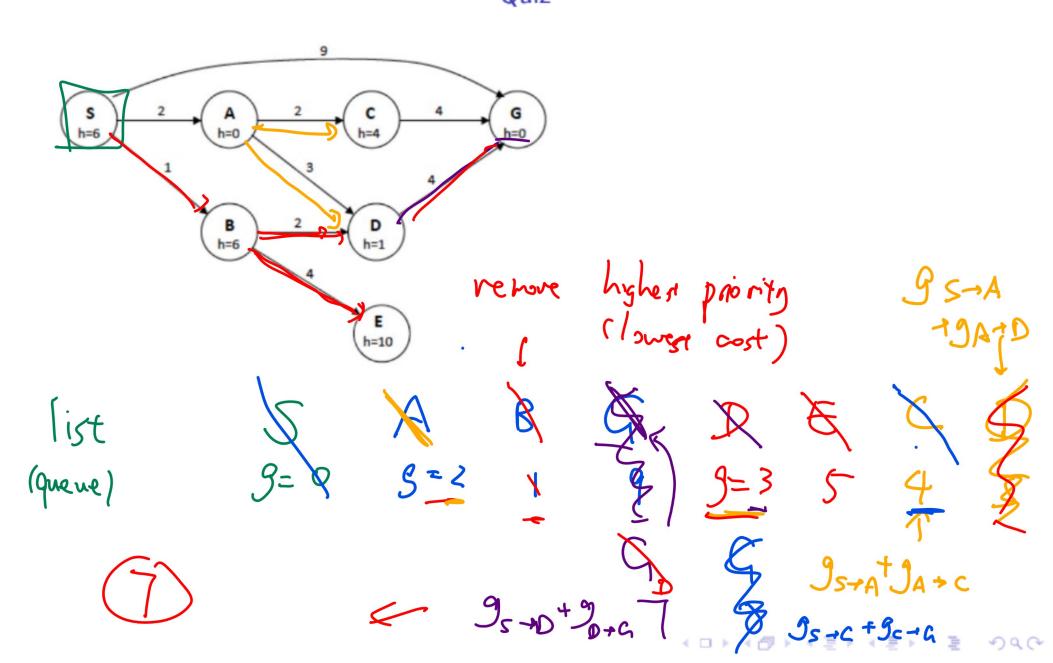
- Expand the vertices with the lowest current path cost g (s) first.
- It is BFS with a priority queue based on g(s).
- It is equivalent to BFS if c = 1 is constant on all edges.
- It is also called Dijkstra's Algorithm.

UCS Example 1 Quiz

 Given the following adjacency matrix. Find UCS expansion path.

[i i	S	А	В	С	D	Ε	G
S	h = 6	2	1	_	_	_	9
Α	_	h = 0	_	2	3	_	_
В	_	_	h = 6	_	2	4	_
C	-	_	_	h=4	-	_	4
D	_	_	— 7	_	h = 1	_	4
E	1	_	_	_	1—	h = 10	_
G	_	-	_	_	_	_	h = 0

UCS Example 1 Diagram



UCS Example 1 Expansion Path

- In last year's lecture, multiple copies of the same state with different costs can be inserted into the frontier at the same time: that is not the standard practice.
- The same state with a lower cost should replace the copy in the frontier. If you refer to solutions or videos from last year, please note this change.

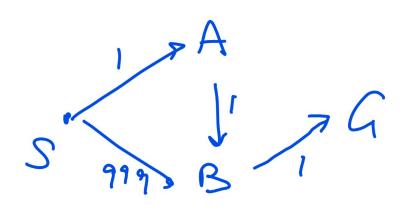
UCS Example 2

Quiz

• Find UCS expansion path, ist of removed states									
	_	5	Α	В	G	15			
	S	h=3	1	999	_				
Q_{2}	Α	_	h = 1000	1	_				
	В	_	_	h = 1	1				
	G		_		h = 0				

- A: S, A, B, G
- B: S, B, G
- C: S, B, A, G
- D: S, B, A, B, G

E: I don't inderford,



UCS Example 2 Diagram

Uniform Cost Search Performance

Discussion

UCS is complete.

UCS is optimal with any c.

Best First Greedy Search

Description

- Expand the vertices with the lowest heuristic cost h(s) first.
- Use a priority queue based on h(s).
- BFGS is not an abbreviation of Best First Greedy Search: BFGS is the Broyden Fletcher Goldfarb Shanno algorithm (a version of gradient descent).

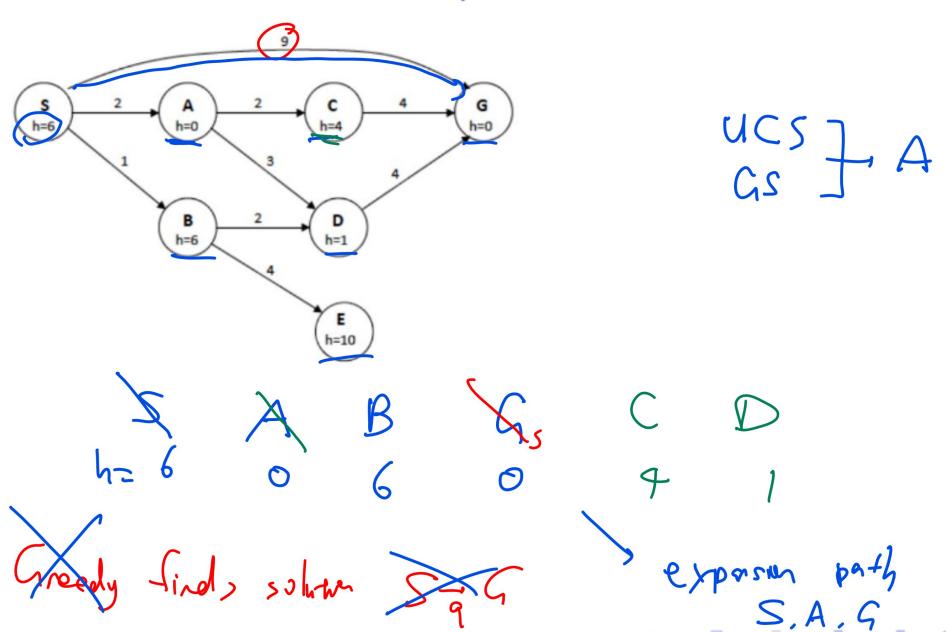
Greedy Example 1 Quiz

 Given the following adjacency matrix. Find Greedy Search expansion path.

	S	А	В	С	D	Ε	G
S	h = 6	2	1	_	_	_	9
Α	_	h = 0	_	2	3	_	_
В	1—	_	h=6	_	2	4	_
С	_	_	_	h = 4	-	_	4
D		_	_	_	h = 1	_	4
E	1	_	_	_	1 —	h = 10	_
G	_	_	_	_	_		h = 0

Greedy Example 1 Diagram

Quiz



Greedy Example 2

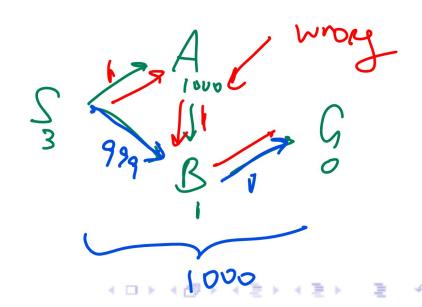
Find Greedy expansion path

_	S	Α	В	G
S	h = 3	1	999	_
Α	_	h = 1000	1	_
В	_	_	h = 1	1
G	_	_	_	h = 0



- A: S, A, B, G
- B : S, B, G
- C: S, B, A, G
- D: S, B, A, B, G

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Greedy Example 2 Diagram

Quiz









Best First Greedy Search Performance

- Greedy is incomplete.
- Greedy is not optimal.

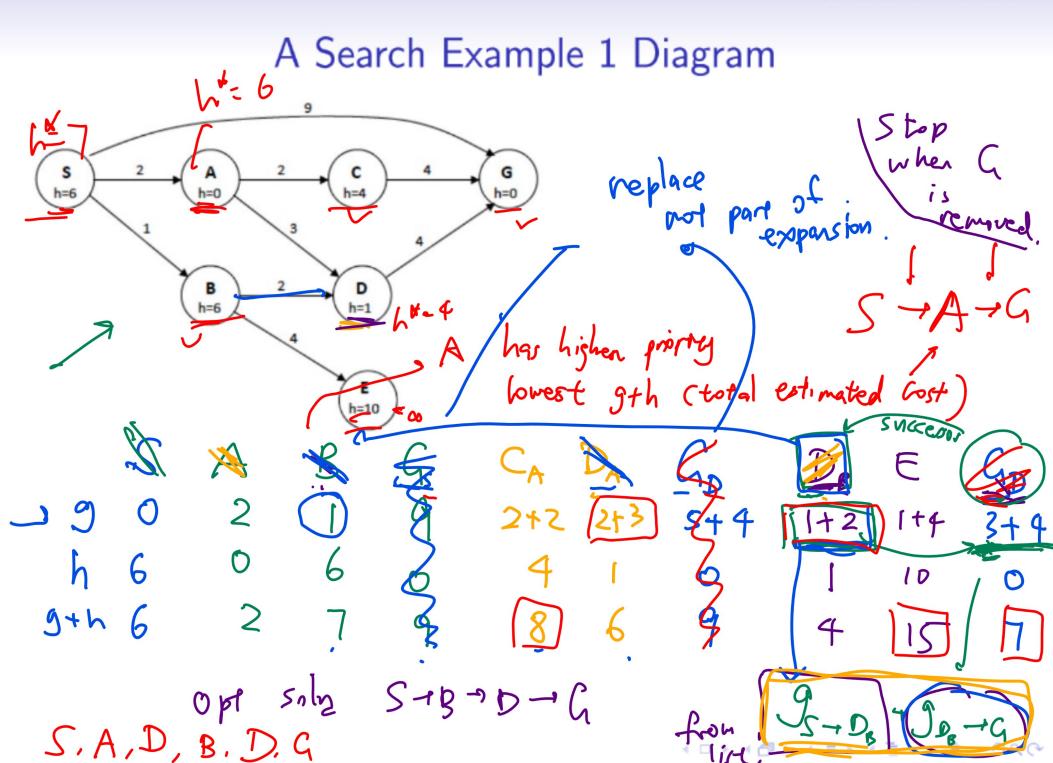


- Expand the vertices with the lowest total cost g (s) + h (s) first.
- Use a priority queue based on g(s) + h(s).
- A stands for Always be optimistic?

A Search Example 1

 Given the following adjacency matrix. Find A Search expansion path.

_	S	А	В	С	D	Ε	G
S	h = 6	2	1	_	_	_	9
Α	_	h = 0	_	2	3	_	_
В	-	_	h=6	_	2	4	_
C	_	_	_	h = 4	-	_	4
D	_	_	— 7	_	h = 1	_	4
E	1	_				h = 10	
G	_	_	_	_	_	_	h=0





from diagram

SABCDEG

Find A search expansion path

-	
17:	Lo

_	S	Α	В	G
S	h = 3	1	999	_
Α	_	h = 1000	1	_
В	_	_	h = 1	1
G			_	h = 0

Q4

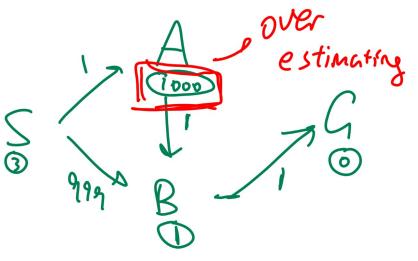
• A: S, A, B, G

• B: S, B, G

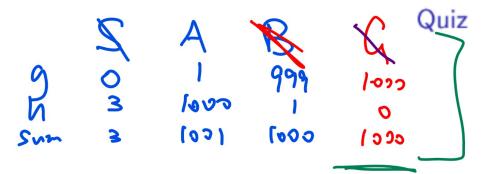
C: S, B, A, G

• D: S, B, A, B, G

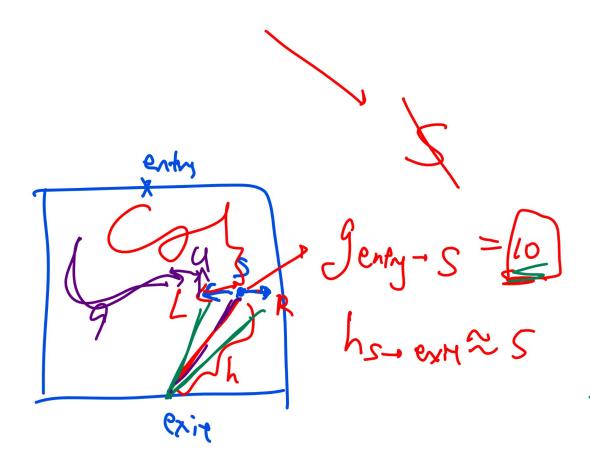


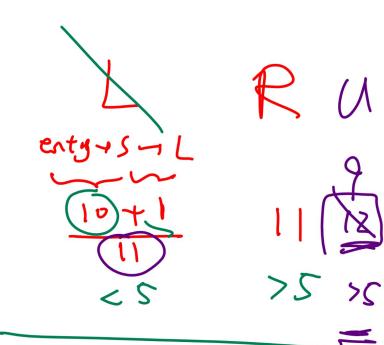


A Search Example 2 Diagram



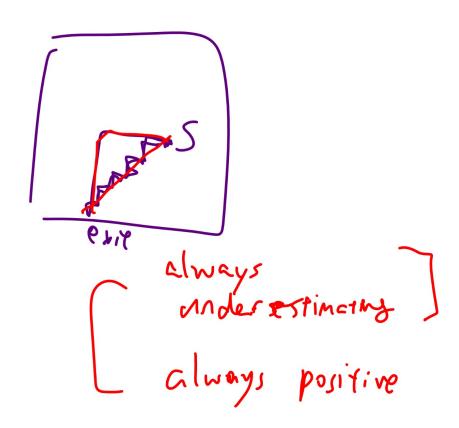






A Search Performance

- A is complete.
- A is not optimal.



A Star Search

Description

• A* search is A search with an admissible heuristic.

Admissible Heuristic

Definition

 A heuristic is admissible if it never over estimates the true cost.

$$0 \leqslant h(s) \leqslant h^{\star}(s)$$

Admissible Heuristic 8 Puzzle Example

Definition

Admissible Heuristic 8 Puzzle Example

- Which ones (select multiple) of the following are admissible heuristic function for the 8 Puzzle?
- $A:h(s) = \text{number of tiles in the wrong position.} \leq h (s)$
- $\frac{b}{a} \frac{h(s) = 0}{h(s)} \rightarrow \frac{1}{a} 4(5) \leq \frac{1}{a} 4(5)$
- D: h(s) = sum of Manhattan distance between each tile and its goal location.
- its goal location. • E:h(s)= sum of Euclidean distance between each tile and its goal location.

A Star Search Example 1

 Given the following adjacency matrix. Find A Star Search expansion path.

	S	А	В	С	D	Ε	G
S	h = 6	2	1	_	_	_	9
Α	_	h = 0	_	2	3	_	_
В	1—	_	h=6	_	2	4	_
С	_	_	_	h = 4	-	_	4
D	· —	_	_	_	h = 1	_	4
E	1	_	_	_	1 —	h = 10	_
G	_	_	_	_	_		h = 0

A Star Search Example 1 Diagram

Admissible Heuristic General Example 1

Quiz



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• Which ones (select multiple) of the following are admissible heuristic function?

$$\bullet \mathcal{A}: h(s) = h^*(s) \cdot 2 \gg h^*$$

• B:
$$h(s) = \sqrt{h^*(s)} \leq h^*$$

$$(s) = h^*(s) + 1$$

$$D h(s) = \min \{1, h^{\star}(s)\}$$

$$E: h(s) = h^{\star}(s) \cdot \frac{1}{2}$$

$$f(s) = h^{\star}(s)^{2}$$

•
$$h(s) = \max\{1, h^*(s)\}$$

•
$$h(s) = h^*(s) - 1$$

$$) = h^{\star}(s) - 1$$



A Search Performance

- A* is complete.
 A* is optimal.

Iterative Deepening A Star Search



- A* can use a lot of memory.
 - Do path checking without expanding any vertex with $g\left(s\right)+h\left(s\right)>1.$



- Do path checking without expanding any vertex with g(s) + h(s) > 2.
- ...
- Do path checking without expanding any vertex with g(s) + h(s) > d.

Iterative Deepening A Star Search Performance Discussion

- IDA* is complete.IDA* is optimal.
- IDA* is more costly than A^* .





Beam Search

- Version 1: Keep a priority queue with fixed size k. Only keep the top k vertices and discard the rest.
- Version 2: Only keep the vertices that are at most ε worse than the best vertex in the queue. ε is called the beam width.



Beam Search Performance

- Beam is incomplete.
- Beam is not optimal.

Summary

- Search:
- Uniformed: Breadth first search.
- Uniformed: Depth first search.
- Uniformed: Itervative deepening search.
- Informed: Uniform cost search \rightarrow Remove states with lowest current cost $(g) \rightarrow$ Complete, Optimal.
- **⑤** Informed: Best first greedy search → Remove states with the lowest heuristic cost (h) → Incomplete, Not optimal.
- o Informed: A search → Remove states with the lowest current plus heuristic cost (g + h) → Complete, Not Optimal.
- Informed: A star search → admissible heuristic (under-estimates true cost) → Complete, Optimal