CS 764: Topics in Database Management Systems

Lecture 14: Blink Tree

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Today's Paper: B-tree Locking

Efficient Locking for Concurrent Operations on B-Trees

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The B-tree and its variants have been found to be highly useful (both theoretically and in practice) for storing large amounts of information, especially on secondary storage devices. We examine the problem of overcoming the inherent difficulty of concurrent operations on such structures, using a practical storage model. A single additional "link" pointer in each node allows a process to easily recover from tree modifications performed by other concurrent processes. Our solution compares favorably with earlier solutions in that the locking scheme is simpler (no read-locks are used) and only a (small) constant number of nodes are locked by any update process at any given time. An informal correctness proof for our system is given.

Key Words and Phrases: database, data structures, B-tree, index organizations, concurrent algorithms, concurrency controls, locking protocols, correctness, consistency, multiway search trees
CR Categories: 3.73, 3.74, 4.32, 4.33, 4.34, 5.24

1. INTRODUCTION

The B-tree [2] and its variants have been widely used in recent years as a data structure for storing large files of information, especially on secondary storage devices [7]. The guaranteed small (average) search, insertion, and deletion time for these structures makes them quite appealing for database applications.

A topic of current interest in database design is the construction of databases that can be manipulated concurrently and correctly by several processes. In this

ACM Trans. Database Syst. 1981

Agenda

B-Tree Index

Lock coupling

B^{link}-tree

- Search
- Insert

Optimistic lock coupling (OLC)

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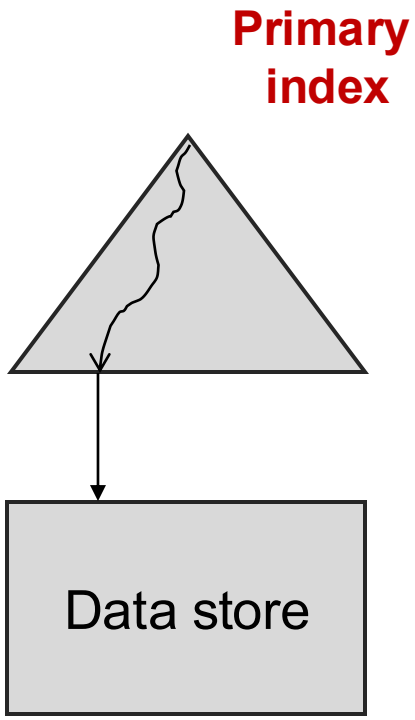
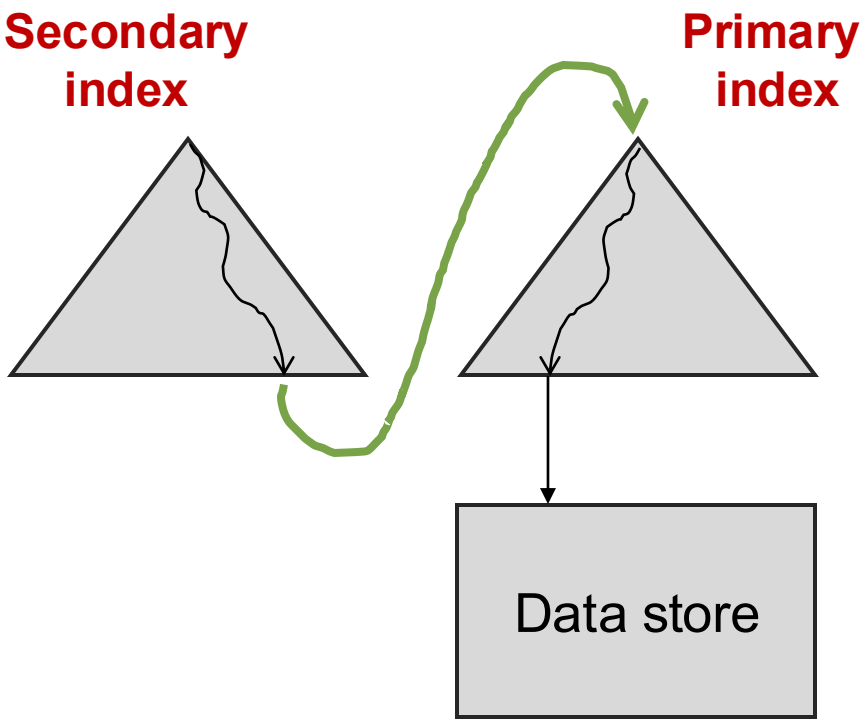


Index

Index: Accelerate data retrieval operations in a database table

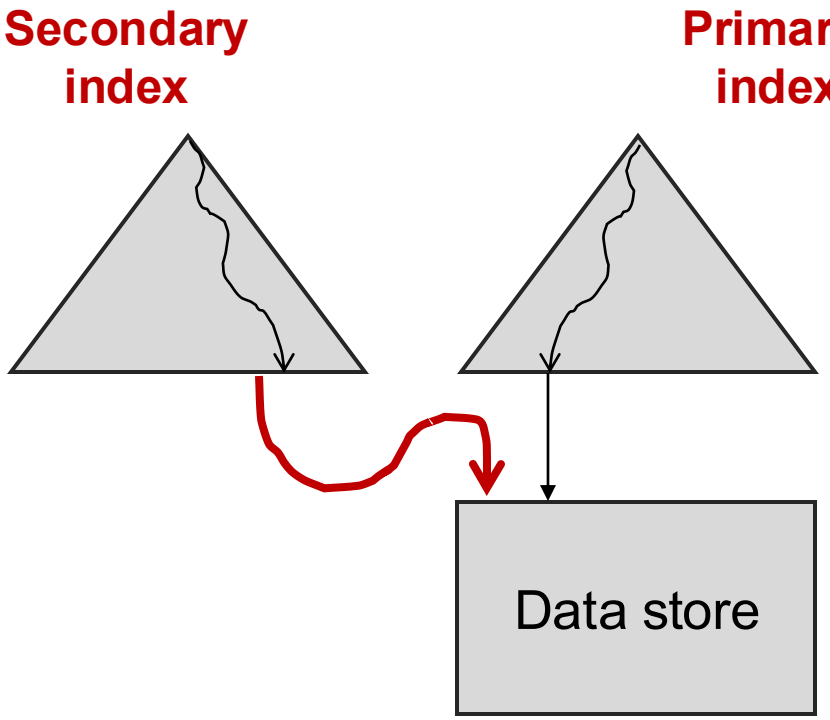
- E.g., random lookup, range scan
- Secondary index usually stores the primary key



Index

Index: Accelerate data retrieval operations in a database table

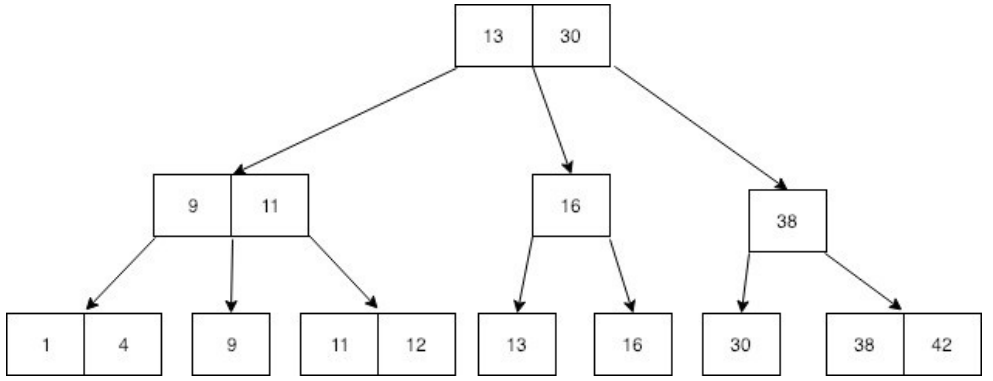
- E.g., random lookup, range scan
- Secondary index can also point to the record directly



B-tree

Balanced tree data structure

- Data is sorted
- Supports: search, sequential scan, inserts, and deletes



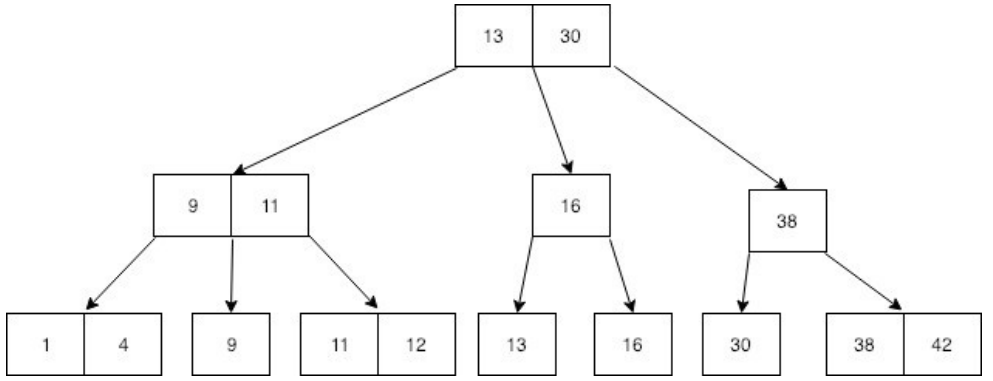
B-tree

Balanced tree data structure

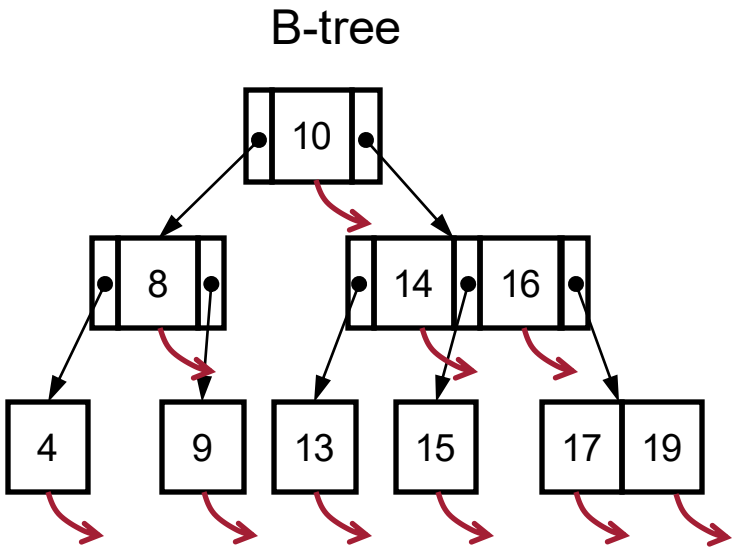
- Data is sorted
- Supports: search, sequential scan, inserts, and deletes

Properties

- Every node contains *k* to *2k* keys (except root)
- All leaf nodes are at the same level
- *k* is typically large; a lookup traverses a small number of levels

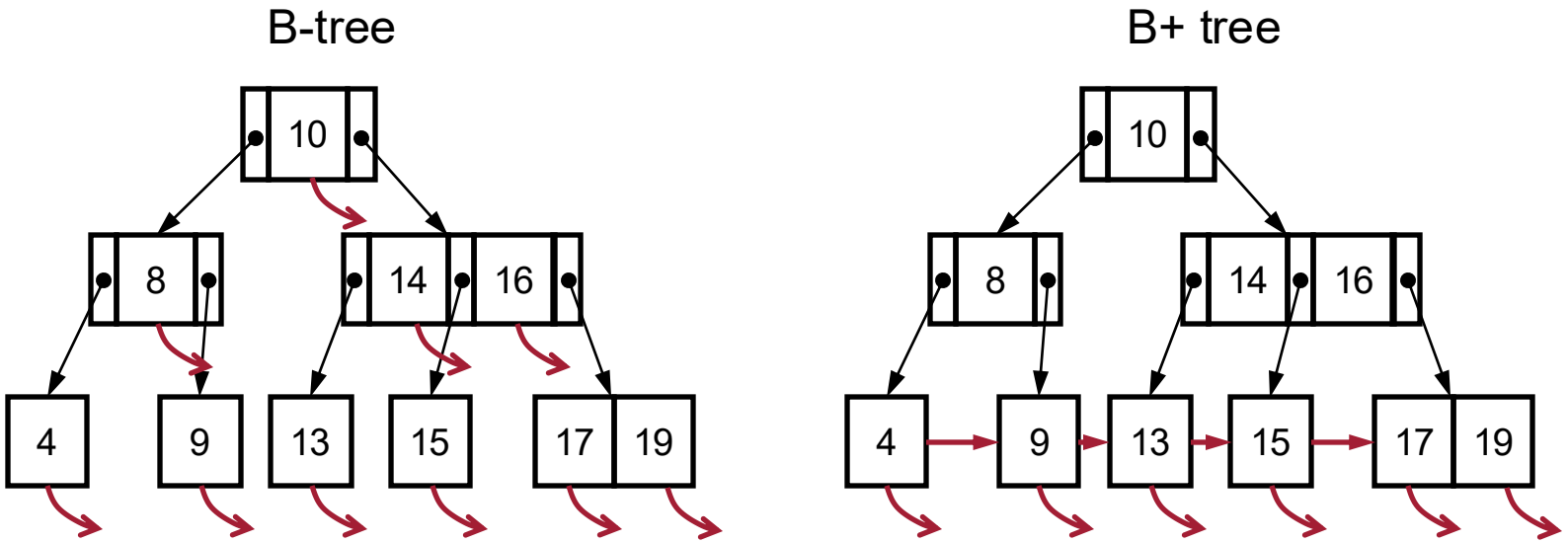


B-tree vs. B+ Tree vs. B* Tree



B-tree: data pointers stored in all nodes

B-tree vs. B+ Tree vs. B* Tree



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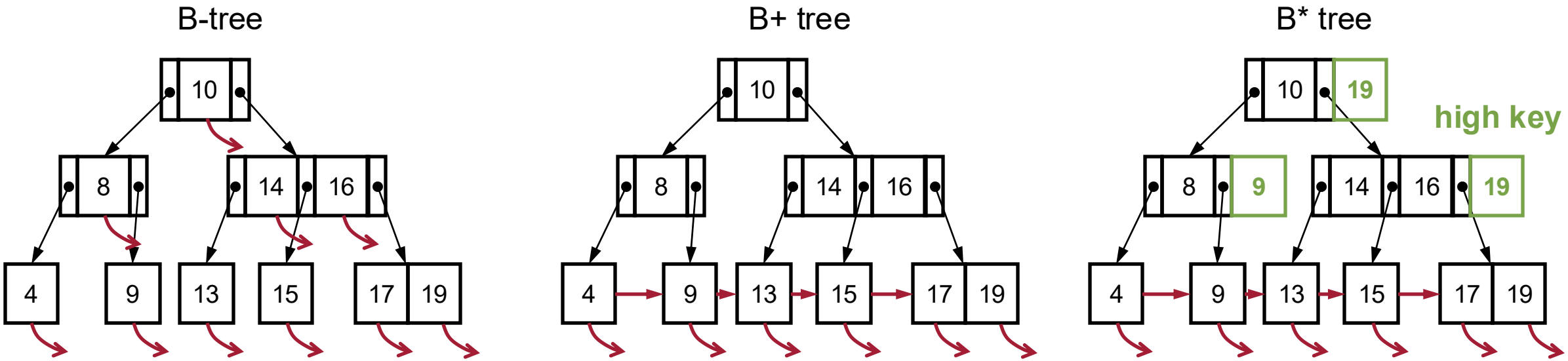
B+ tree:

- Data pointers stored only in leaf nodes
- The leaf nodes are linked

B-tree vs. B+ Tree vs. B* Tree



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B+ tree:

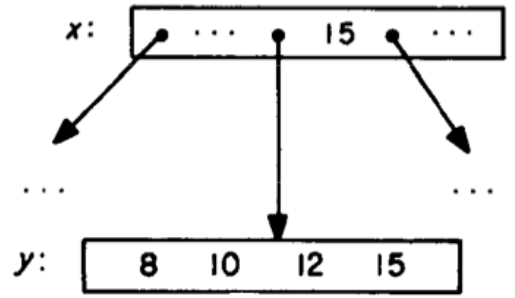
- Data pointers stored only in leaf nodes
- The leaf nodes are linked

B* tree is a misused term in B-tree literature

- Typically means a variant of B+ tree in which each node is least 2/3 full
- In this paper: B+ tree with high key appended to non-leaf nodes (upper bound on values)

Insert Example

Assume k = 2 (at most 4 keys per node)

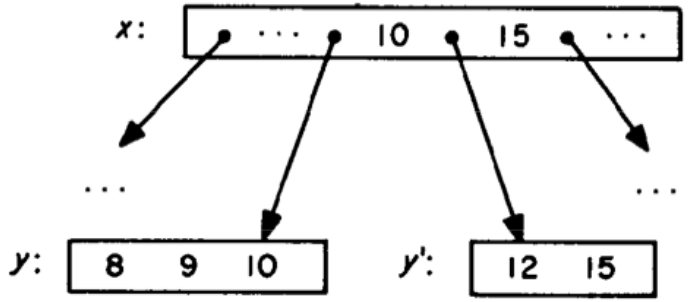


(a)

insert(9)

$A \leftarrow$ read(x)

examine A; get ptr to y
$A \leftarrow$ read(y)
insert 9 into A; must split into A, B
put(B, y')
put(A, y)
Add to node x a pointer to node y'.



Search Example

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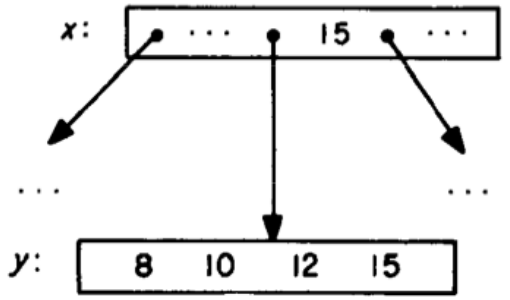


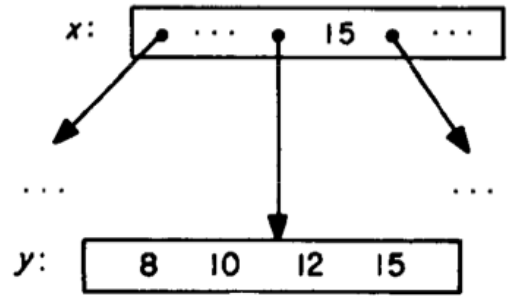
search(15)

1. $C \leftarrow \text{read}(x)$
2.
3. examine C; get ptr to y
4.
5.
6.
7.
8.
9.
10. $C \leftarrow \text{read}(y)$

Concurrency Challenge

Assume k = 2 (at most 4 keys per node)

Concurrent search and insert can cause problems



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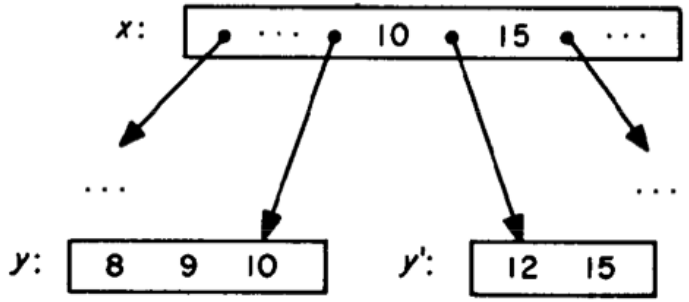

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B-Tree Index

Lock coupling

B^{link}-tree

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Optimistic lock coupling (OLC)

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A node is **unsafe** (wrt. insertion) if it is full (i.e., contains 2k keys)

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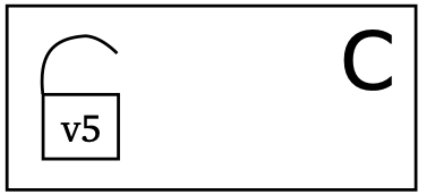
Lock coupling (aka. lock crabbing)

- Lock parent
- Access parent
- Lock child
- Release parent if child is safe

1. lock node A
2. access node A

3. lock node B
4. unlock node A
5. access node B

6. lock node C
7. unlock node B
8. access node C
9. unlock node C



Lock Coupling

A node is **unsafe** (wrt. insertion) if it is full (i.e., contains 2k keys)

Lock coupling (aka. lock crabbing)

- Lock parent
- Access parent
- Lock child
- Release parent if child is safe

What if the child is unsafe?

- One solution: split immediately if child is unsafe

1. lock node A
2. access node A

3. lock node B
4. unlock node A
5. access node B

6. lock node C
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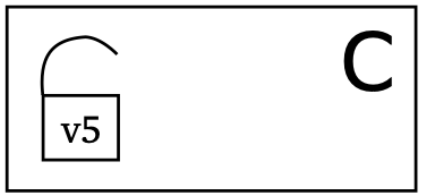
8. access node C
9. unlock node C



Limitation of Lock Coupling

The root is locked for every index access and becomes a scalability bottleneck

Observation: root and upper levels are rarely changed; lock coupling is too conservative

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Observation: root and upper levels are rarely changed; lock coupling is too conservative

Concurrency challenge: search may read wrong node due to split

- **Lock coupling solution**: guard split using a lock
- **B^{link} tree solution**: allow search to find the right node

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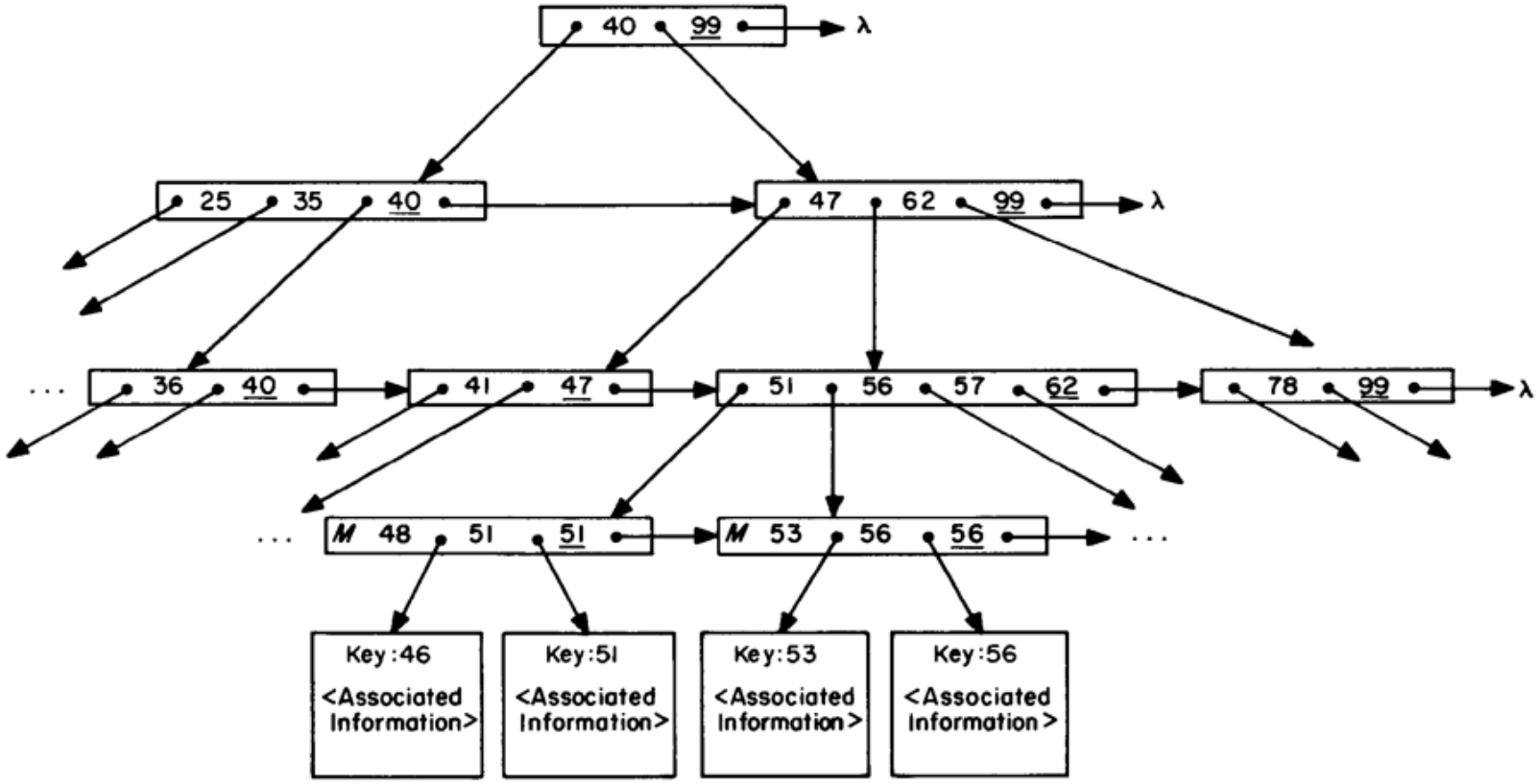
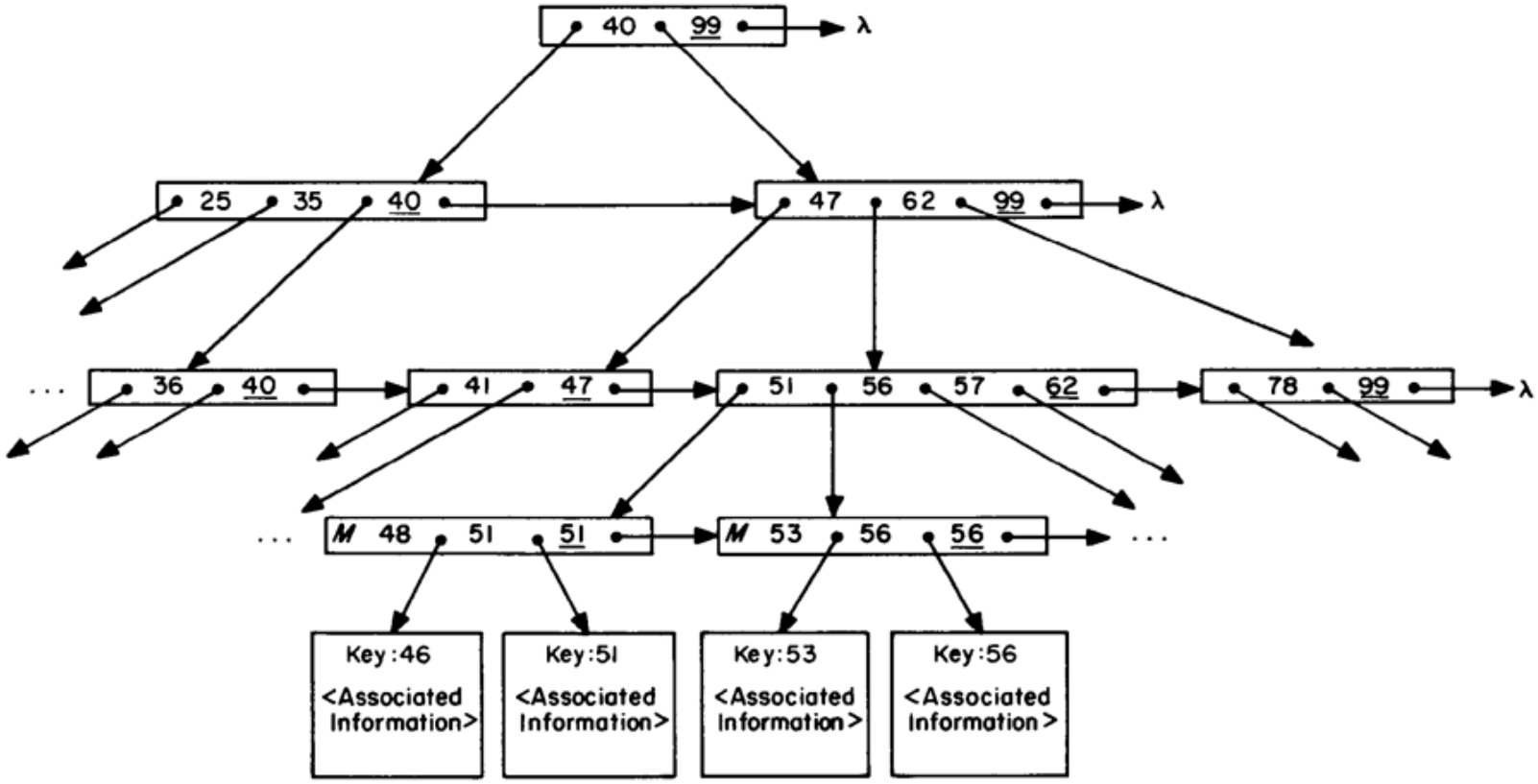
B^{link}-Tree



Feature 1: **link pointer** to next node at each level → **key idea**

B^{link}-Tree



Feature 1: **link pointer** to next node at each level → **key idea**

Feature 2: **high key** for each node

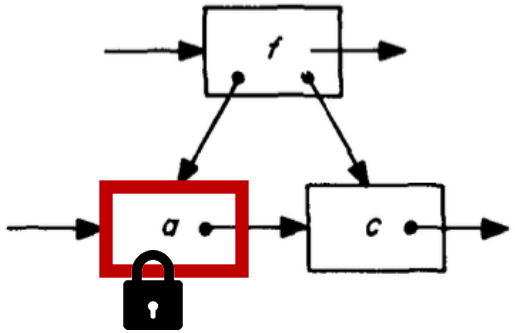
B^{link}-Tree: Locks

- Hold only a small number of locks at any time
- Reads are not blocked by locks
- Locks prevent only multiple updates

B^{link}-Tree: Insert Algorithm

Insert to leaf if the leaf node if not full

Illustration of node split (node *a* is split into *a'* and *b'*)



Before split

B^{link}-Tree: Insert Algorithm

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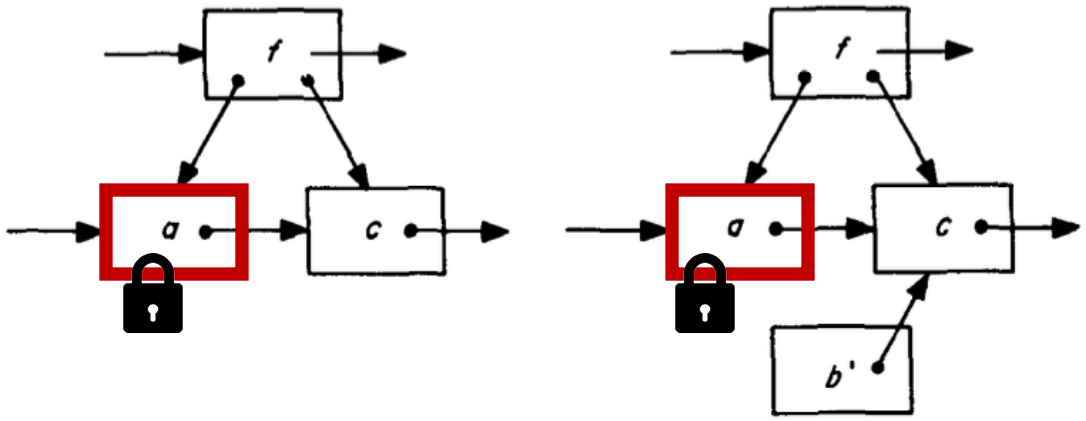

Before split Step 1

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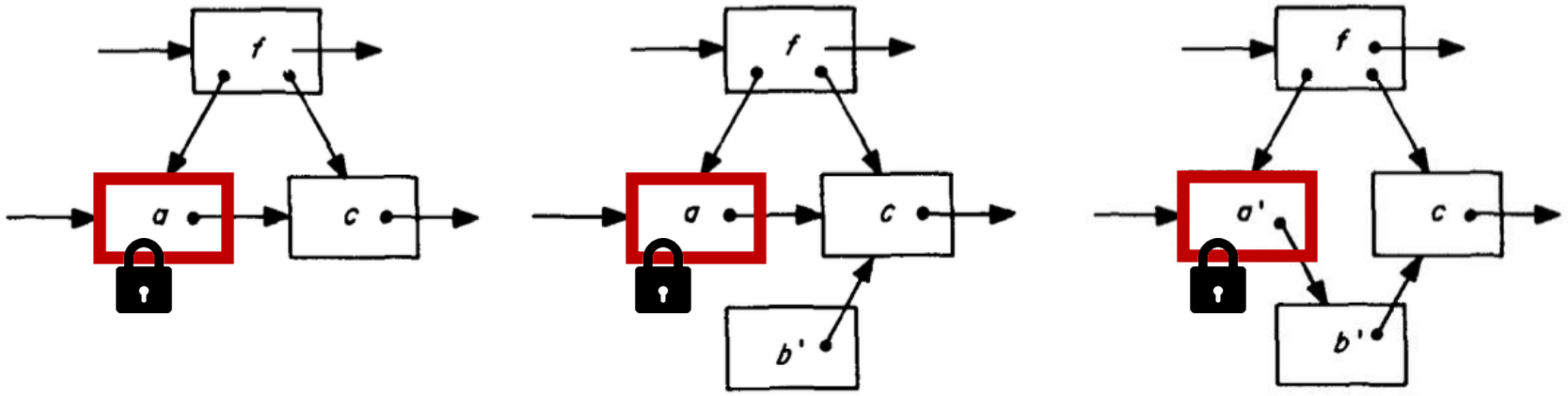

Before split Step 1 Step 2

B^{link}-Tree: Insert Algorithm

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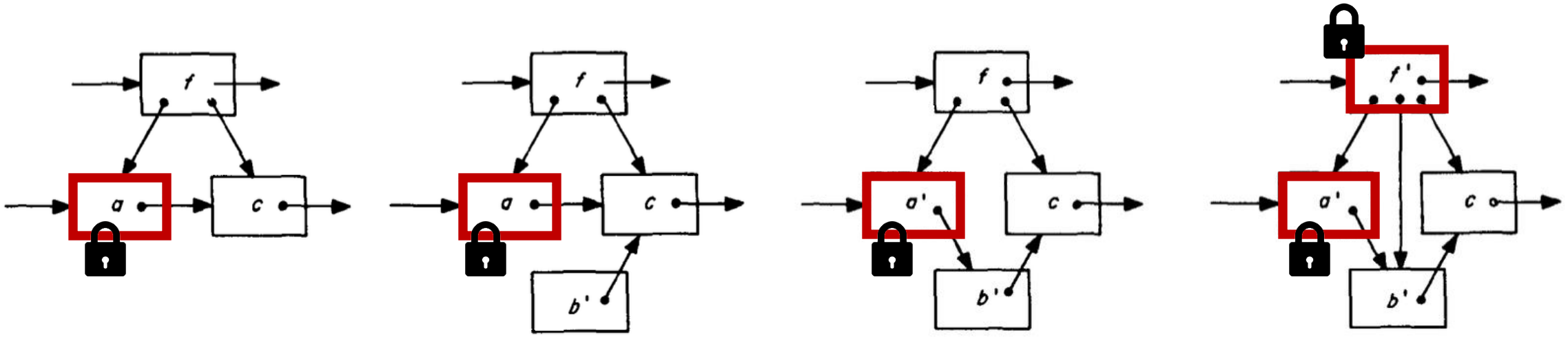

Before split | Step 1 | Step 2 | Step 3

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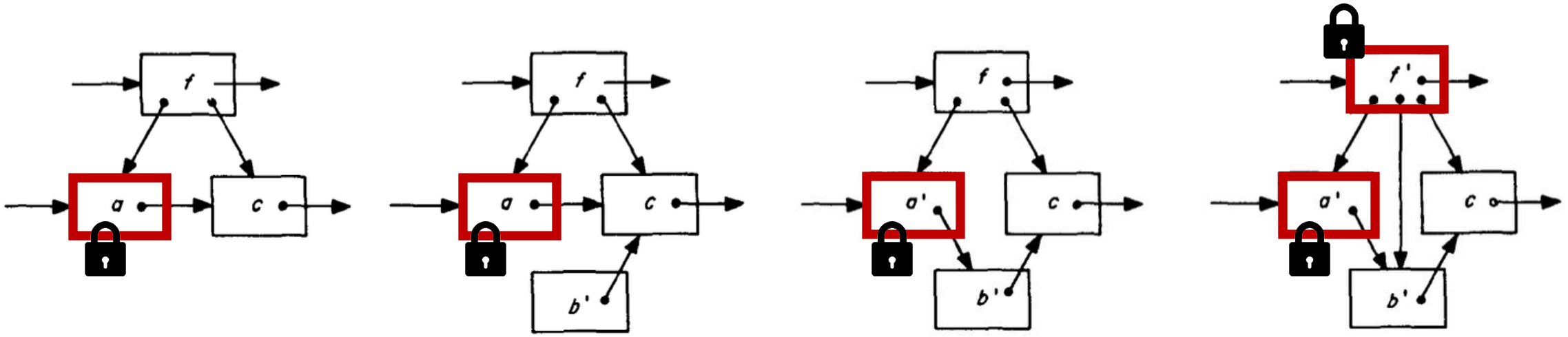
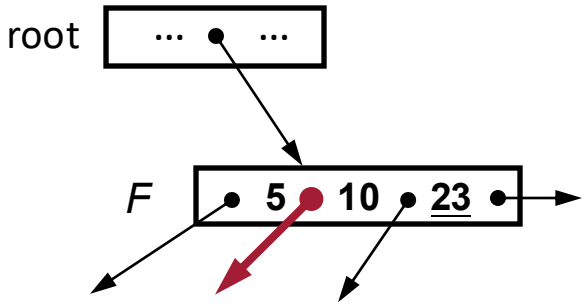


Before split | Step 1 | Step 2 | Step 3

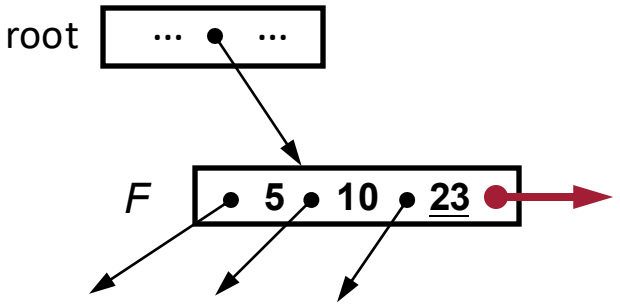
Q: What if another txn searches a key in b' before step 3 finishes?

B^{link}-Tree: Search Algorithm

May follow the link pointer to find a key



If search for Key=8

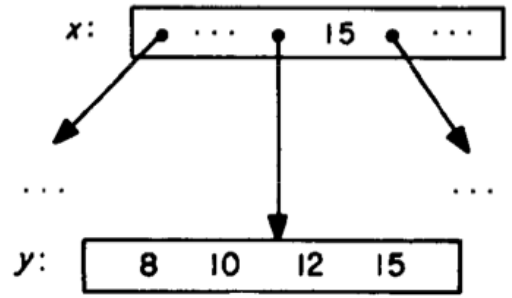


If search for Key=24

Concurrent Search & Insert

Assume k = 2 (at most 4 keys per node)

Concurrency problem is solved in B^{link} tree



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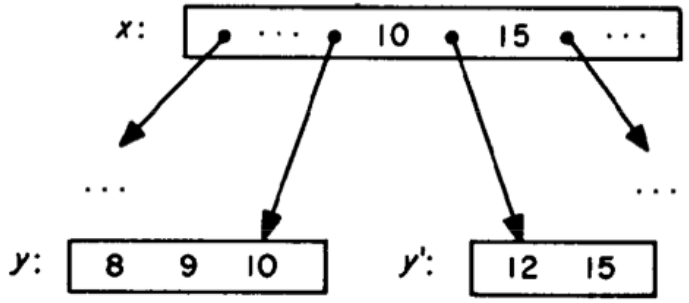

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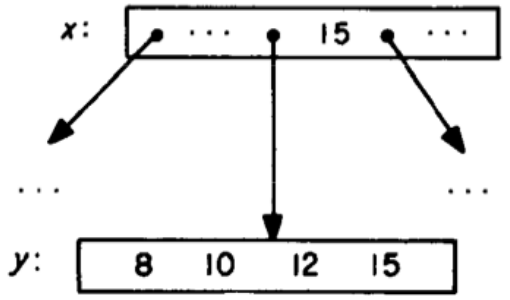
Concurrent Search & Insert

Assume k = 2 (at most 4 keys per node)

Concurrency problem is solved in B^{link} tree

High key indicates when to follow link pointer



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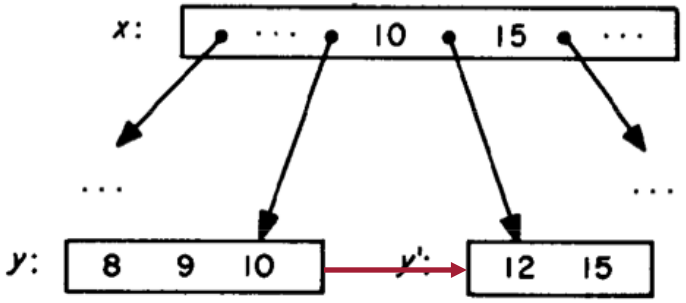

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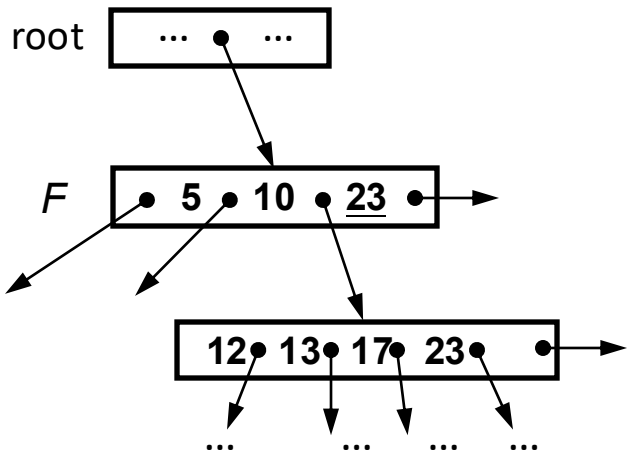
11. ~~*error: 15 not found!*~~	

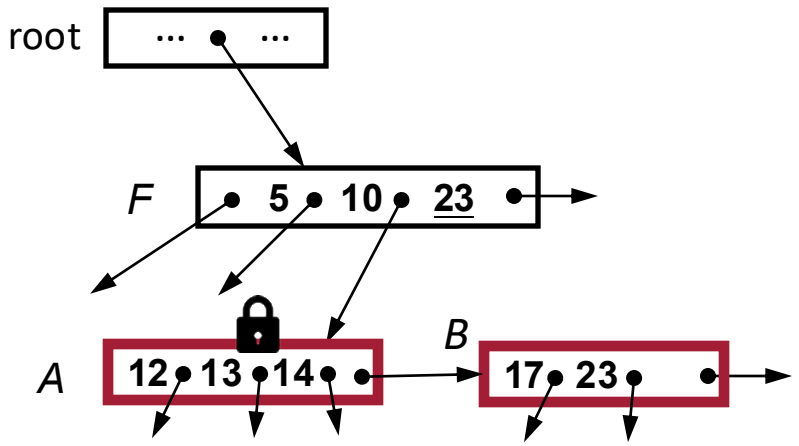
15 is found following the link pointer

Concurrent Insert & Insert

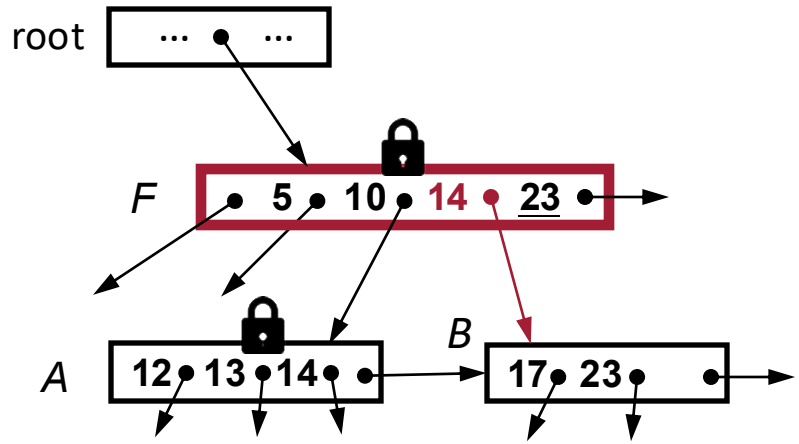
Before insert 14



Leaf node split



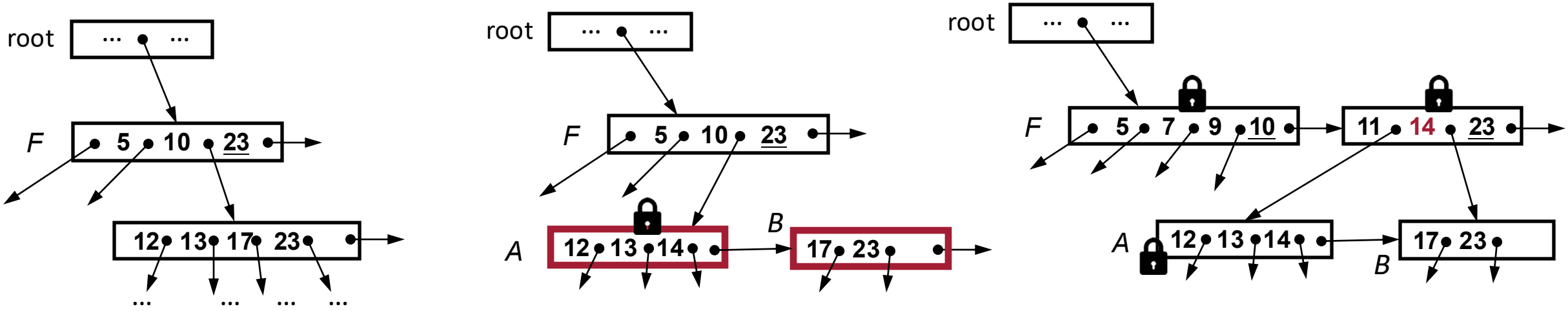
Insert to parent node



Regular insert process

Concurrent Insert & Insert

Before insert 14 | Leaf node split | Insert to parent node



During an insert, the parent node is split by another transaction

- Follow the link point to find the real parent node
- The transaction holds 3 locks in this scenario

Agenda

B-Tree Index

Lock coupling

B^{link}-tree

- Search
- Insert

Optimistic lock coupling (OLC)

Optimistic Lock Coupling (OLC)

Each tuple contains a 64-bit version counter

1. lock node A
2. access node A

3. lock node B
4. unlock node A
5. access node B

6. lock node C
7. unlock node B
8. access node C
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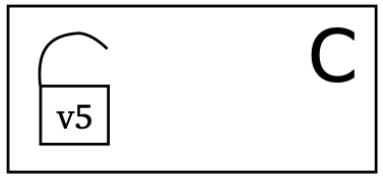


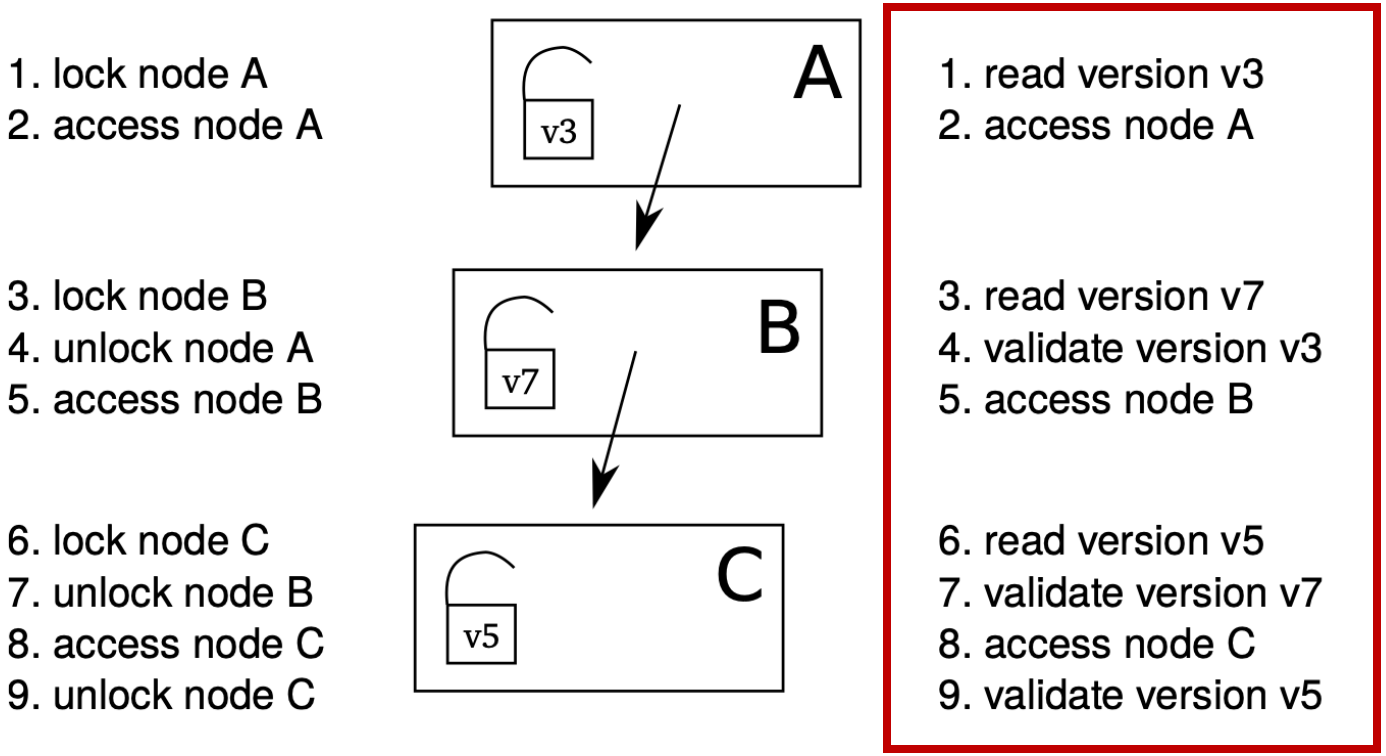
1. read version v3
2. access node A

3. read version v7
4. validate version v3
5. access node B

6. read version v5
7. validate version v7
8. access node C
9. validate version v5

Optimistic Lock Coupling (OLC)

Each tuple contains a 64-bit version counter



No scalability bottleneck

- No write to shared memory during traversal
- Upon conflict, retry from root
- Performance similar to B^{link} tree

Evaluation

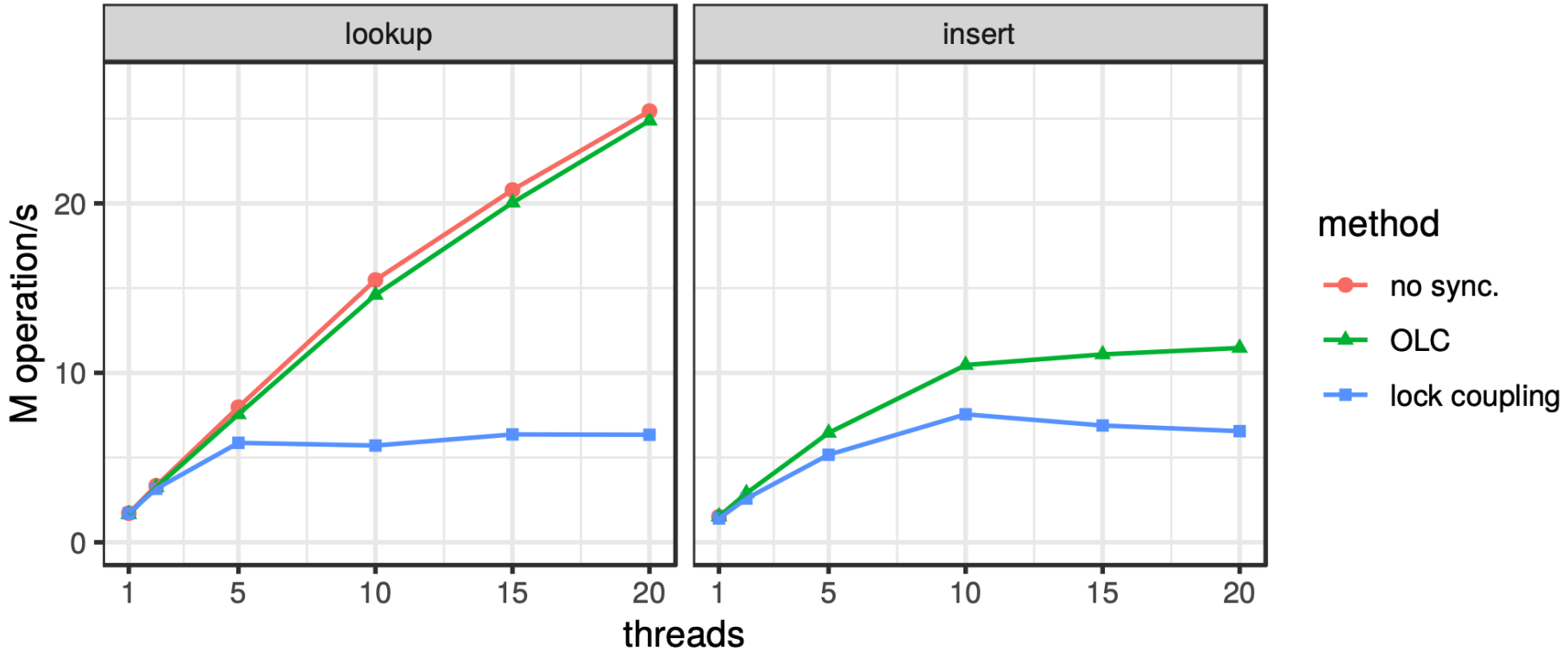


Figure 3: Scalability on 10-core system for B-tree operations (100M values).

Leis, Viktor et al. *Optimistic Lock Coupling: A Scalable and Efficient General-Purpose Synchronization Method. IEEE Data Eng. Bull.* 42 (2019): 73-84.

Q/A – Blink Tree

Recovery protocol?

Scalability under heavy update workloads?

Repeated splits near the same region?

For high concurrency, contention on upper-level node still negligible?

Excessive link pointer chain-following in the worst case?

Extend to a distributed system?

Next Lecture

Viktor Leis, et al., The Adaptive Radix Tree: ARTful Indexing for Main-Memory Databases. ICDE, 2013