Auctions

Mechanism Design 0000

▲□▶▲□▶▲≡▶▲≡▶ ≡ めぬる

# CS540 Introduction to Artificial Intelligence Lecture 24

#### Young Wu

Based on lecture slides by Jerry Zhu, Yingyu Liang, and Charles Dyer

August 15, 2022

Auctions 000000000 Mechanism Design 0000

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

# Efficient Market Game

- The last two digits of your ID is your productivity (how much you can help a company produce). Choose between two companies to work for:
- A : you get paid how much you produce (your productivity).
- *B* : you get paid the average productivity of everyone working for this company.

Auctions 000000000 Mechanism Design 0000

▲□▶ ▲□▶ ▲□▶ ▲□▶ ▲□ ● ● ●

# Mechanism Design Problem

- Players have hidden (private) information (type).
- Designer designs a game so that players with different types will choose different actions (thus reveal their type) in an equilibrium.

Auctions 000000000 Mechanism Design 0000

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

## Adversarial Machine Learning

- Motivations:
- Adversarial attack.
- Ø Machine teaching.
- **③** Ethics: equality and fairness.
  - Types of attack:
- Test time.
- **②** Training time: misreport features or labels (misinformation).
- **③** Training time: select subset of data points (disinformation).

Auctions 000000000 Mechanism Design

## Test Time Attack Example

Auctions 000000000 Mechanism Design 0000

▲□▶ ▲□▶ ▲ 三▶ ▲ 三▶ 三三 - のへぐ

#### Misinformation Attack of Linear Regression

Auctions 000000000 Mechanism Design

▲□▶ ▲□▶ ▲ 三▶ ▲ 三▶ 三三 - のへぐ

## Disinformation Attack of Linear Classifiers

Auctions 000000000 Mechanism Design

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

#### Attack Prevention

- Ways to prevent adversarial attacks on machine learning algorithms:
- Regularization (train more general models)
- Ø Mechanism design (implement truthful report).
- 3 Competitive data provider.

Auctions •00000000 Mechanism Design 0000

<□ > < 同 > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ < つ < ○</p>

#### VCG Mechanism

- Vickrey Clarke Groves Mechanism.
- Clarke Pivot Rule: players pay their externality.
- Example: Second Price Sealed Bid Auction.

Mechanism Design 0000

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

#### First Price Sealed Bid Auction

- Enter a bid, the highest bidder gets the object and pay the bid.
- If the value of the object to you is v<sub>i</sub>, and your bid is b<sub>i</sub>, the (net) payoff is:

$$v_i - b_i \text{ if } b_i = \max_j b_j.$$

O otherwise.

Auctions

Mechanism Design

▲□▶ ▲□▶ ▲ 三▶ ▲ 三▶ 三三 - のへぐ

#### First Price Sealed Bid Auction Bid

- $A: b_i > v_i$
- $B: b_i = v_i$
- *C* : *b<sub>i</sub>* < *v<sub>i</sub>*
- $D: b_i = 0$

Mechanism Design 0000

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

## Second Price Sealed Bid Auction

- Enter a bid, the highest bidder gets the object and pay the second highest bid.
- If the value of the object to you is v<sub>i</sub>, and your bid is b<sub>i</sub>, the (net) payoff is:

$$v_i - \max_{j \neq i} b_j \text{ if } b_i = \max_j b_j.$$

O otherwise.

Auctions 000000000 Mechanism Design

▲□▶ ▲□▶ ▲□▶ ▲□▶ □ のQ@

#### Second Price Sealed Bid Auction Bid

- $A: b_i > v_i$
- $B: b_i = v_i$
- *C* : *b<sub>i</sub>* < *v<sub>i</sub>*
- $D: b_i = 0$

Auctions 000000000 Mechanism Design 0000

▲□▶ ▲□▶ ▲□▶ ▲□▶ ▲□ ● ● ●

# All Pay Auction

- Enter a bid, the highest bidder gets the object, but all players pay their bids.
- If the value of the object to you is v<sub>i</sub>, and your bid is b<sub>i</sub>, the (net) payoff is:

$$v_i - b_i \text{ if } b_i = \max_j b_j.$$

2 -  $b_i$  otherwise.

Auctions 0000000000

Mechanism Design

▲□▶ ▲□▶ ▲ 三▶ ▲ 三▶ 三三 - のへぐ

#### All Pay Auction Bid

- $A: b_i > v_i$
- $B: b_i = v_i$
- *C* : *b<sub>i</sub>* < *v<sub>i</sub>*
- $D: b_i = 0$

Auctions 000000000 Mechanism Design 0000

▲□▶ ▲□▶ ▲ 三▶ ▲ 三▶ 三三 - のへぐ

## Incentive Compatibility

• In second price auction, bidders do not have incentive to lie about their value.

Auctions 00000000 Mechanism Design 0000

▲□▶ ▲□▶ ▲□▶ ▲□▶ □ のQで

# Public Good Provision

- Suppose the object is a public good (for example a highway, everyone can enjoy for free).
- The public good is provided if the sum of the bids is higher than the cost of providing the public good.
- Everyone pays the cost of the public good minus the sum of the other bidder's bids.
- The bidders do not have incentive to lie about their values.

Mechanism Design

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

# Insurance Example No Mechanism

- Suppose the probability that you have an accident is proportional to the last two digits of your ID.
- You plan to buy an insurance, the insurance company asks if you are a safe driver.
- If you answer yes: you pay a low insurance premium (e.g.50 dollars).
- If you answer no: you pay a high insurance premium (e.g.100 dollars).
  - A : YES
  - *B* : NO

▲□▶ ▲□▶ ▲□▶ ▲□▶ ▲□ ● ● ●

# Insurance Example Indirect Mechanism

- Suppose the probability that you have an accident is proportional to the last two digits of your ID.
- You plan to buy an insurance, the insurance company asks you to select one of two contracts.
- Contract 1: you pay a low insurance premium (e.g.50 dollars) with a high deductible (e.g.250 dollars).
- Contract 2: you pay a high insurance premium (*e.g.*100 dollars) with a low deductible of (*e.g.*50 dollars).
  - A : Contract 1
  - B : Contract 2

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

## Insurance Example Direct Mechanism

- Suppose the probability that you have an accident is proportional to the last two digits of your ID.
- You plan to buy an insurance, the insurance company asks if you are a safe driver.
- If you answer yes: you pay a low insurance premium (e.g.50 dollars) with a high deductible (e.g.250 dollars).
- **2** If you answer no: you pay a high insurance premium (e.g.100 dollars) with a low deductible of (e.g.50 dollars).
  - *A* : YES
  - *B* : NO

Auctions 000000000 Mechanism Design

▲ロ ▶ ▲周 ▶ ▲ 国 ▶ ▲ 国 ▶ ● の Q @

#### **Revelation Principle**

- Direct mechanism: ask the insurer to report their risk.
- Indirect mechanism: ask the insurer to select a contract.
- Revelation principle says, (under technical conditions), if there is an incentive compatible mechanism, there must be an incentive compatible direct mechanism.