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#### CS540 Introduction to Artificial Intelligence Lecture 18

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Based on lecture slides by Jerry Zhu, Yingyu Liang, and Charles Dyer

August 2, 2022

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### River Crossing Problem

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#### Homework Admin

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#### Summary Discussion

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#### Uniformed vs. Informed Search Motivation

- Uninformed search means only the goal G and the successor functions s' are given.
- Informed search means which non-goal states are better is also known.

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#### Heuristic Diagram

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#### Uniform Cost Search Description

- Expand the vertices with the lowest current path cost g(s) first.
- It is BFS with a priority queue based on g(s).
- It is equivalent to BFS if c = 1 is constant on all edges.
- It is also called Dijkstra's Algorithm.

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### UCS Example 1

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# UCS Example 1 Diagram

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### UCS Example 1 Expansion Path

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### UCS Example 2



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# UCS Example 2 Diagram

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#### Uniform Cost Search Performance

- UCS is complete.
- UCS is optimal with any c.

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#### Best First Greedy Search Description

- Expand the vertices with the lowest heuristic cost h(s) first.
- Use a priority queue based on h(s).
- BFGS is not an abbreviation of Best First Greedy Search: BFGS is the Broyden Fletcher Goldfarb Shanno algorithm (a version of gradient descent).

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### Greedy Example 1

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### Greedy Example 1 Diagram

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#### Greedy Example 2 <sub>Quiz</sub>

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### Greedy Example 2 Diagram

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### Best First Greedy Search Performance

- Greedy is incomplete.
- Greedy is not optimal.

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#### A Search Description

- Expand the vertices with the lowest total cost g(s) + h(s) first.
- Use a priority queue based on g(s) + h(s).
- A stands for Always be optimistic?

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# A Search Example 1 $_{Quiz}$

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### A Search Example 1 Diagram

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#### A Search Example 2 <sub>Quiz</sub>

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# A Search Example 2 Diagram

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#### A Search Performance

Discussion

- A is complete.
- A is not optimal.

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#### A Star Search Description

•  $A^*$  search is A search with an admissible heuristic.

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#### Admissible Heuristic

• A heuristic is admissible if it never over estimates the true cost.

$$0\leqslant h\left(s
ight)\leqslant h^{\star}\left(s
ight)$$

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#### Admissible Heuristic 8 Puzzle Example

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### Admissible Heuristic 8 Puzzle Example

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#### A Star Search Example 1

Quiz

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### A Star Search Example 1 Diagram

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### Admissible Heuristic General Example 1

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#### A Search Performance

Discussion

- A<sup>\*</sup> is complete.
- A<sup>\*</sup> is optimal.

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### Iterative Deepening A Star Search

- $A^*$  can use a lot of memory.
- Do path checking without expanding any vertex with g(s) + h(s) > 1.
- Do path checking without expanding any vertex with g(s) + h(s) > 2.
- ...
- Do path checking without expanding any vertex with g(s) + h(s) > d.

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#### Iterative Deepening A Star Search Performance

- IDA\* is complete.
- IDA\* is optimal.
- IDA<sup>\*</sup> is more costly than  $A^*$ .

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### Beam Search

- Version 1: Keep a priority queue with fixed size *k*. Only keep the top *k* vertices and discard the rest.
- Version 2: Only keep the vertices that are at most ε worse than the best vertex in the queue. ε is called the beam width.

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### Beam Search Performance

- Beam is incomplete.
- Beam is not optimal.

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#### Summary Discussion

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